



Image-based Shaving

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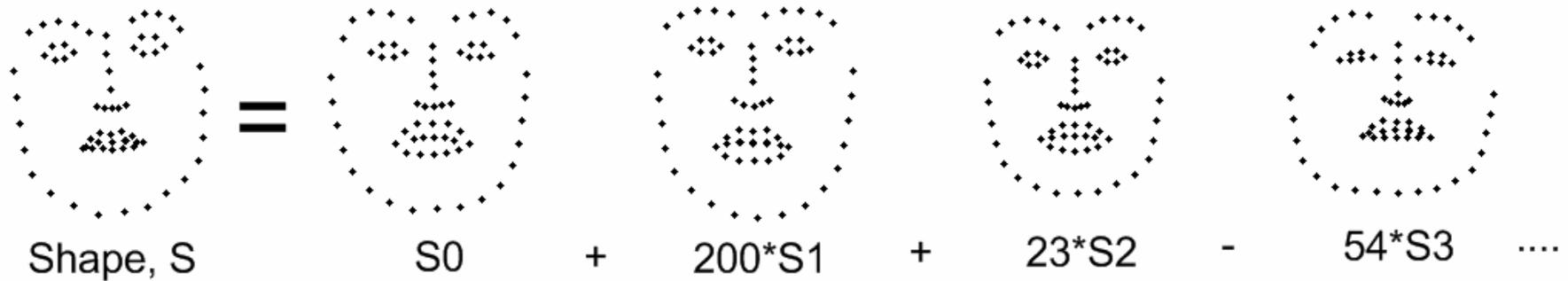
A goal



synthesize

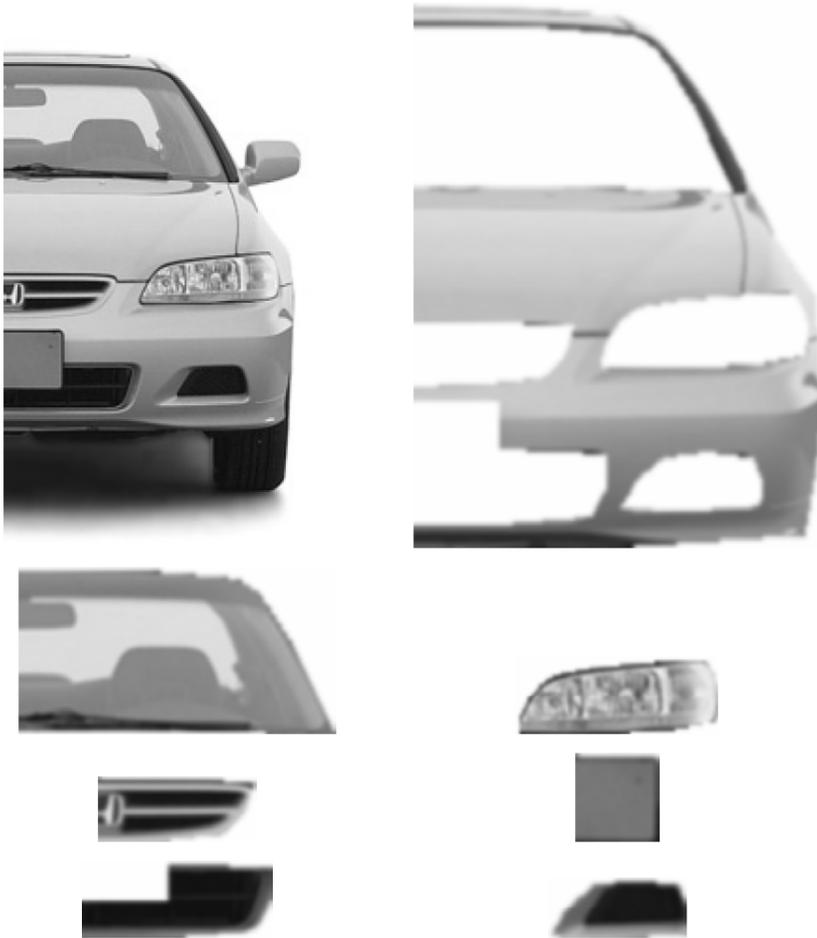


Active Appearance Models (Cootes et al ECCV98)



- Issues:
 - Global model
 - No support for modification of local structure.

Layered AAMs (Jones & Soatto ICCV05)



- Layers:
 - Defined manually
 - Require extensive set of hand labeled landmarks.
- This work:
 - Attempt to extract layers automatically.

The idea

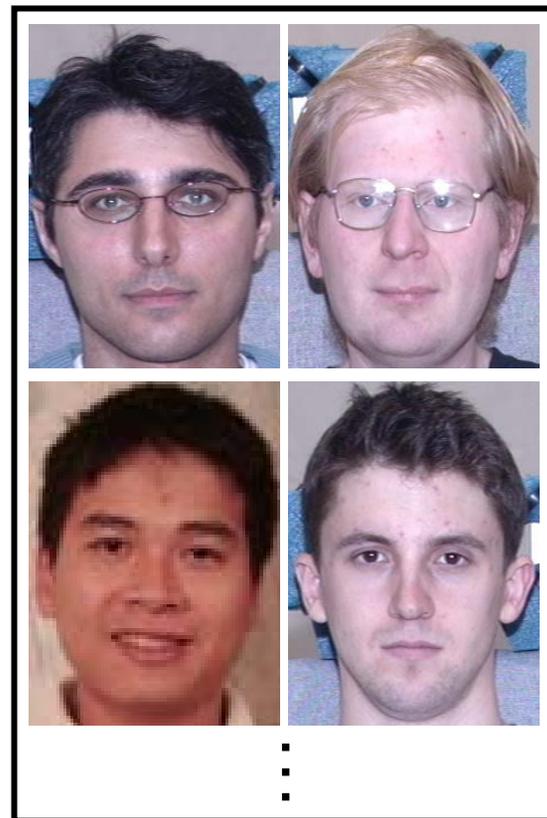


The idea



Differences
???

