Ray tracing and simple shading

http://graphics.cs.cmu.edu/courses/15-468
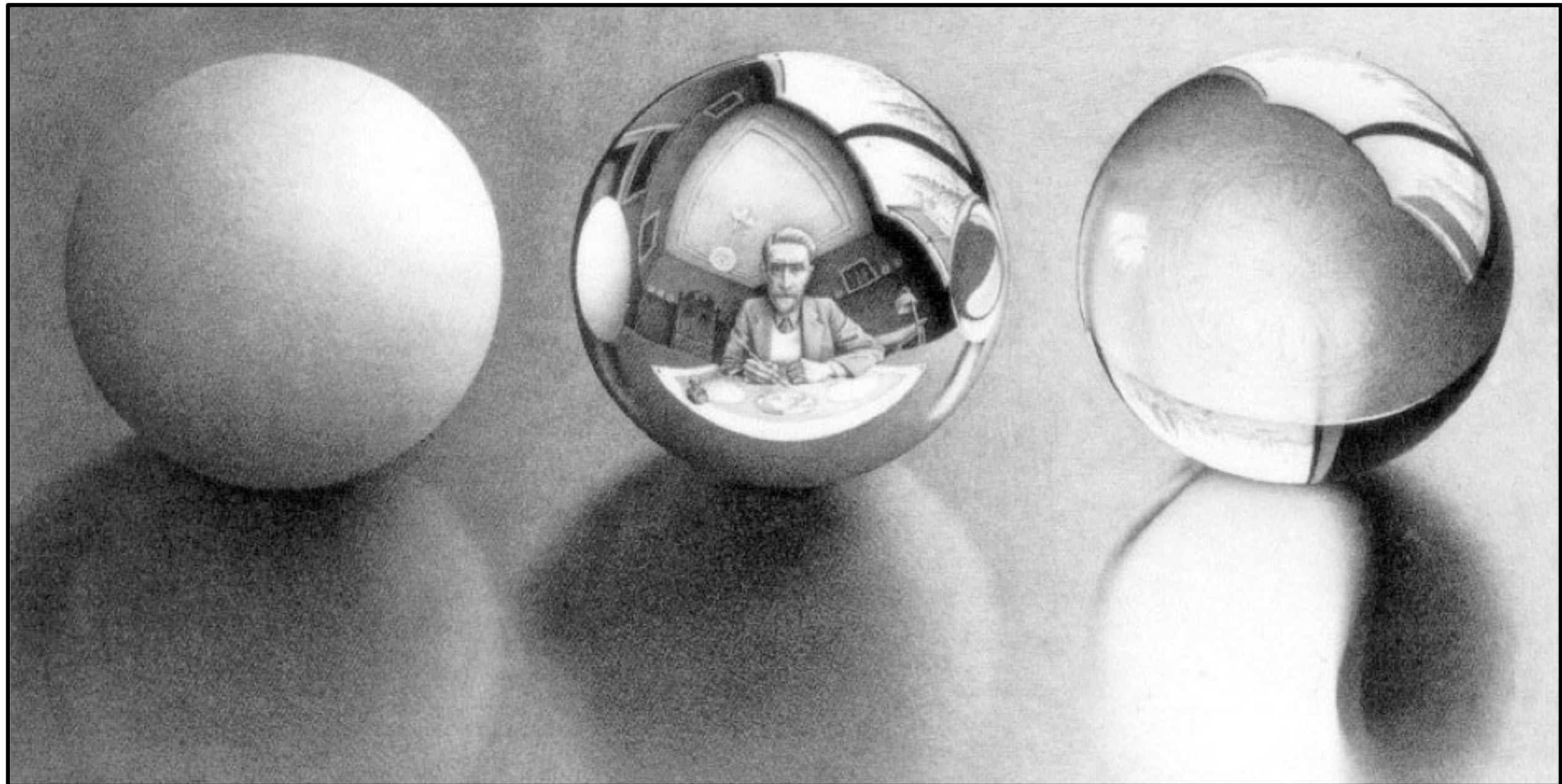
Course announcements

- Programming assignment 0 available on Canvas tonight.
  - Ungraded, no due date.
  - Used to set up rendering environment and github-based submission system.
  - Should take no more than 1-2 hours max.

- Programming assignment 1 will be posted on Friday 1/27, will be due two weeks later.

- Take-home quiz 1 available online, will be due Tuesday 1/31.

- All other logistics (office hours, recitations, reading groups) on course website.

- Office hours on Friday: Yannis, 2-4 pm.
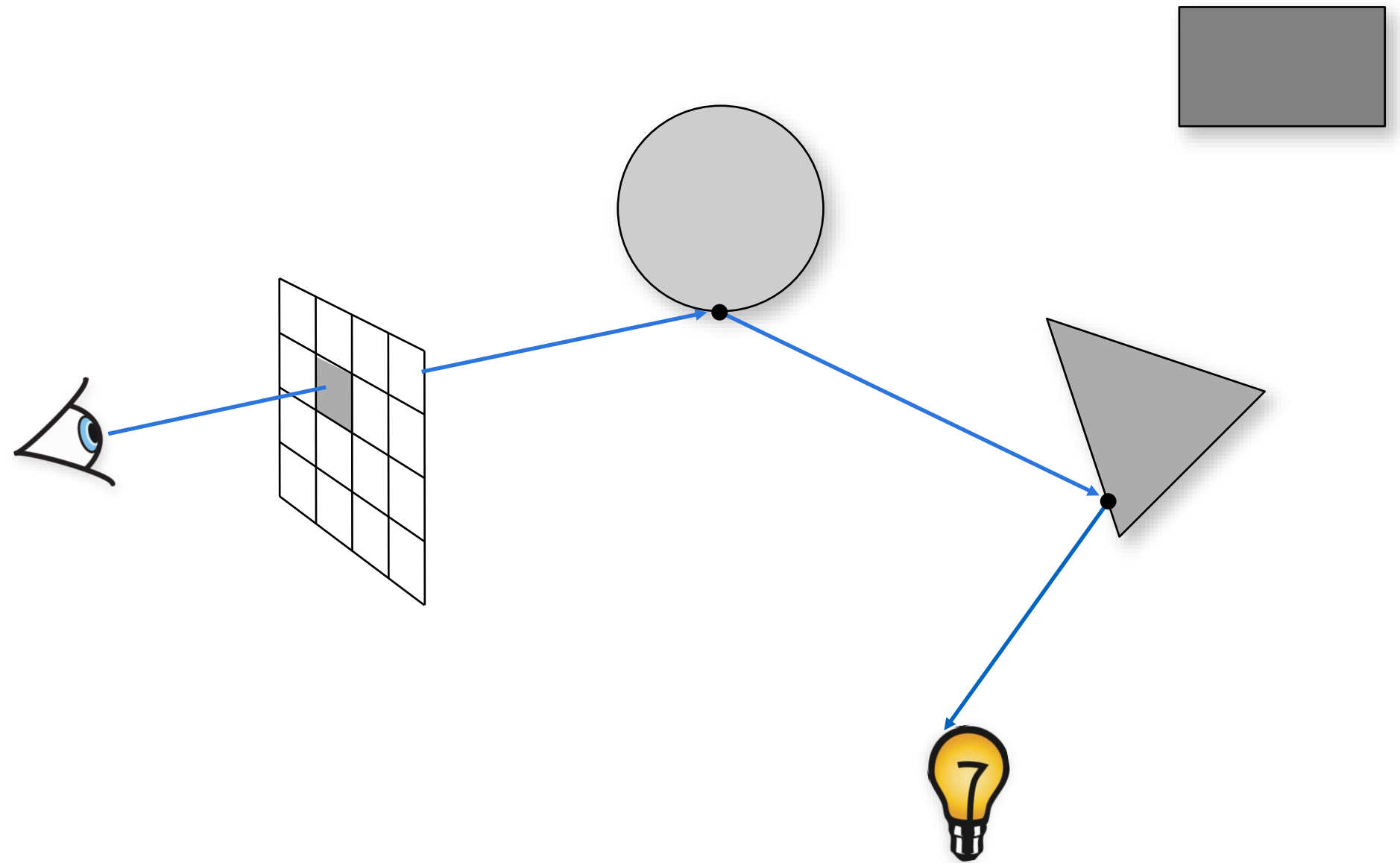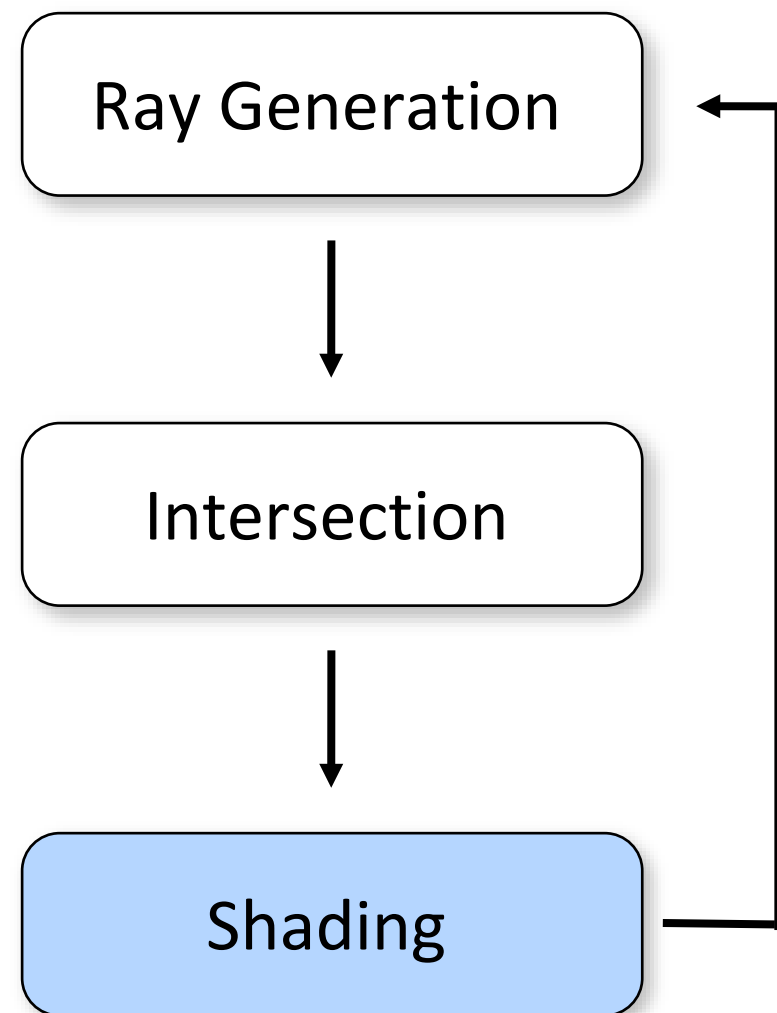
Overview of today's lecture

- Leftover from previous lecture: intersections, meshes, acceleration structures.

- Basics of shading.

- Basic reflection models.

Slide credits

Most of these slides were directly adapted from:

- Wojciech Jarosz (Dartmouth).

Recap: Raytracing

Ray Generation

Intersection

Shading

Shading

When ray hits a surface we perform *lighting/shading*

Determine "what color/light should we see at this location?"

Surfaces can scatter and/or emit light

- Surface emits light? just return emitted color (determined by the material)

- Surface scatters/reflects/refracts light? (recursively) trace a ray in a scattering direction (determined by the underlying material)
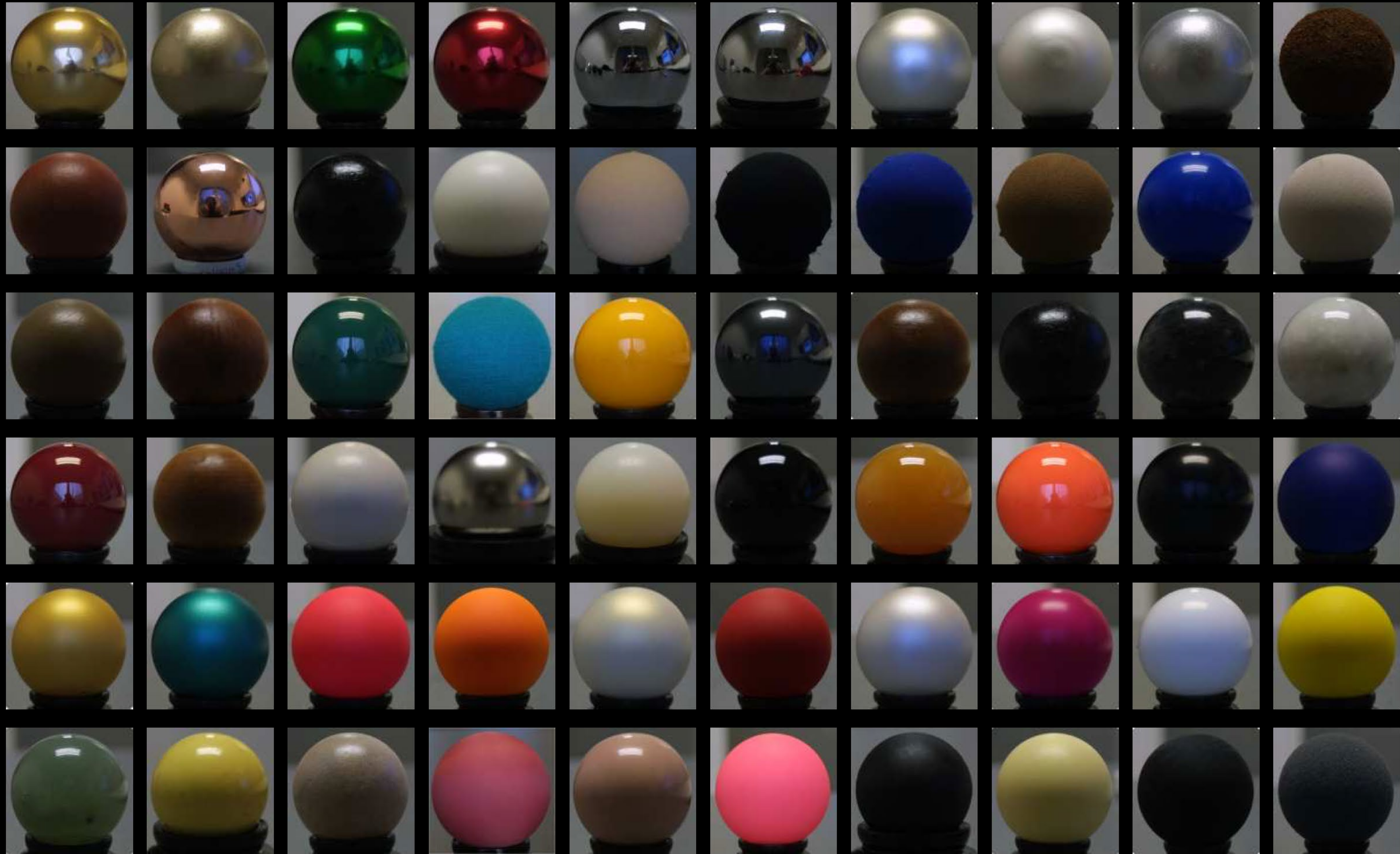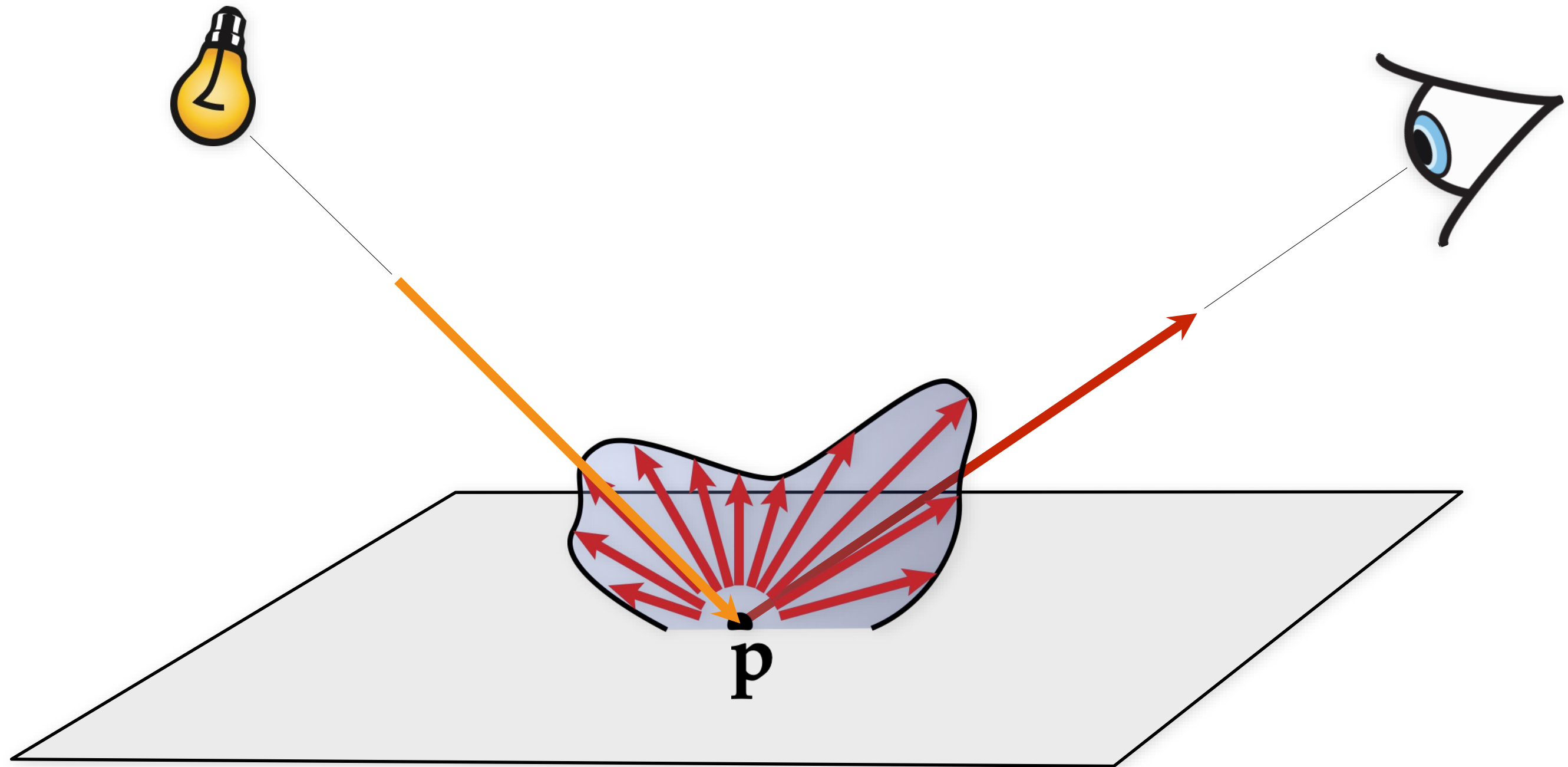
Overview

Diffuse shading
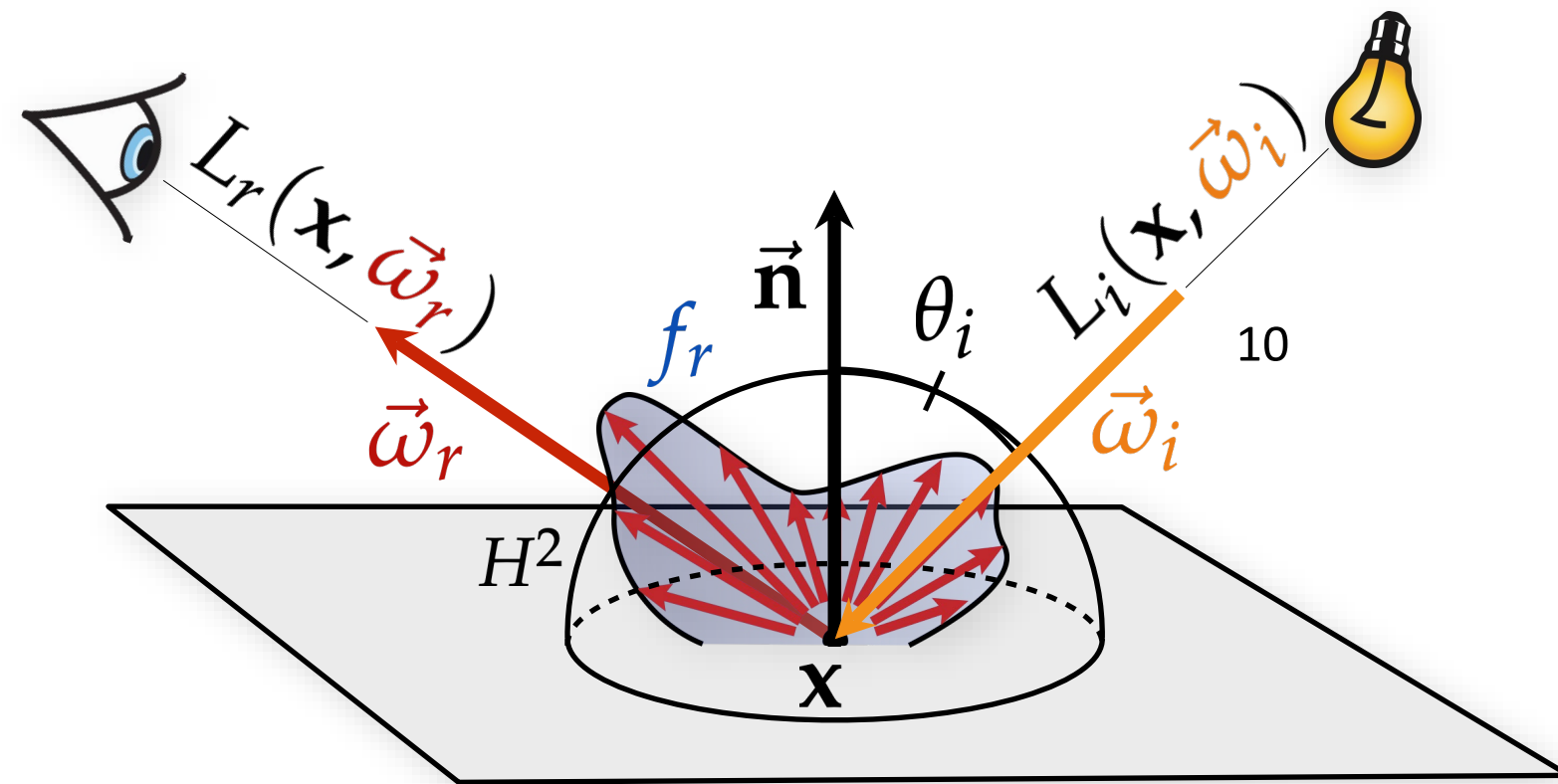
Specular reflection

Refraction

Diffuse emission

Light-material interactions

The reflection equation

Reflected radiance is a (hemi)spherical integral of incident radiance from all directions

$$L_r(\mathbf{x}, \vec{\omega}_r) = \int_{H^2} f_r(\mathbf{x}, \vec{\omega}_i, \vec{\omega}_r) L_i(\mathbf{x}, \vec{\omega}_i) \cos\theta_i \, d\vec{\omega}_i$$
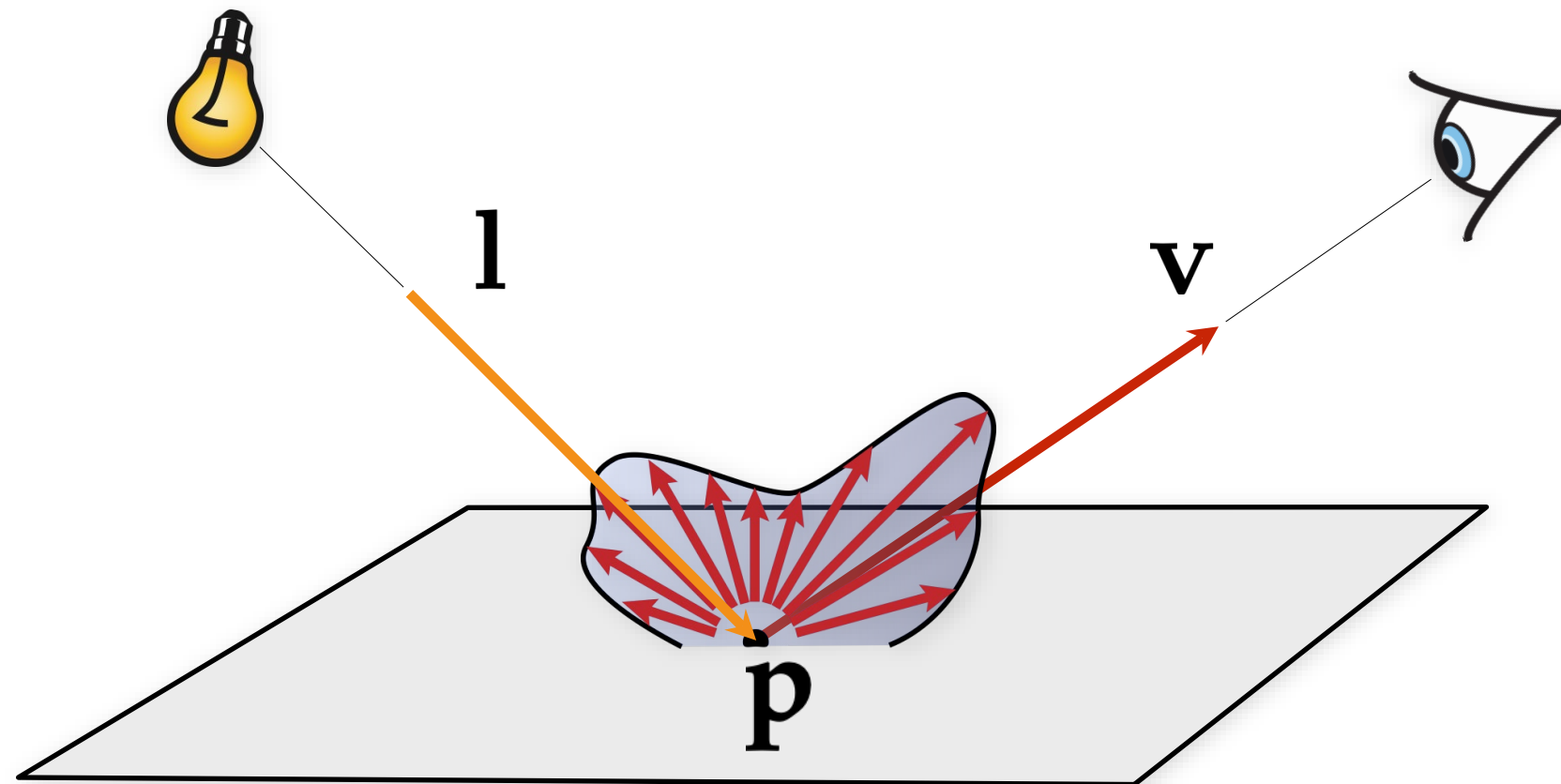

