# Three-dimensional Proxies for Hand-drawn Characters

Eakta Jain Yaser Sheikh Moshe Mahler Jessica Hodgins

1 Carnegie Mellon University

<sup>2</sup>Disney Research Pittsburgh

Hand-drawn animation

3D CG animation

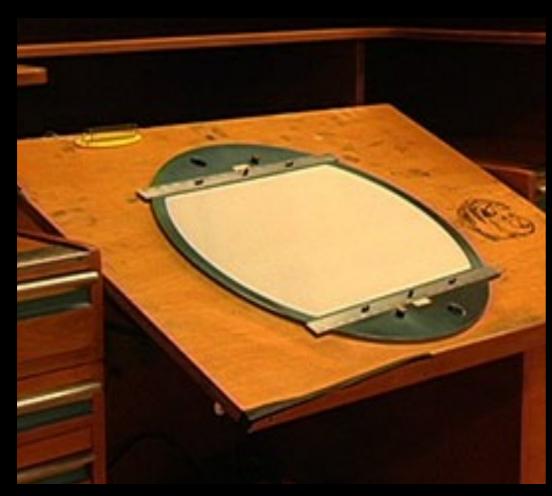




Hand-drawn animation

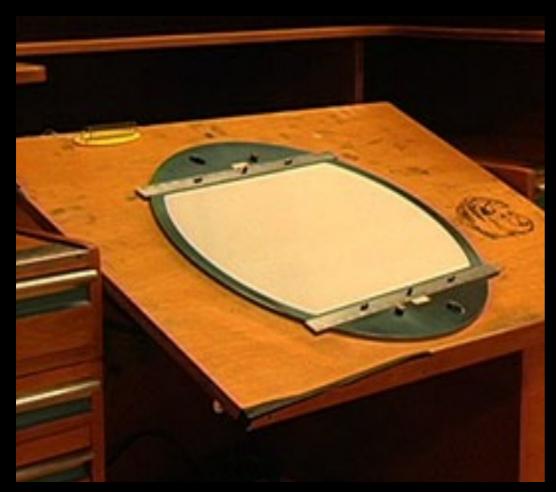
3D CG animation

# Differences between hand animation and computer animation

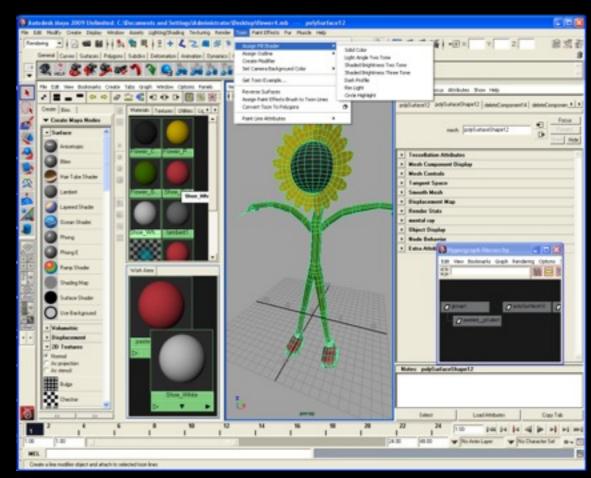


Hand animator's workdesk

# Differences between hand animation and computer animation



Hand animator's workdesk



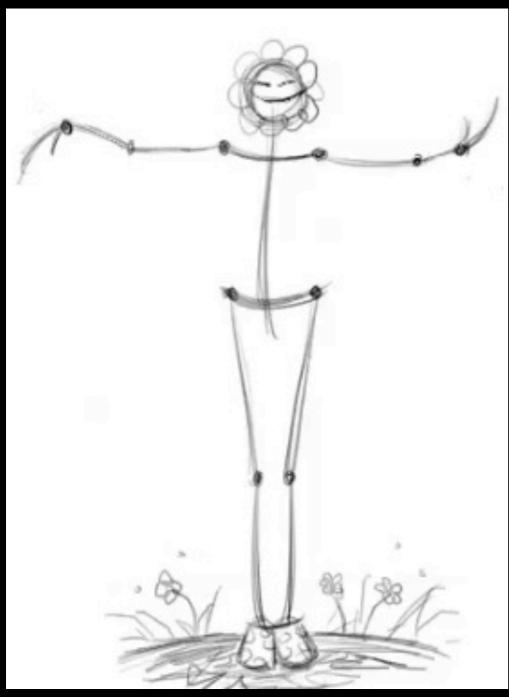
3D animation software

# Input

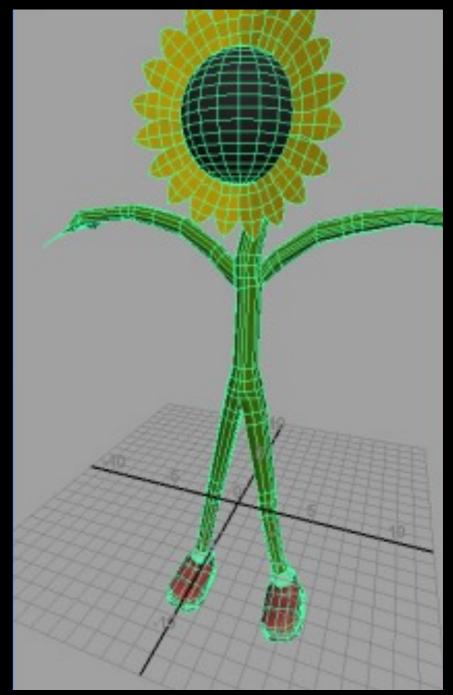
## Input







Hand-drawn character

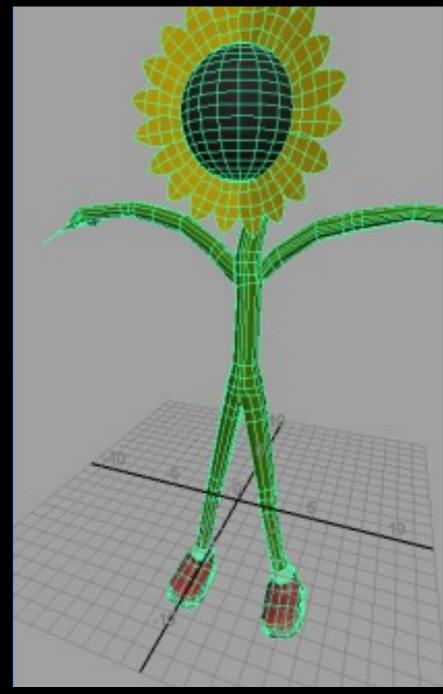


3D proxy



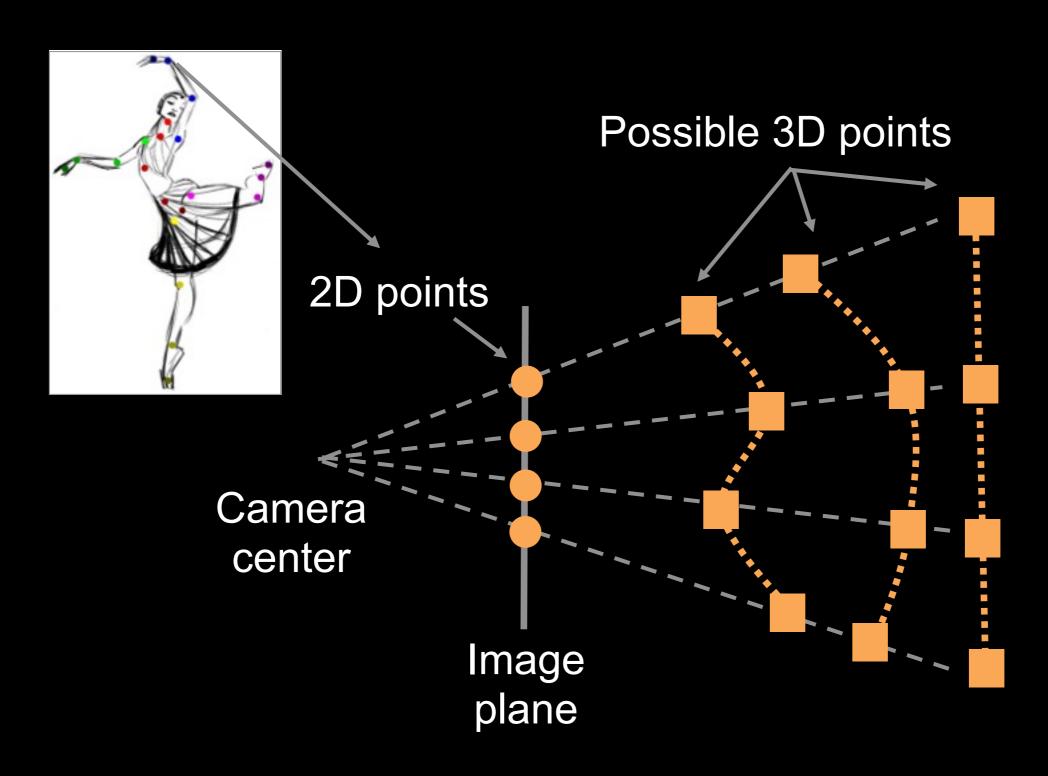
Hand-drawn character

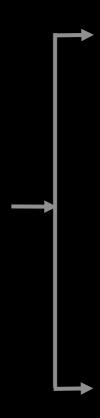
Geometry Motion

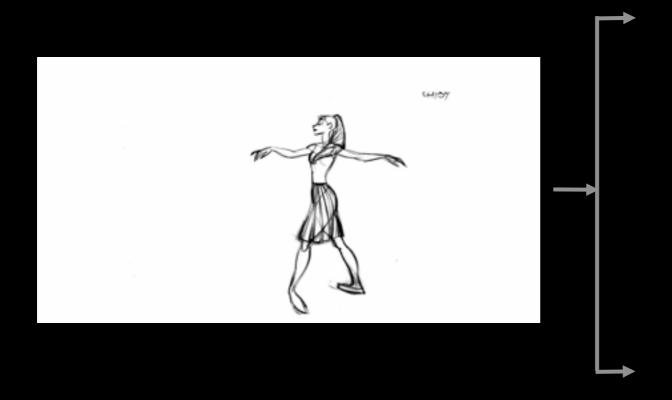


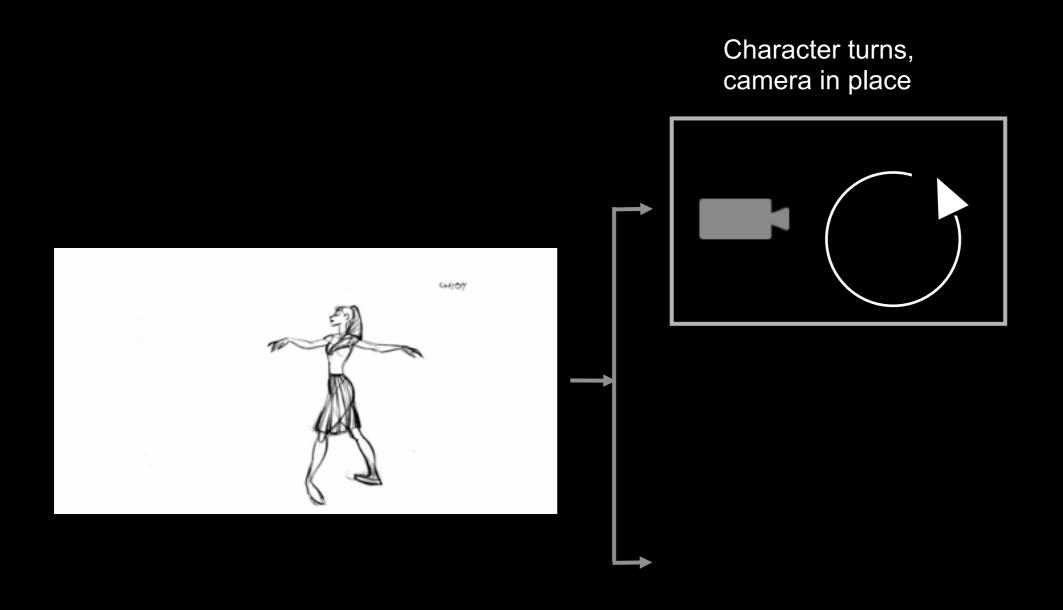
3D proxy

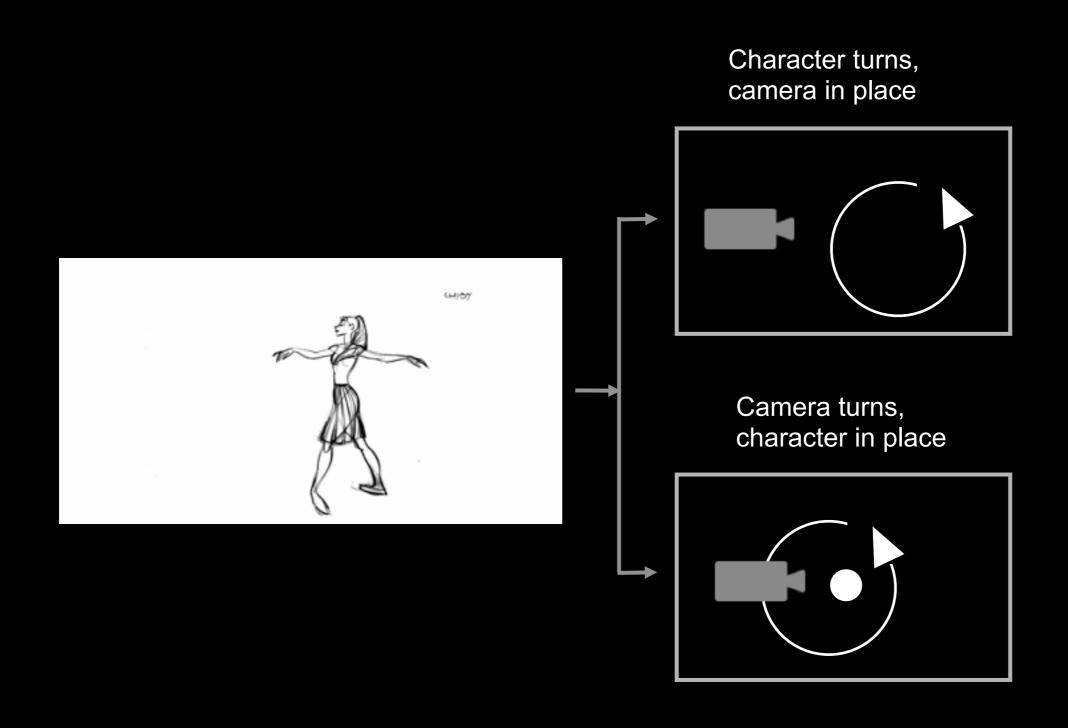
#### Challenge: Inferring third dimension