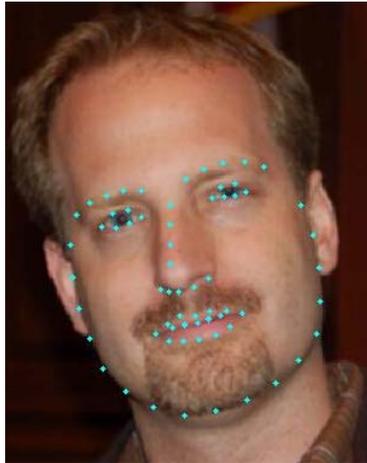
Beard Layer
Model



+



Processing steps



68 landmarks

a



b



c

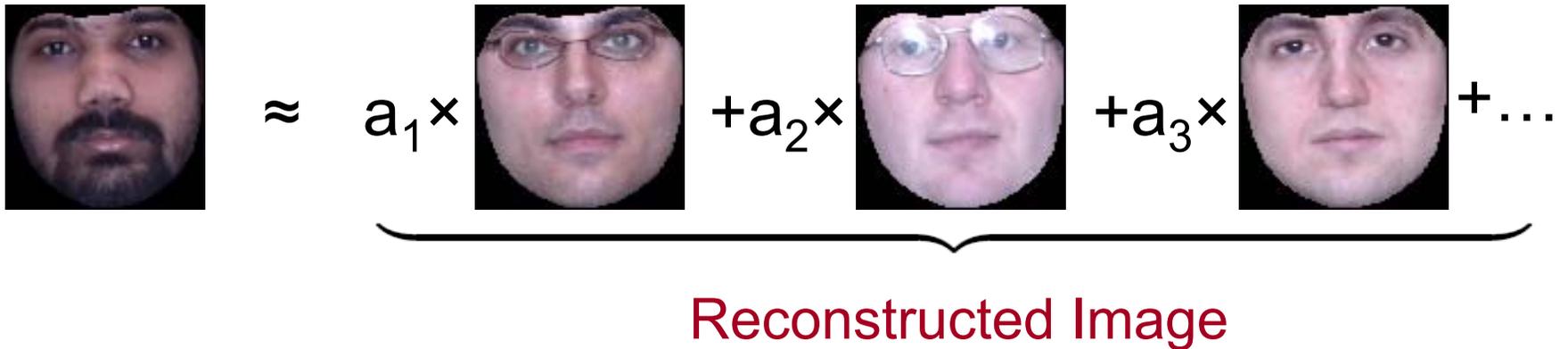


d



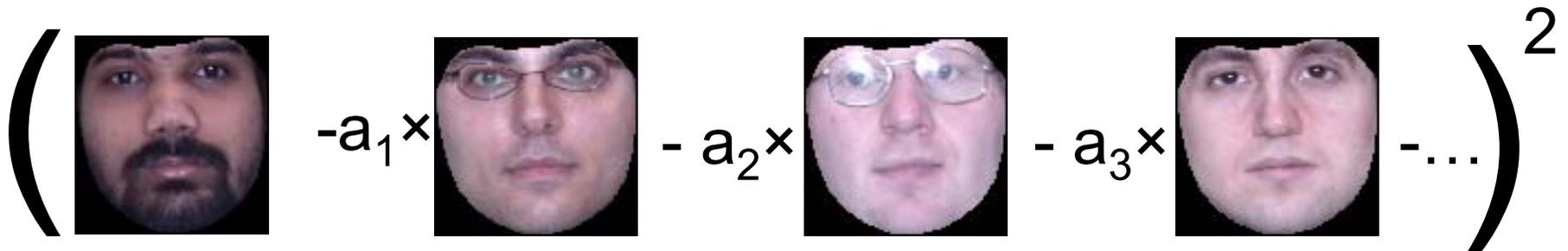
A naïve approach

- Reconstruct a bearded face by non-beard subspace


$$\approx a_1 \times \text{[Image 1]} + a_2 \times \text{[Image 2]} + a_3 \times \text{[Image 3]} + \dots$$

Reconstructed Image

- This is equivalent to minimizing:


$$\left(\text{[Target Image]} - a_1 \times \text{[Image 1]} - a_2 \times \text{[Image 2]} - a_3 \times \text{[Image 3]} - \dots \right)^2$$