This describes a local illumination model

The BSDF

Bidirectional **S**cattering **D**istribution **F**unction

- informally: how much the material scatters light coming from one direction $\mathbf{l}$ into some other direction $\mathbf{v}$, at each point $\mathbf{p}$
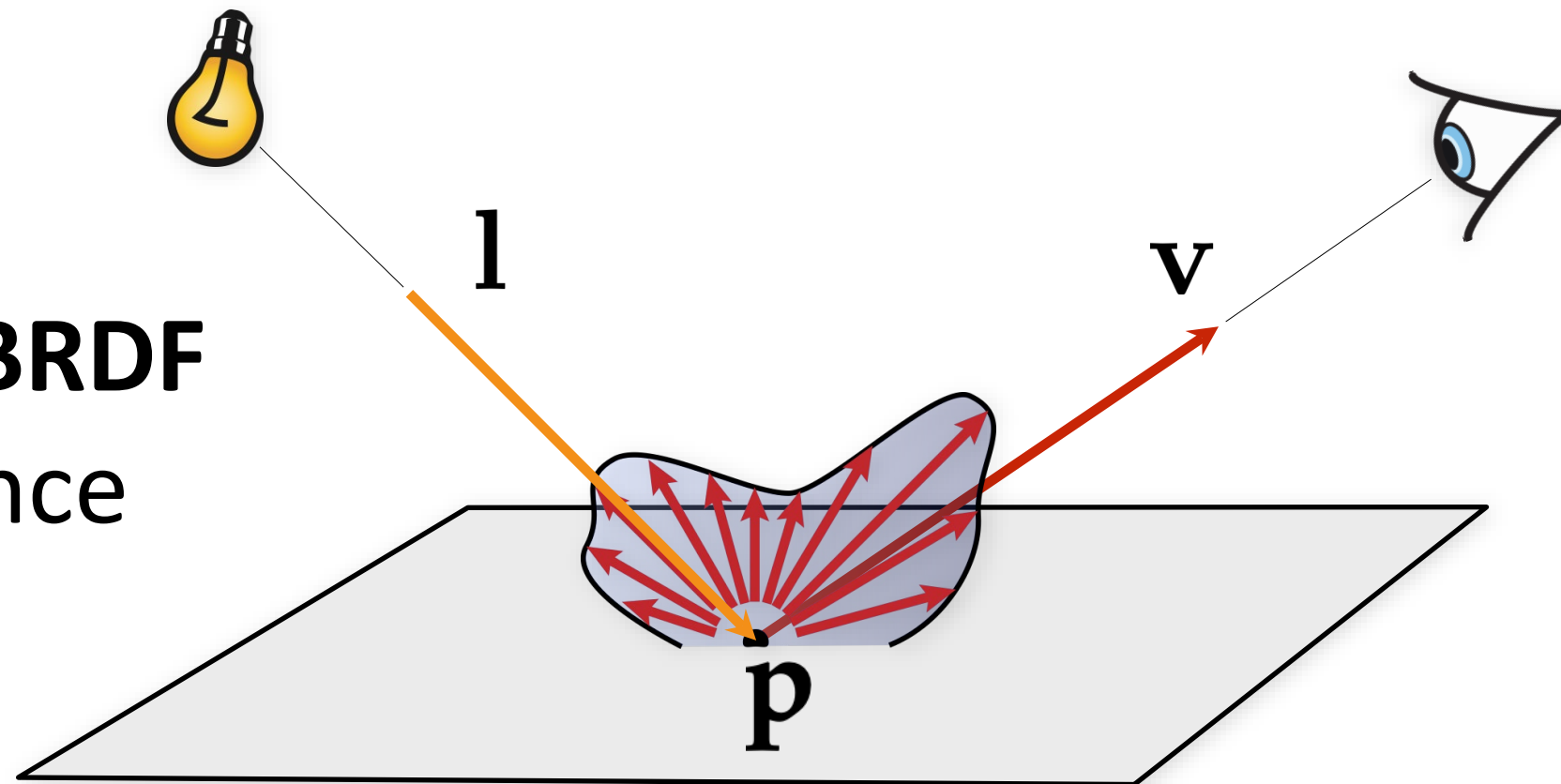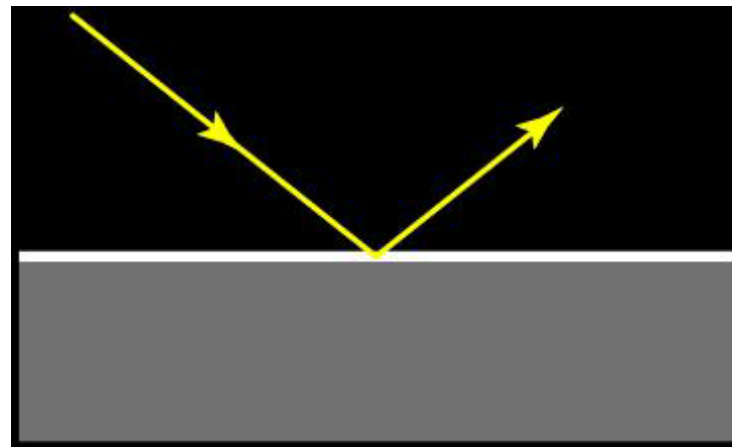
The BSDF

Bidirectional **S**cattering **D**istribution **F**unction

- informally: how much the material scatters light coming from one direction $\mathbf{l}$ into some other direction $\mathbf{v}$, at each point $\mathbf{p}$

You'll also see **BRDF**
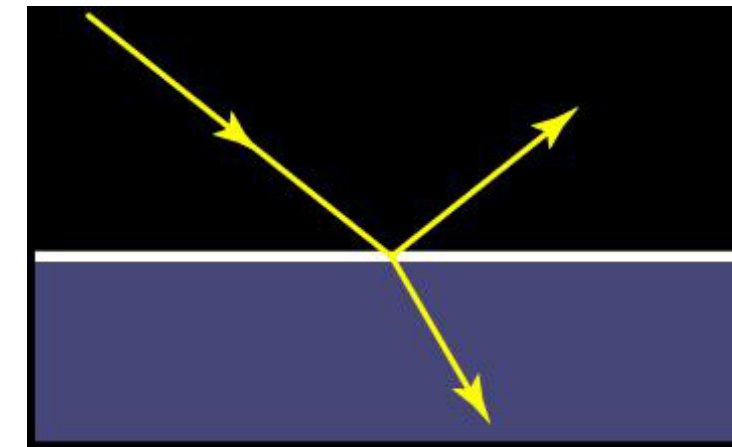   **R** for reflectance

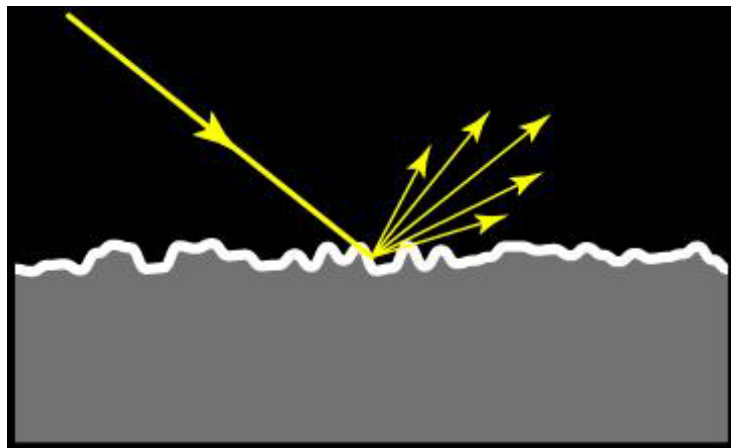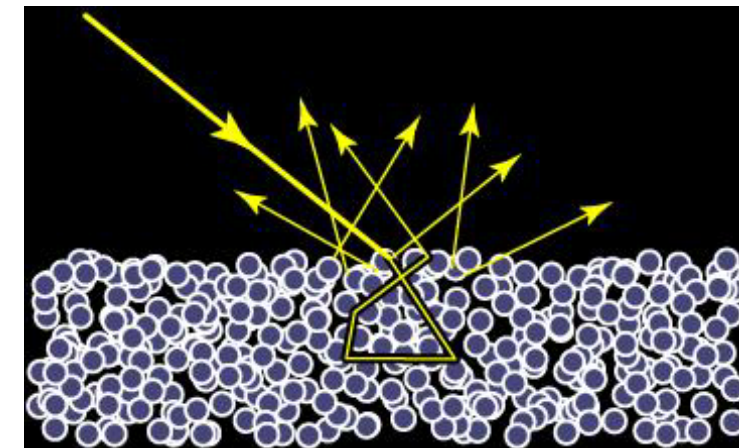# Real-world materials

Metals

Dielectric

Real-world materials
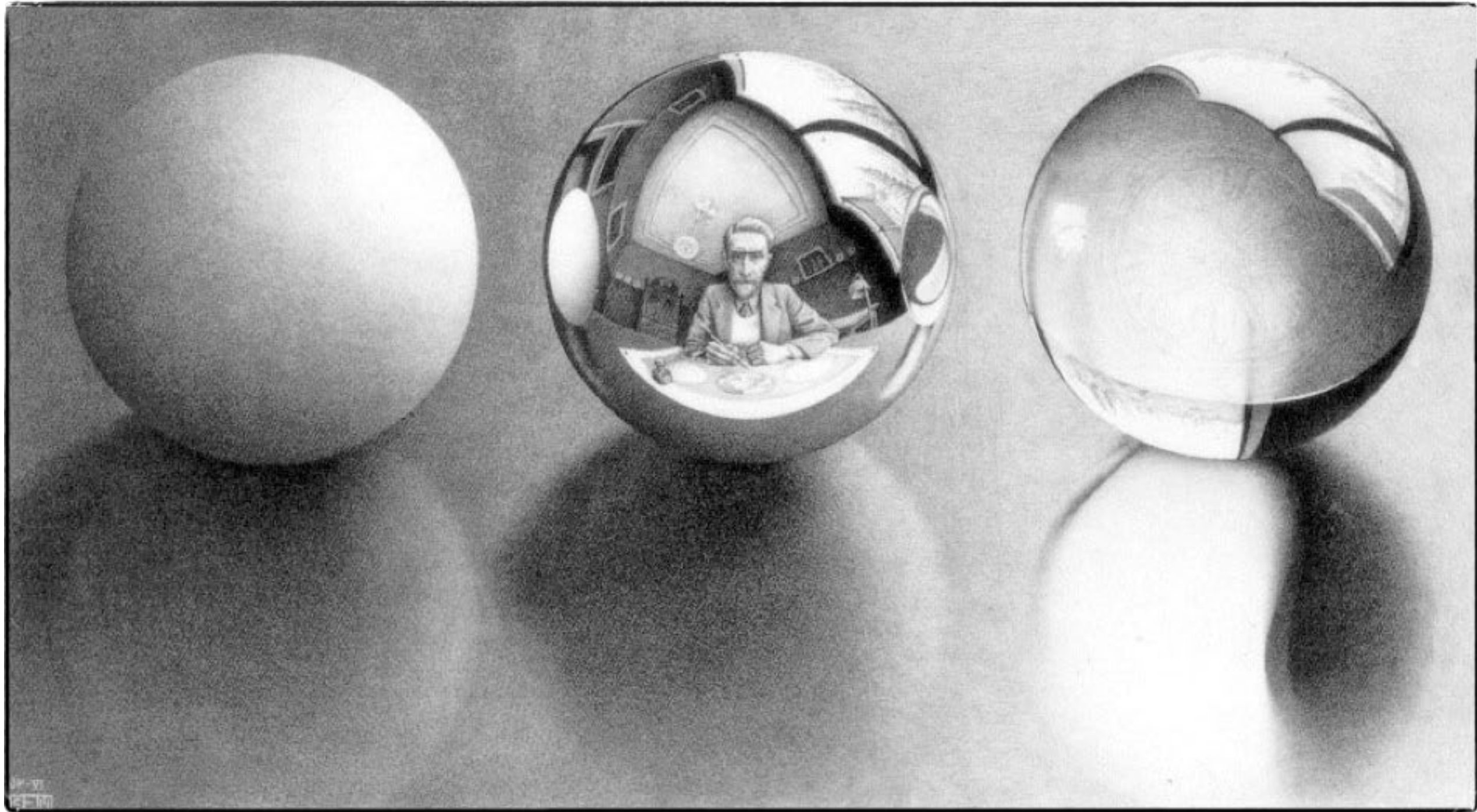
Metals

Dielectric

Idealized material models

Diffuse reflection

- light is reflected in all directions
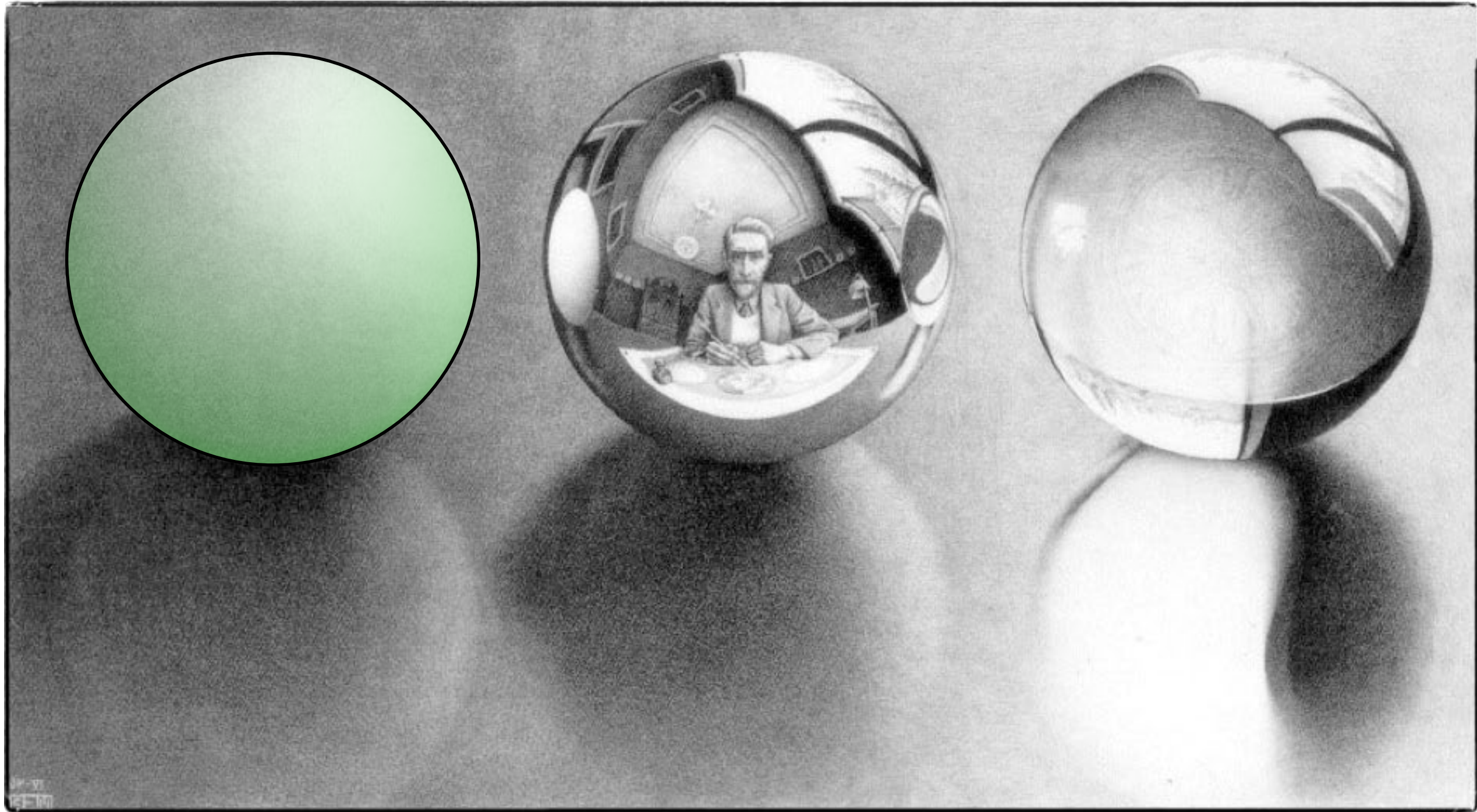
- colored by surface color

Smooth specular reflection/refraction
(e.g., chrome, glass, glaze/varnish)

- light reflected/refracted only in a single direction
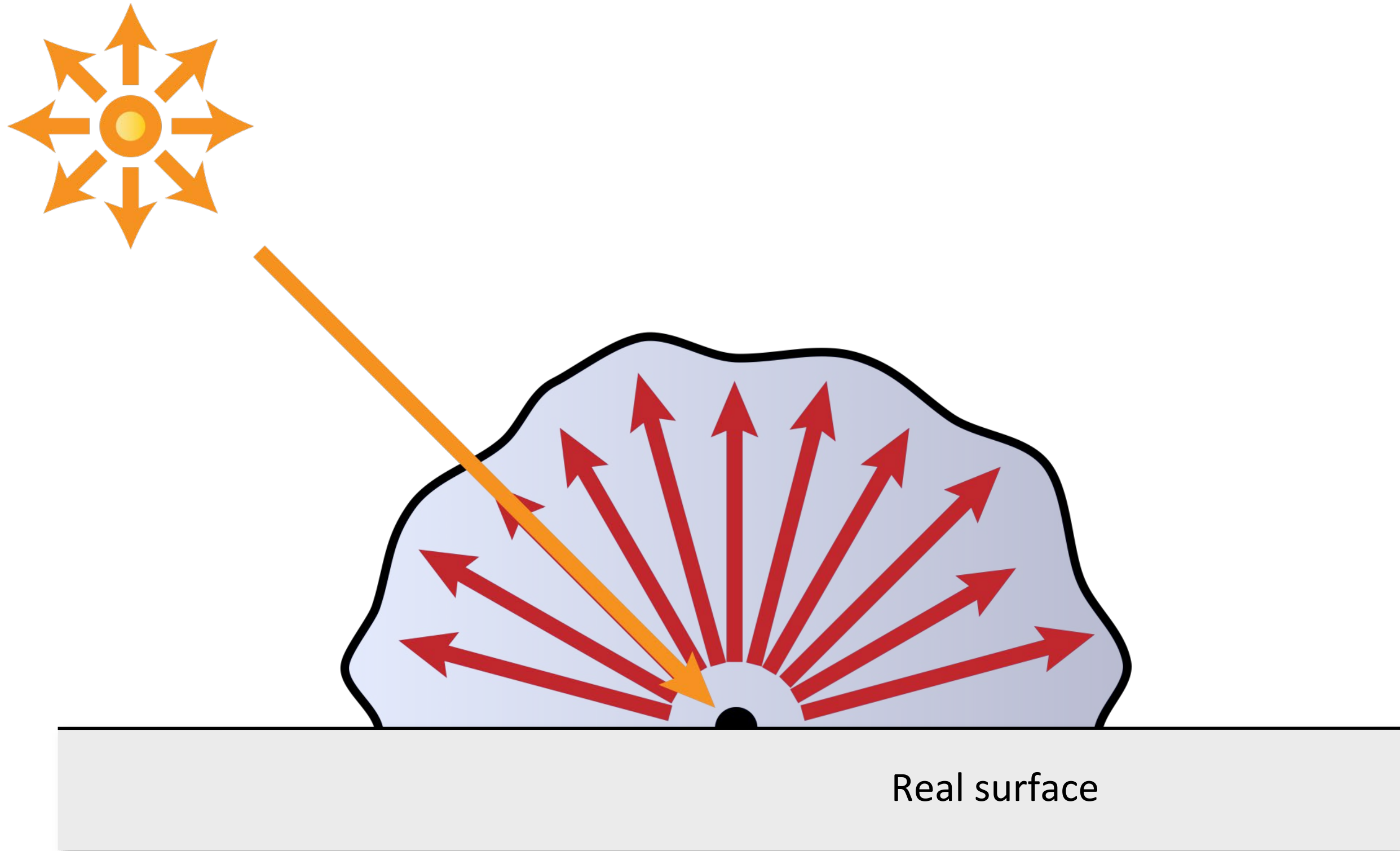
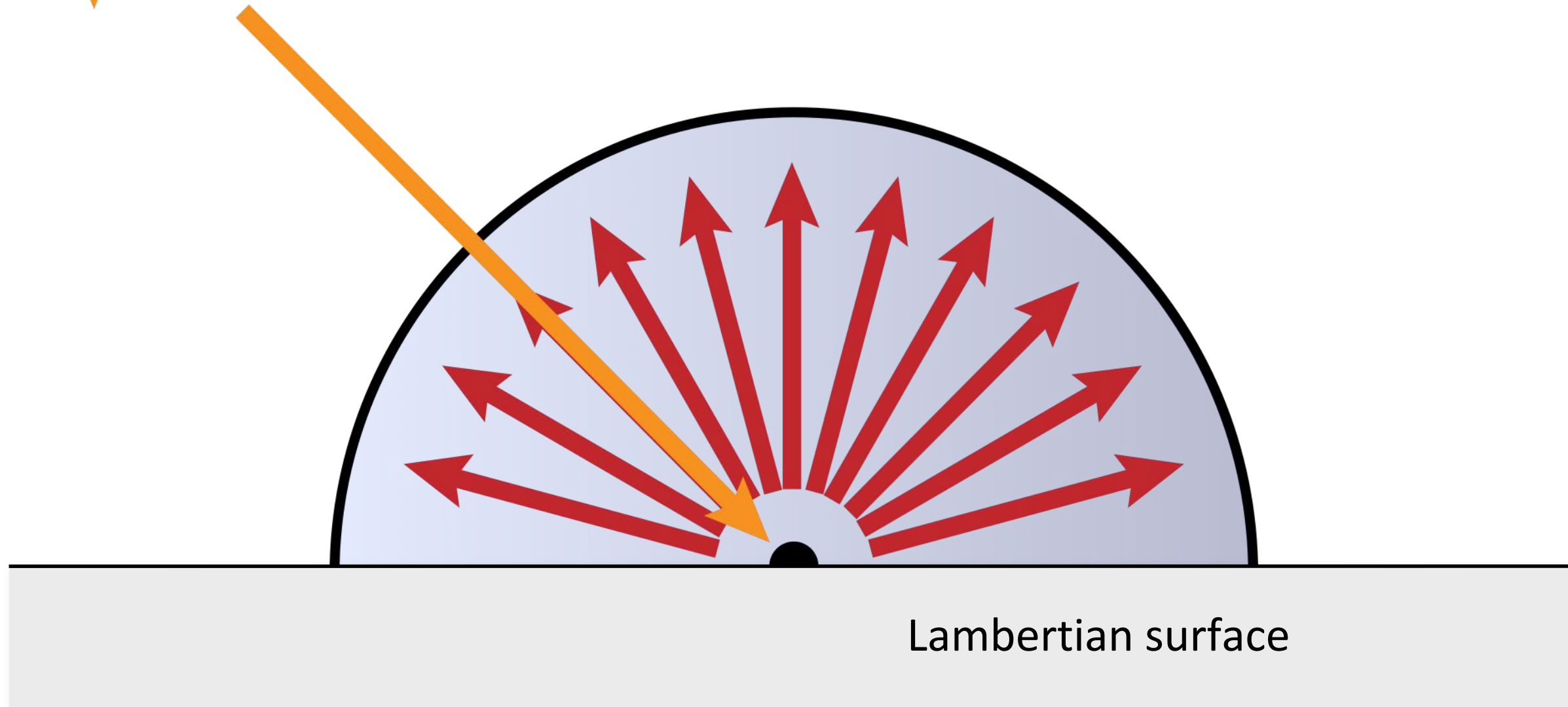- colored by source color