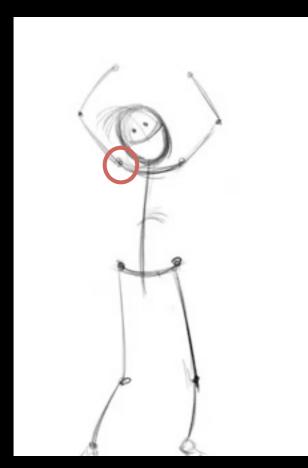




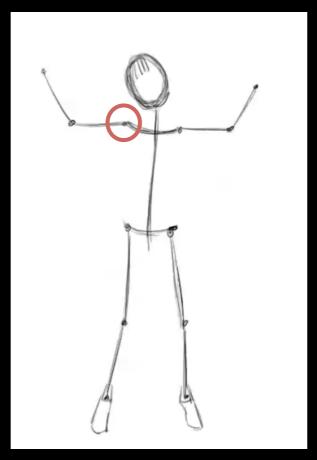




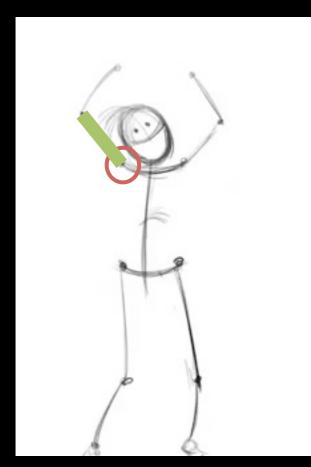




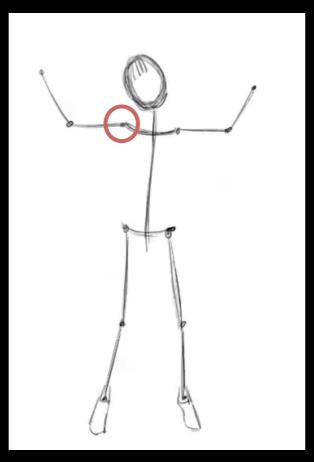
Frame #1



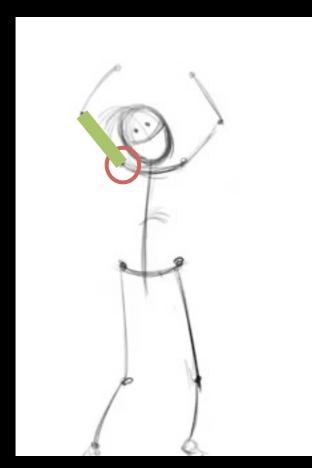
Frame #40



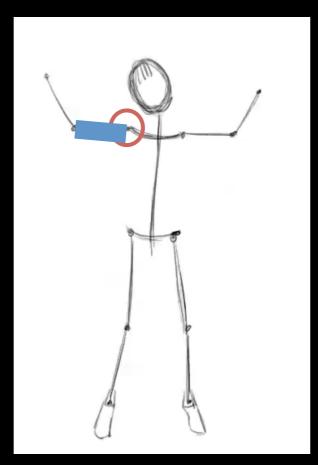
Frame #1



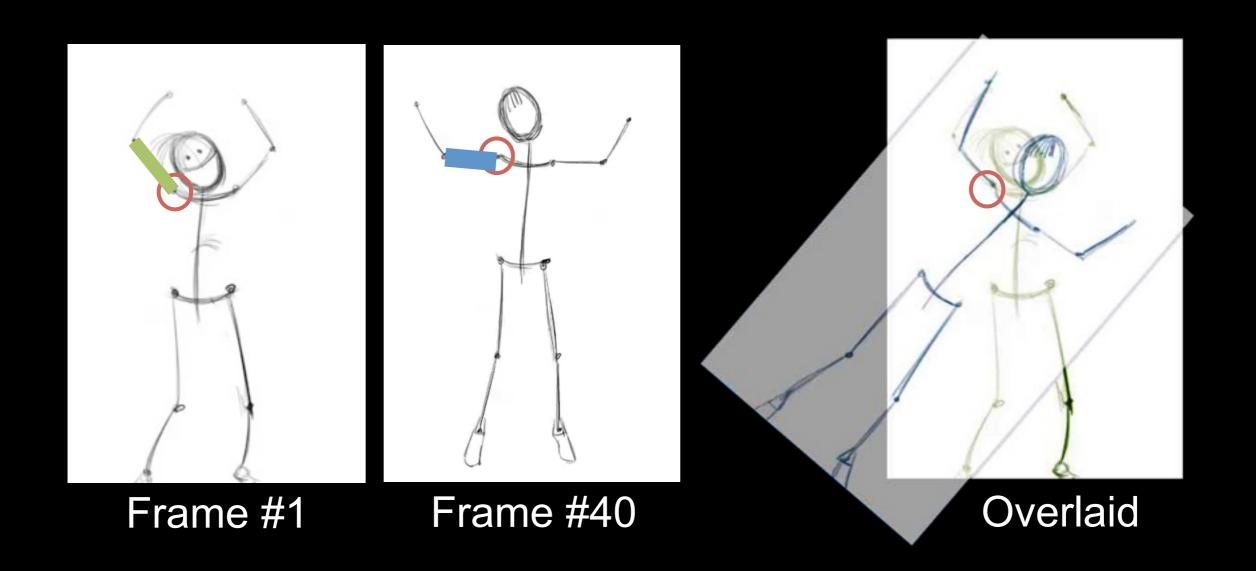
Frame #40

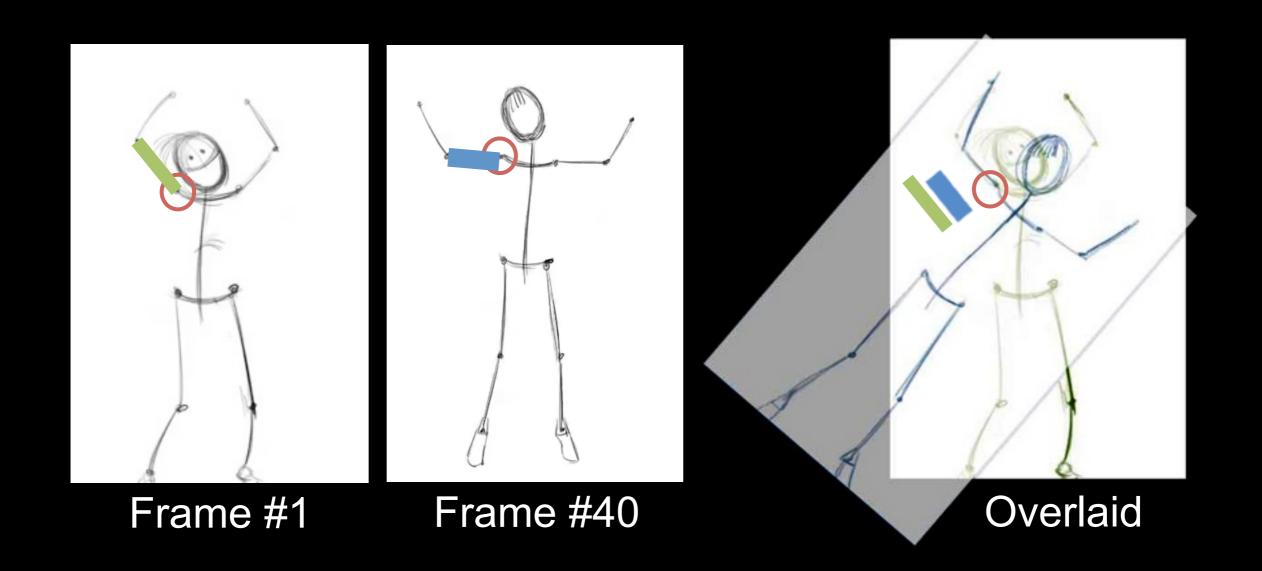


Frame #1

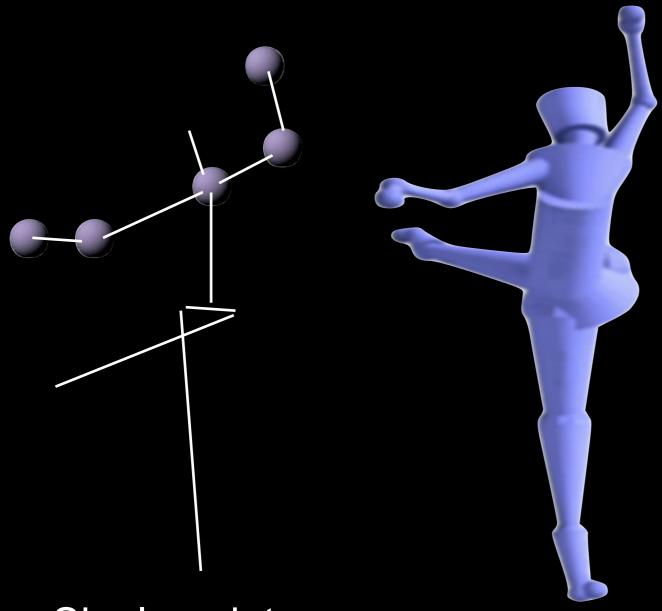


Frame #40





# Three-dimensional proxies with different levels of detail



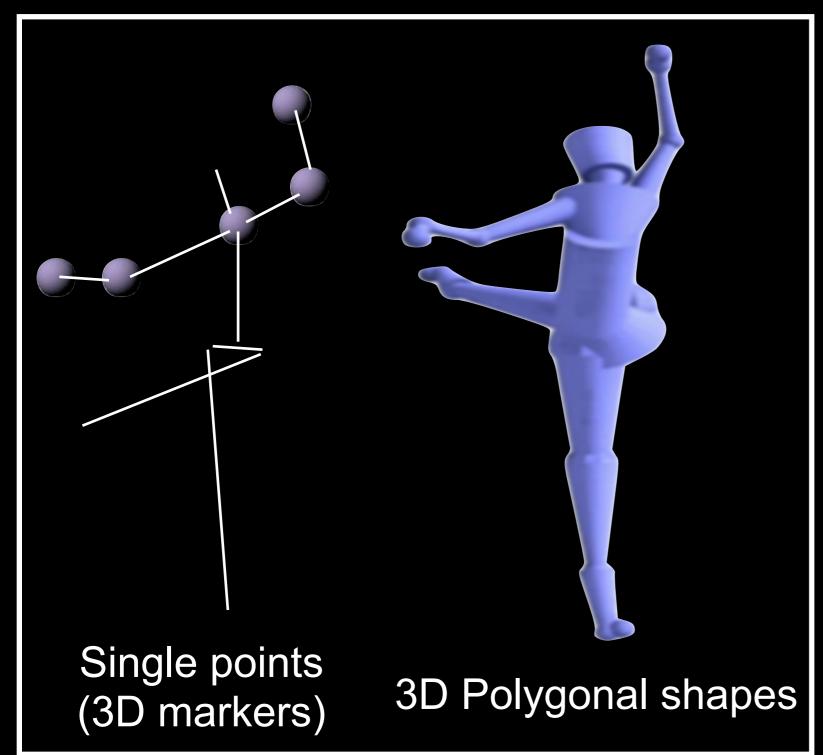
Single points (3D markers)

3D Polygonal shapes



Joint hierarchy based skeleton

# Three-dimensional proxies with different levels of detail





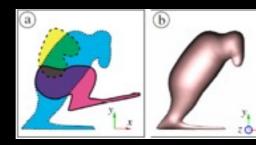
Joint hierarchy based skeleton

#### Past work

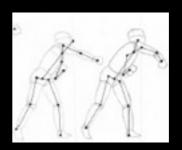




Correa et al. (1998)



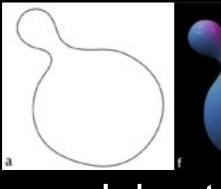
Petrovic et al. (2000)



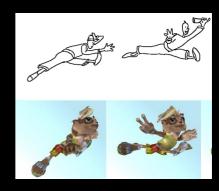
Davis et al. Li et al. (2003)



(2003)



**Johnston** (2002)



Bregler et al. (2002)