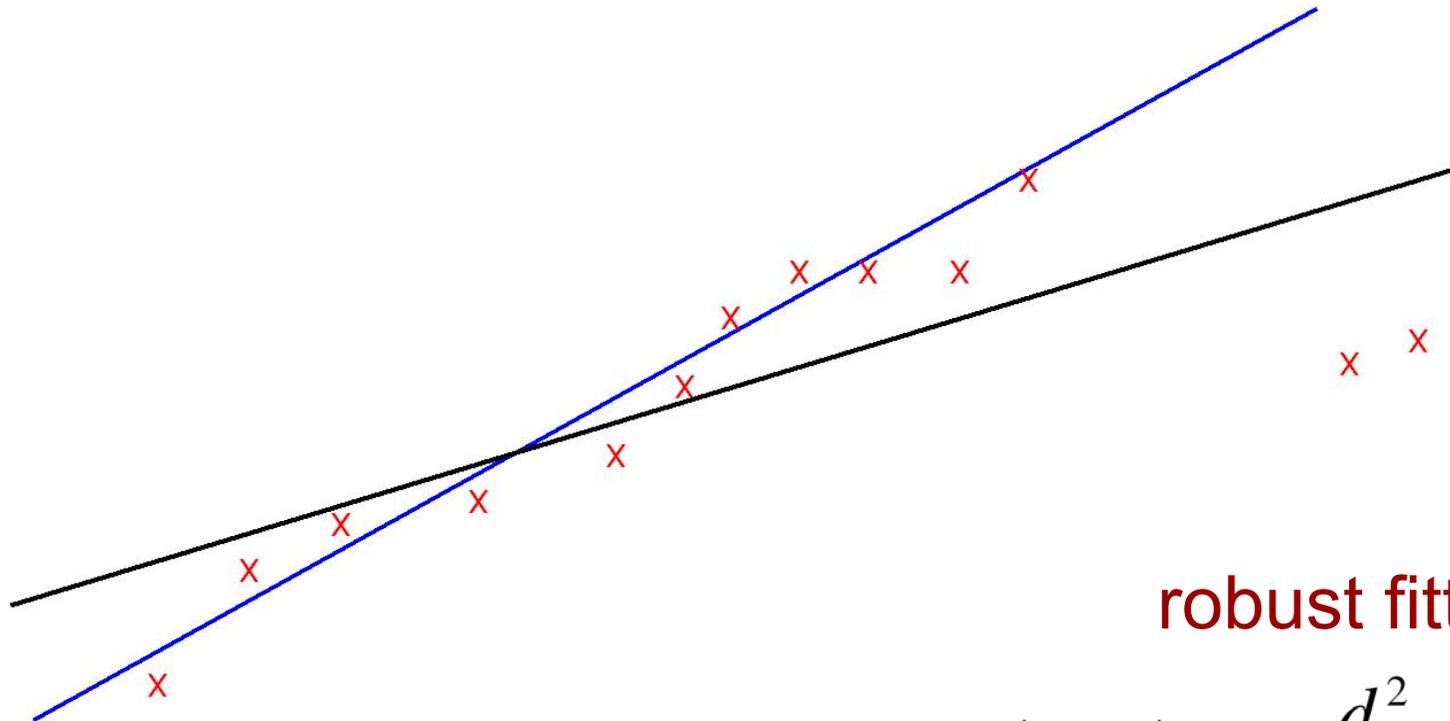
Naiïve reconstruction



Problem: reconstruct what we don't want to!

$$\left(\begin{array}{c} \text{Image 1} \\ -a_1 \times \text{Image 2} \\ -a_2 \times \text{Image 3} \\ -a_3 \times \text{Image 4} \\ \dots \end{array} \right)^2$$

Least square fitting



robust fitting

$$\rho(d, \sigma) = \frac{d^2}{\sigma^2 + d^2}$$

Iteratively Reweighted Least Square Fitting

Robust Fitting

$$\left(\text{Image}_1 - a_1 \times \text{Image}_2 - a_2 \times \text{Image}_3 - a_3 \times \text{Image}_4 - \dots \right)^2$$



$$\rho(d, \sigma) = \frac{d^2}{\sigma^2 + d^2}$$

$$\rho \left(\text{Image}_1 - a_1 \times \text{Image}_2 - a_2 \times \text{Image}_3 - a_3 \times \text{Image}_4 - \dots \right)$$

Robustly reconstructed image

Reconstruction Results



Original

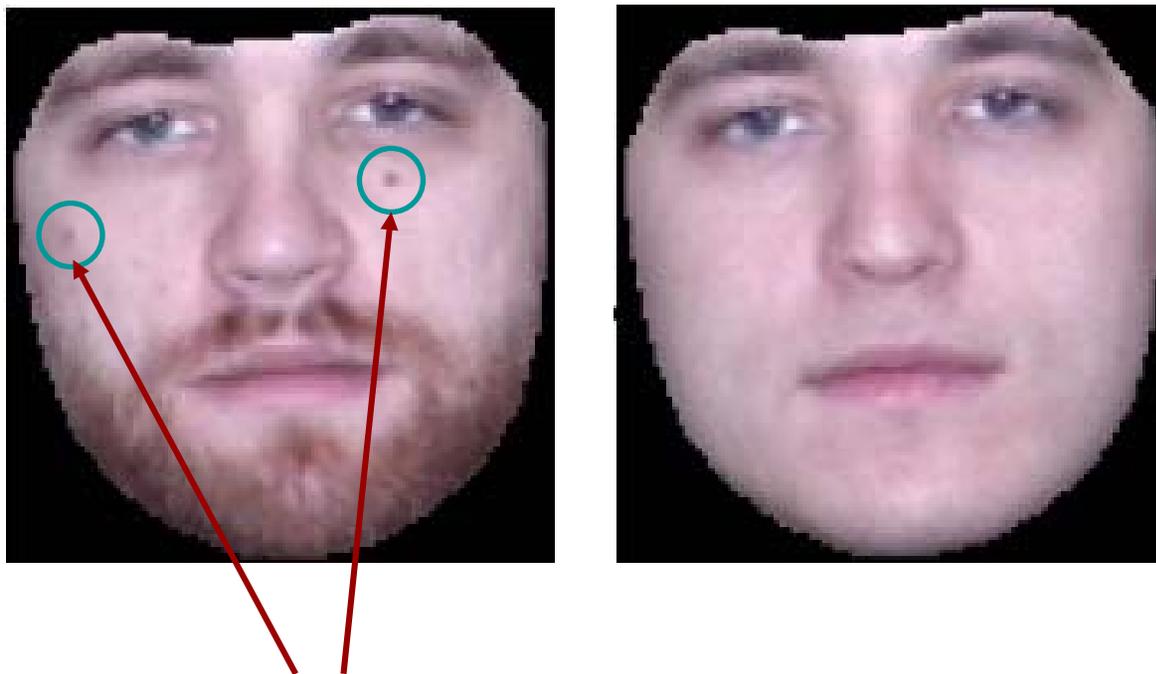


Naive
reconstruction



Robust
reconstruction

There is a problem



Characteristic moles are also removed

- Beards are outliers of non-beard subspace.
- But there are other outliers

The idea



Differences
???