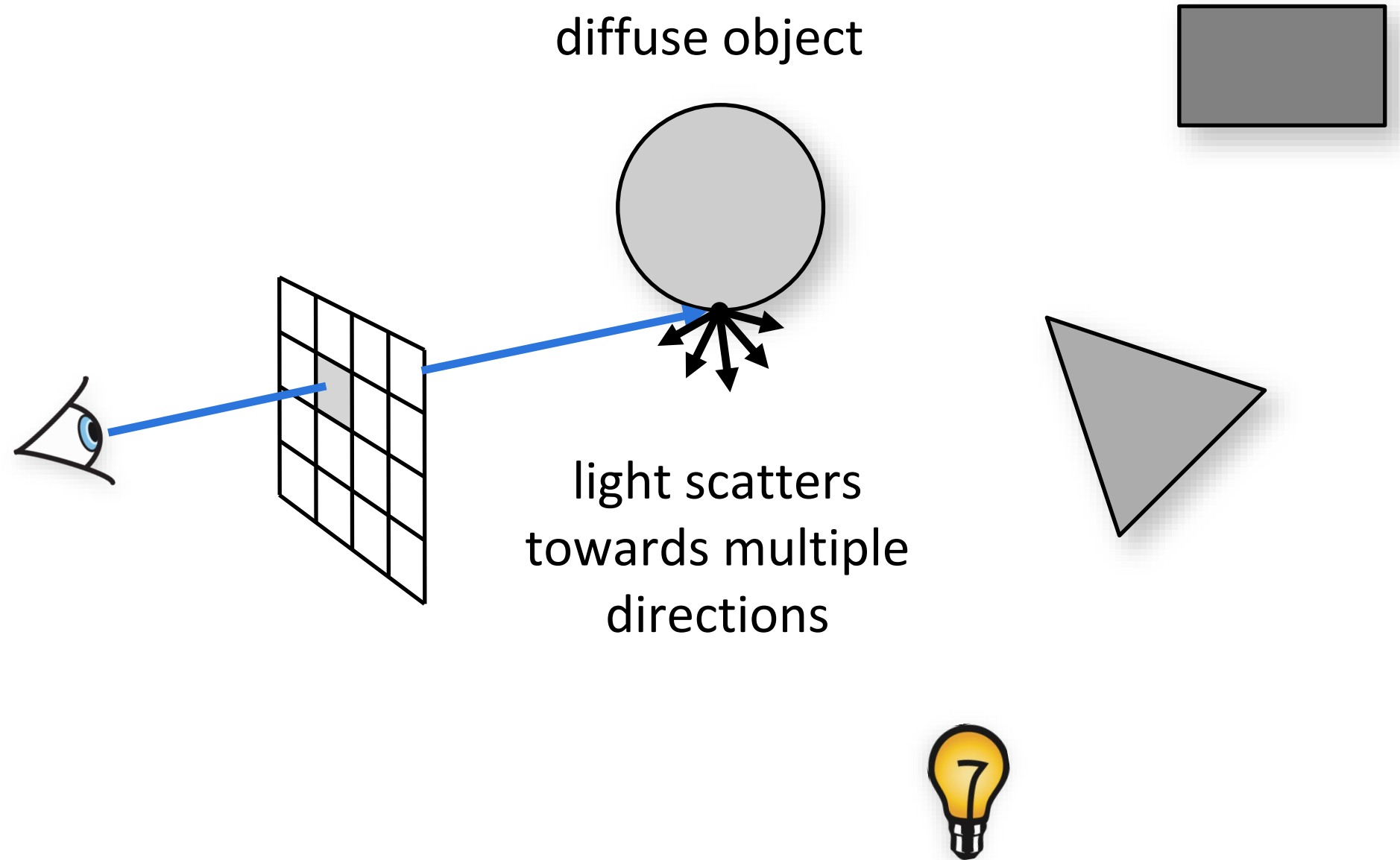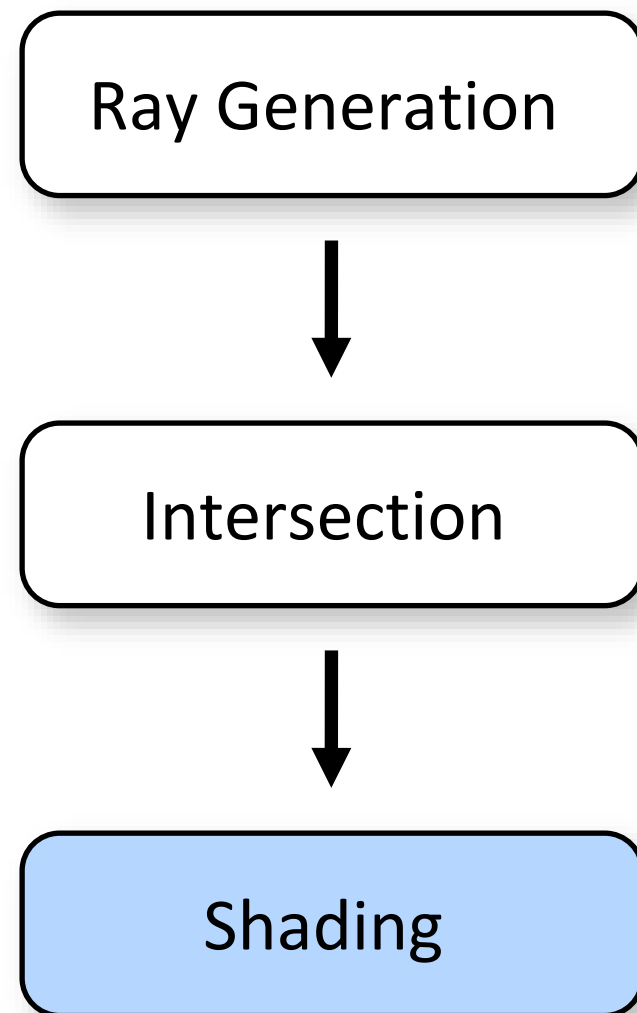# Idealized materials

Diffuse reflection

Diffuse reflection

Real surface

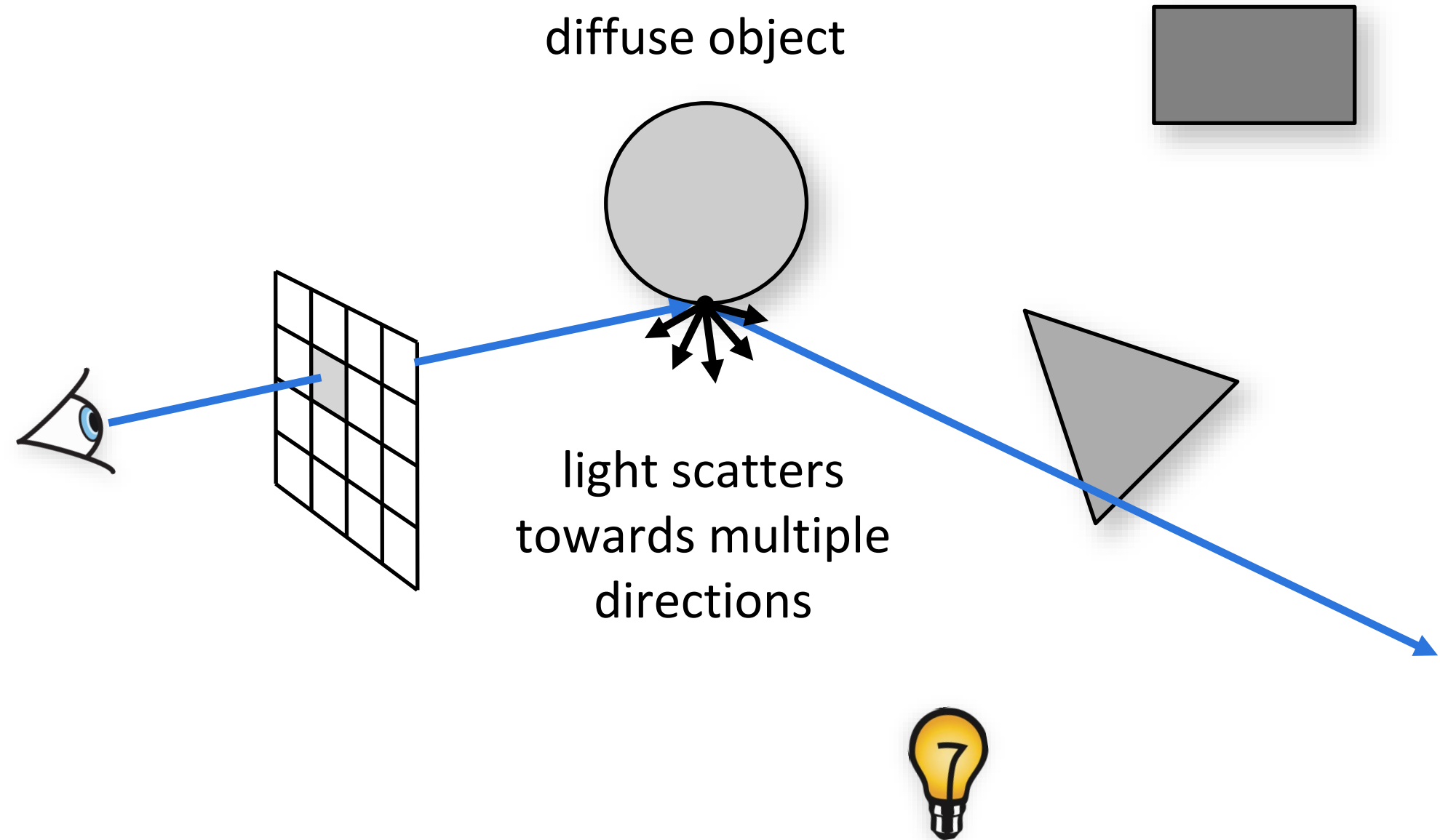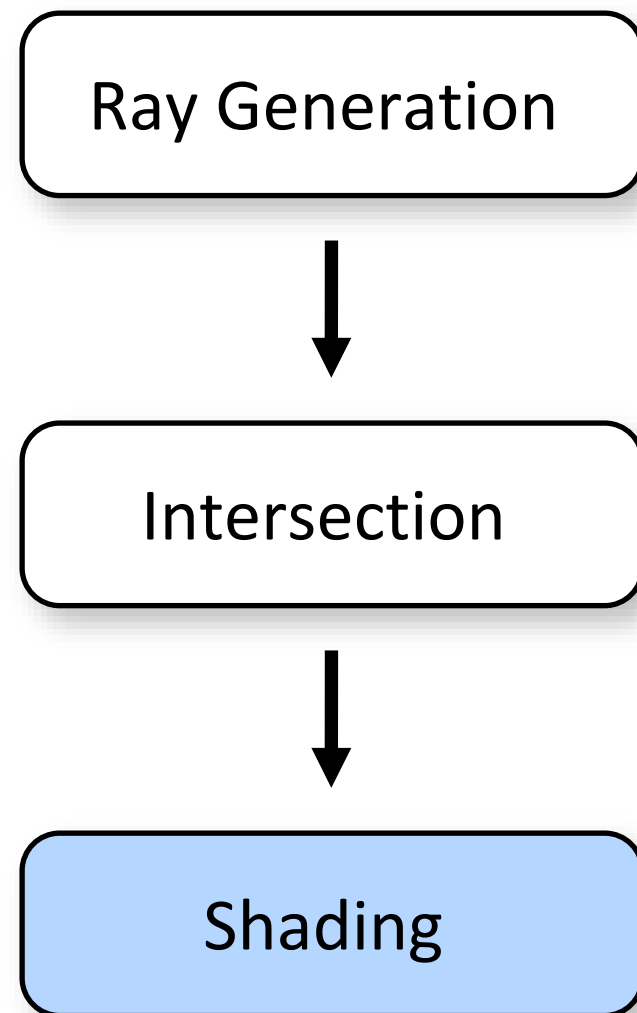# Lambertian reflection

Also called ideal diffuse reflection

Lambertian surface

Basic Ray Tracing Pipeline

Ray Generation

Intersection

Shading

diffuse object

light scatters towards multiple directions

What direction should we trace a new ray towards?

Basic Ray Tracing Pipeline

diffuse object

Ray Generation

Intersection

Shading

light scatters
towards multiple
directions

What direction should we trace a new ray towards?

- Pick a direction at random!

Sampling Lambertian scattering

From what distribution should we sample directions?
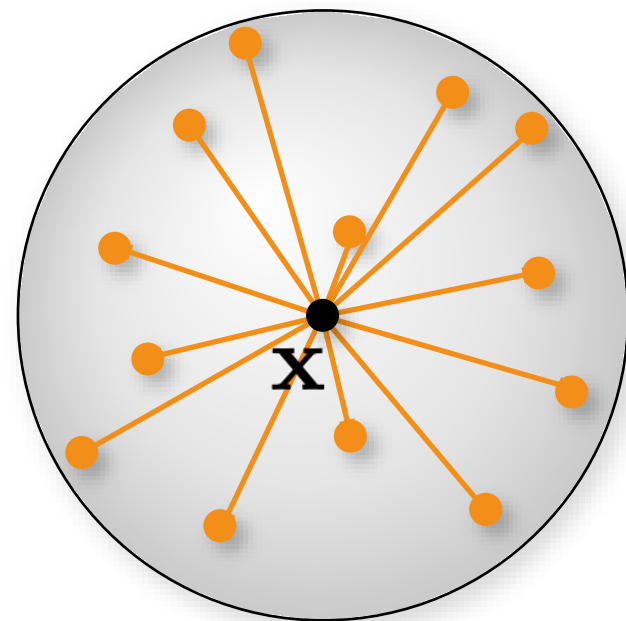
Sampling Lambertian scattering

From what distribution should we sample directions?

- Probability proportional to $\cos(\hat{n} \cdot \hat{\omega})$.

- Even though BSDF scatters to all directions uniformly, we need to account for foreshortening.

How do we sample directions based on this *cosine-weighted* distribution?
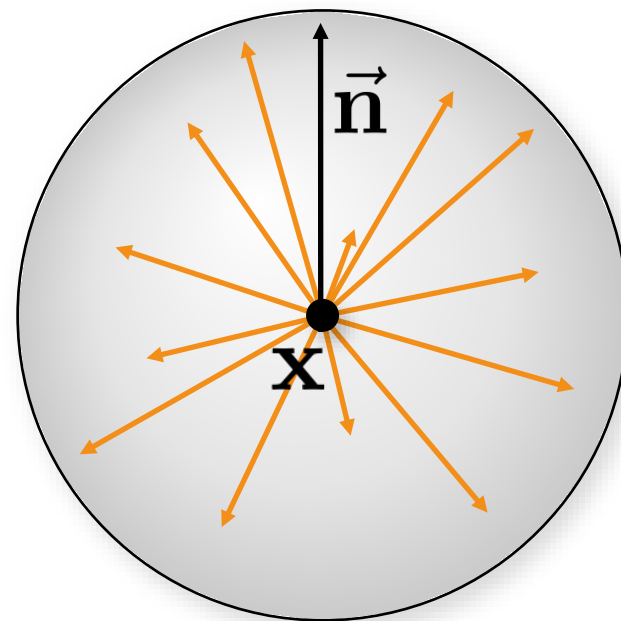
Sampling Lambertian scattering

Generate points
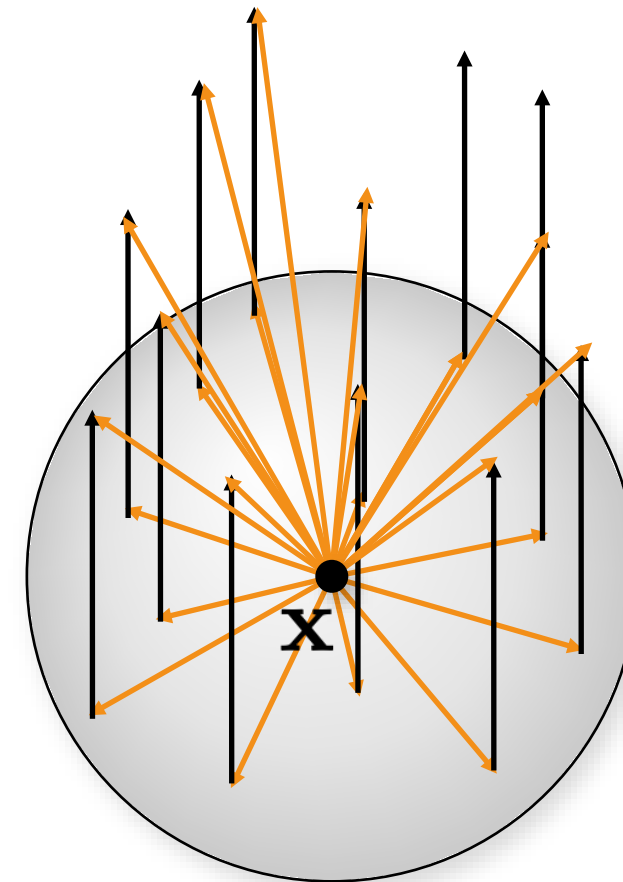uniformly on sphere

(unit directions)

Sampling Lambertian scattering

Generate points
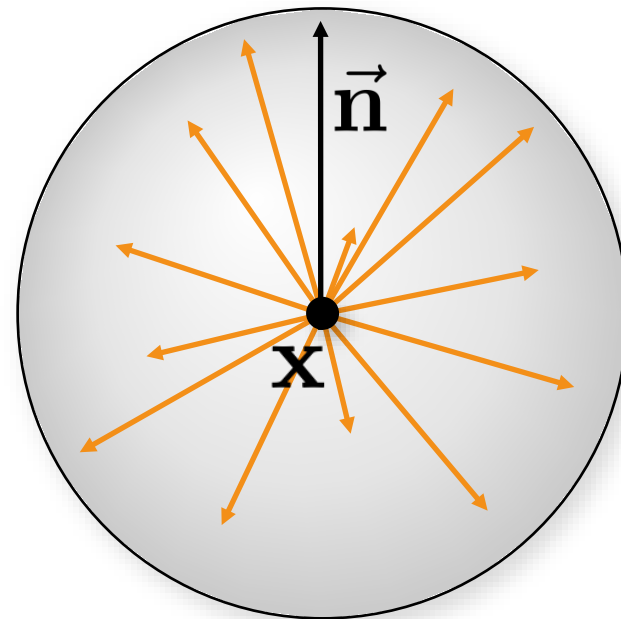uniformly on sphere

(unit directions)