### User Input



Virtual markers

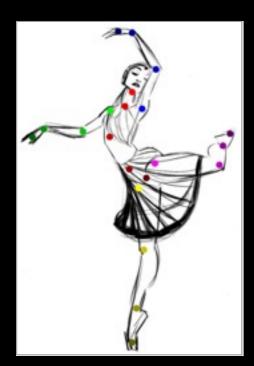


Limb bounding boxes



Color coded body parts

#### User Input



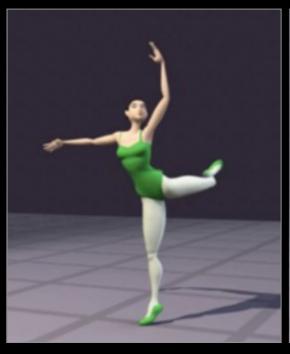
Virtual markers



Limb bounding boxes



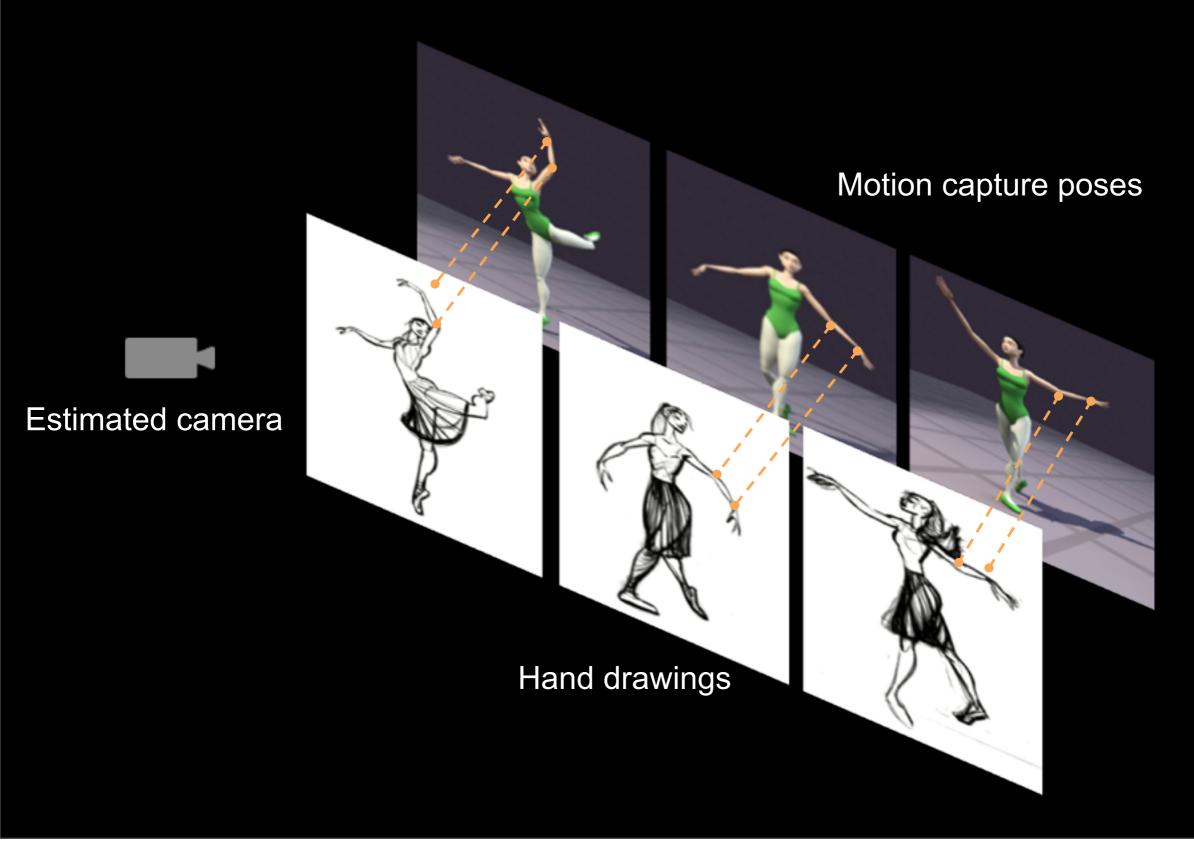
Color coded body parts

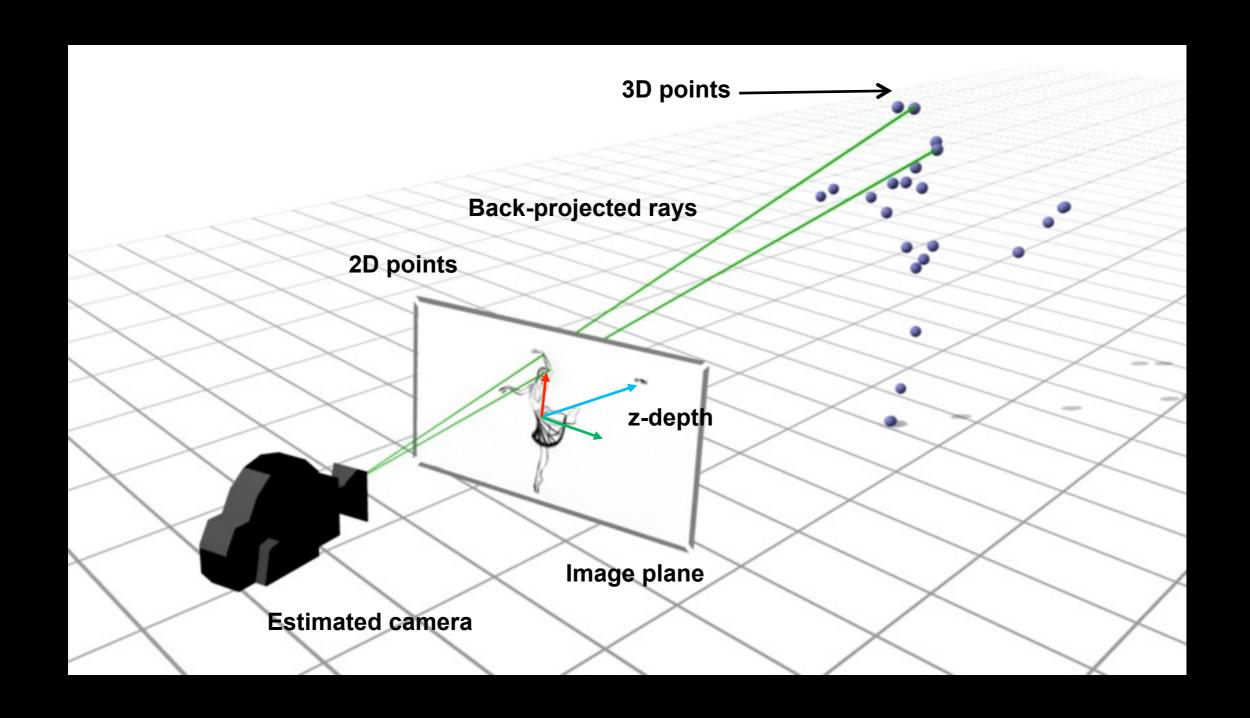




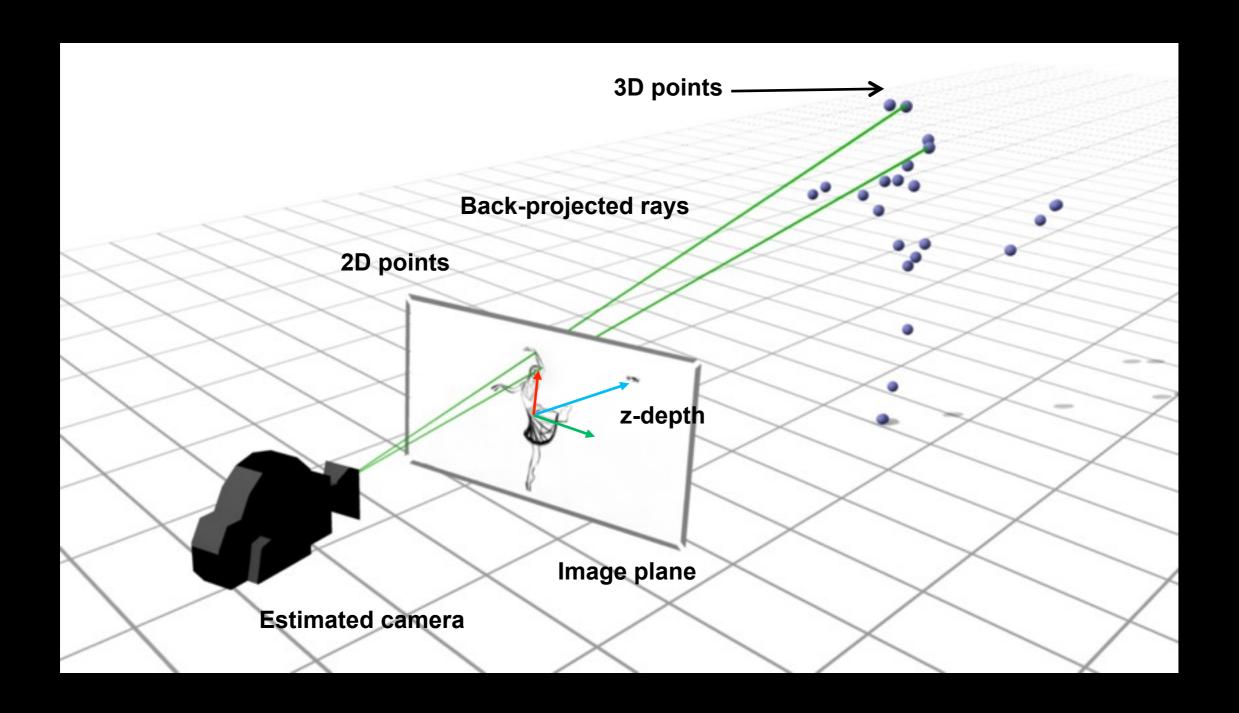