Beard Layer
Model



+



Subspace for beard layer



$$\mathbf{U} = [\mathbf{u}_1 \dots \mathbf{u}_n] \in \mathbb{R}^{d \times n}$$

$$\mathbf{V} = [\mathbf{v}_1 \dots \mathbf{v}_m] \in \mathbb{R}^{d \times m}$$

$$\mathbf{u}_i \xrightarrow{\text{Robust Fitting}} \mathbf{u}_i^*$$

Perform PCA on the residuals:

$$\mathbf{u}_1 - \mathbf{u}_1^*, \dots, \mathbf{u}_n - \mathbf{u}_n^*$$

retaining 95% energy to get **B** subspace for beard layers

The first 6 principal components of **B**



super-imposed on the mean face

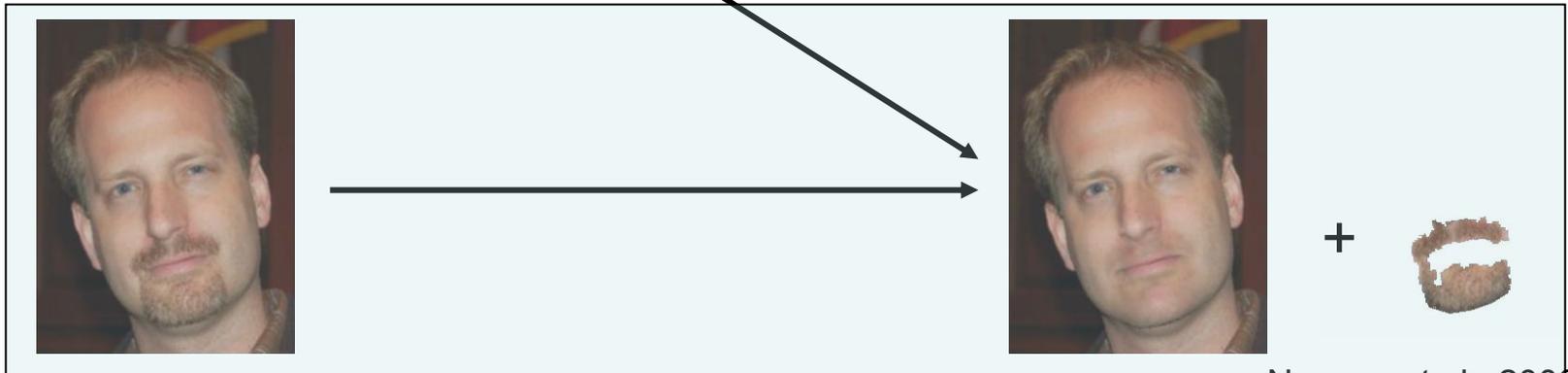
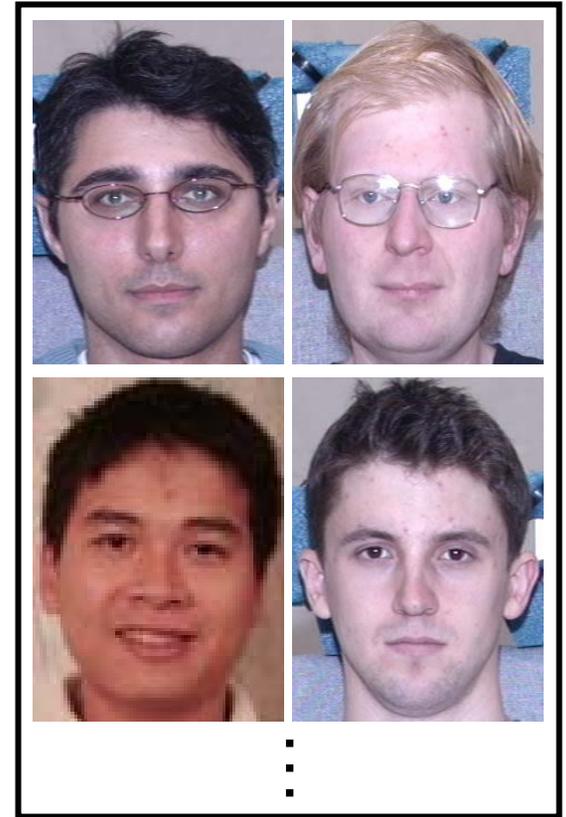
Where we are



Differences
???