unit normal

$\vec{\mathbf{n}}$

x

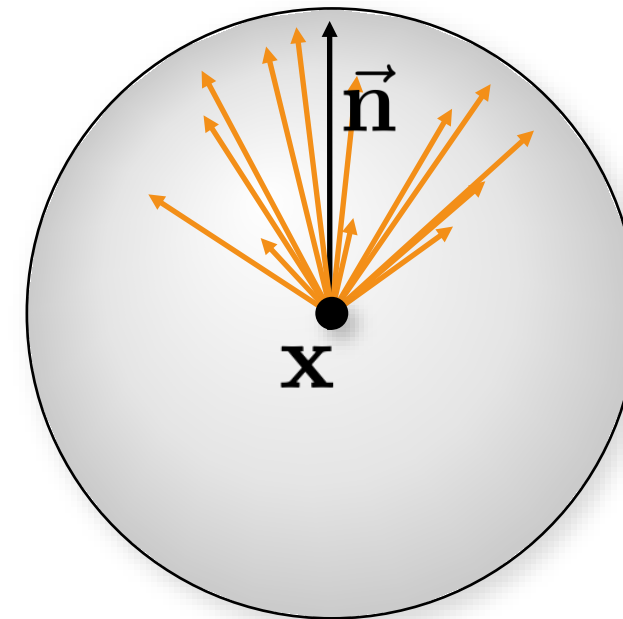*Add* unit normal

x

Sampling Lambertian scattering

Generate points
uniformly on sphere

(unit directions)
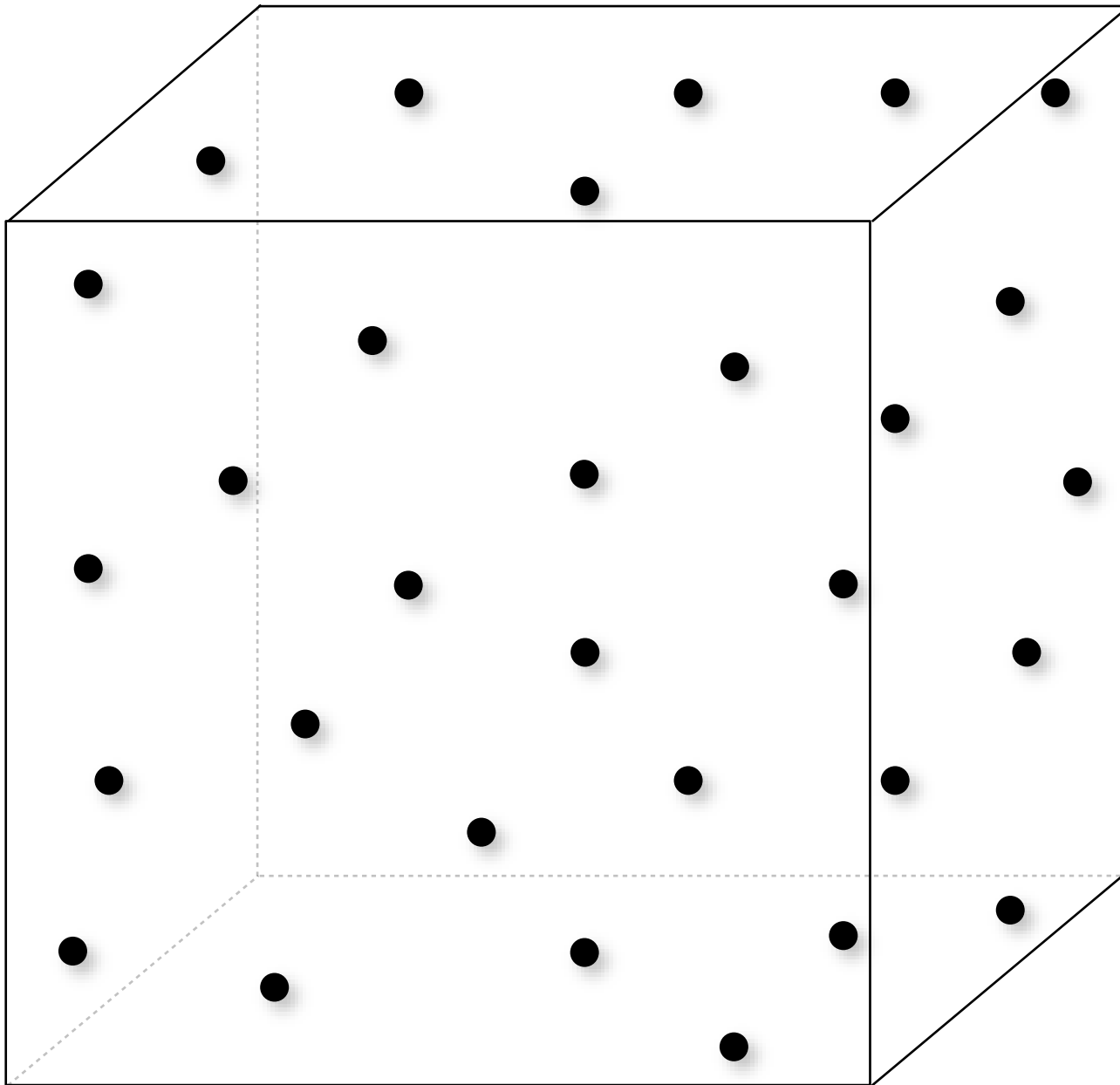
unit normal

Add unit normal

normalize

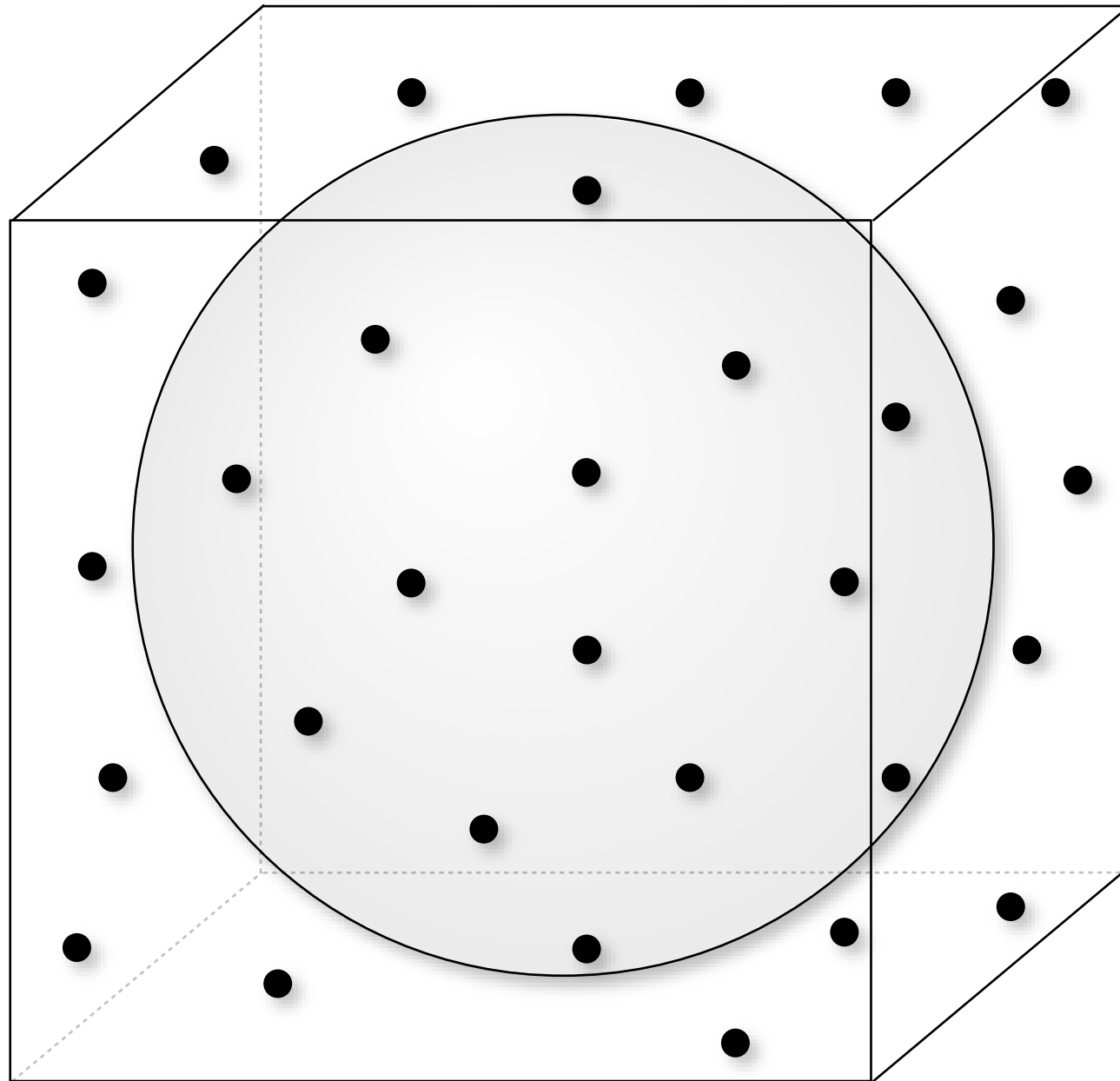# Rejection Sampling a Sphere

```
Vector3D v;

v.x = 1-2*randf();
v.y = 1-2*randf();
v.z = 1-2*randf();
```
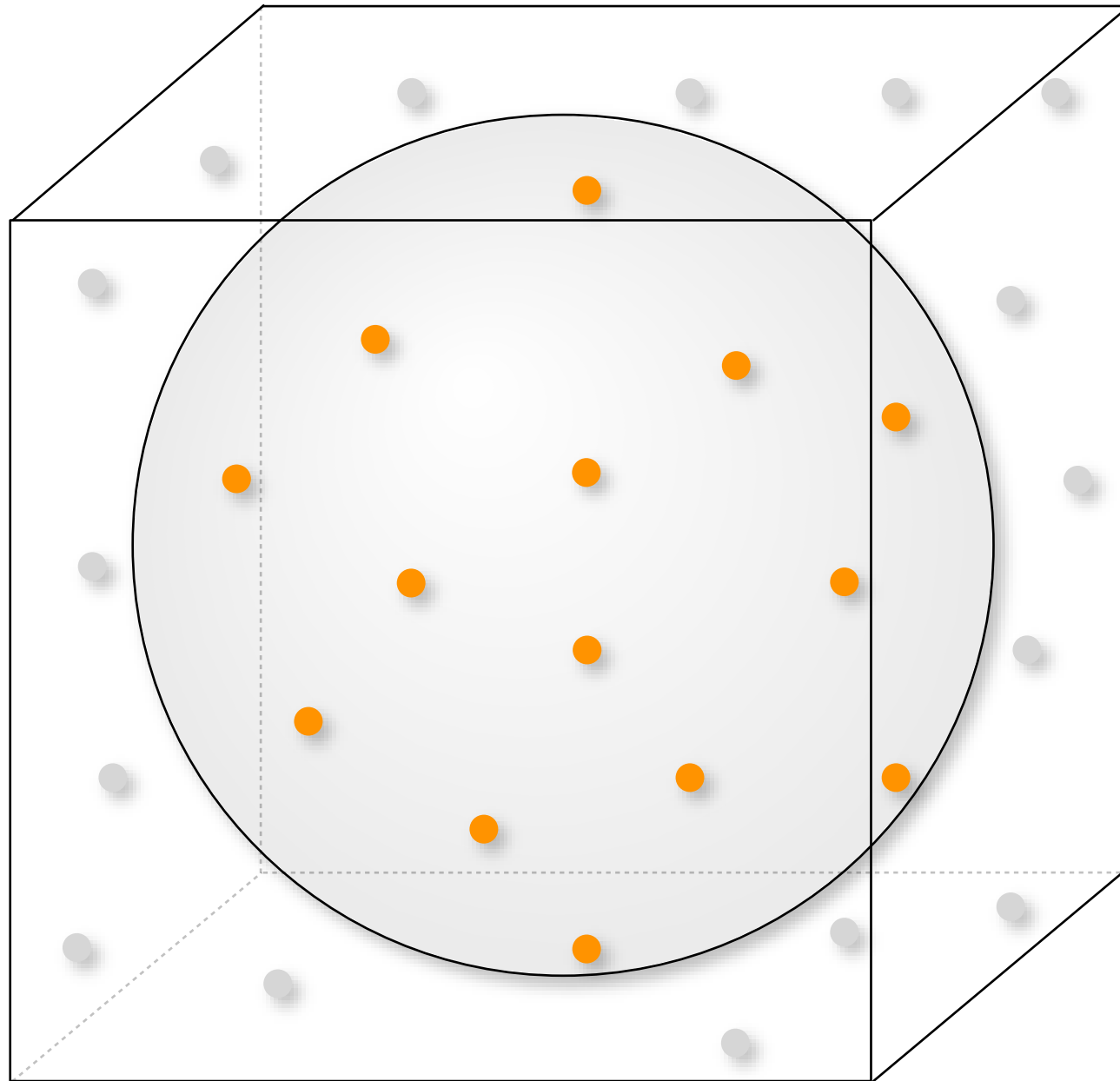
Rejection Sampling a Sphere

```
Vector3D v;
do
{
    v.x = 1-2*randf();
    v.y = 1-2*randf();
    v.z = 1-2*randf();
} while(v.length²() > 1)
```

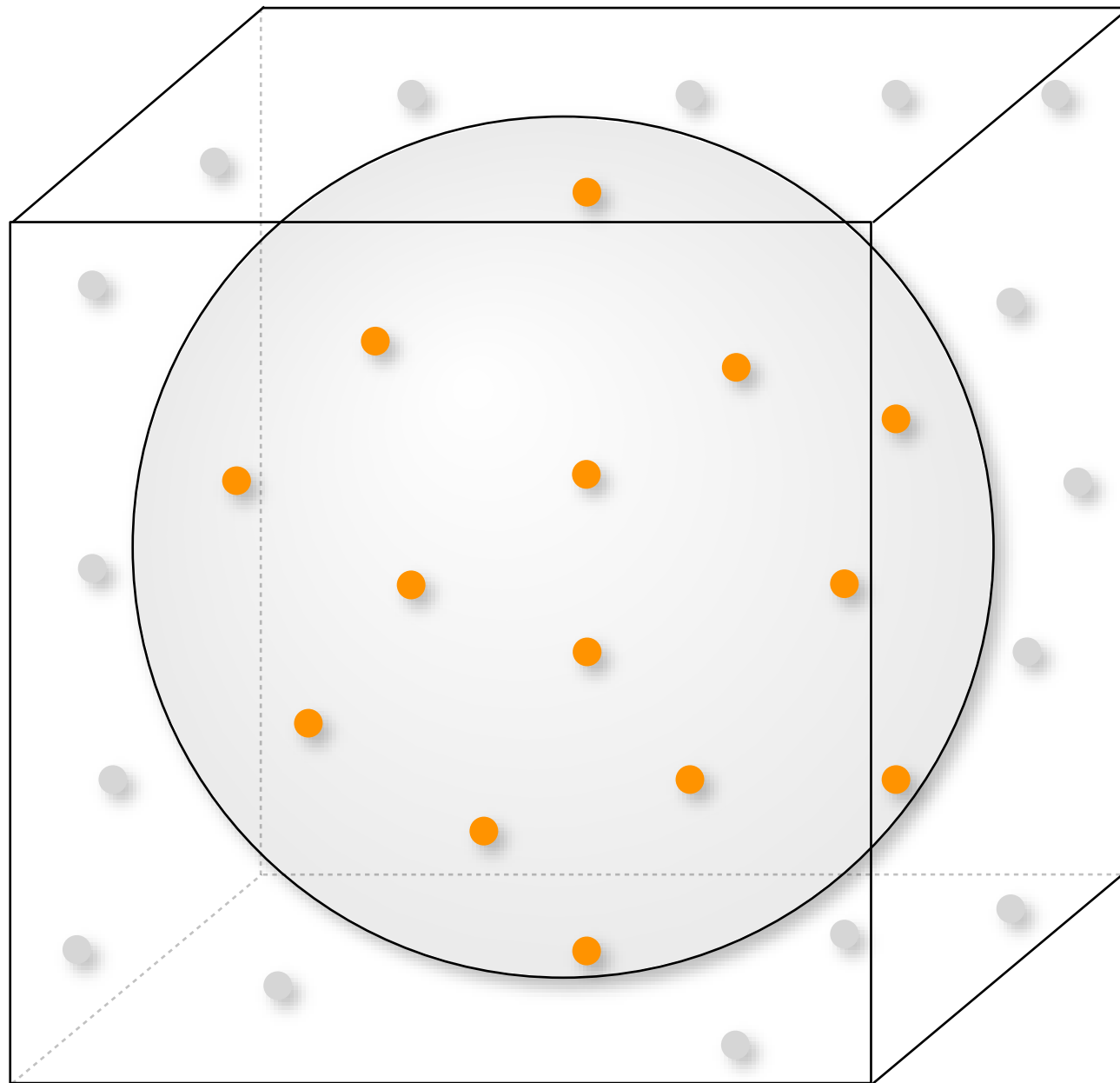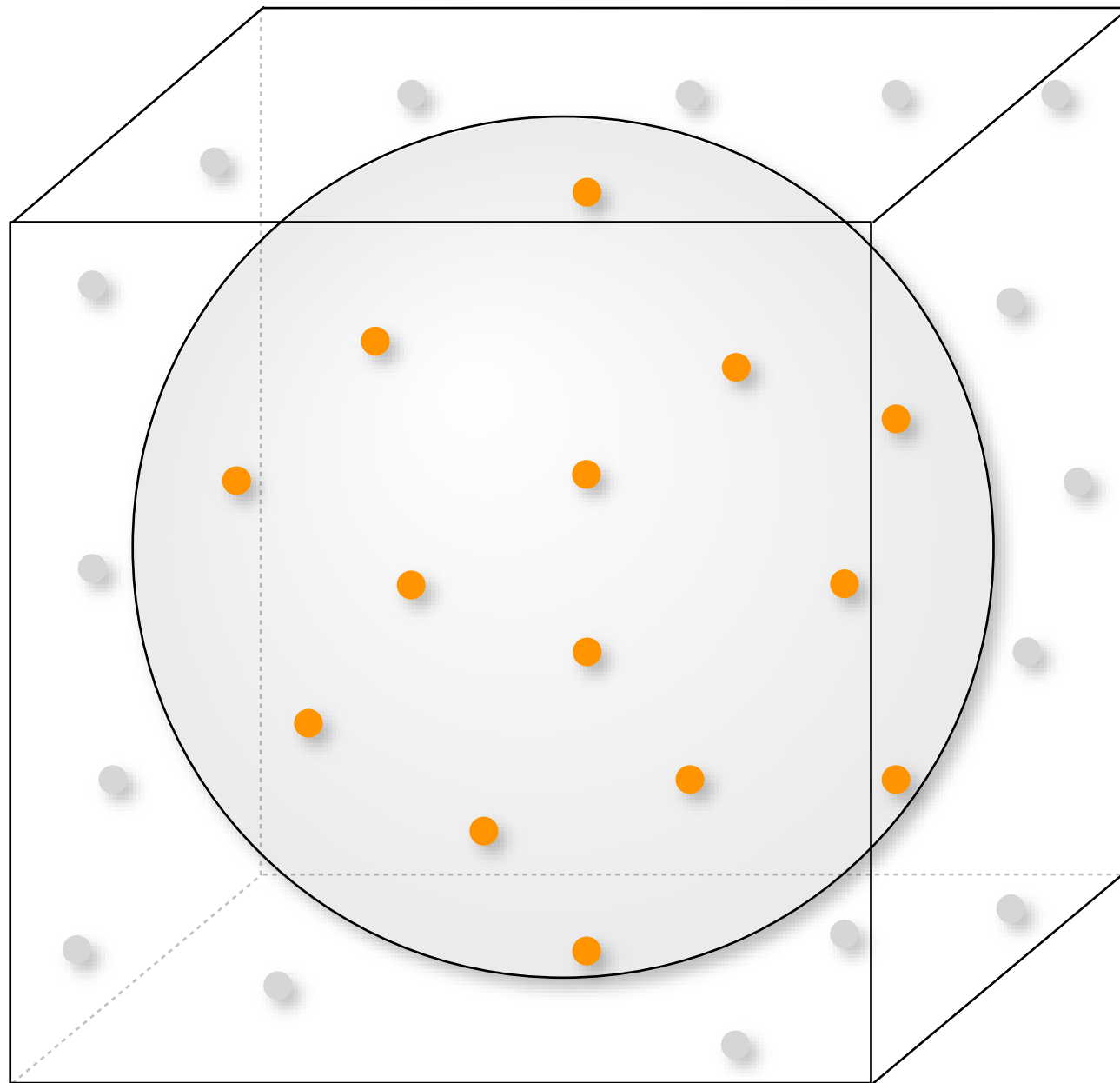# Rejection Sampling a Sphere


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} while(v.length²() > 1)
```

Rejection Sampling a Sphere

```
Vector3D v;
do
{
    v.x = 1-2*randf();
    v.y = 1-2*randf();
    v.z = 1-2*randf();
} while(v.length²() > 1)
// Project onto sphere
v /= v.length();
```

Sampling a Sphere using normal samples

```
Vector3D v;
v.x = randnf();
v.y = randnf();
v.z = randnf();
// Project onto sphere
v /= v.length();
```

- No rejection sampling required (no `while` loop).

- Need to use normal, rather than uniform, samples.

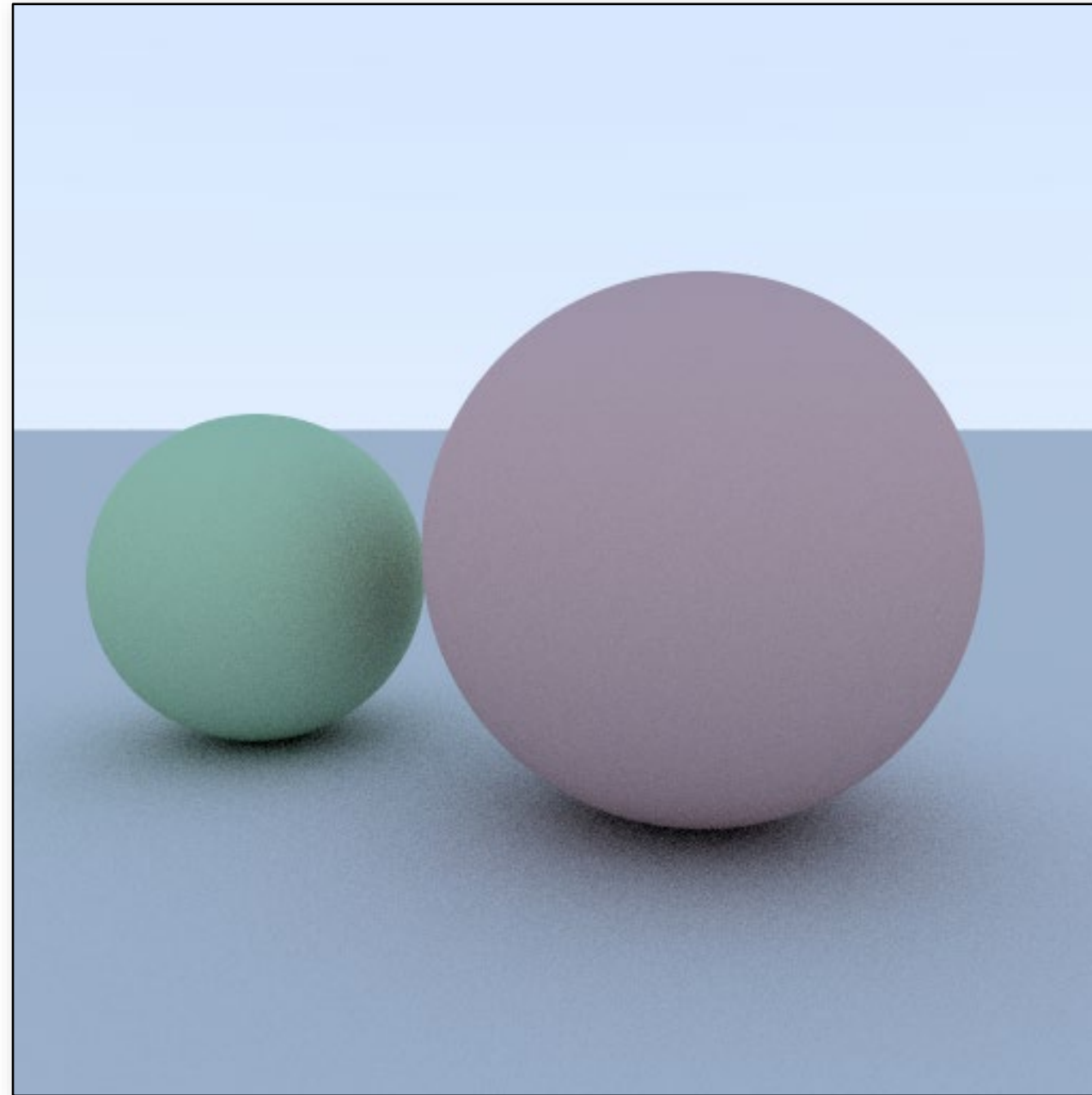# Diffuse shading
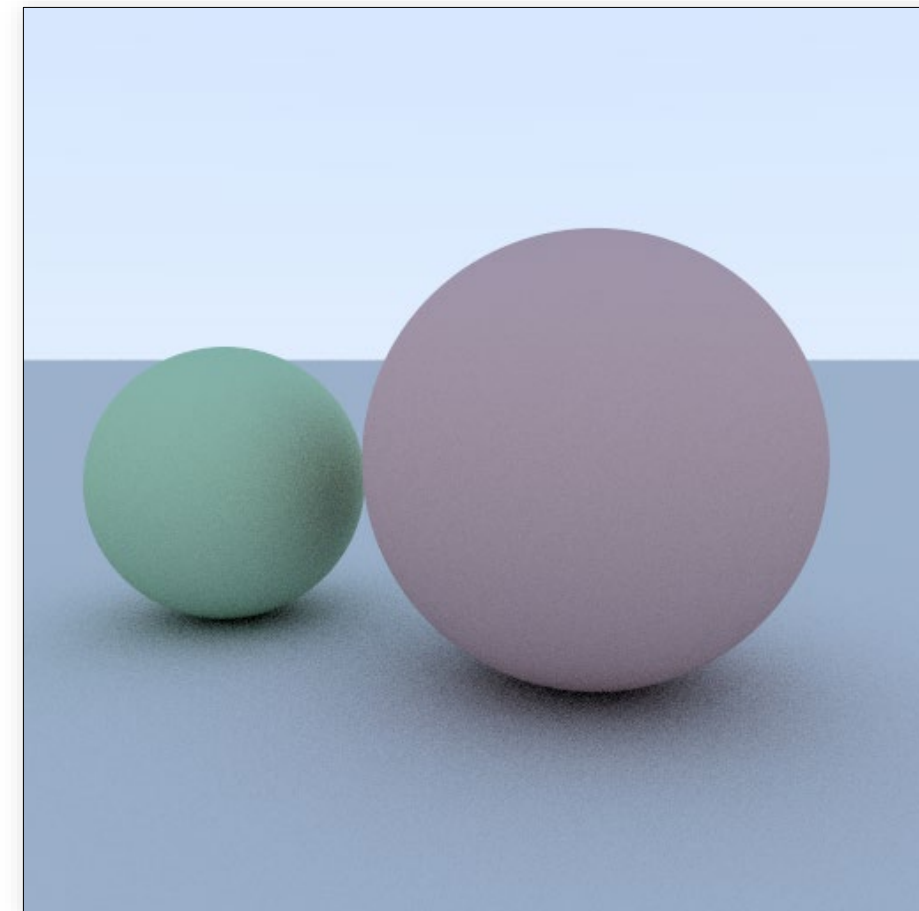
Image so far