Motion capture segment with similar depth information, time-warped via Dynamic Time Warping

#### Camera Estimation

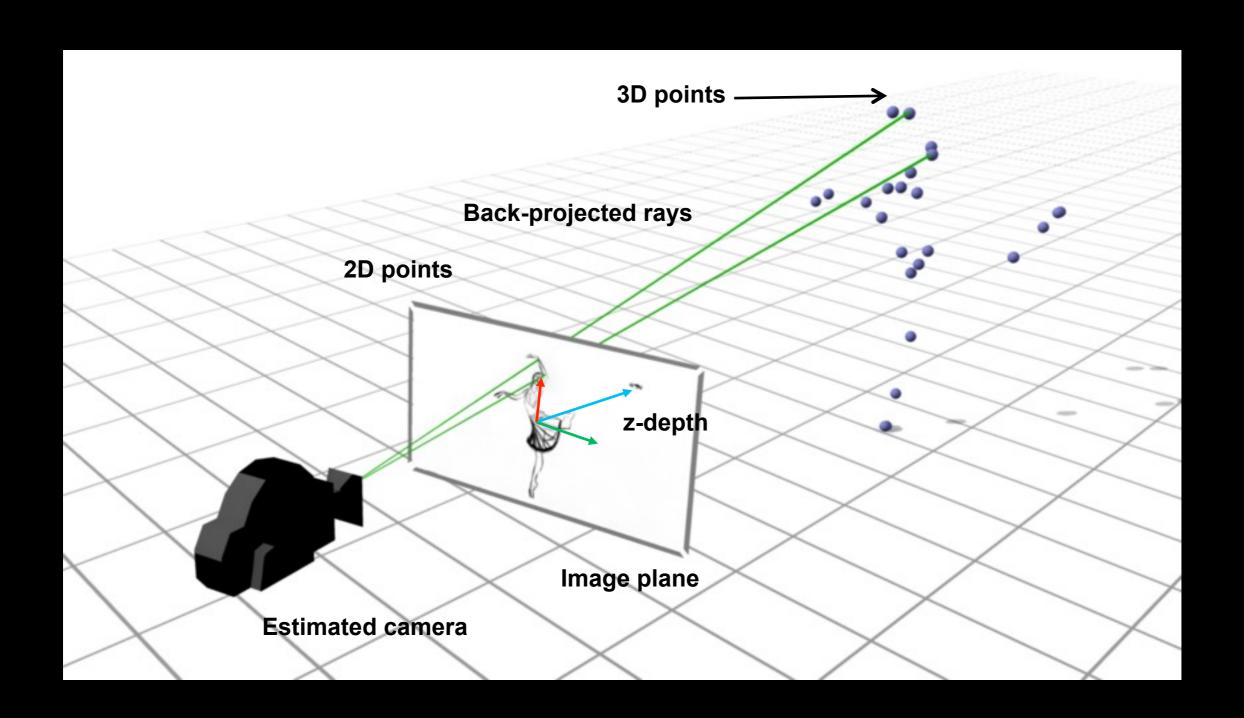




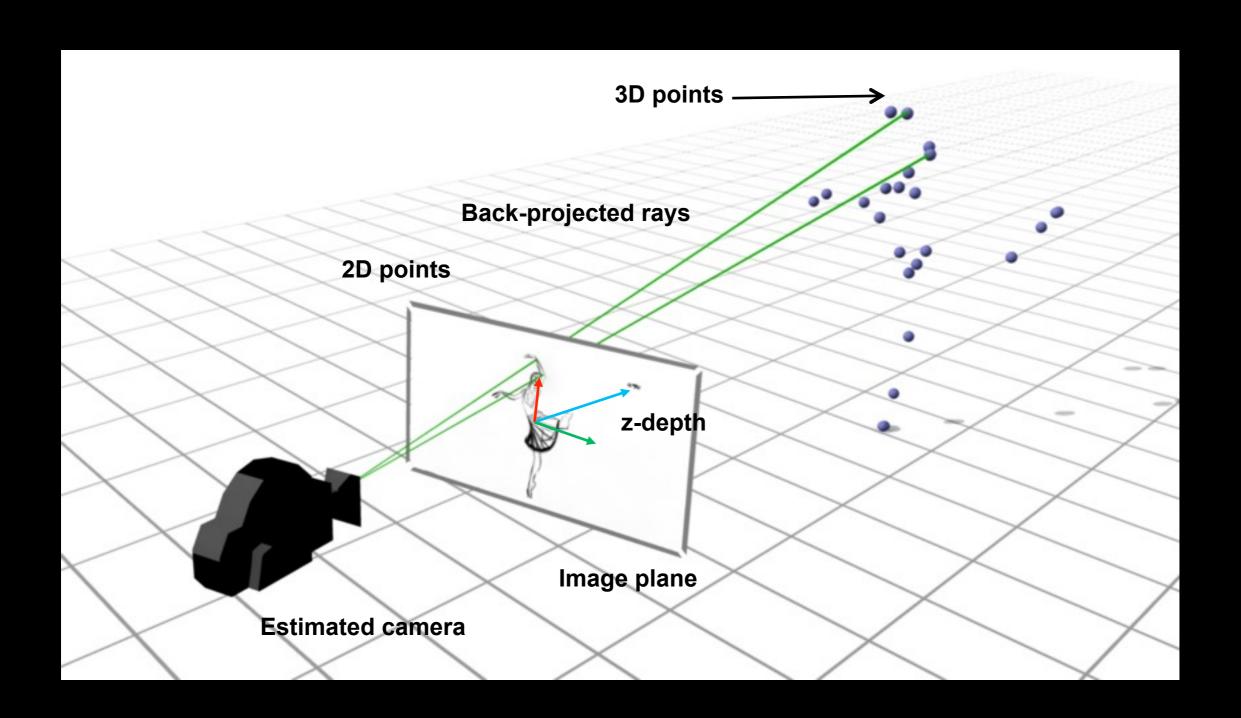
$$\underset{x}{\operatorname{arg\,min}}(e_a(x) + e_m(x) + e_s(x))$$



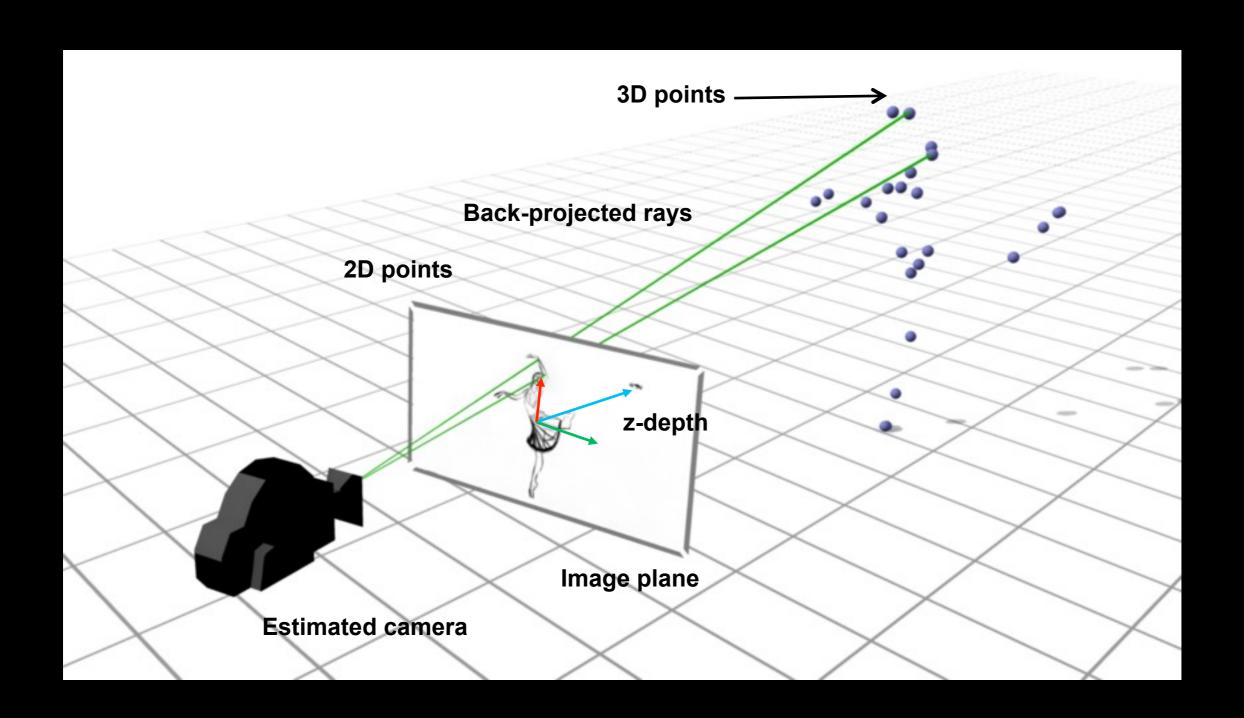
$$\underset{x \text{ input-matching}}{\min(e_a(x) + e_m(x) + e_s(x))}$$