B

Beard Layer
Model



Factorizing beard layer

Given a face: \mathbf{d}

$$\hat{\alpha}, \hat{\beta} = \arg \min_{\alpha, \beta} \|\mathbf{d} - \mathbf{V}\alpha - \mathbf{B}\beta\|_2^2$$

Non-beard subspace

Beard-layer subspace

$$\mathbf{d} = \mathbf{V}\hat{\alpha} + \mathbf{B}\hat{\beta} + \bar{\mathbf{d}}$$

Non-beard layer

Beard layer

Residual
(e.g. scar, mole)

Using the beard layer

$$\mathbf{d} = \mathbf{V}\hat{\boldsymbol{\alpha}} + \lambda \mathbf{B}\hat{\boldsymbol{\beta}} + \bar{\mathbf{d}}$$

Non-beard layer Beard layer Residual
(e.g. scar, mole)

$\lambda = 0$ Remove beard

$\lambda > 1$ Enhance beard

$0 < \lambda < 1$ Reduce beard

Changing contribution of the beard layer



Original

$$\lambda = 1$$



Beard
removed

$$\lambda = 0$$



Beard
reduced

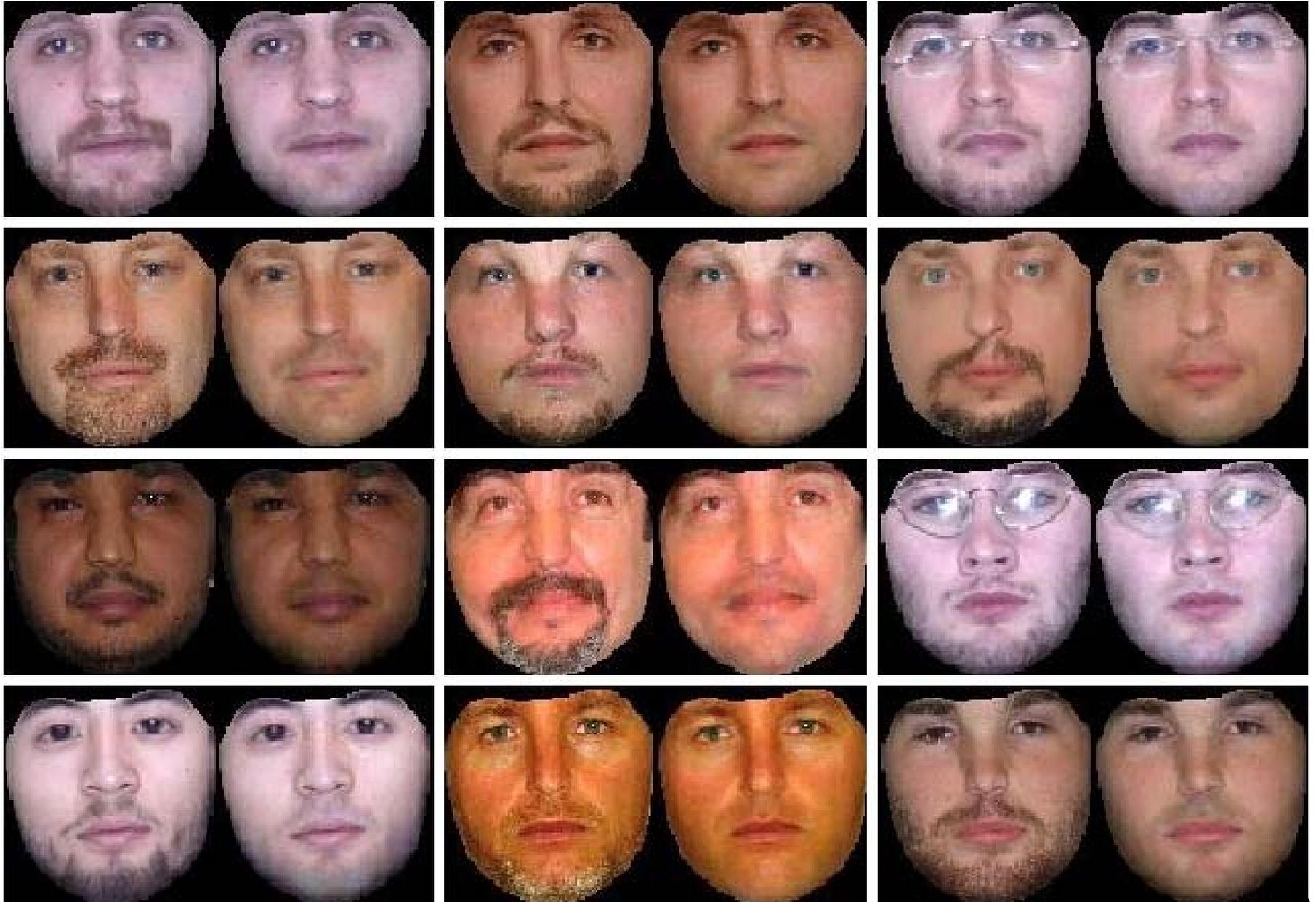
$$\lambda = 0.5$$



Beard
enhanced

$$\lambda = 1.5$$

Some results



More results



Failed cases



Too much beard!

Breakdown point of robust fitting is reached.

Utilizing domain knowledge

- So far:
 - Generic technique
- For beard removal:
 - Additional cues

A pixel is likely to be beard pixel if most of its neighbors are.