```
Scene::trace(Ray ray)
   hit = surfaces.intersect(ray);
   if hit
      [col, sRay] = hit->mat->scatter(ray)
      return col * trace(sRay);
   else
      return backgroundColor;
```

Rounding errors

Don't fall victim to one of the classic blunders:
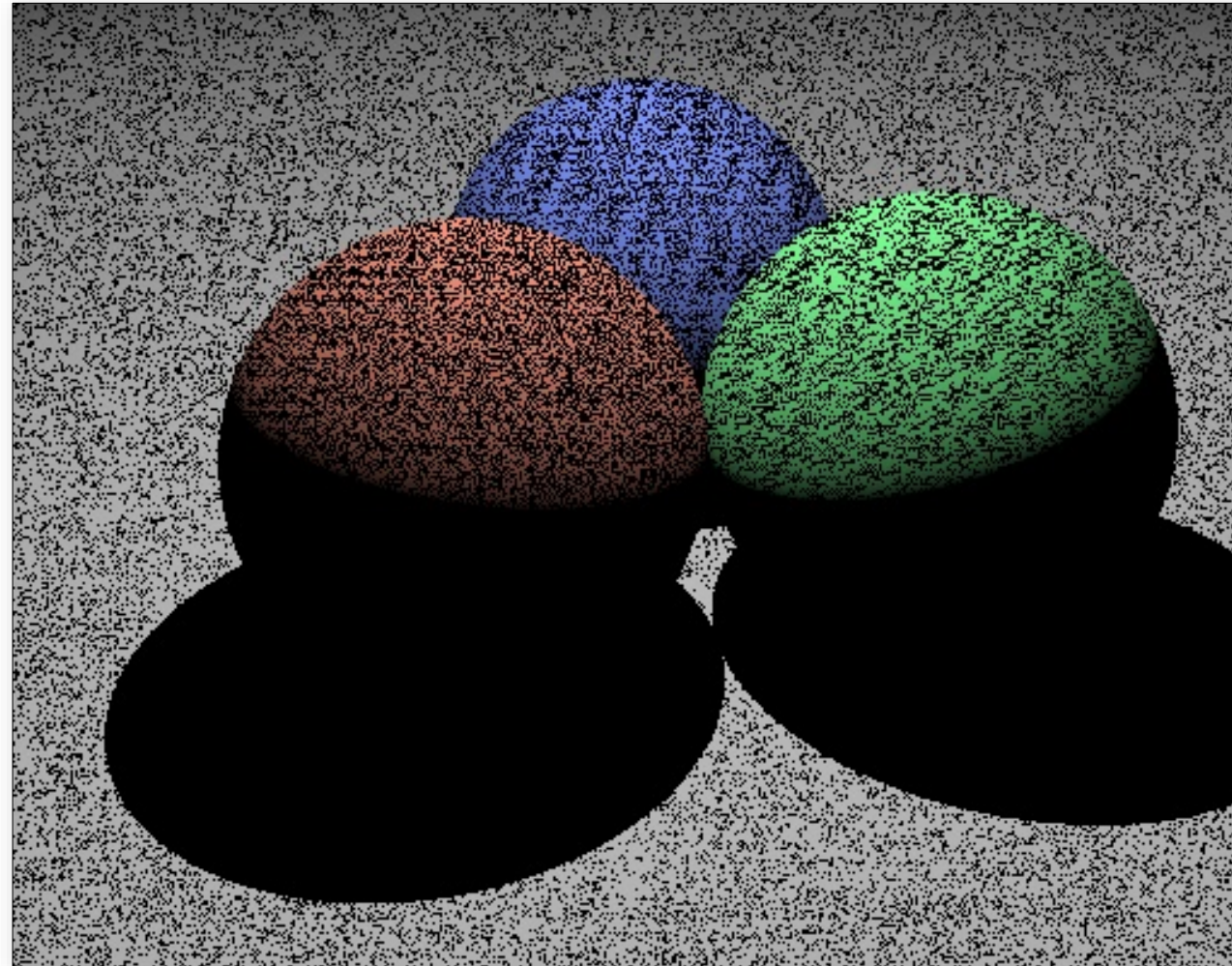
affectionately called
"shadow acne"

What's going on?

Rounding errors

Don't fall victim to one of the classic blunders:
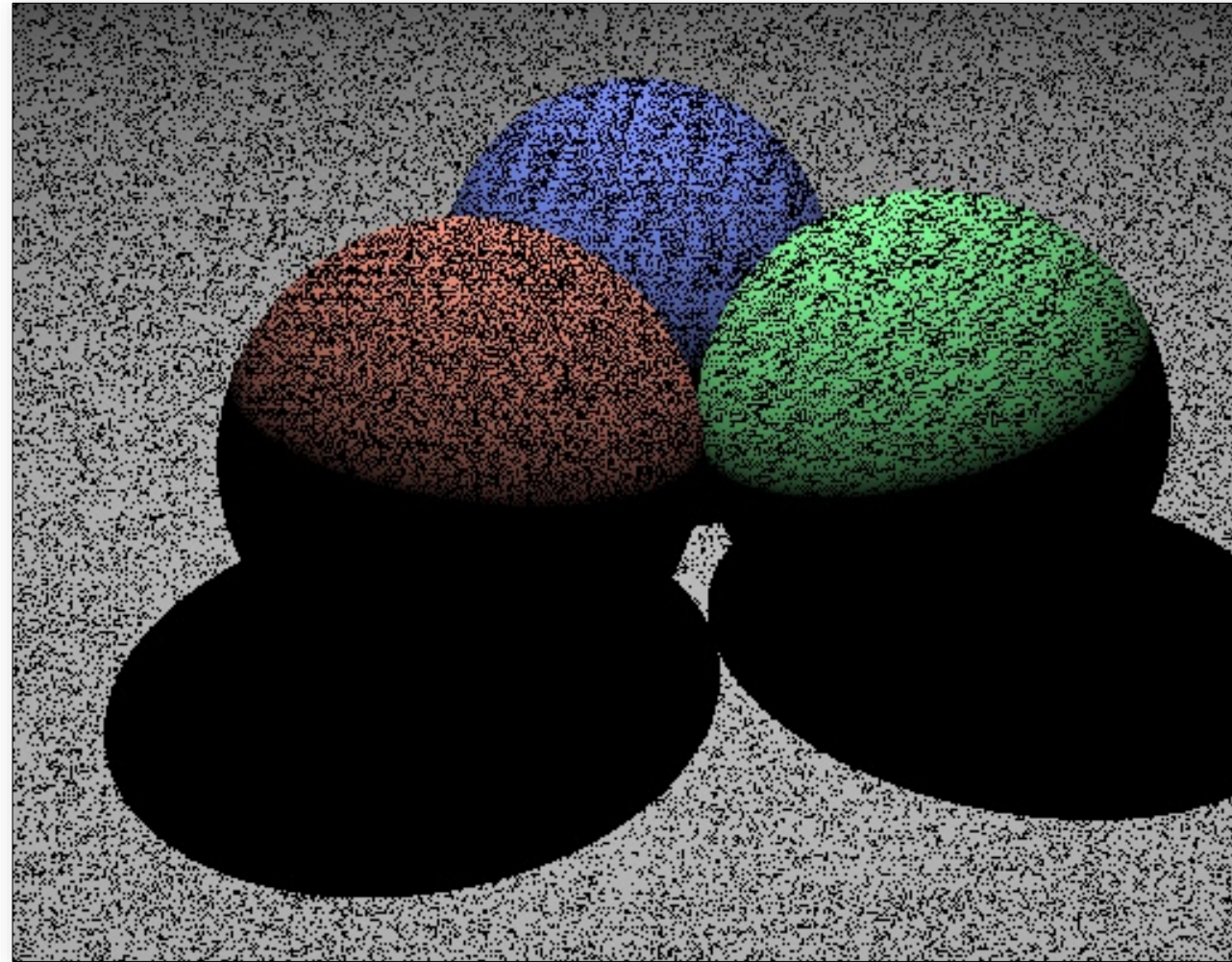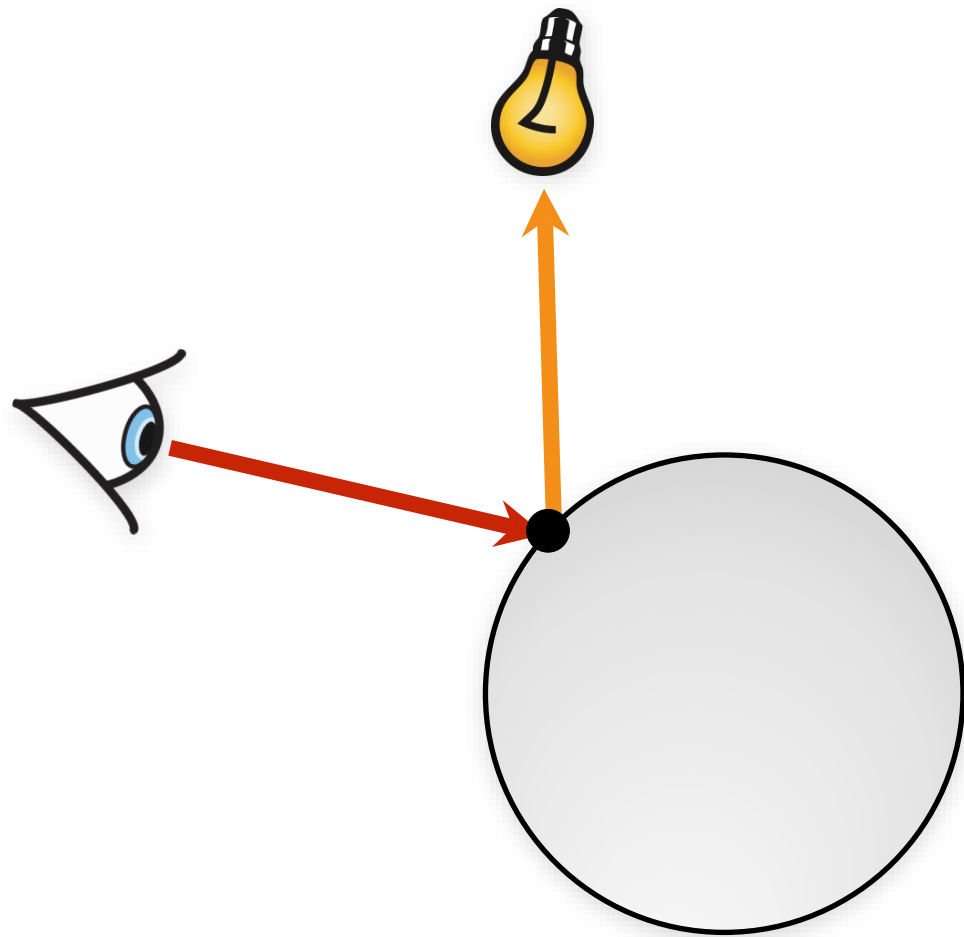
intersection inside due to floating point error

ray blocked by self-intersection

Shadow rounding errors
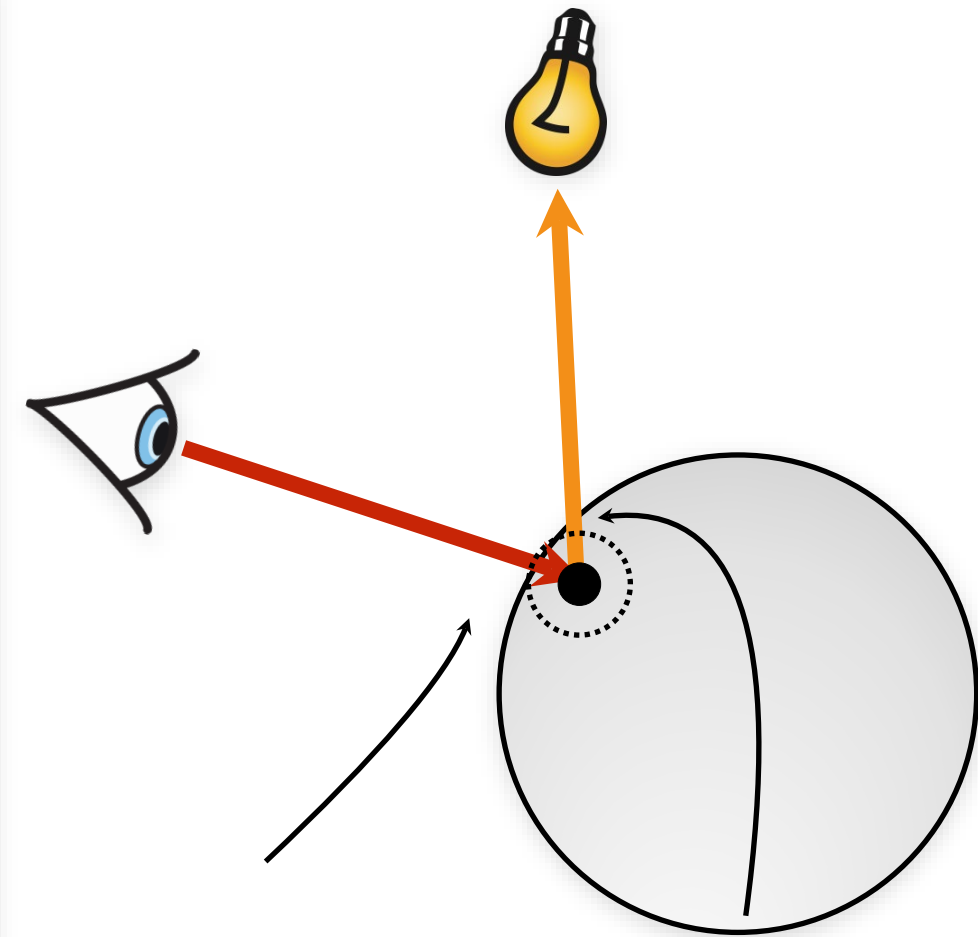
Solution: recursive rays start a tiny distance from the surface
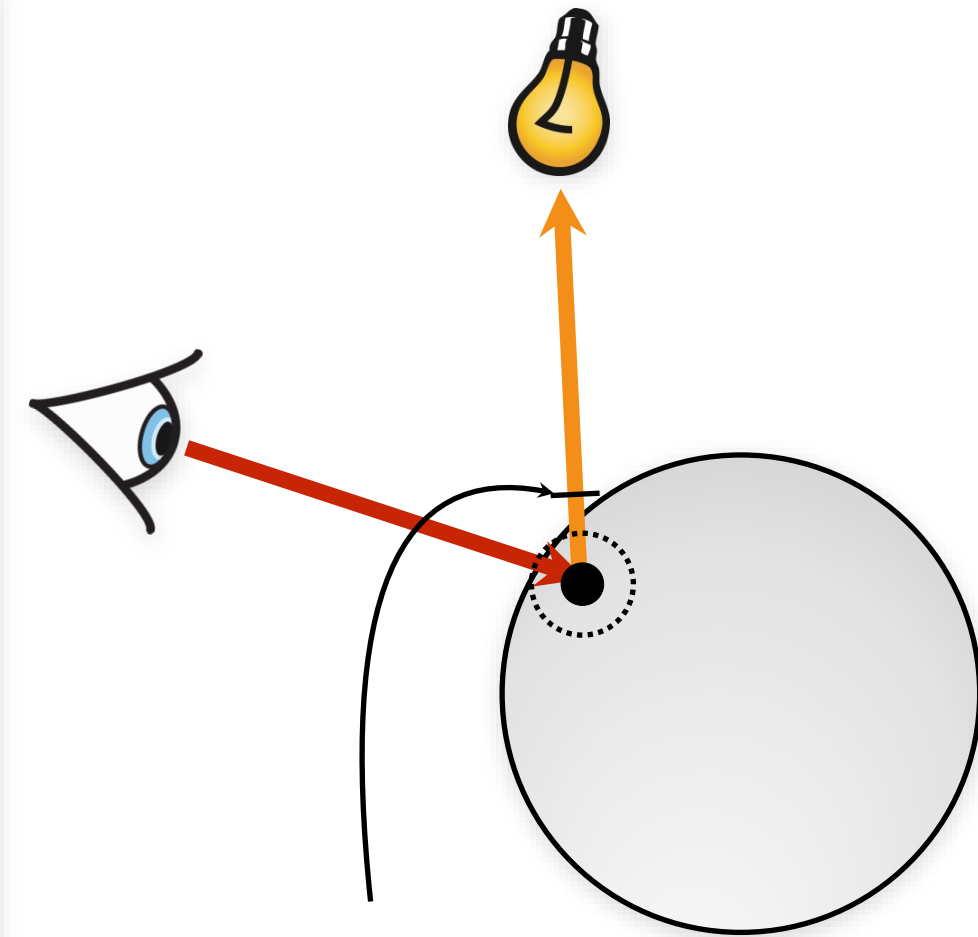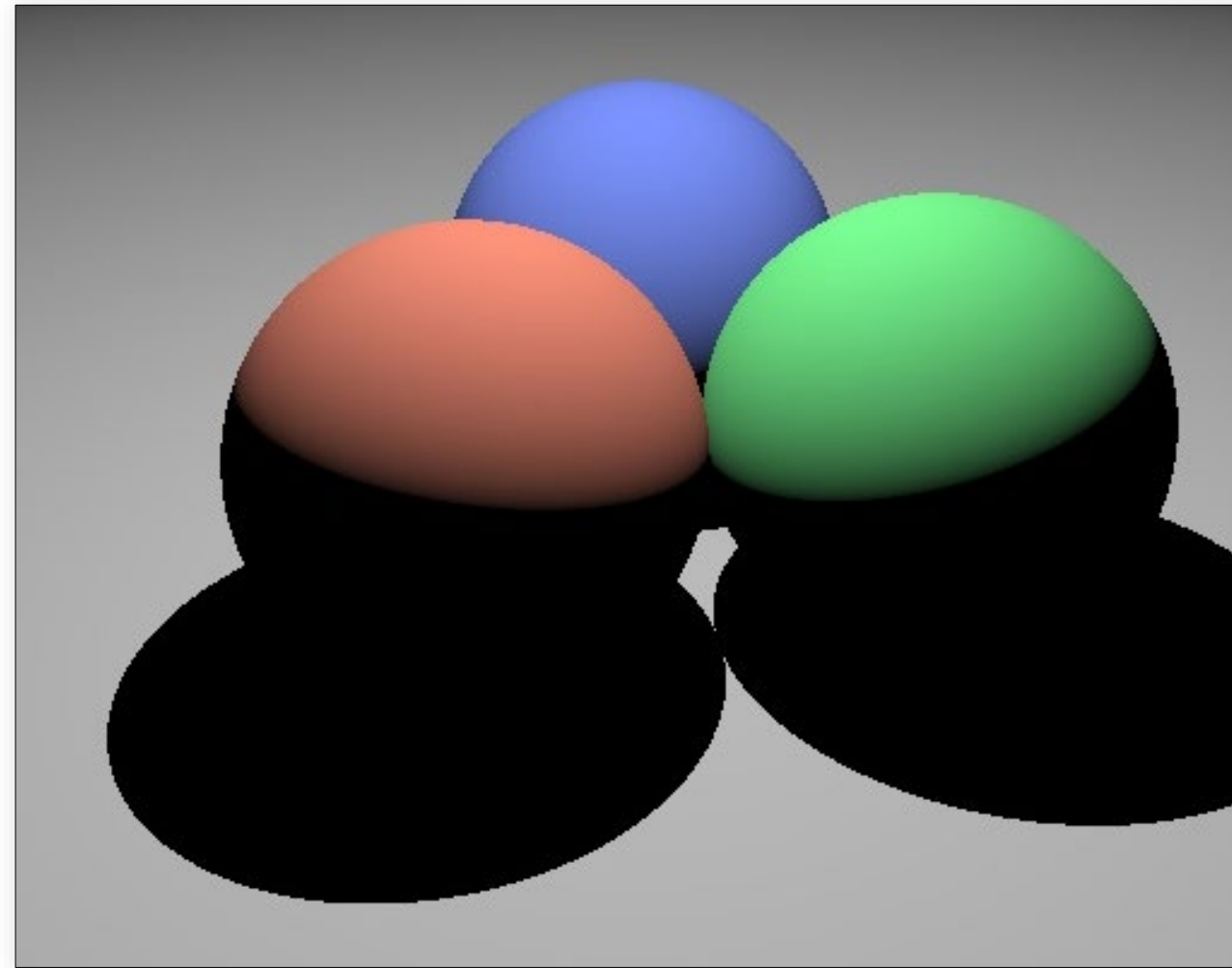
Do this by limiting
the *t* range

Specular/Mirror reflection
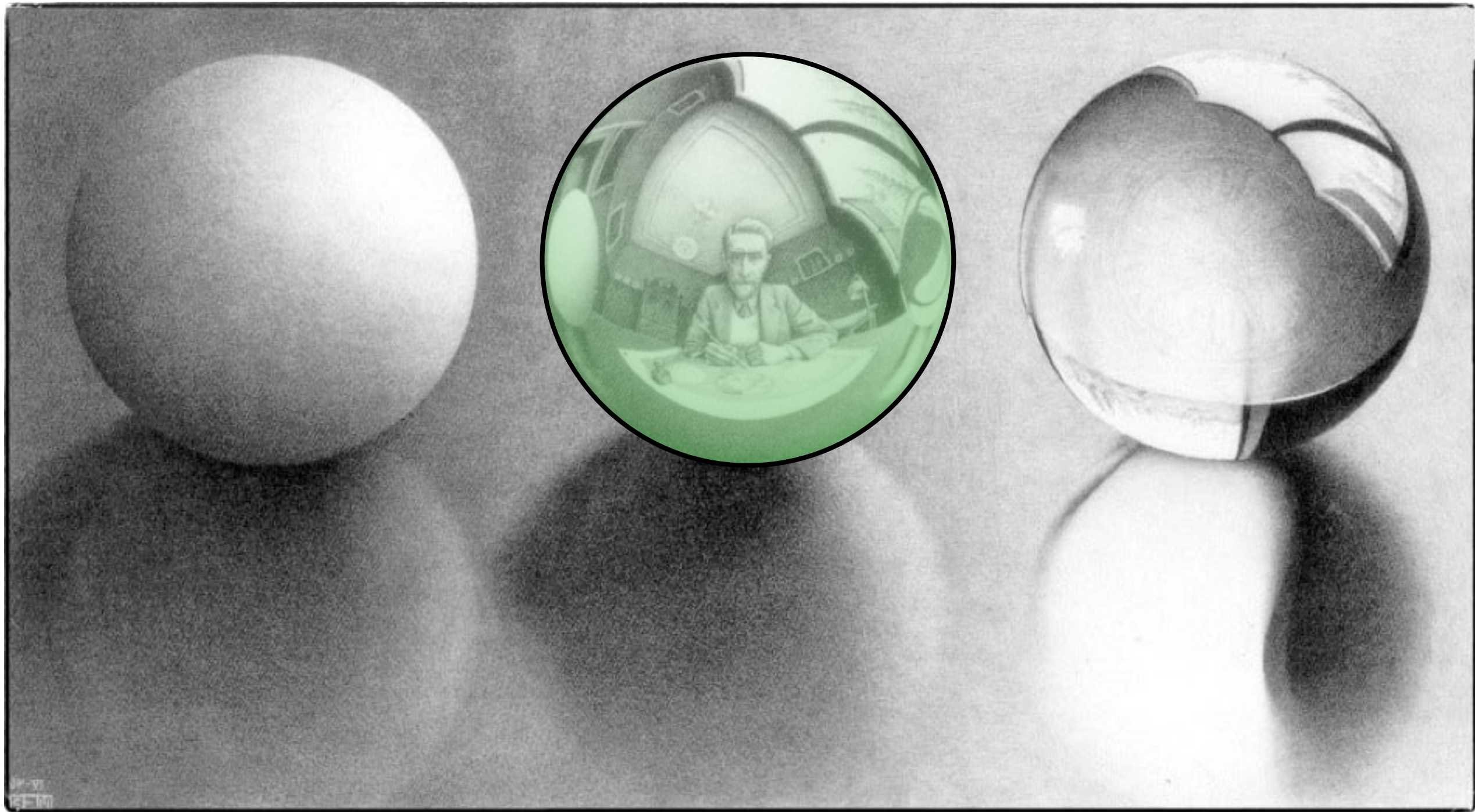
Basic Ray Tracing Pipeline
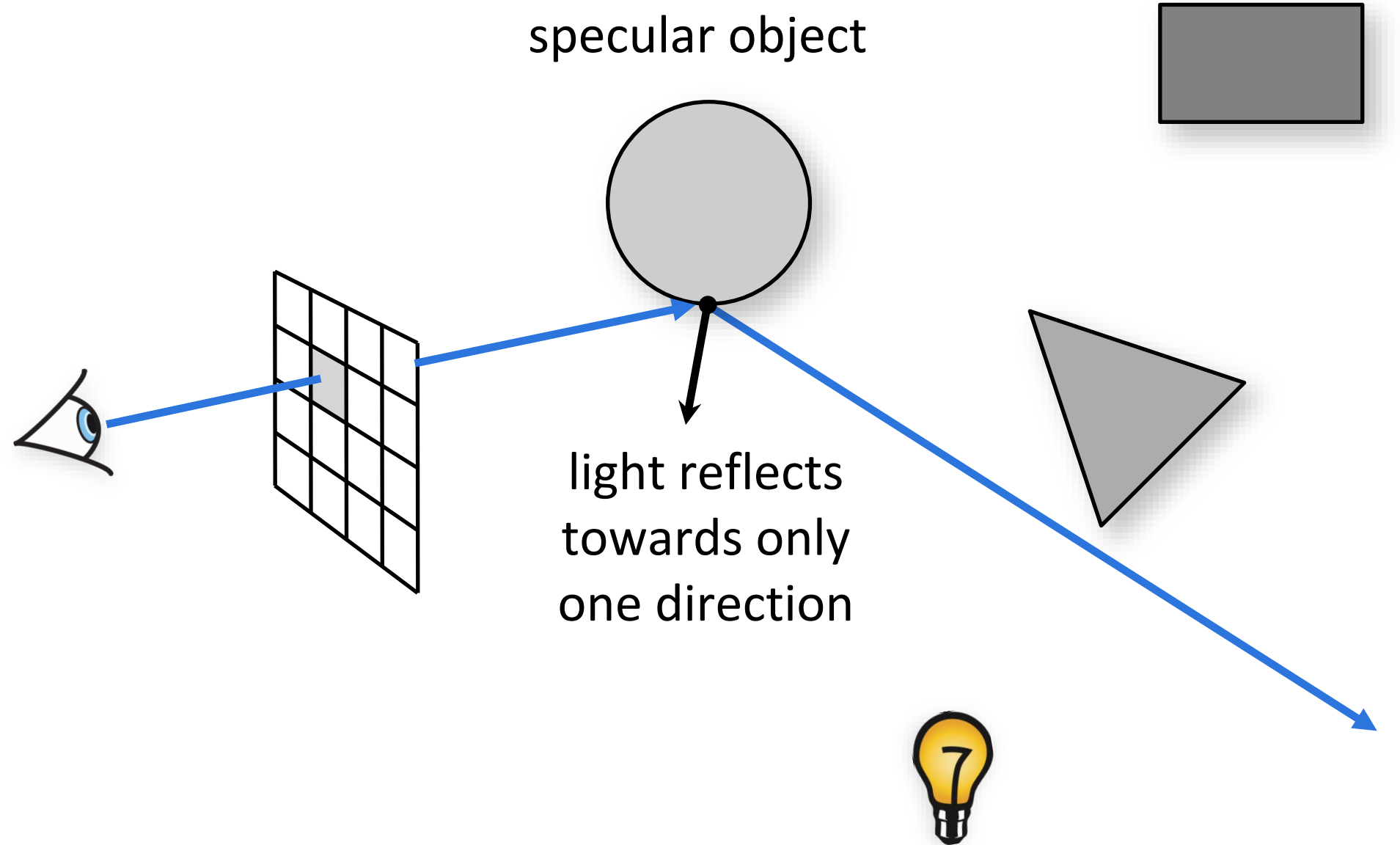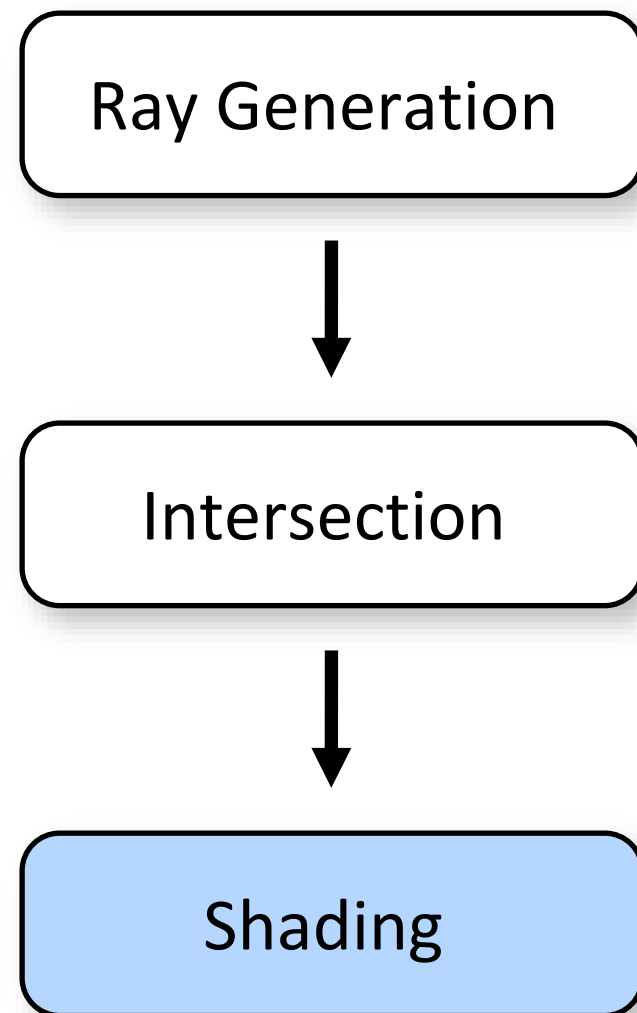
specular object

Ray Generation

↓

Intersection

↓

Shading

light reflects
towards only
one direction

What direction should we trace a new ray towards?