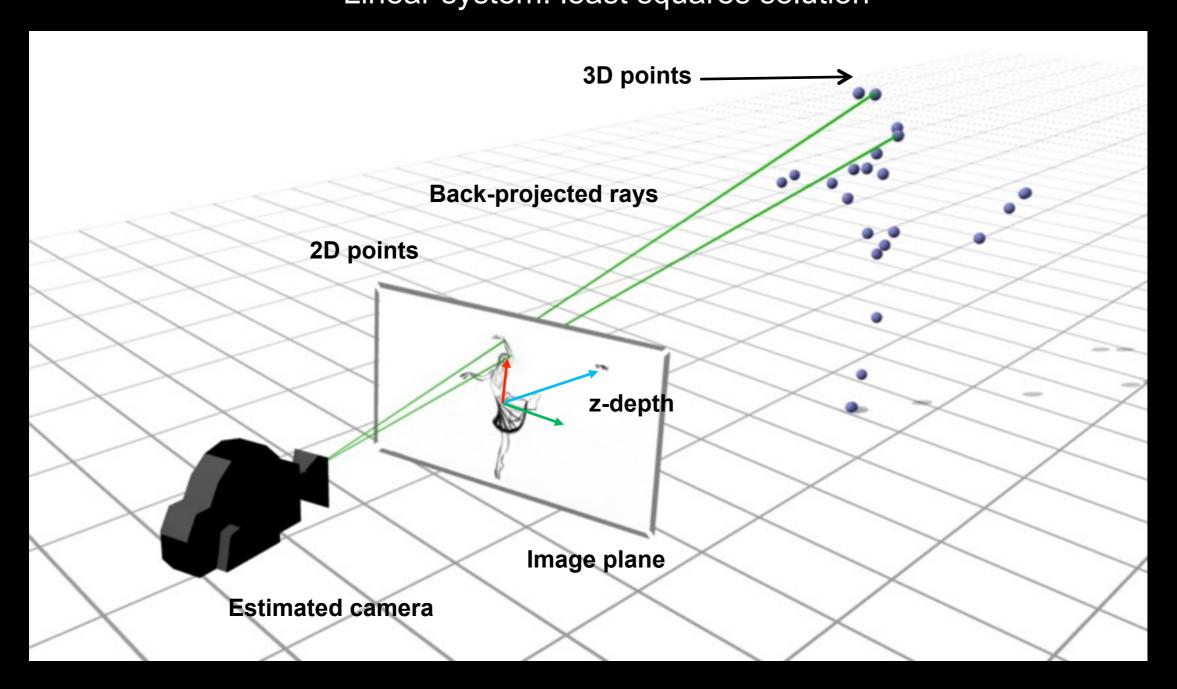
$$\underset{x \text{ input-matching depth prior}}{\operatorname{arg\,min}(e_a(x) + e_m(x) + e_s(x))}$$



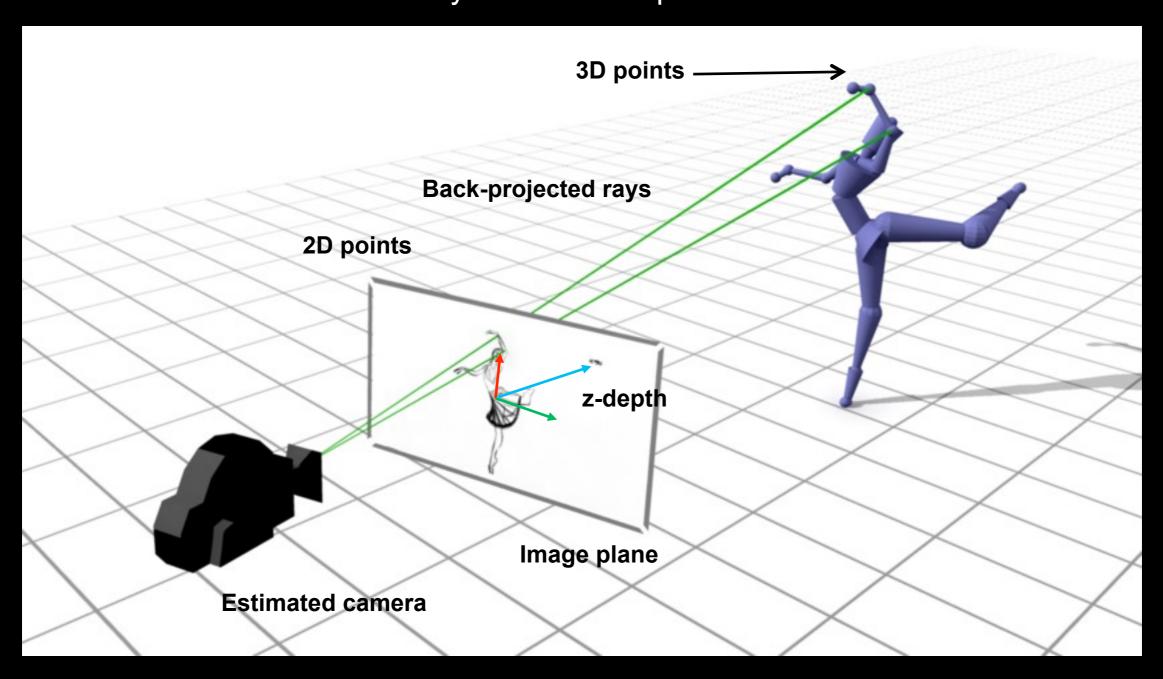
$$\underset{x \text{ input-matching depth prior smoothing term}}{\operatorname{arg\,min}(e_a(x) + e_m(x) + e_s(x))}$$



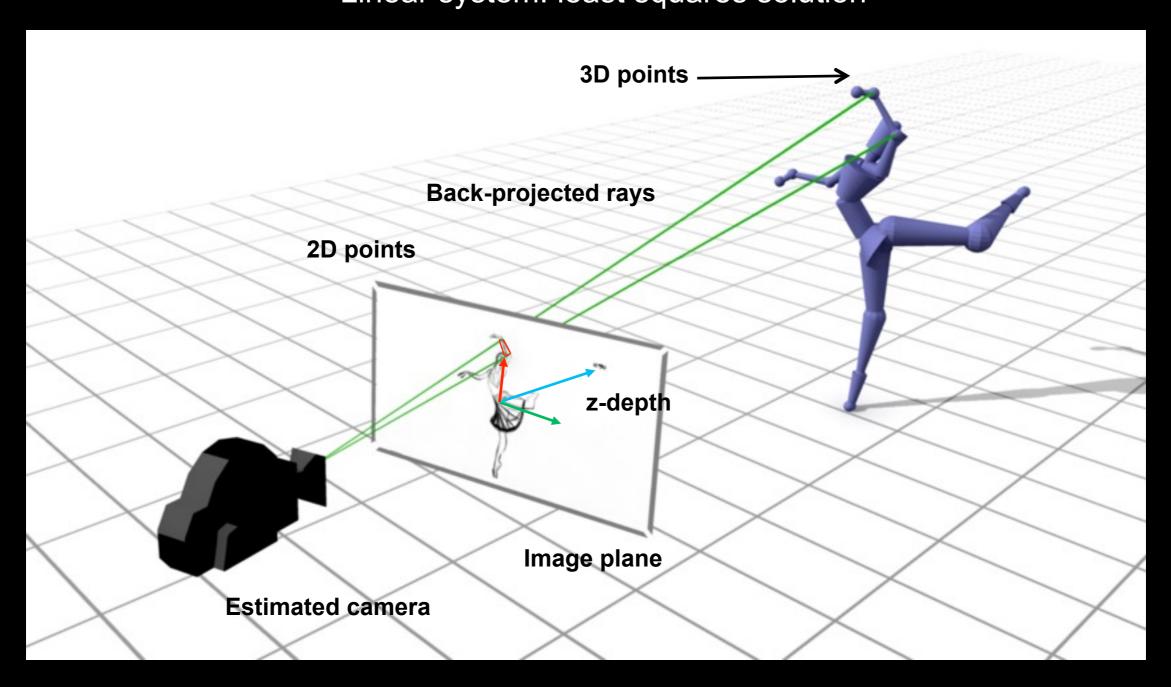
$$\operatorname*{arg\,min}(e_a(x) + e_m(x) + e_s(x)) \\ x \qquad \text{input-matching depth prior smoothing term}$$
 Linear system: least squares solution



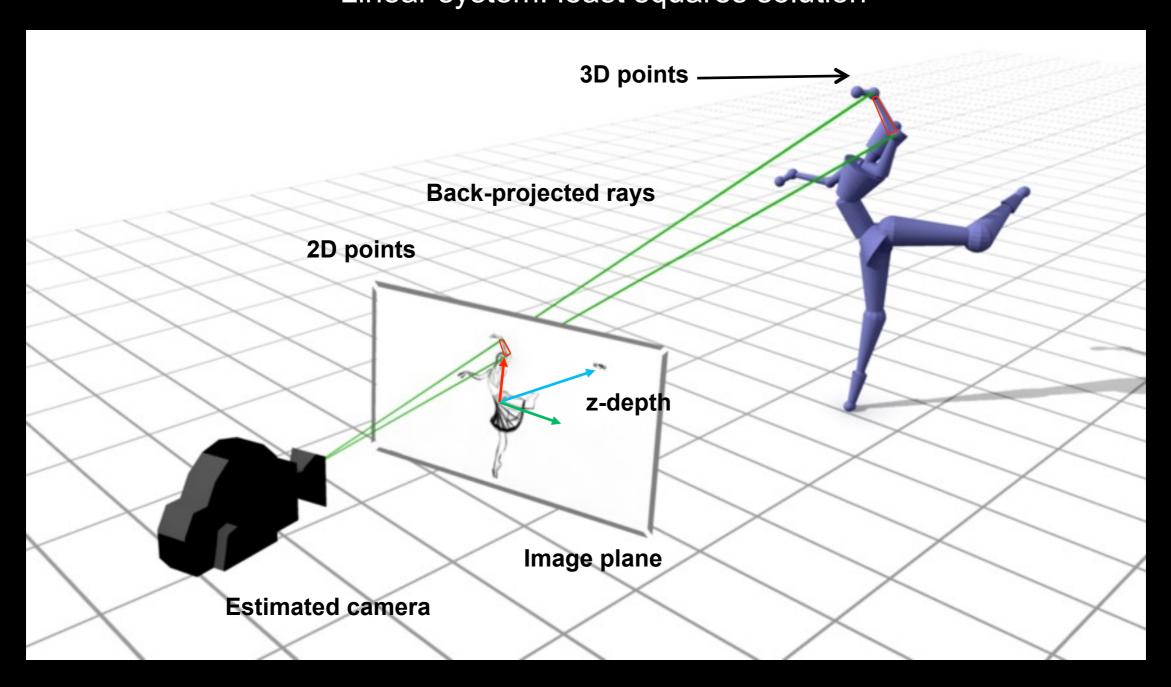
$$\operatorname*{arg\,min}(e_a(x) + e_m(x) + e_s(x)) \\ x \qquad \text{input-matching depth prior smoothing term}$$
 Linear system: least squares solution



$$\operatorname*{arg\,min}(e_a(x) + e_m(x) + e_s(x)) \\ x \qquad \text{input-matching depth prior smoothing term}$$
 Linear system: least squares solution