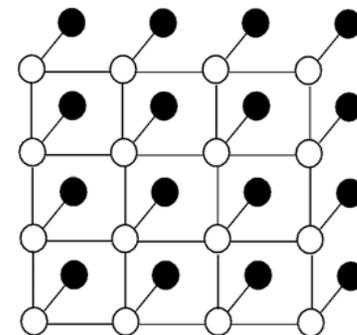
Beard Mask Segmentation

- Formulate as graph labeling problem:

$$\mathcal{G} = \langle \mathcal{V}, \mathcal{E} \rangle$$

One vertex
per pixel

Edges for
neighboring
pixels



Label the vertices $L = \{l_i | i \in \mathcal{V}\}$

that minimize:

$$E(L) = \sum_{i \in \mathcal{V}} E_i^1(l_i) + \sum_{(i,j) \in \mathcal{E}} E_{ij}^2(l_i, l_j)$$

unary
potential

binary
potential

Unary Potential

$$\mathbf{d} = \mathbf{V}\hat{\alpha} + \mathbf{B}\hat{\beta} + \bar{\mathbf{d}}$$

Non-beard
layer

Beard layer

Residual
(e.g. scar, mole)

$$\mathbf{d}^B$$

\mathbf{d}_i^B corresponds to i^{th} pixel

Beard pixel

Non-beard pixel

$$E_i^1(l_i) = \begin{cases} 0 & \text{if } l_i = 1 \\ |\mathbf{d}_i^B| - a & \text{if } l_i = 0 \text{ \& } ||\mathbf{d}_i^B| - a| \leq b \\ b & \text{if } l_i = 0 \text{ \& } |\mathbf{d}_i^B| - a > b \\ -b & \text{if } l_i = 0 \text{ \& } |\mathbf{d}_i^B| - a < -b \end{cases}$$

Unary potential: favors beard label if $|\mathbf{d}_i^B|$ is big.

Binary Potential

$$E_{ij}^2(l_i, l_j) = \begin{cases} 0 & \text{if } l_i = l_j \\ \frac{b}{2} & \text{if } l_i \neq l_j \end{cases}$$

Binary potential: prefers same labels for neighboring pixels

Optimization using graph-cuts

(Boykov *et al* PAMI01)

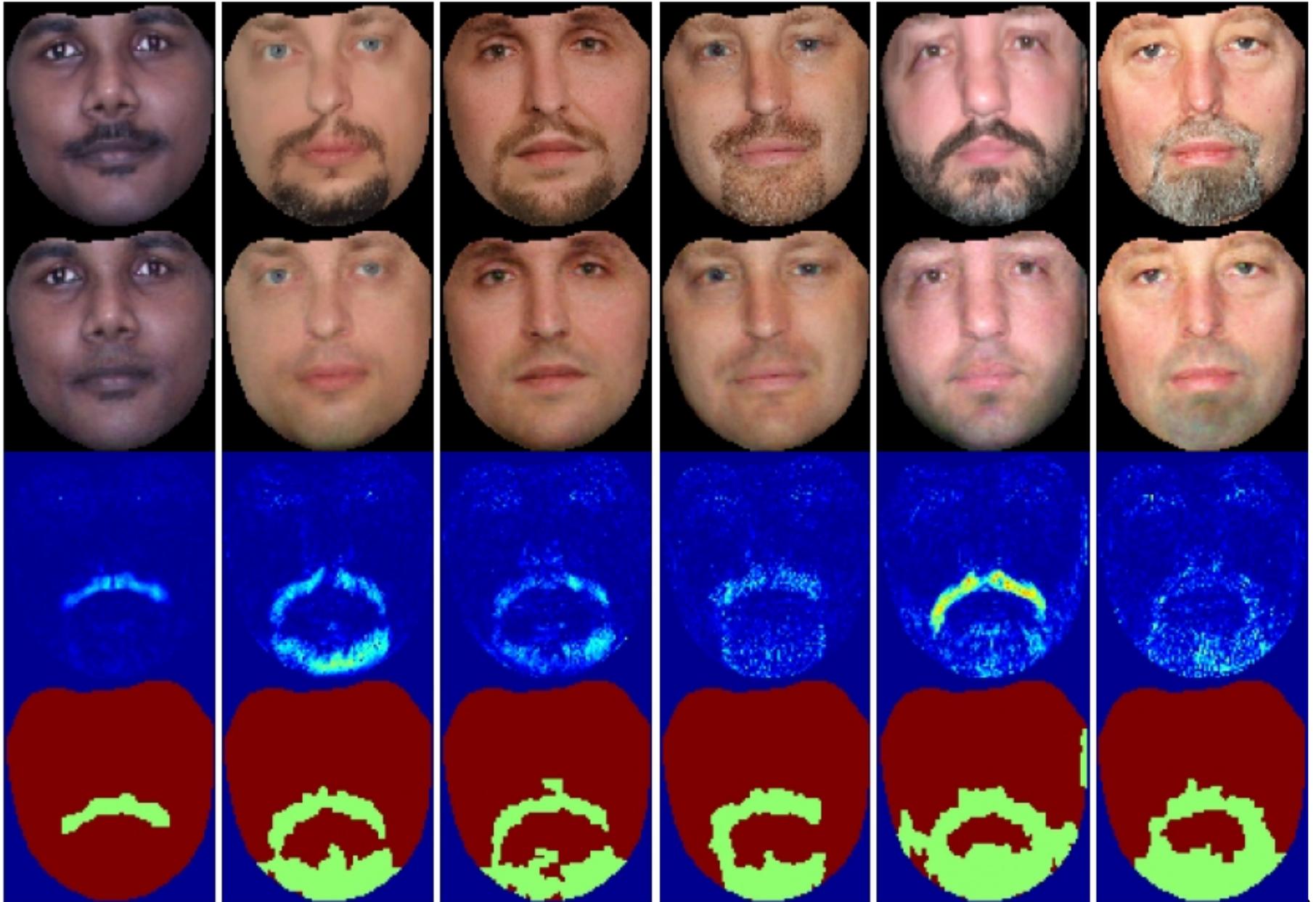
Label the vertices $L = \{l_i | i \in \mathcal{V}\}$

that minimize:

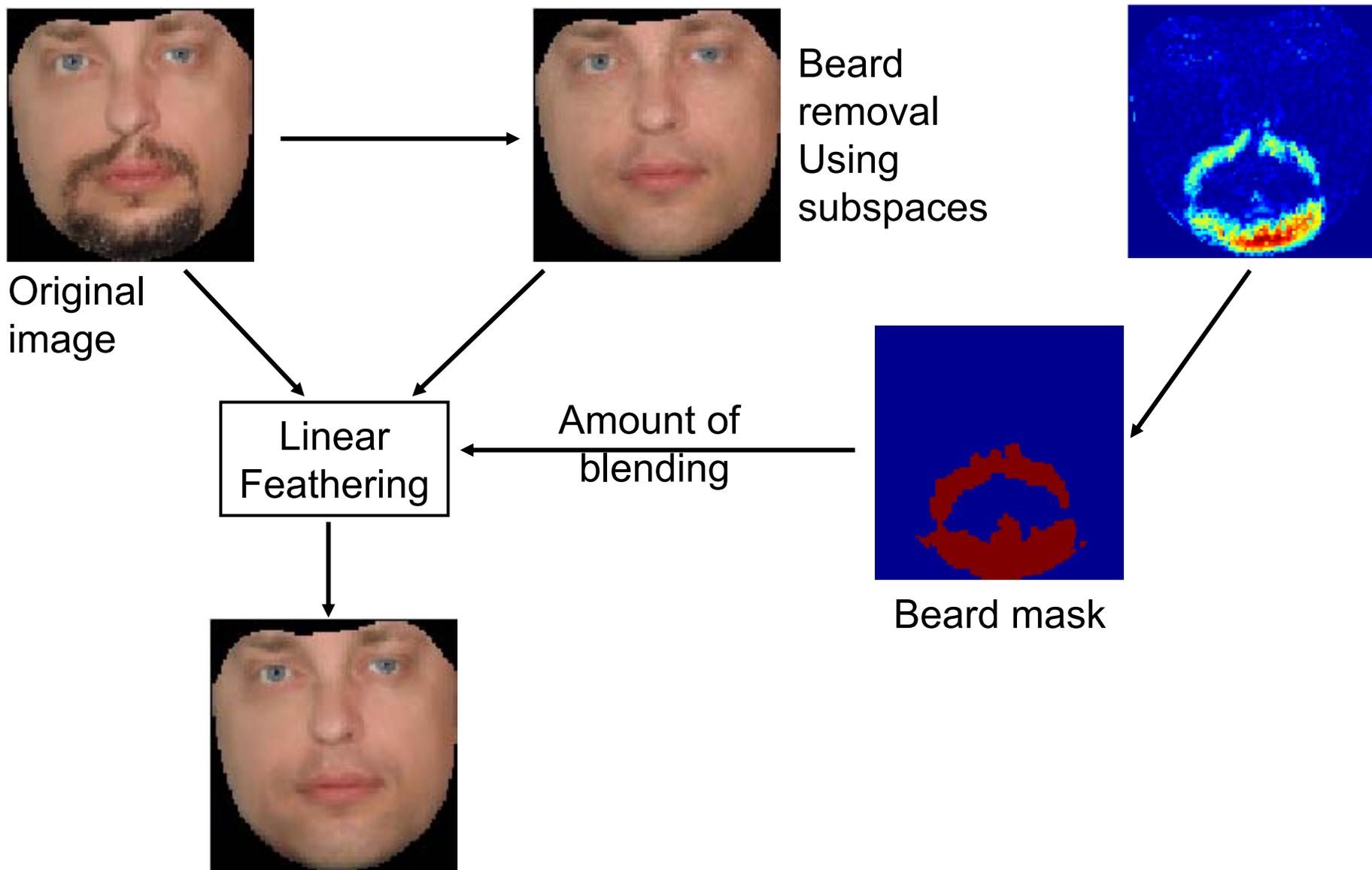
$$E(L) = \sum_{i \in \mathcal{V}} E_i^1(l_i) + \sum_{(i,j) \in \mathcal{E}} E_{ij}^2(l_i, l_j)$$