Basic Ray Tracing Pipeline

specular object

Ray Generation

Intersection

Shading

light reflects
towards only
one direction
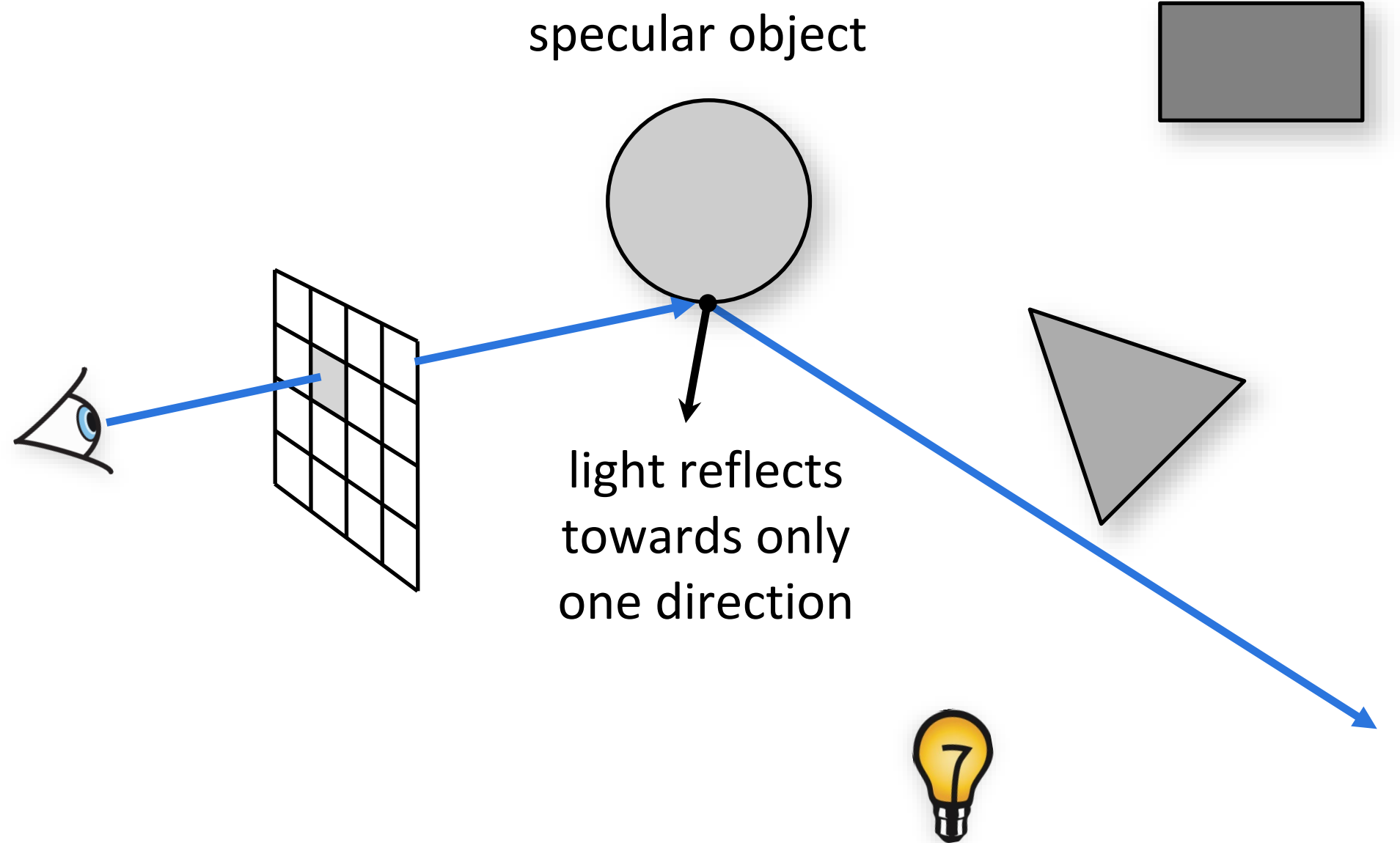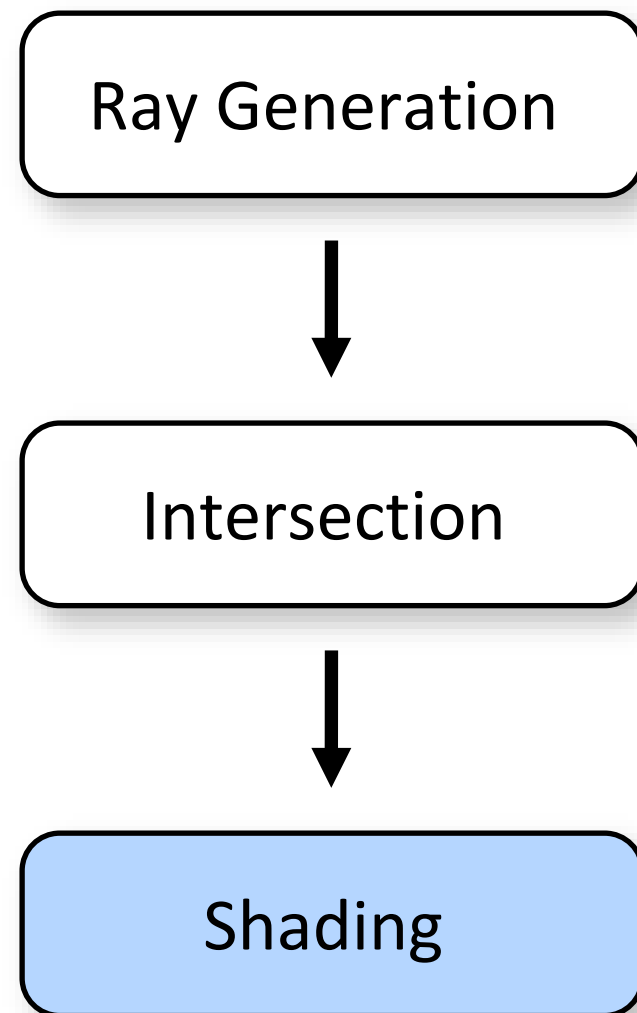
What direction should we trace a new ray towards?

- Just use law of mirror reflection, no need for random selection!

Mirror reflection

Consider perfectly shiny surface

- there's a reflection of other objects

Can render this using recursive ray tracing

- to find out mirror reflection color ask:
  "what color is seen from surface point in reflection direction?"

Mirror reflection

Evaluated by tracing a new ray:

$$L_r = k_r \text{trace}(\mathbf{p}, \mathbf{r})$$

reflected
light

reflection scaled
down/tinted
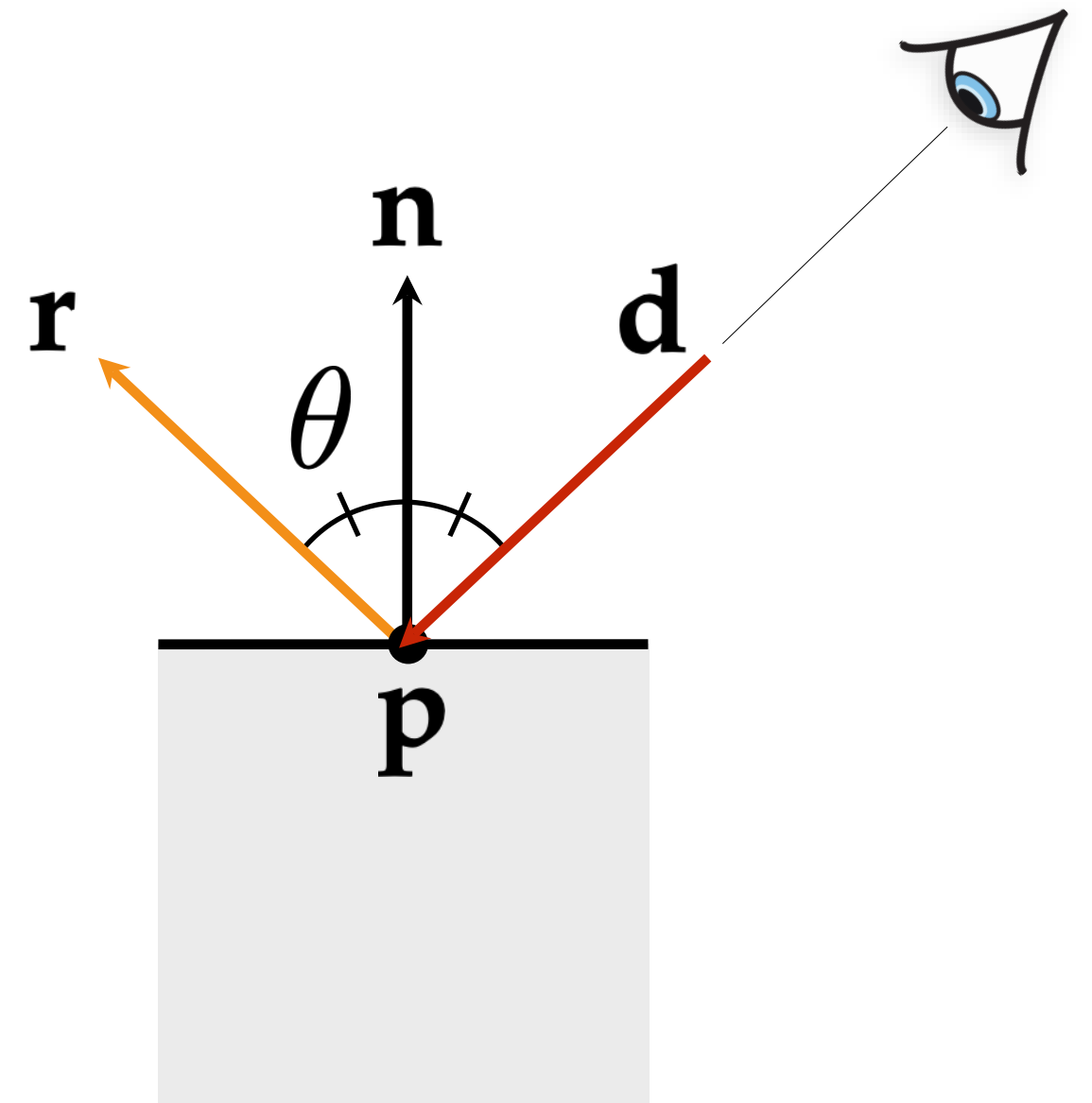
recursive
call

Mirror reflection

Evaluated by tracing a new ray:

$$L_r = k_r \text{trace}(\mathbf{p}, \mathbf{r})$$

reflected
light

reflection scaled
down/tinted

recursive
call

Implementation details:

- don't self-intersect ($t_{min} > \epsilon$)
- don't recurse indefinitely
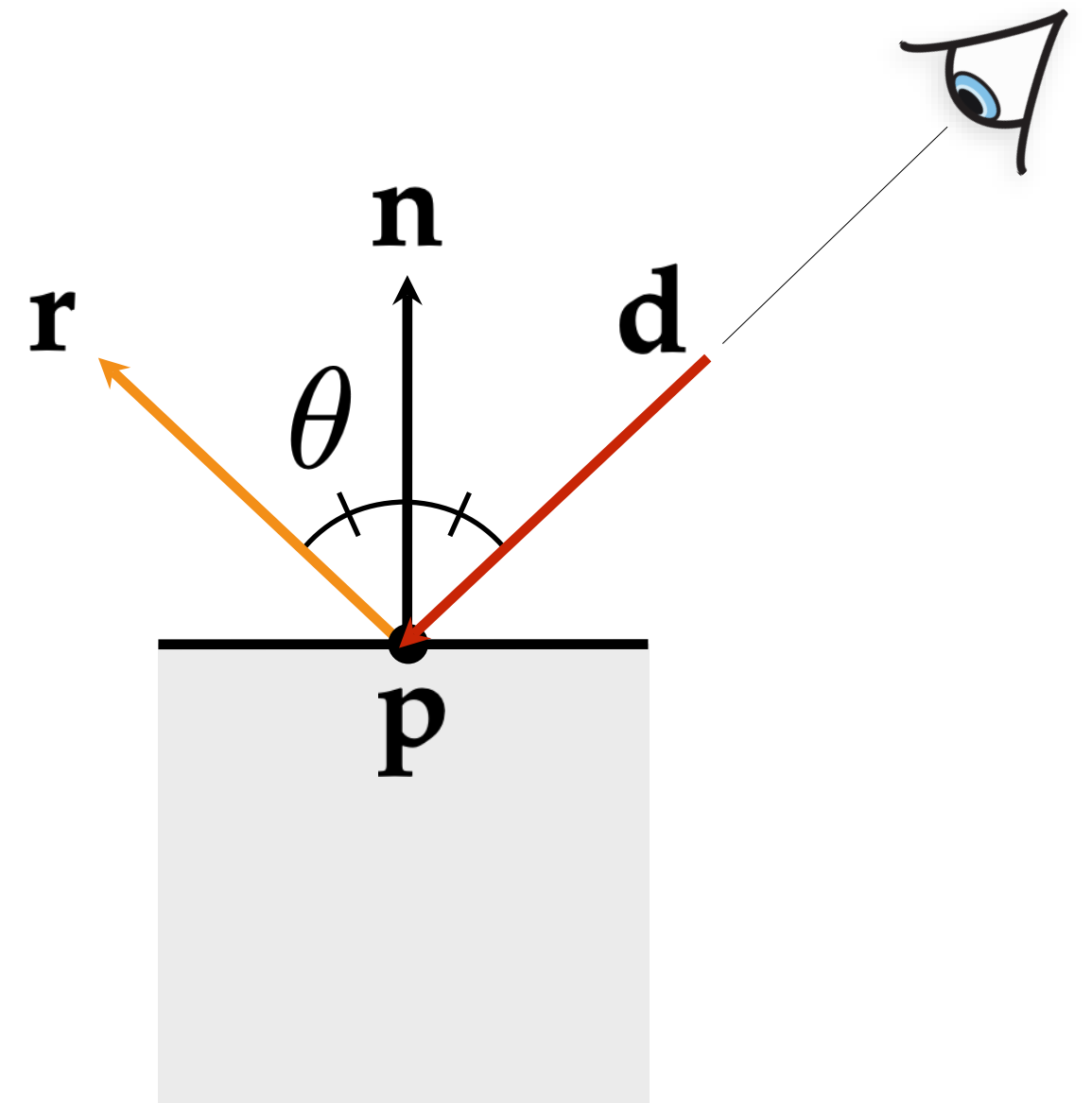
Same pseudo-code