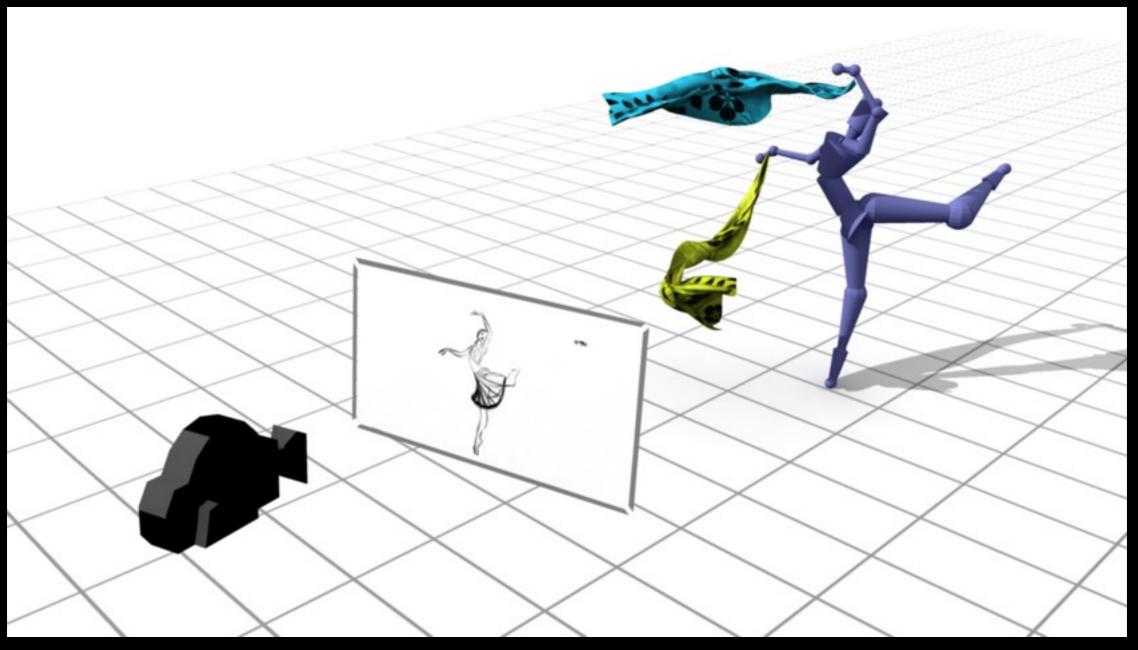


$$\operatorname*{arg\,min}(e_a(x) + e_m(x) + e_s(x)) \\ x \qquad \text{input-matching depth prior smoothing term}$$
 Linear system: least squares solution



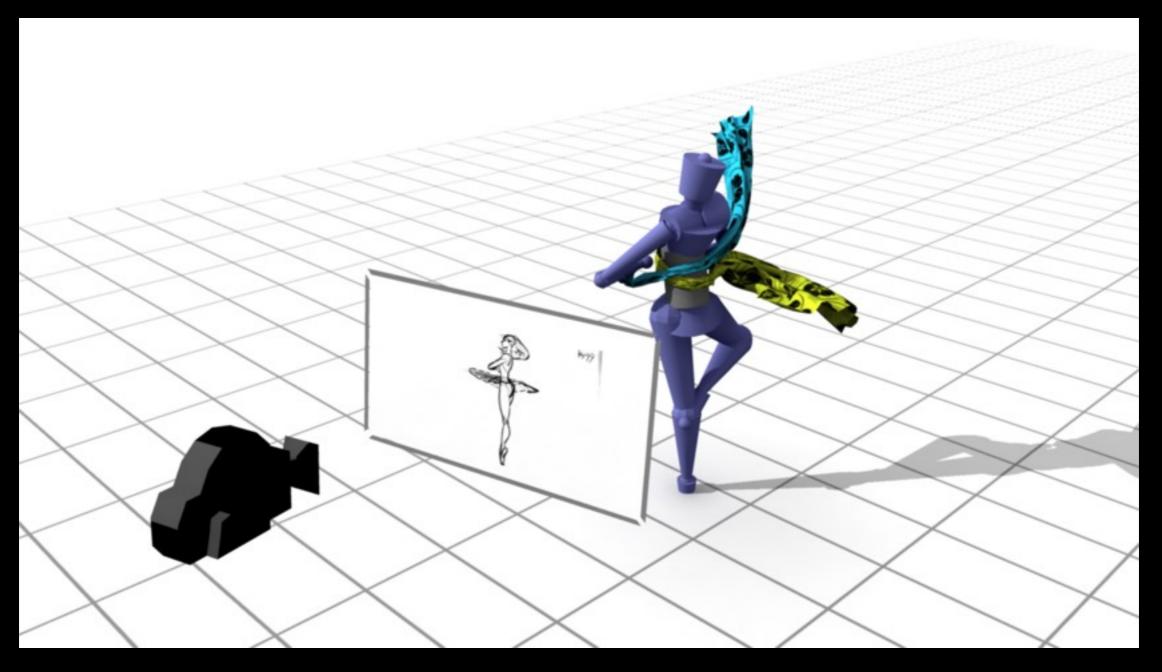
$$\underset{x \text{ input-matching depth prior smoothing term}}{\operatorname{arg\,min}(e_a(x) + e_m(x) + e_s(x))}$$

Linear system: least squares solution



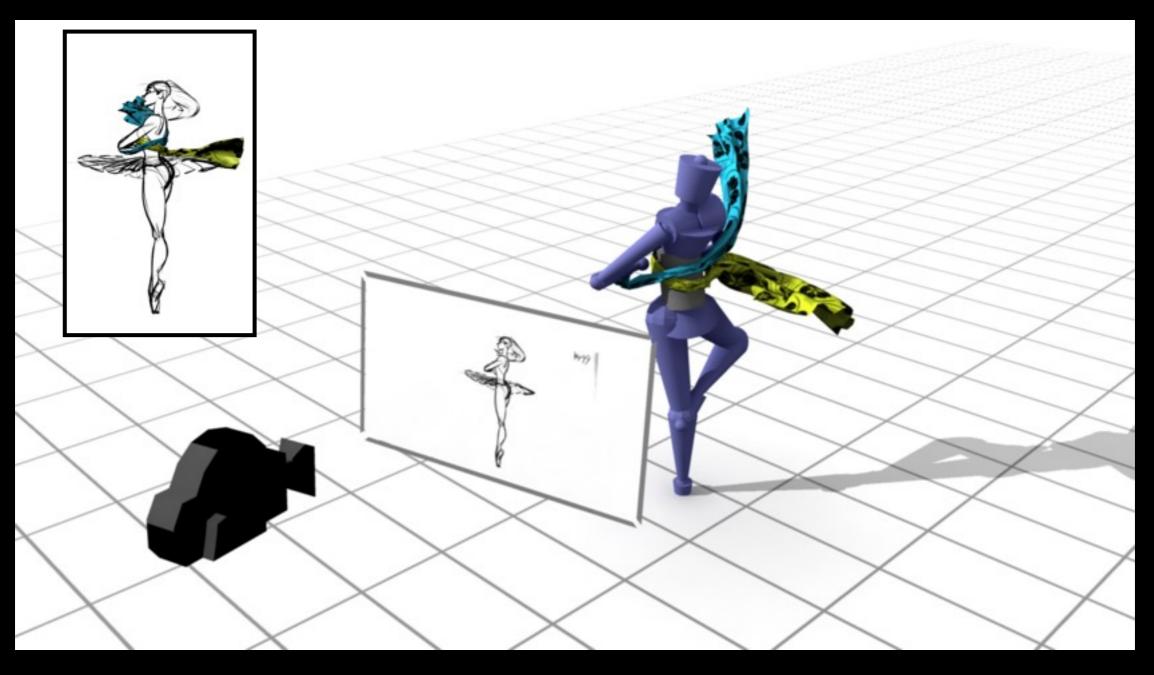
$$\underset{x}{\operatorname{arg\,min}}(e_a(x) + e_m(x) + e_s(x))$$

Linear system: least squares solution



$$\underset{x \text{ input-matching depth prior smoothing term}}{\operatorname{arg\,min}(e_a(x) + e_m(x) + e_s(x))}$$