**Exact global optimum solution can
be found efficiently!**

Beard mask results



Refinement



Final results 1



Final results 2



Final results 3



Final results 4



Final results 5



Beard removal, failure



Failure occurs at the robust fitting step

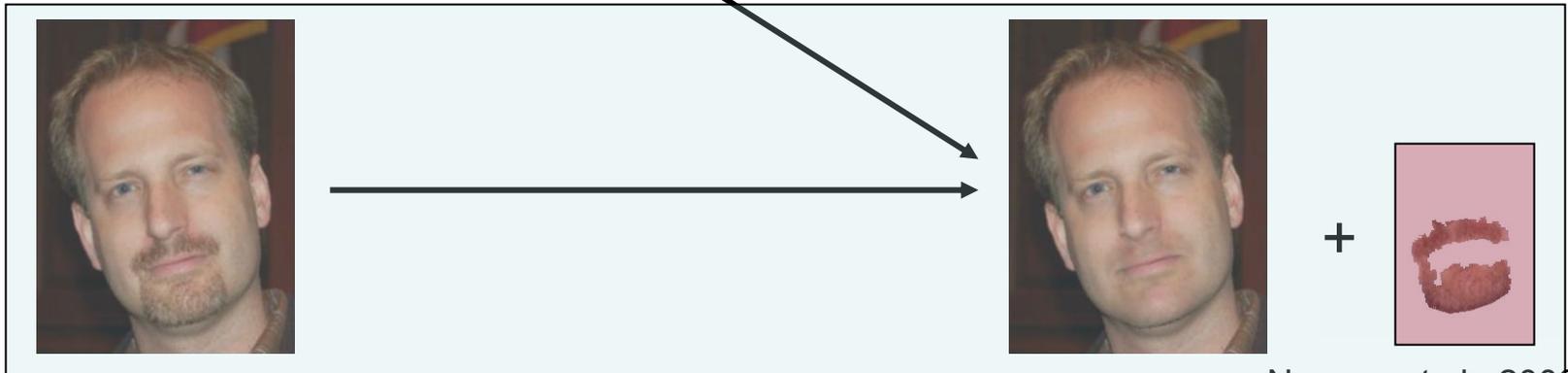
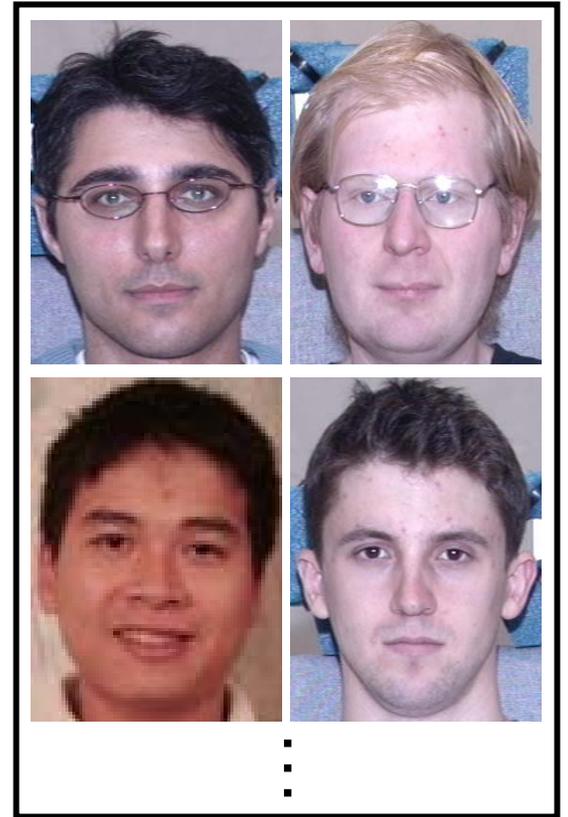
Where we are



Differences
???



Beard Layer
Model



Beard Transfer



So far, we talked about

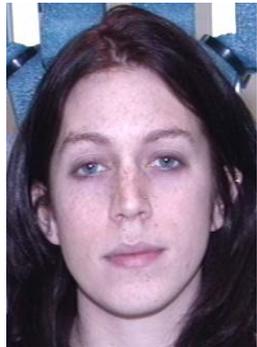
Beards

Beards

Lots of Beards

But our method is generic!

Glasses Removal



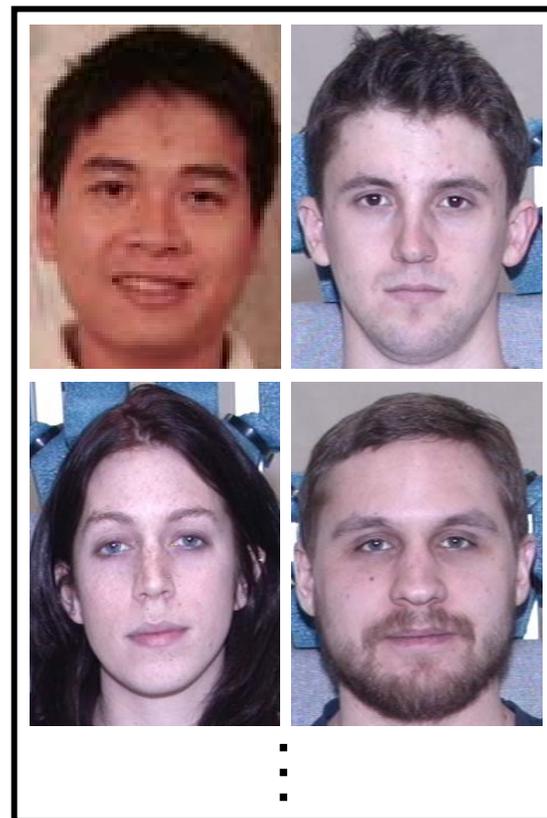
Glasses Removal



Differences
???



Glasses Layer
Model



Preliminary results for glasses



Preliminary results for glasses



Glasses removal, failure



Multi-PIE database

- 1140 frontal, neutral faces
 - 68 landmarks
 - From Multipie
- Female: 341
 - With glasses: 82
 - Without glasses: 259
- Male: 799
 - With little or no facial hair: 480
 - With some facial hair: 319
 - With glasses: 340
 - Without glasses: 459

91 additional
bearded faces
from the Internet.

References

- Nguyen, M.H., Lalonde, J.F., Efros, A.A. & De la Torre, F. '**Image-based Shaving.**' Eurographics 08.
- Cootes, T, Edwards, Taylor, G. '**Active Appearance Models**', ECCV98.
- Jones, E. & Soatto, S.(2005) '**Layered Active Appearance Models.**' ICCV05.
- Boykov, Y., Veksler, O. & Zabih, R. '**Fast Approximate Energy Minimization via Graph Cuts.**' PAMI01.
- Gross, R., Matthews, I., Cohn, J., Kanade, T. & Baker, S. '**The CMU Multi-pose, Illumination, and Expression (Multi-PIE) Face Database.**' CMU TR-07-08.