```
Scene::trace(Ray ray)
   hit = surfaces.intersect(ray);
   if hit
      [col, sRay] = hit->mat->scatter(ray)
      return col * trace(sRay);
   else
      return backgroundColor;
```

Diffuse & mirror spheres

Mirror reflection
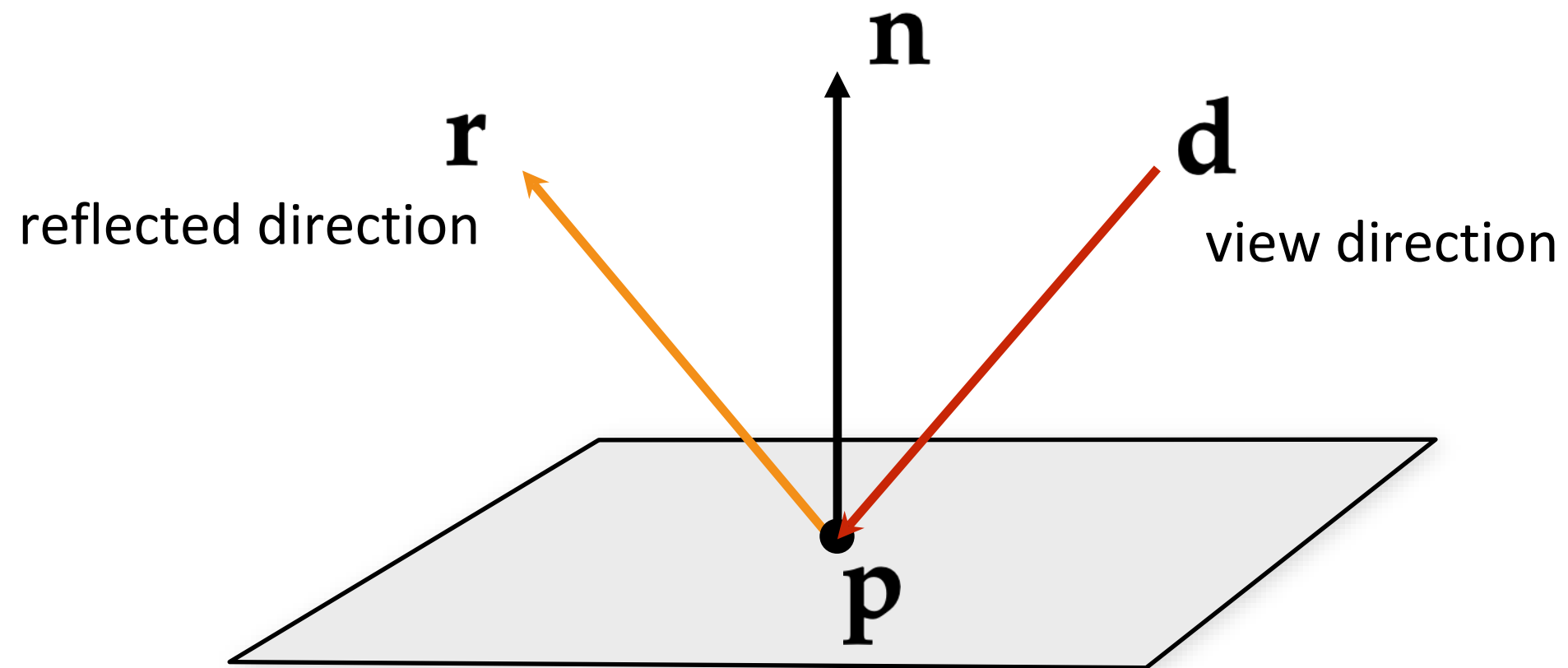
n

r

reflected direction

d

view direction

p

What <u>two</u> properties defined reflection direction?

Mirror reflection

reflected direction

view direction

θ θ
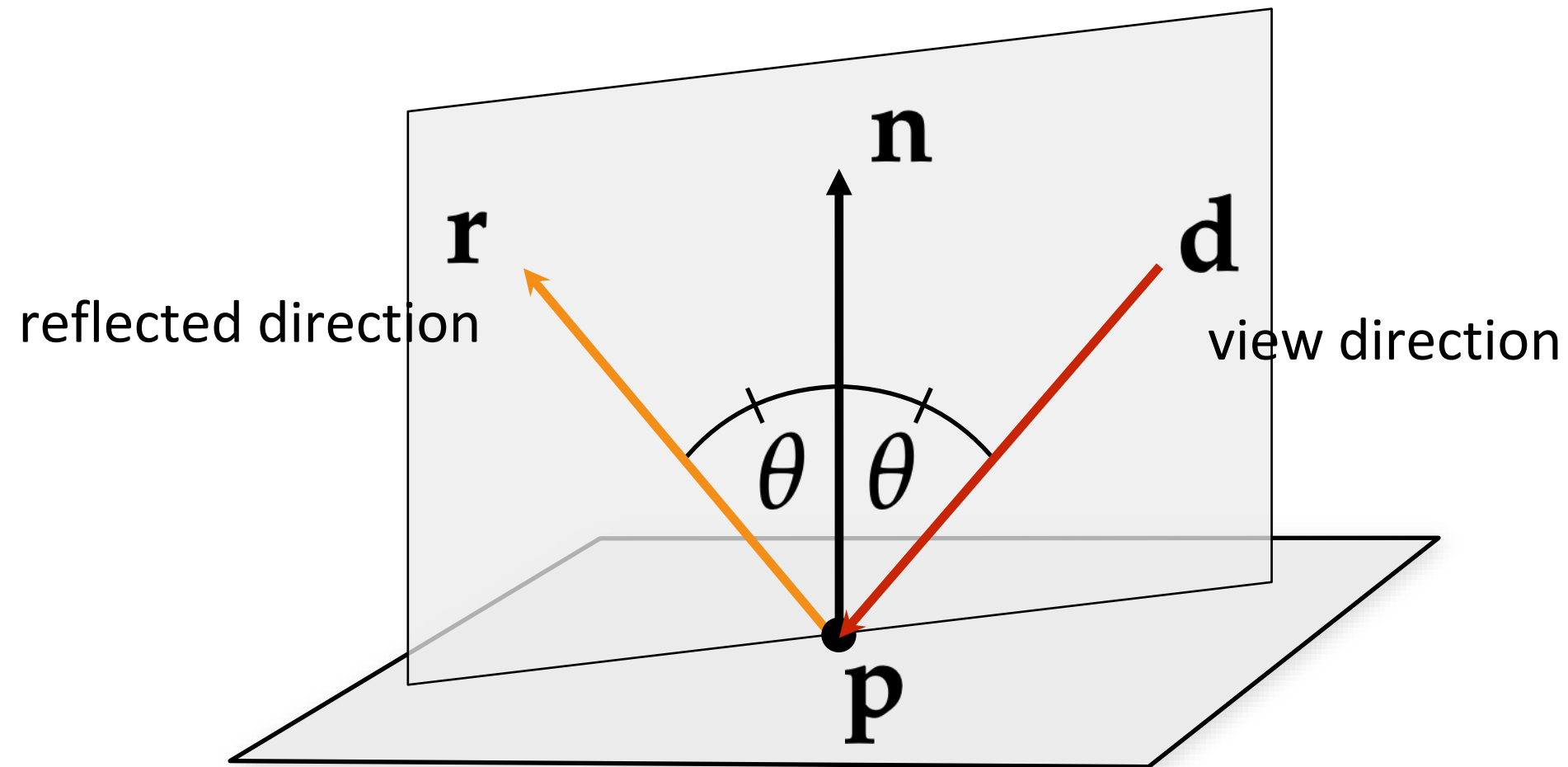
What <u>two</u> properties defined reflection direction?

- co-planar view direction, reflected direction, and normal direction

- equal angles between normal-view directions, and normal-reflected directions

Mirror reflection

reflected direction

view direction

Mirror reflection

reflected direction

view direction

Mirror reflection

reflected direction

view direction

$$-\mathbf{n}(\mathbf{n}\cdot\mathbf{d})$$
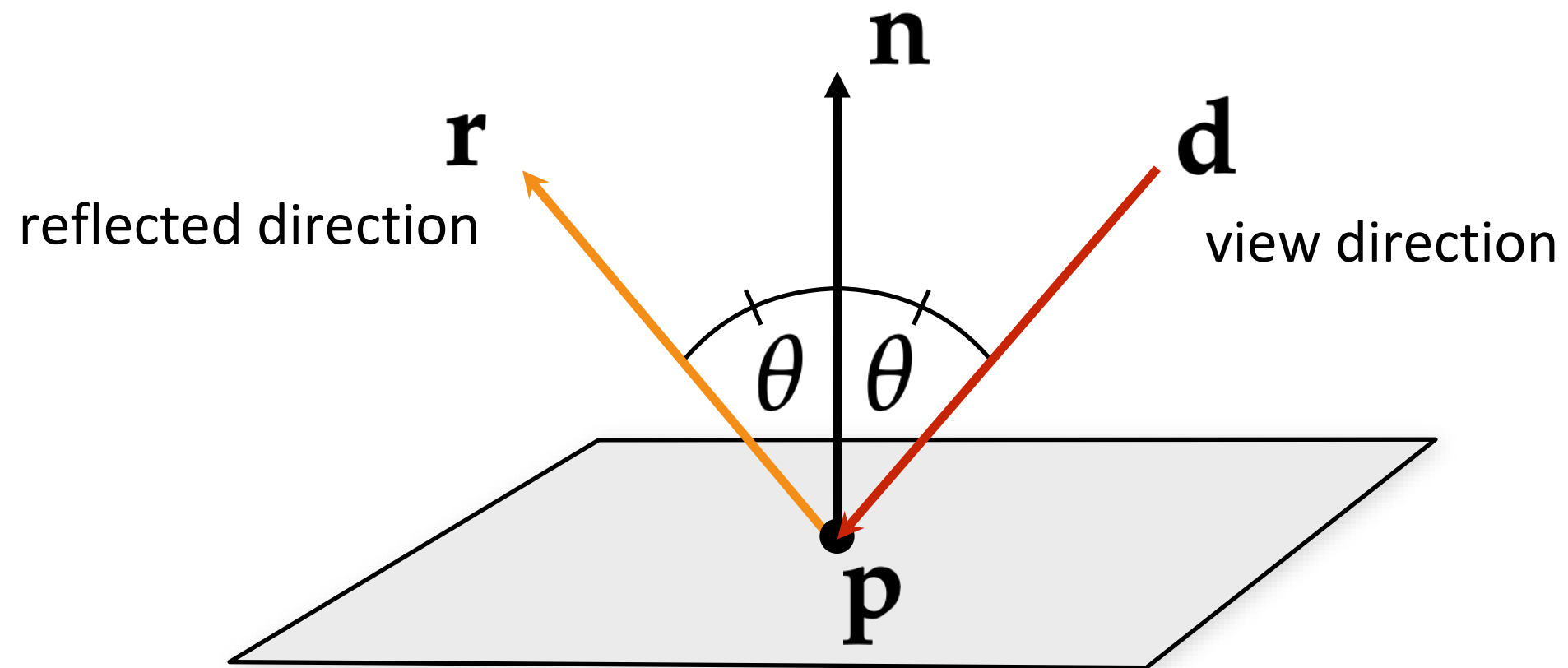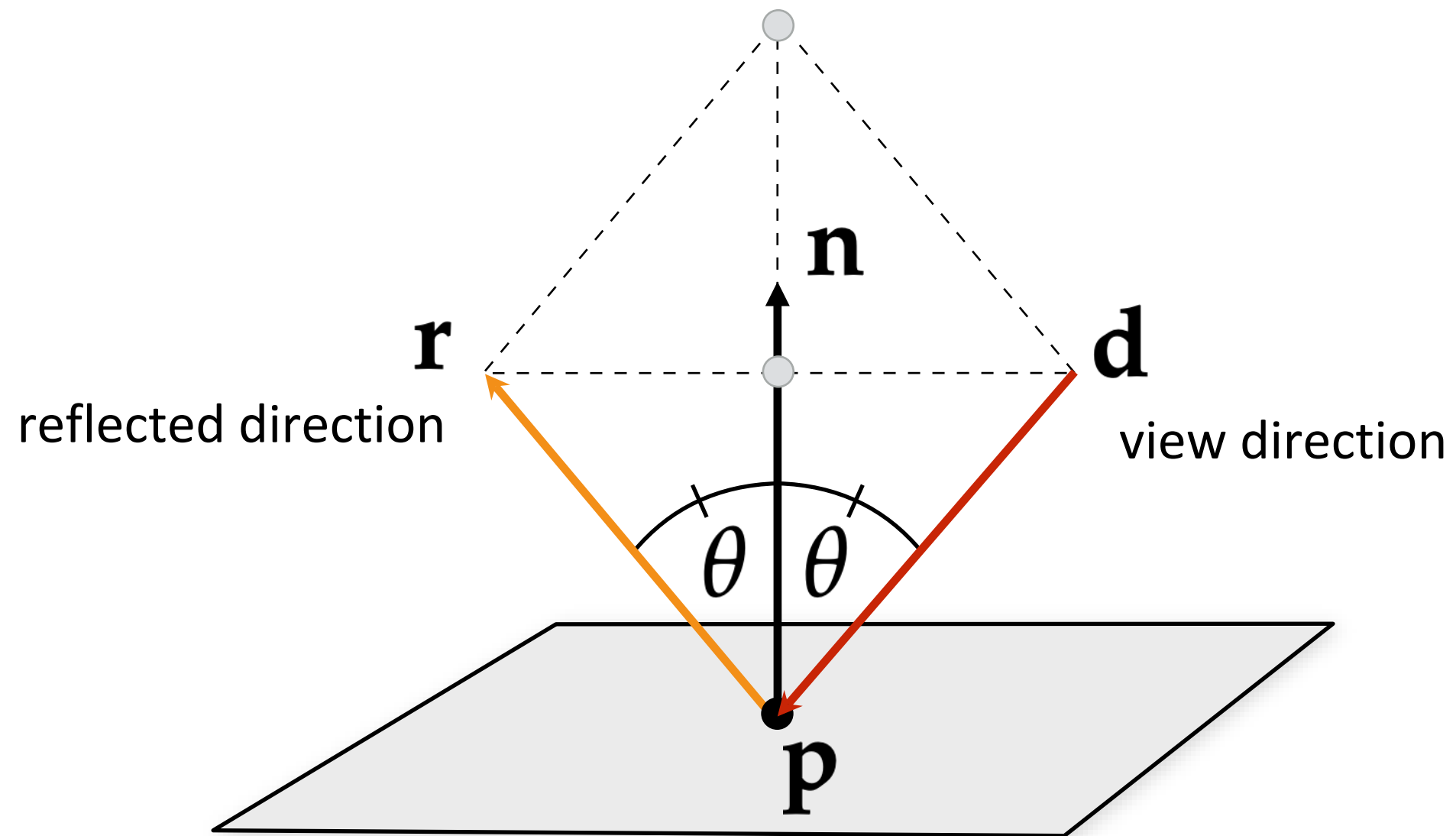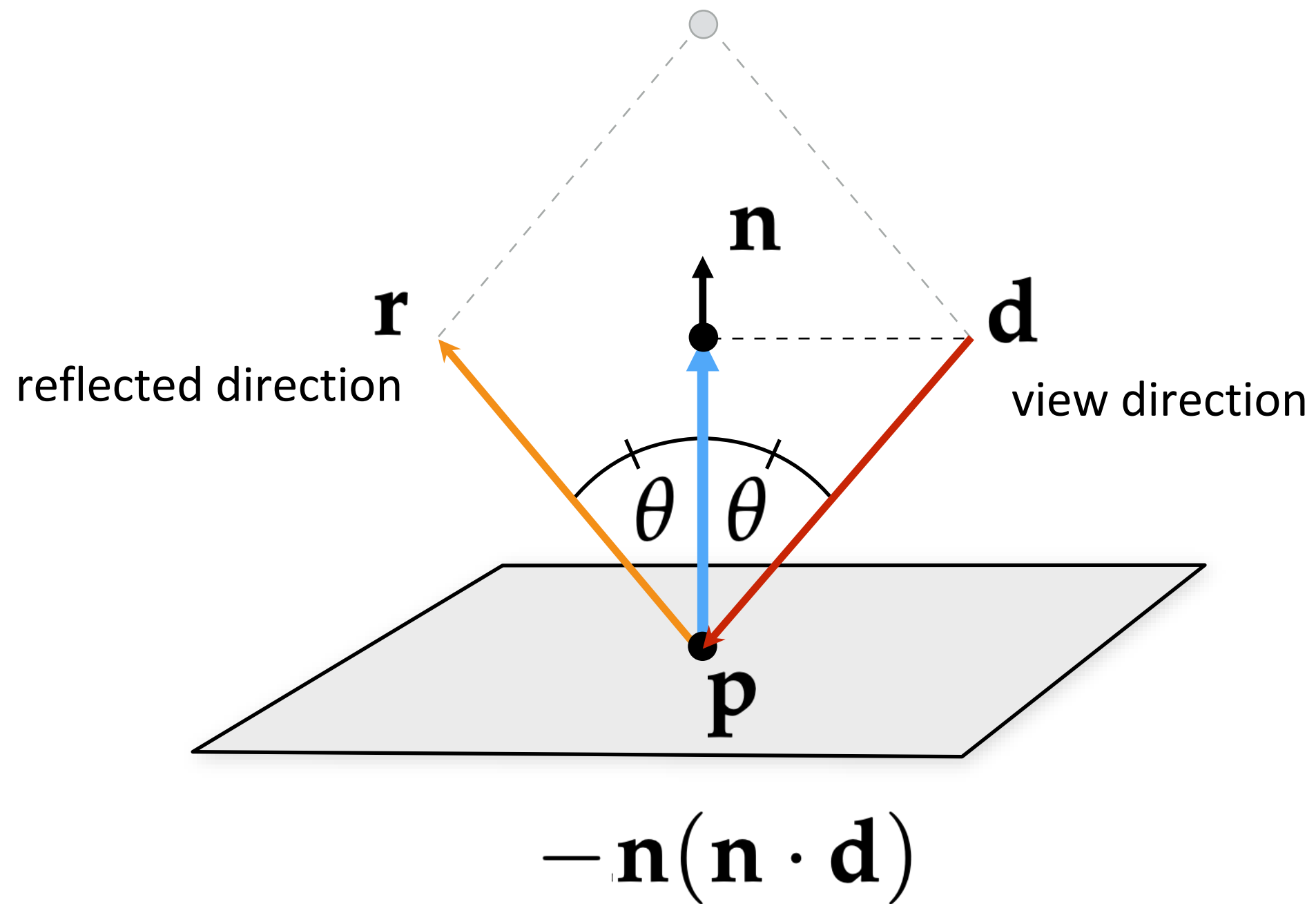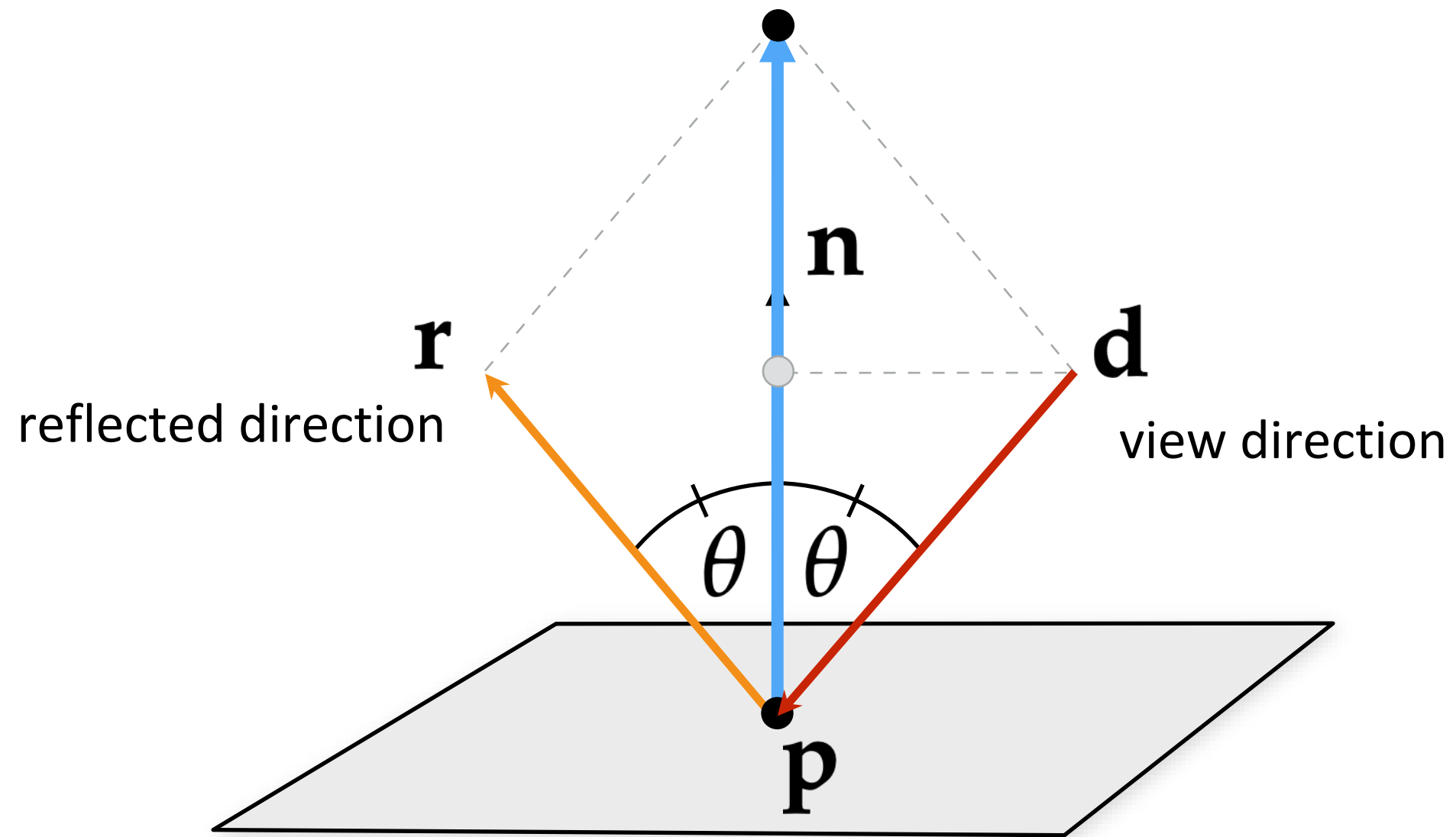
Mirror reflection

$$-2\mathbf{n}(\mathbf{n} \cdot \mathbf{d})$$

Mirror reflection

reflected direction

view direction
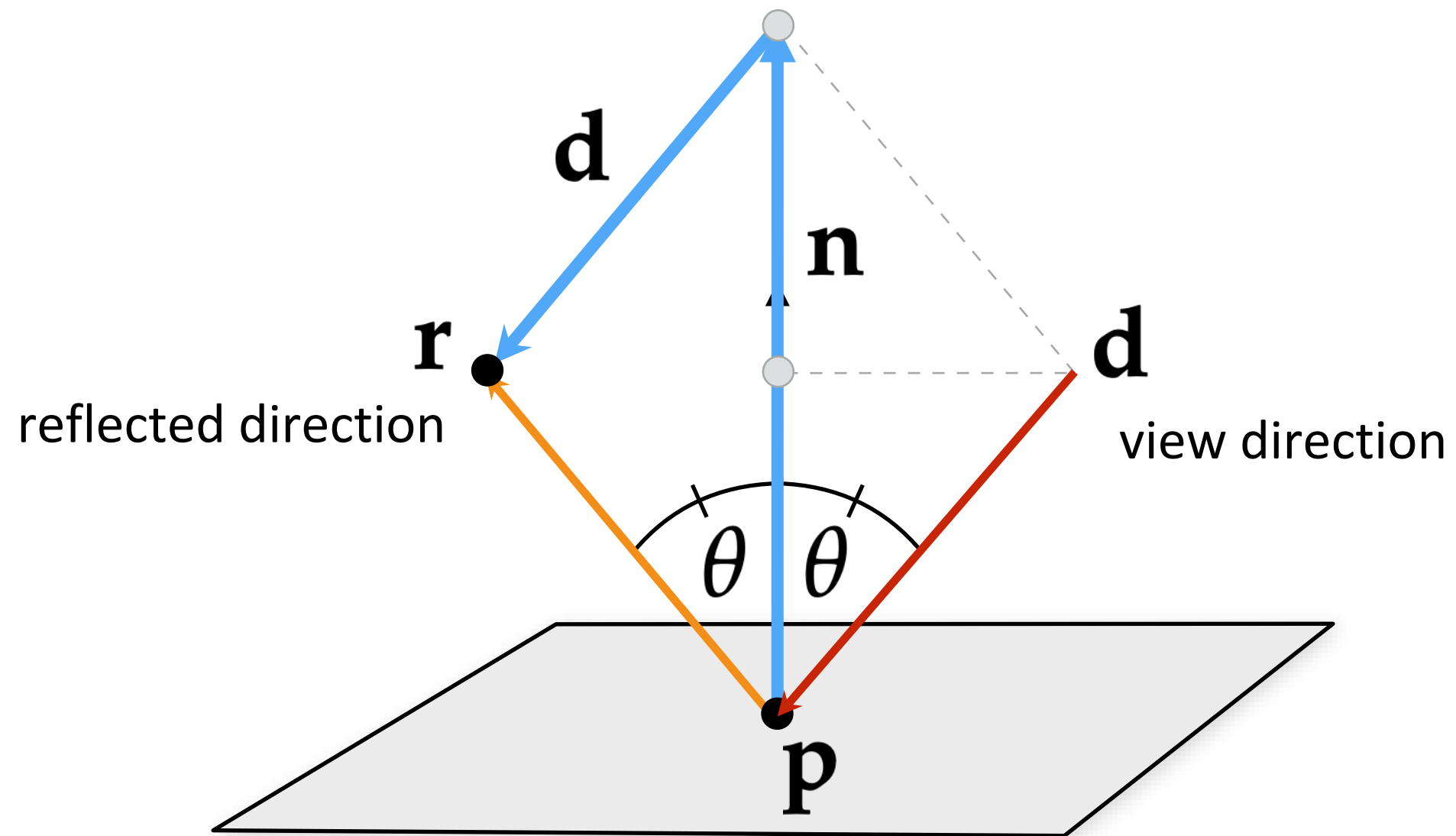
$$\mathbf{r} = -2\mathbf{n}(\mathbf{n} \cdot \mathbf{d}) + \mathbf{d}$$

Specular refraction
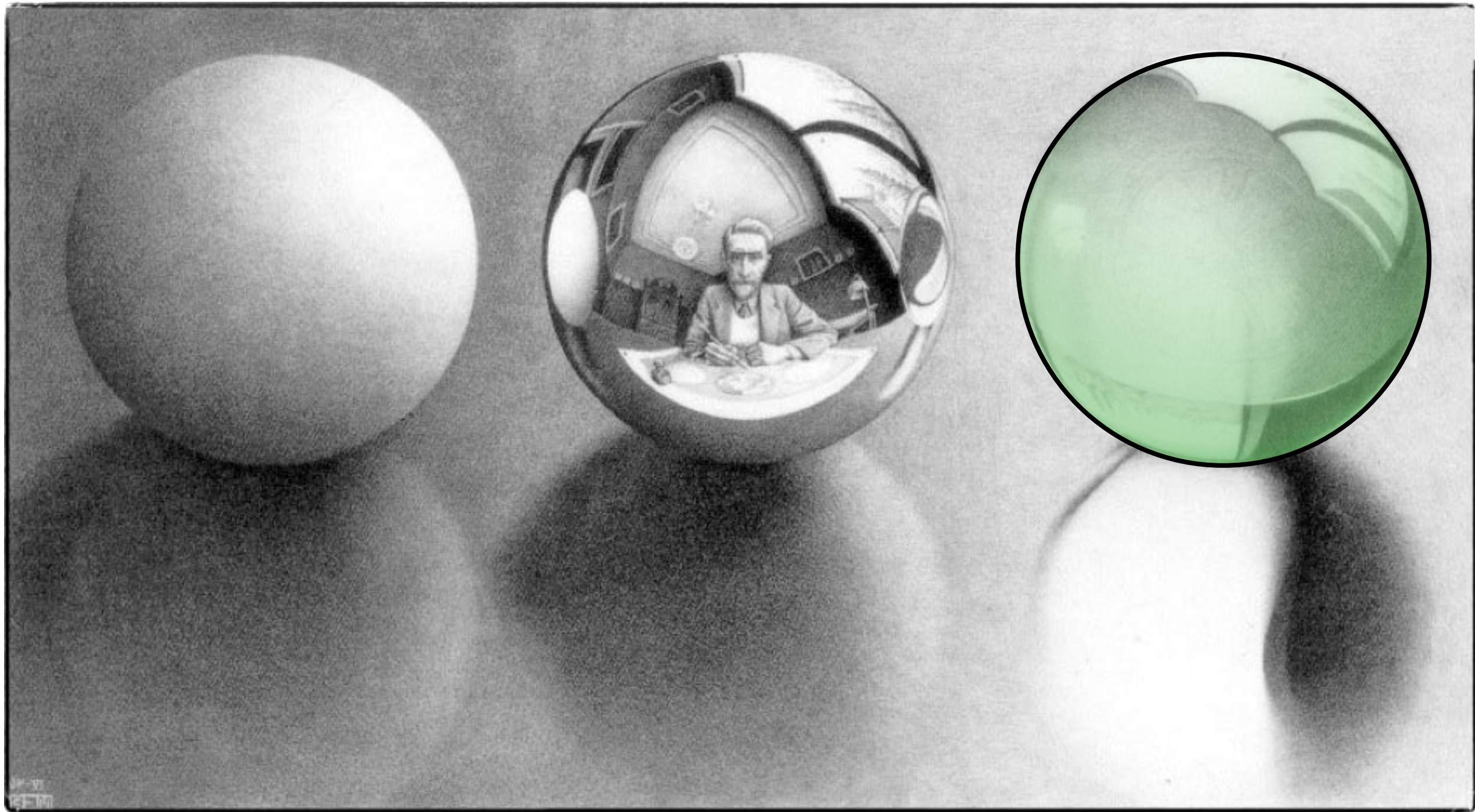
Refraction

Refraction
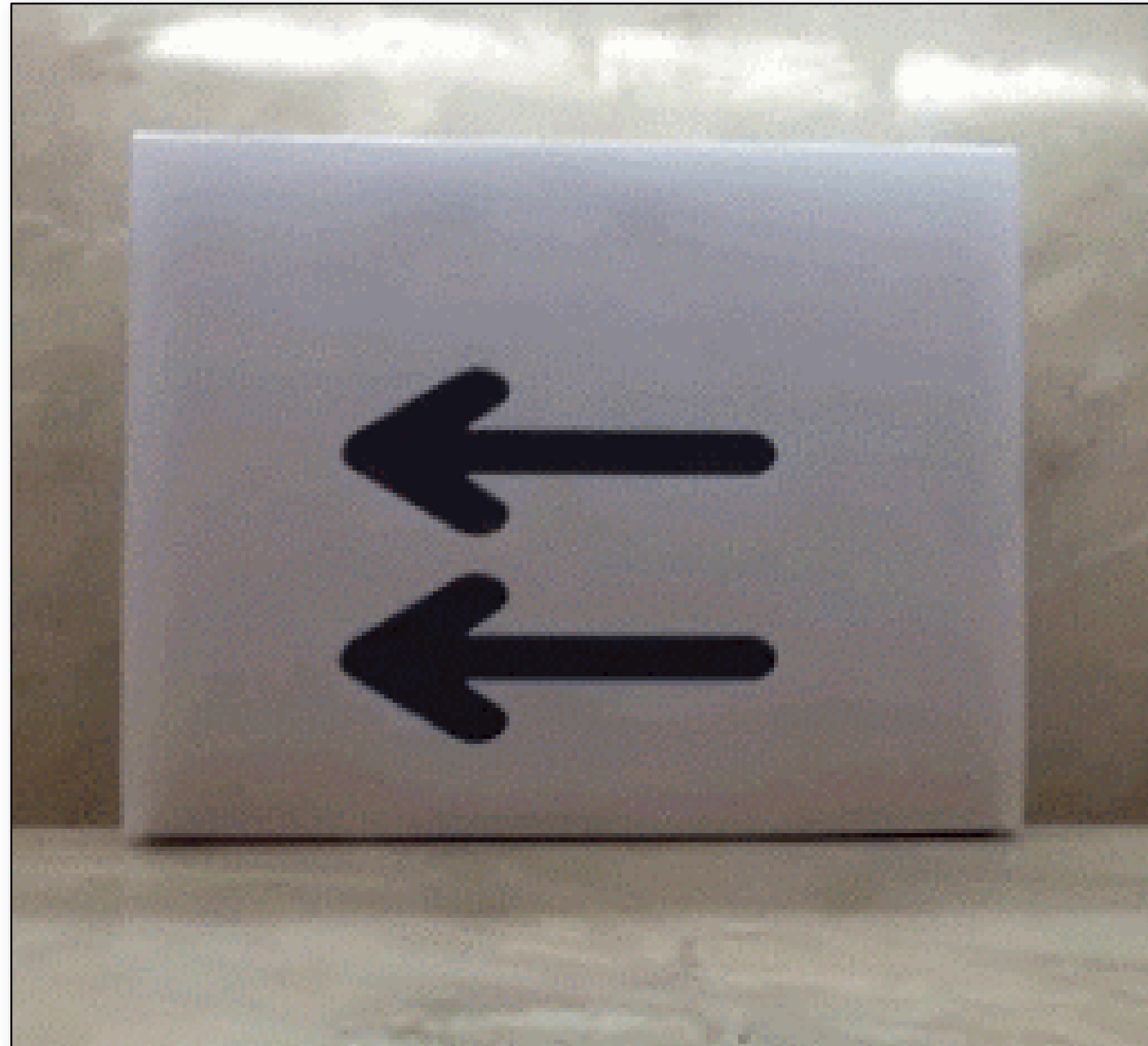
Index of Refraction

Speed of light in vacuum / speed of light in medium

Some values of η	
Vacuum	1
Air at STP	1.00029
Ice	1.31
Water	1.33
Crown glass	1.52 - 1.65
Diamond	2.417

Specular transmission/refraction

Materials like water, glass, etc., also refract/bend light

Trace a recursive ray in the refraction direction

$$L_t = k_t \text{trace}(\mathbf{p}, \mathbf{t})$$

refracted light

refraction scaled down

recursive call
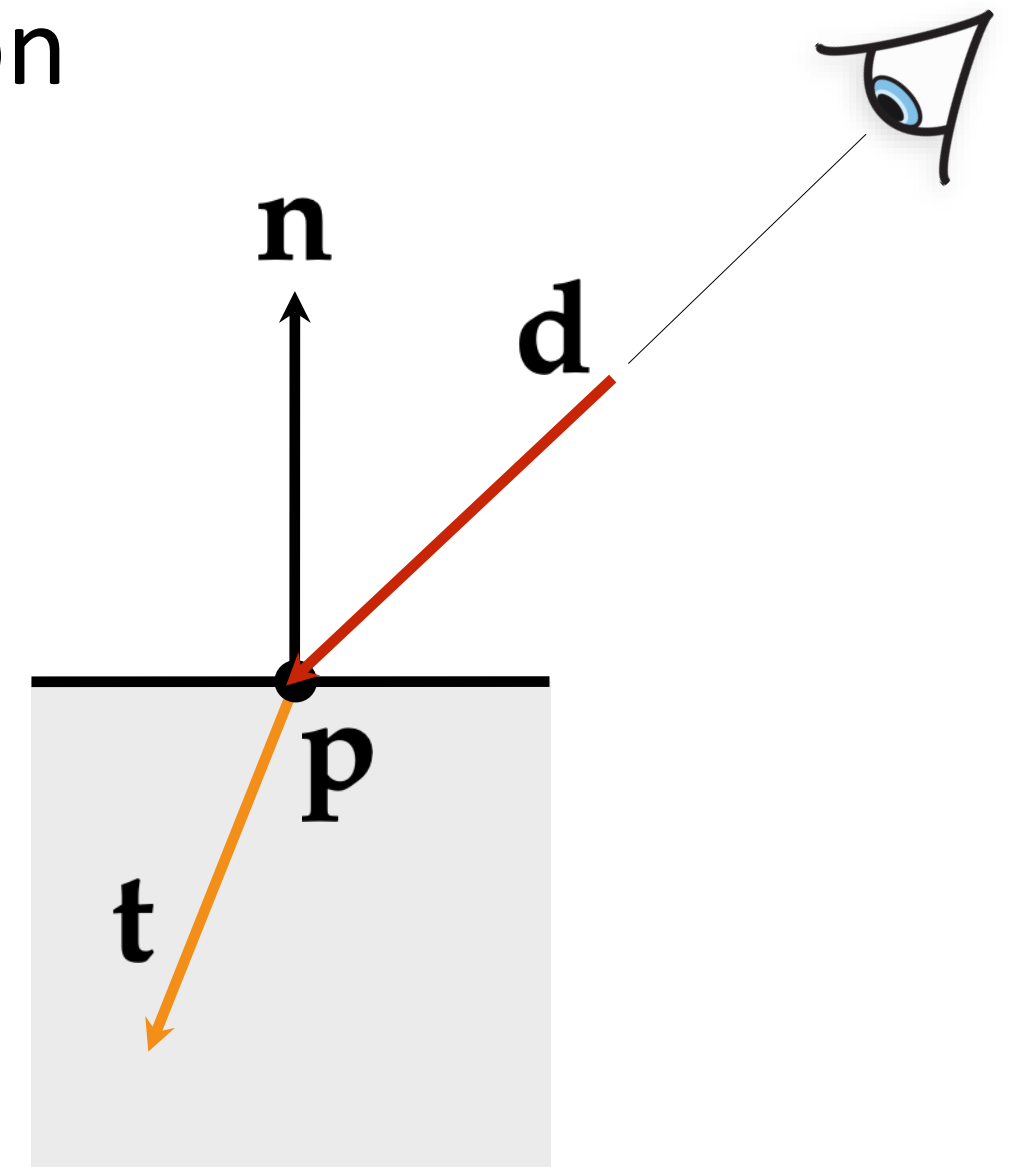
Specular transmission/refraction