Linear system: least squares solution





Rendered image



Rendered image



Depth map for rendered image



Rendered image



Depth map for rendered image



Depth map for hand drawing



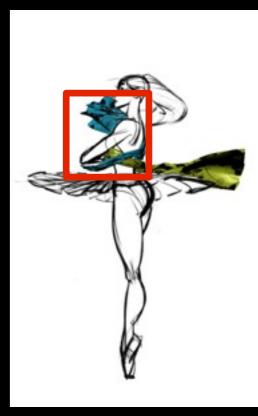
Rendered image



Depth map for rendered image



Depth map for hand drawing



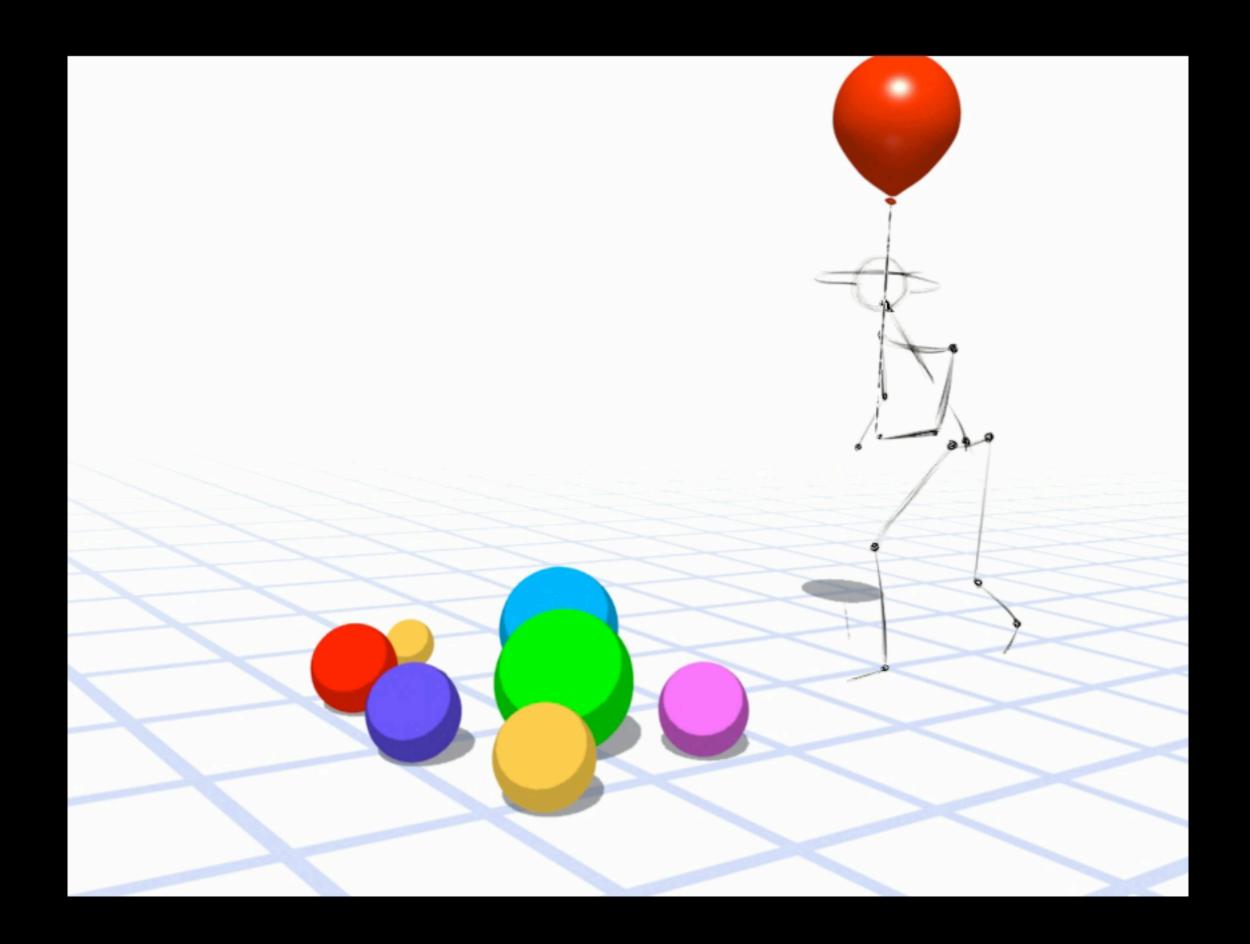
Composited frame

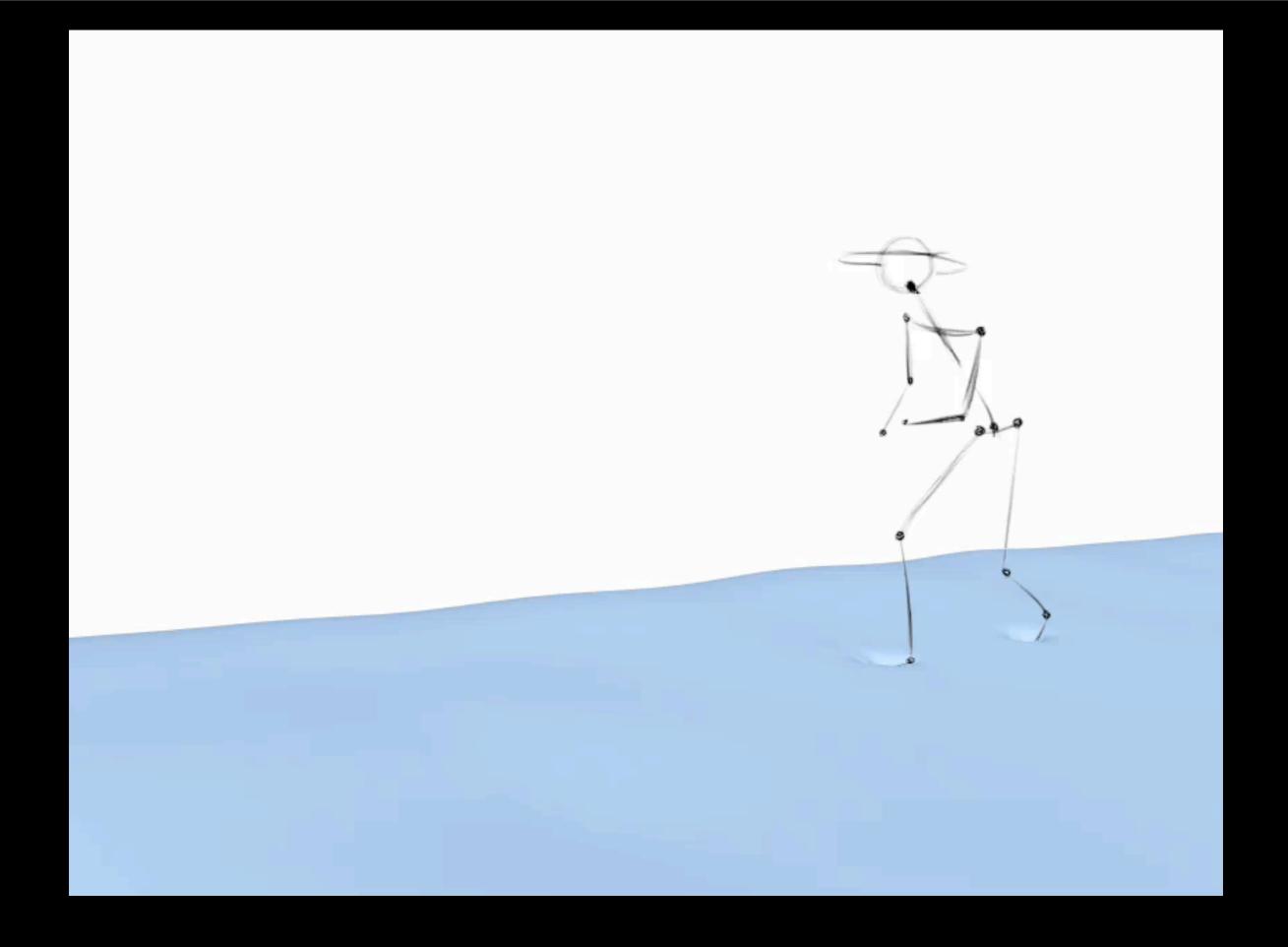


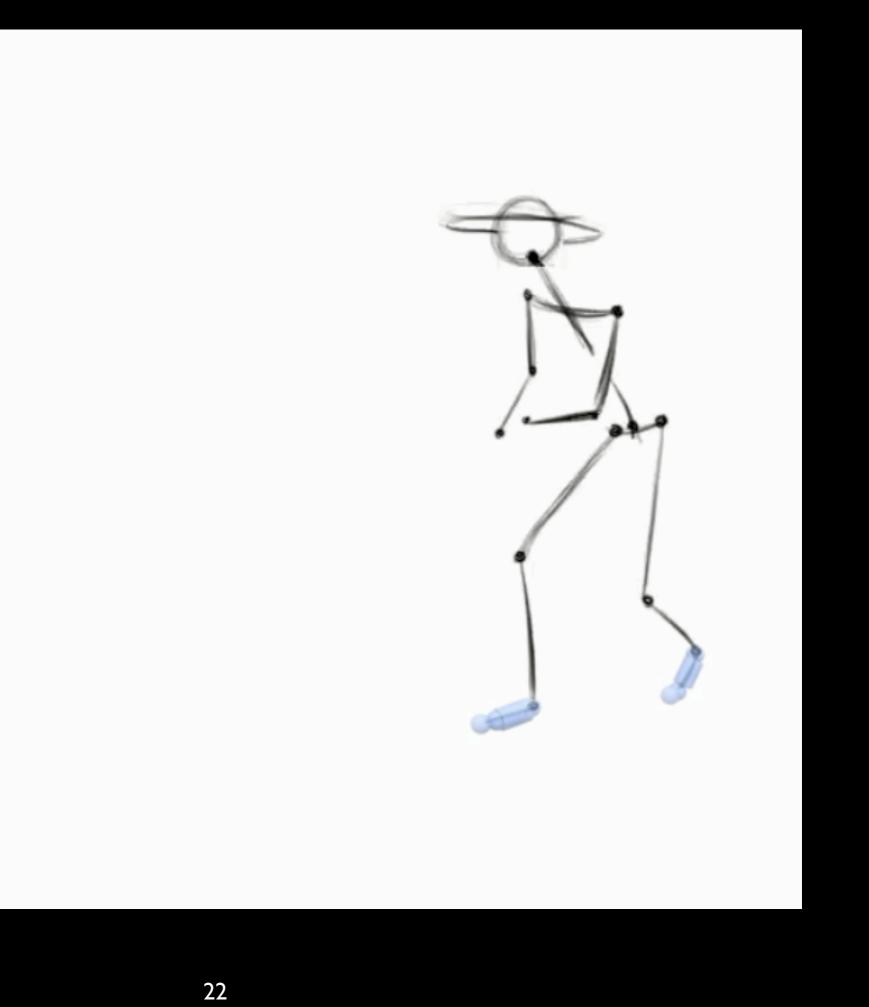








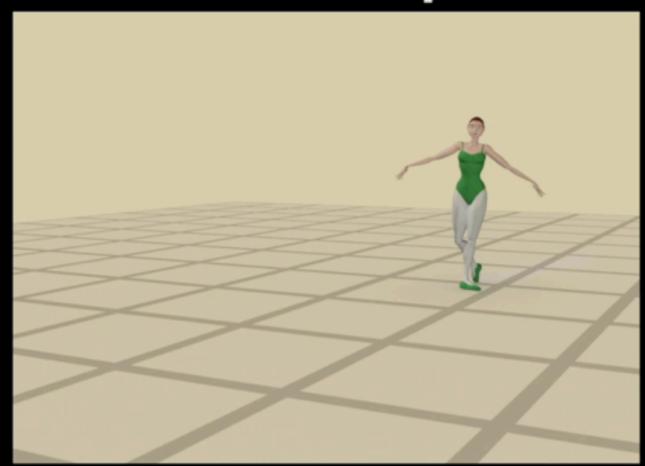


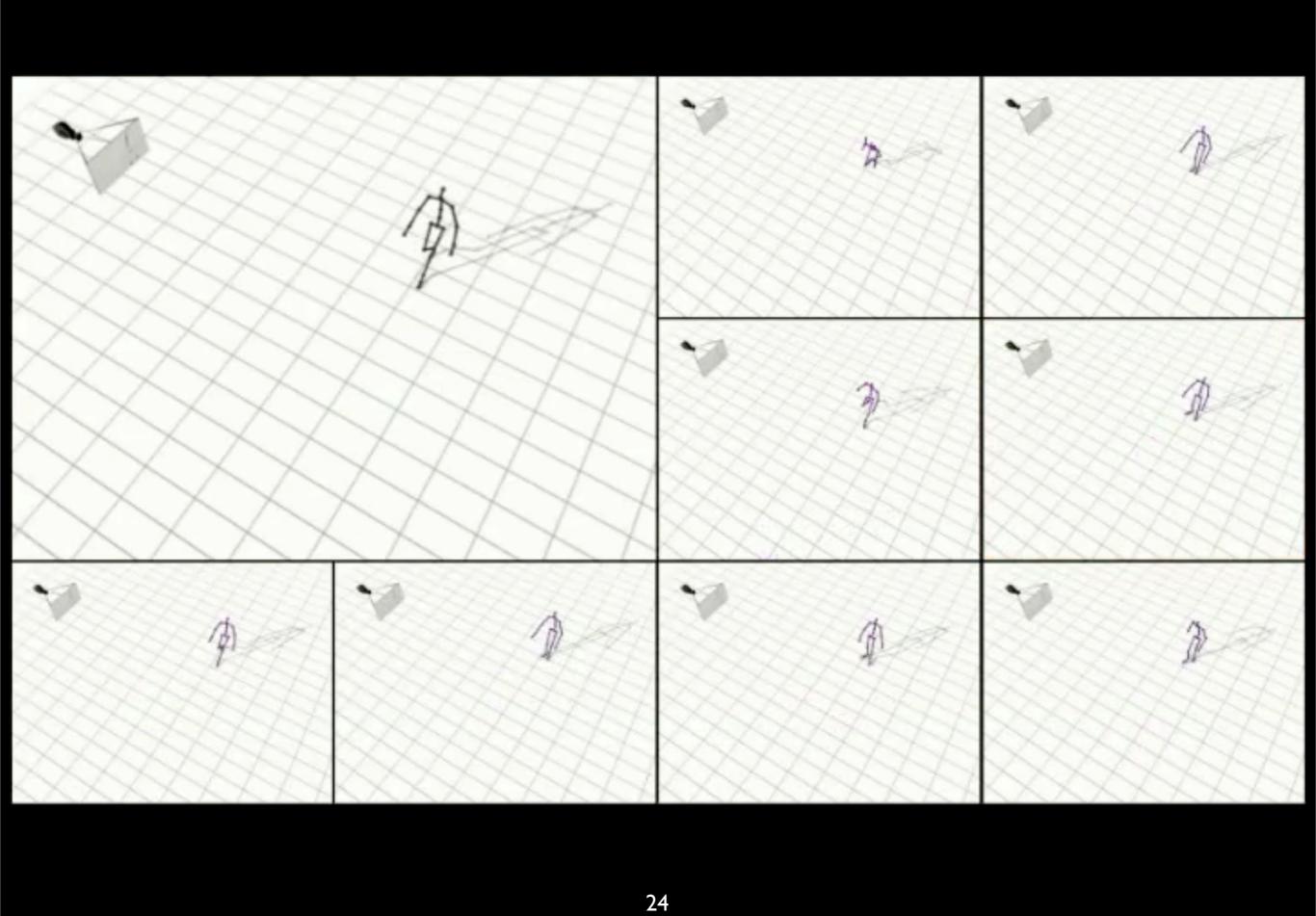


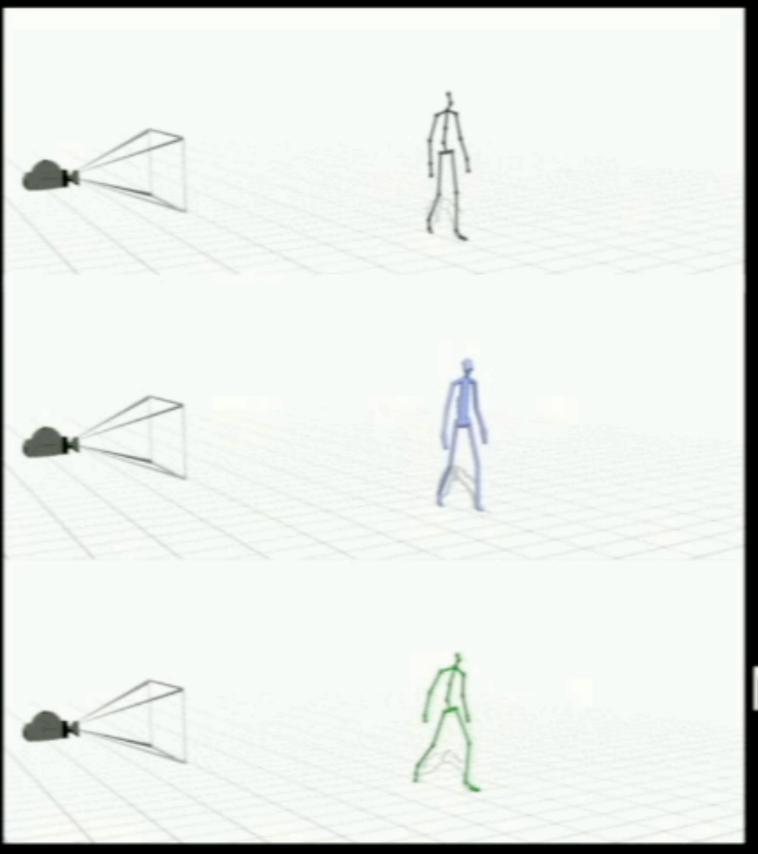
# Hand-drawn



# Motion capture







Ground truth

Output

Motion capture: happy walk

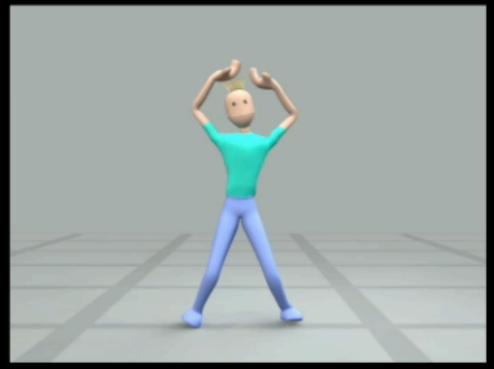
3D Polygonal shapes



3D Polygonal shapes



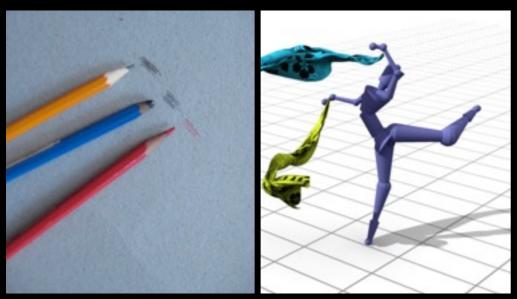
3D Polygonal shapes



3D Joint hierarchy skeleton



3D Polygonal shapes



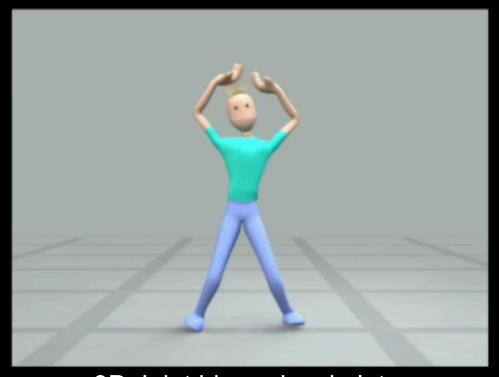
Hand animator modifies physical simulation?



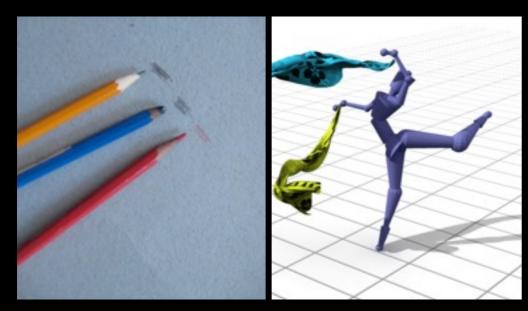
3D Joint hierarchy skeleton



3D Polygonal shapes



3D Joint hierarchy skeleton



Hand animator modifies physical simulation?







Learn cartoon physics?

# Extra Slides

#### Camera Estimation

Camera rotation and translation

$$\rho(i) = (\theta_x(i), \theta_y(i), \theta_z(i), t_x(i), t_y(i), t_z(i))^T$$

$$\rho^*(i) = \underset{\rho}{\operatorname{arg\,min}}(w_1 e_g + w_2 e_l + w_3 e_o + w_4 e_s)$$

#### Camera Estimation

Camera rotation and translation

$$\rho(i) = (\theta_x(i), \theta_y(i), \theta_z(i), t_x(i), t_y(i), t_z(i))^T$$

$$\rho^*(i) = \underset{\rho}{\operatorname{arg\,min}}(w_1 e_g + w_2 e_l + w_3 e_o + w_4 e_s)$$

Geometric projection error

$$e_g = \sum_{t=-K/2}^{K/2} || ilde{\mathbf{x}}_{i+t} - \mathbf{x}_{i+t}^{proj} ||$$

where 
$$\mathbf{x}_{i+t}^{proj} \cong \mathbf{M}_i \tilde{\mathbf{X}}_{i+t}$$
Motion capture poses

$$\underset{x}{\operatorname{arg\,min}}(\lambda_a e_a(x) + \lambda_m e_m(x) + \lambda_s e_s(x))$$

$$egin{aligned} e_a &= || \mathbf{ ilde{x}}_{ij} - \mathbf{x}_{ij}^{proj} || | | | \\ \mathbf{x}_{ij}^{proj} &\cong \mathbf{M}_i \mathbf{X}_{ij}^w \\ \mathbf{ ilde{x}}_{ij} &\times \mathbf{M}_i \mathbf{X}_{ij}^w = 0 \end{aligned}$$
 $\mathbf{C}\mathbf{M}_i \begin{bmatrix} X_{ij}^w \\ Y_{ij}^w \\ Z_{ij}^w \\ 1 \end{bmatrix} = 0$ 
 $\mathbf{M} = \begin{bmatrix} \mathbf{m}_1^T \\ \mathbf{m}_2^T \\ \mathbf{m}_2^T \end{bmatrix}$ 

$$\underset{x}{\operatorname{arg\,min}}(\lambda_a e_a(x) + \lambda_m e_m(x) + \lambda_s e_s(x))$$

$$e_a = ||\tilde{\mathbf{x}}_{ij} - \mathbf{x}_{ij}^{proj}||$$

$$\mathbf{x}_{ij}^{proj} \cong \mathbf{M}_i \mathbf{X}_{ij}^w$$

$$\tilde{\mathbf{x}}_{ij} \times \mathbf{M}_i \mathbf{X}_{ij}^w = 0$$

$$egin{array}{c} egin{array}{c} X_{ij}^w \ Y_{ij}^w \ Z_{ij}^w \ 1 \end{array} = 0 \end{array}$$

$$\mathbf{M} = egin{bmatrix} \mathbf{m}_1^T \ \mathbf{m}_2^T \ \mathbf{m}_3^T \end{bmatrix}$$

$$e_a = ||\tilde{\mathbf{x}}_{ij} - \mathbf{x}_{ij}^{proj}||$$

$$e_m = ||\mathbf{m}_3^T \mathbf{X}_{ij}^w - \mathbf{m}_3^T \tilde{\mathbf{X}}_{ij}||$$

$$\mathbf{m}_3^T \mathbf{X}_{ij}^w = \mathbf{m}_3^T \tilde{\mathbf{X}}_{ij}$$

$$\mathop{\arg\min}_{x}(\lambda_a e_a(x) + \lambda_m e_m(x) + \lambda_s e_s(x))$$
 input-matching motion prior smoothing term

$$e_a = ||\tilde{\mathbf{x}}_{ij} - \mathbf{x}_{ij}^{proj}||$$

$$\mathbf{x}_{ij}^{proj} \cong \mathbf{M}_i \mathbf{X}_{ij}^w$$

$$\tilde{\mathbf{x}}_{ij} \times \mathbf{M}_i \mathbf{X}_{ij}^w = 0$$

$$\mathbf{CM}_i \left[ egin{array}{c} X_{ij}^w \ Y_{ij}^w \ Z_{ij}^w \ 1 \end{array} 
ight] = 0$$

$$\mathbf{M} = egin{bmatrix} \mathbf{m}_1^T \ \mathbf{m}_2^T \ \mathbf{m}_3^T \end{bmatrix}$$

$$e_a = ||\tilde{\mathbf{x}}_{ij} - \mathbf{x}_{ij}^{proj}||$$

$$e_m = ||\mathbf{m}_3^T \mathbf{X}_{ij}^w - \mathbf{m}_3^T \tilde{\mathbf{X}}_{ij}||$$

$$\mathbf{m}_3^T \mathbf{X}_{ij}^w = \mathbf{m}_3^T \tilde{\mathbf{X}}_{ij}$$

$$e_s = ||\mathbf{X}_{ij}^w - \mathbf{X}_{(i+1)j}^w||$$

$$\mathop{\arg\min}_{x}(\lambda_a e_a(x) + \lambda_m e_m(x) + \lambda_s e_s(x))$$
 input-matching motion prior smoothing term

$$e_a = ||\tilde{\mathbf{x}}_{ij} - \mathbf{x}_{ij}^{proj}||$$

$$\mathbf{x}_{ij}^{proj} \cong \mathbf{M}_i \mathbf{X}_{ij}^w$$

$$\tilde{\mathbf{x}}_{ij} \times \mathbf{M}_i \mathbf{X}_{ij}^w = 0$$

$$\mathbf{CM}_i \left[ egin{array}{c} X_{ij}^w \ Y_{ij}^w \ Z_{ij}^w \ 1 \end{array} 
ight] = 0$$

$$\mathbf{M} = egin{bmatrix} \mathbf{m}_1^T \ \mathbf{m}_2^T \ \mathbf{m}_3^T \end{bmatrix}$$

$$e_a = ||\tilde{\mathbf{x}}_{ij} - \mathbf{x}_{ij}^{proj}||$$

$$e_m = ||\mathbf{m}_3^T \mathbf{X}_{ij}^w - \mathbf{m}_3^T \tilde{\mathbf{X}}_{ij}||$$

$$\mathbf{m}_3^T \mathbf{X}_{ij}^w = \mathbf{m}_3^T \tilde{\mathbf{X}}_{ij}$$

$$e_s = ||\mathbf{X}_{ij}^w - \mathbf{X}_{(i+1)j}^w||$$

$$\left[egin{array}{cccc} \mathbf{I} & -\mathbf{I} \end{array}
ight] \left[egin{array}{c} \mathbf{X}_{ij}^w \ \mathbf{X}_{(i+1)j}^w \end{array}
ight] = \left[egin{array}{c} \mathbf{0} \end{array}
ight]$$

$$\mathbf{W}\mathbf{A}_i\mathbf{X}_i^w=\mathbf{b}_i$$

## Hand-drawn



# Time warped motion capture