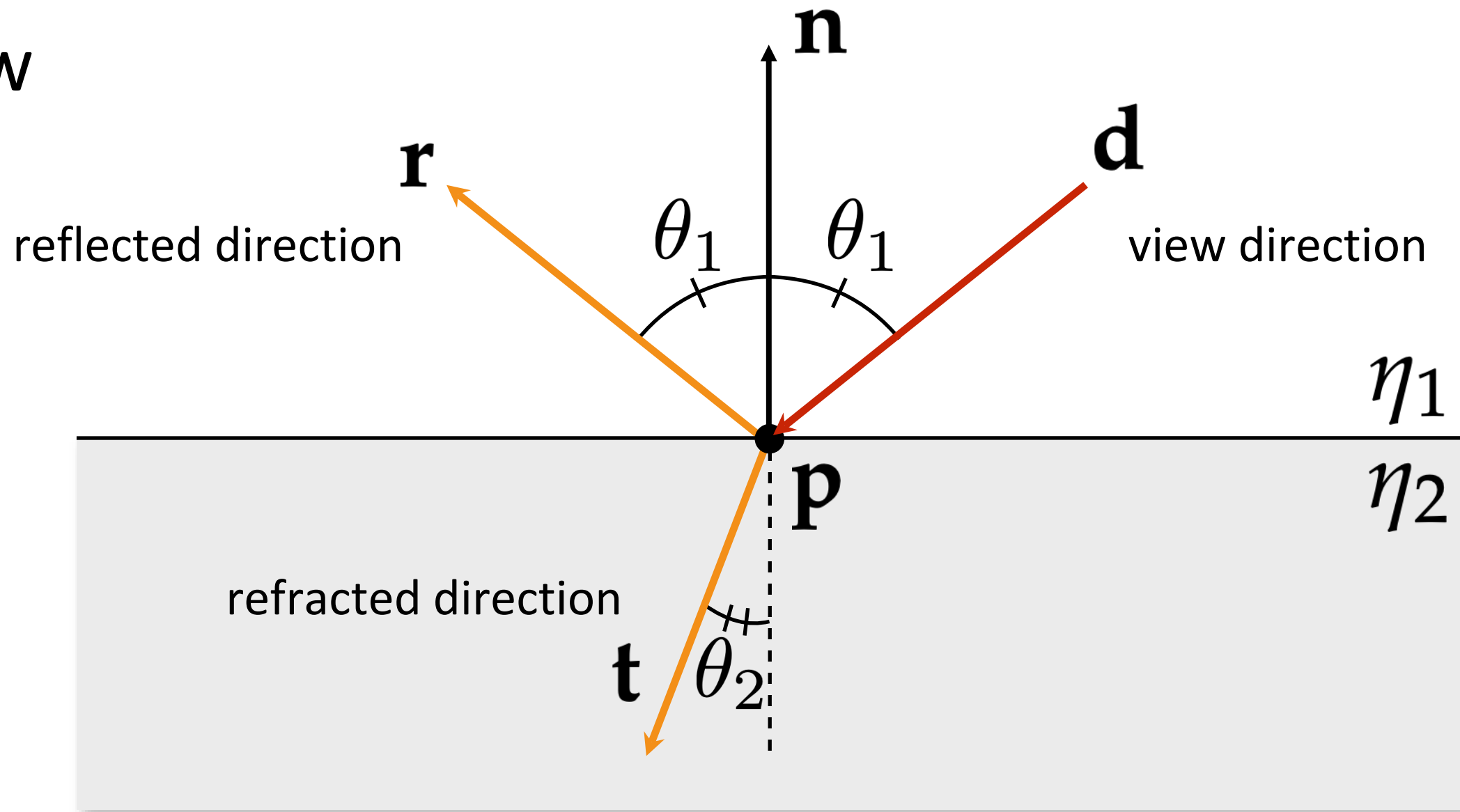
Snell's law

$$\eta_1 \sin \theta_1 = \eta_2 \sin \theta_2$$

Specular transmission/refraction

Snell's law
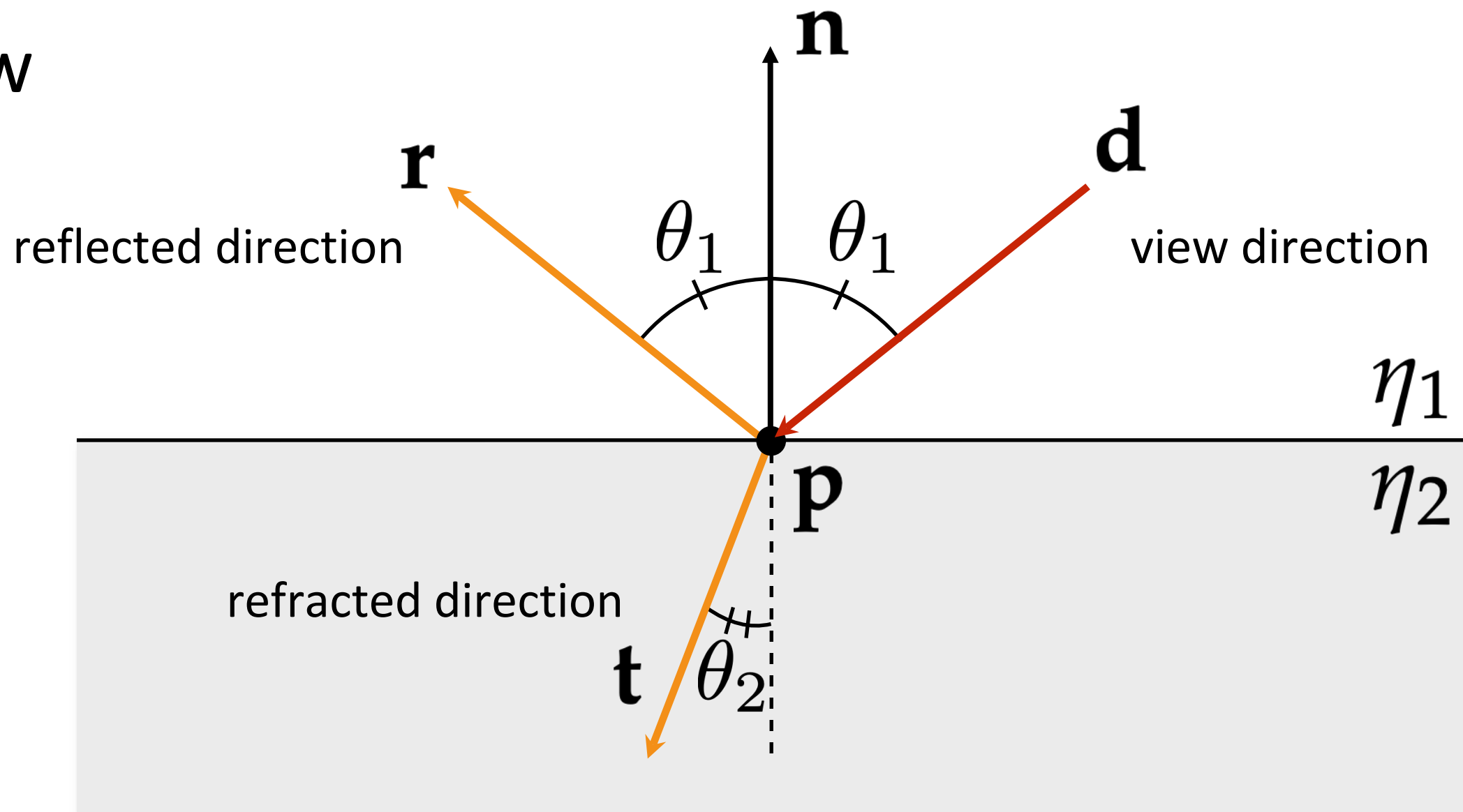
$$\mathbf{t} = \eta_1/\eta_2 \left(\mathbf{d} - (\mathbf{d} \cdot \mathbf{n})\,\mathbf{n}\right) - \mathbf{n}\sqrt{1 - \eta_1^2/\eta_2^2 \left(1 - (\mathbf{d} \cdot \mathbf{n})^2\right)}$$

Index of Refraction

Speed of light in vacuum / speed of light in medium

Some values of η	
Vacuum	1
Air at STP	1.00029
Ice	1.31
Water	1.33
Crown glass	1.52 - 1.65
Diamond	2.417

These are actually wavelength dependent!

Dispersion

Refraction in a Waterdrop
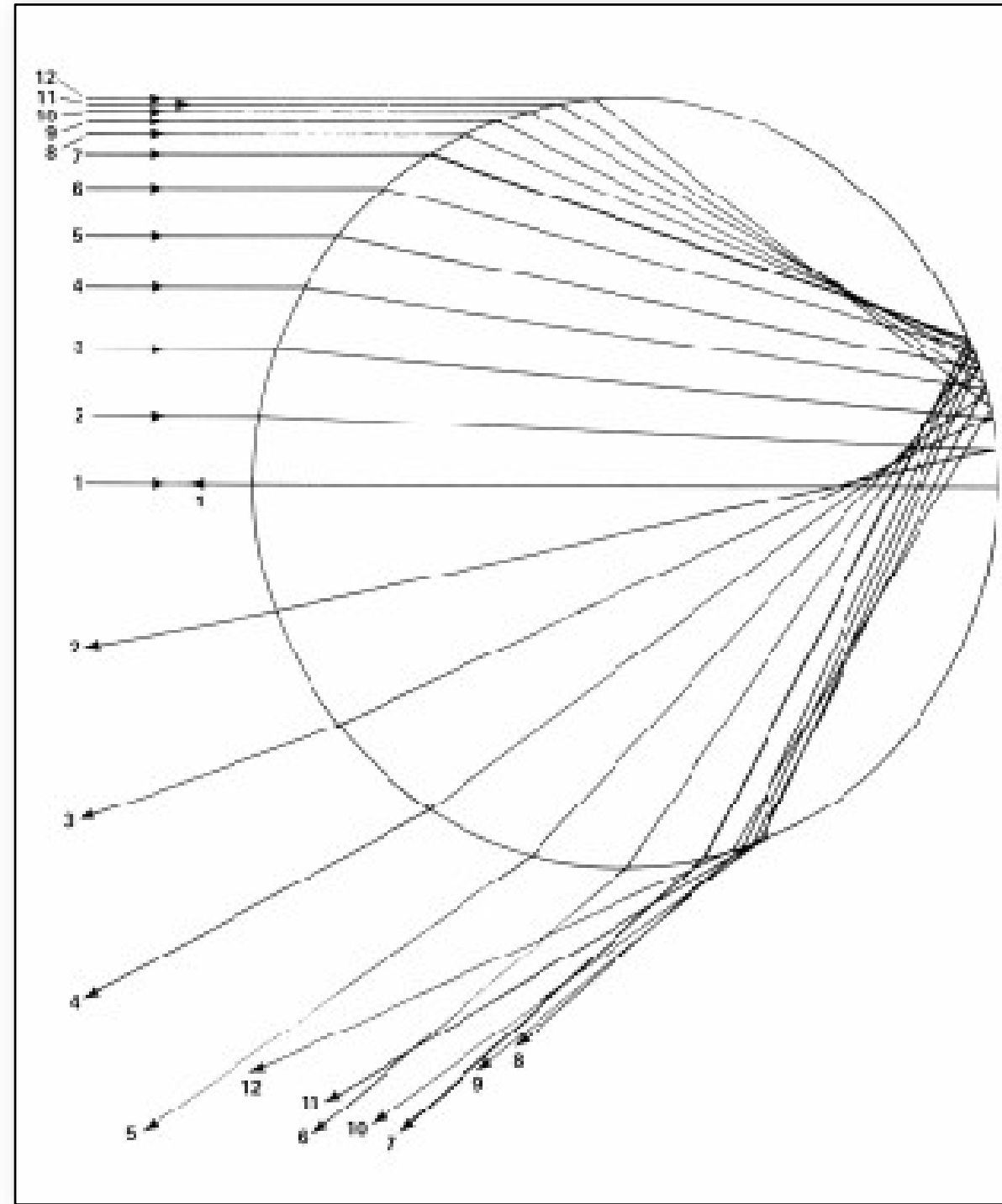
Double rainbow all the way across the sky!

Dispersion: "Halos" and "Sun dogs"

Halos and Sundogs

Sundogs are produced by hexagonal plate shaped ice crystals drifting with their large faces nearly horizontal.

Sundog rays pass through crystal faces inclined 60° to each other.

©Les Cowley

60°

22° and greater

Rays are deviated by 22° or more. Red is deviated least, giving the 'dog' a red inner edge.

All crystals refract the sun's rays but we see only those that glint their light towards our eyes. They are the crystals that, to us, are 22° or more from the sun and at the same altitude. Their collective glints form the sundogs.

Dispersion

What is this dark circle?

What is this dark circle?

Called
"Snell's window"

Caused by total
internal reflection
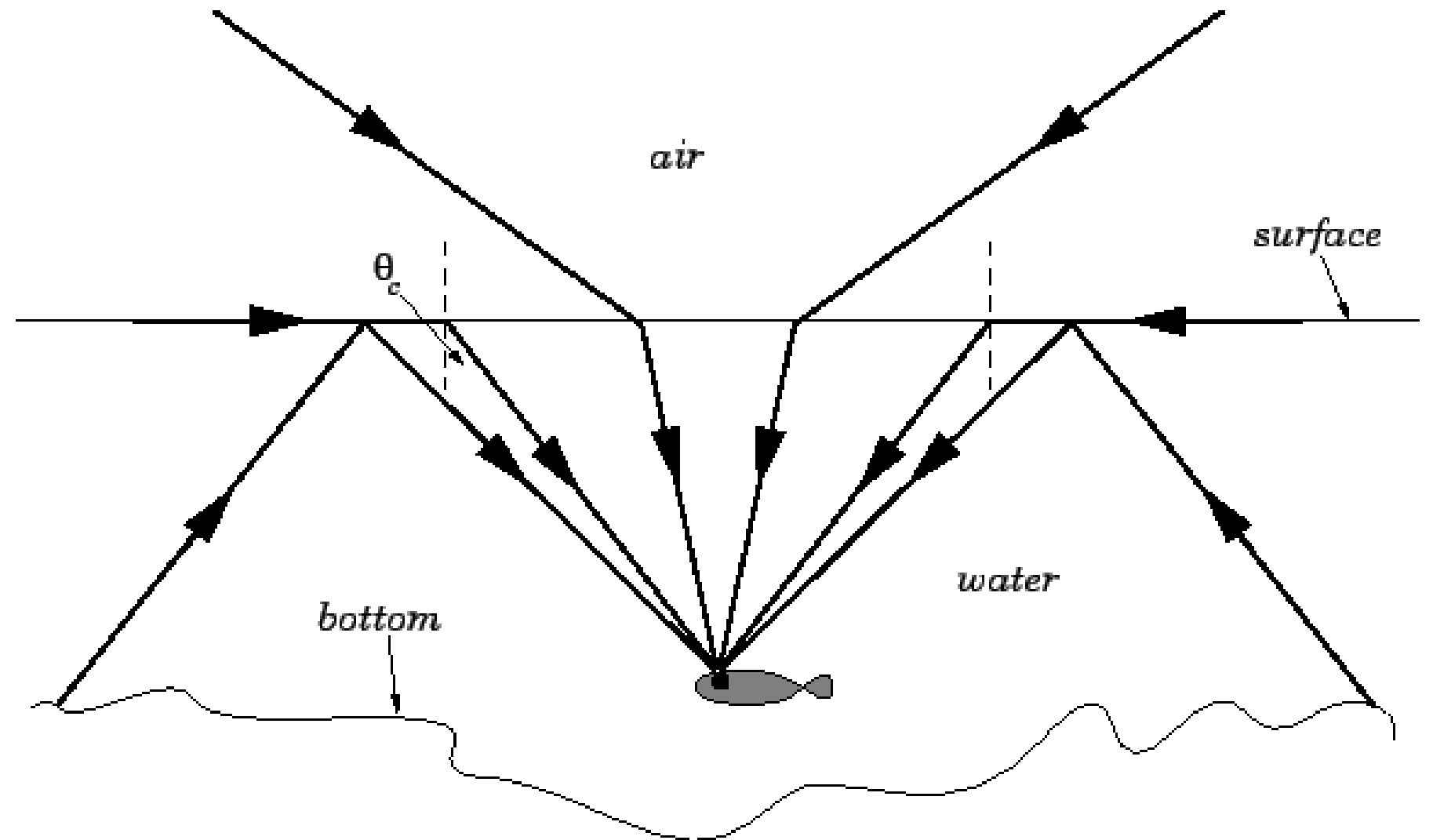
Recall…

Snell's law
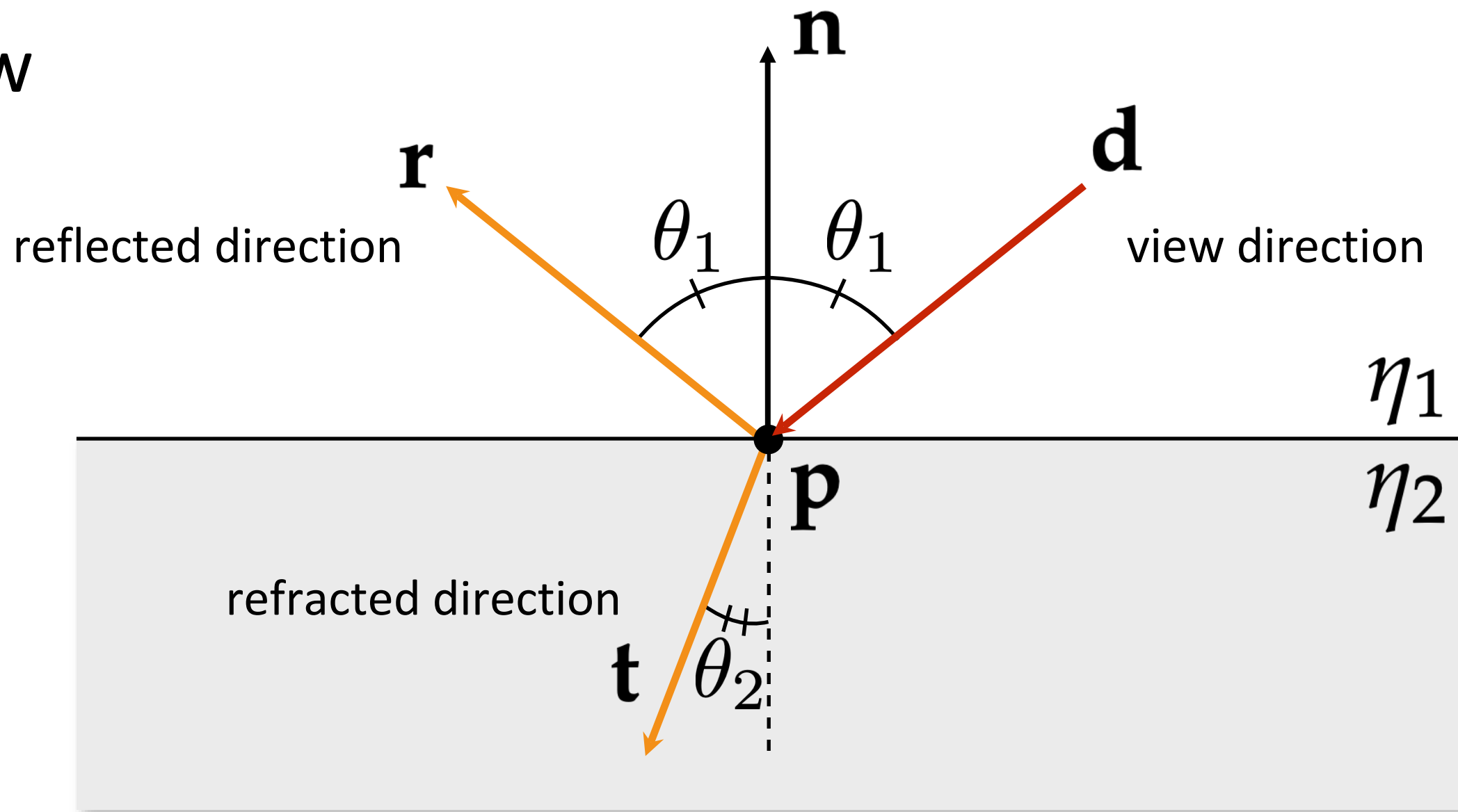
$$\mathbf{t} = \eta_1/\eta_2 \left(\mathbf{d} - (\mathbf{d} \cdot \mathbf{n})\,\mathbf{n}\right) - \mathbf{n}\sqrt{1 - \eta_1^2/\eta_2^2 \left(1 - (\mathbf{d} \cdot \mathbf{n})^2\right)}$$
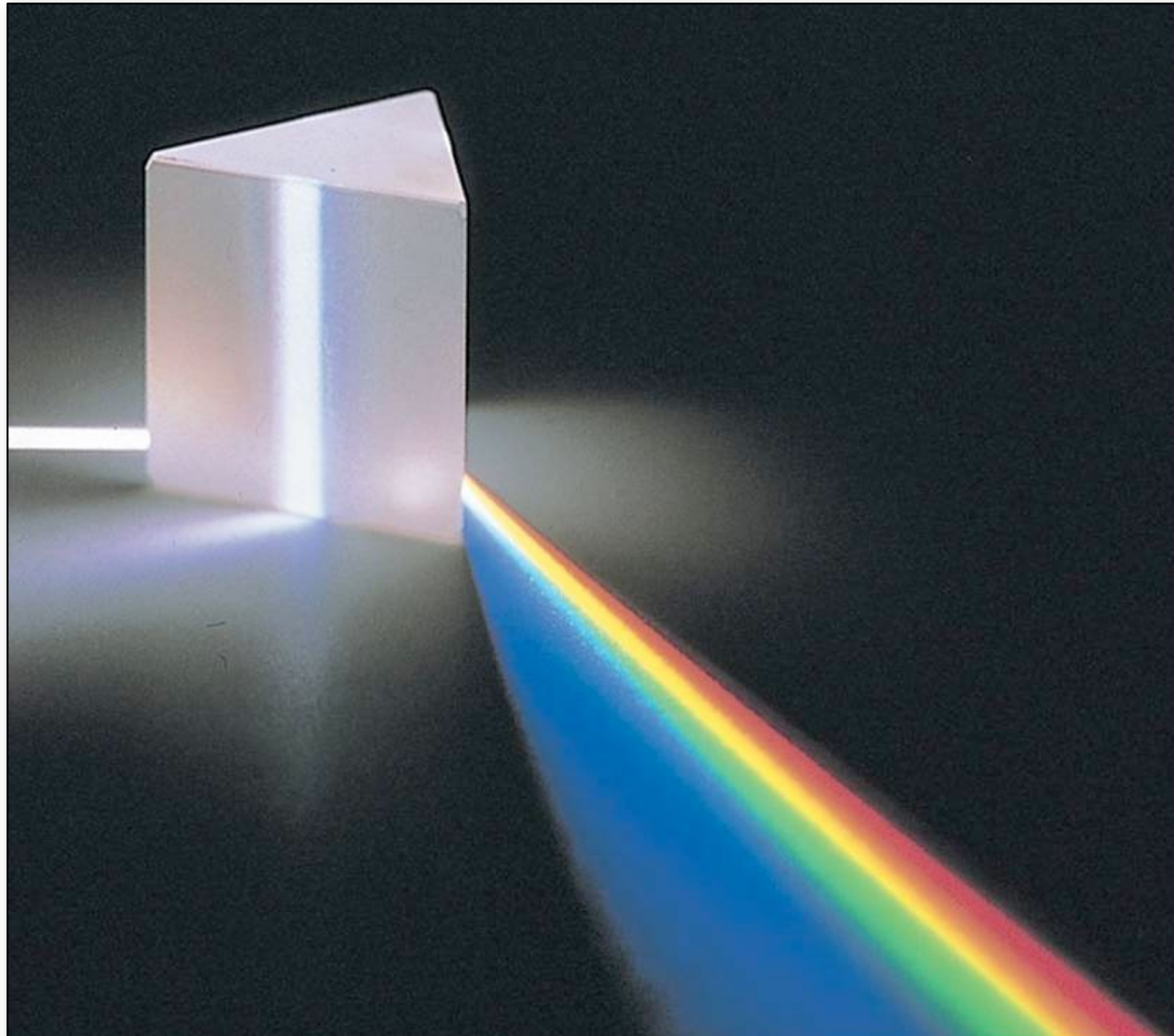
When can total internal reflection happen?

Can only happen when the ray starts in the higher index medium

Total Internal Reflection
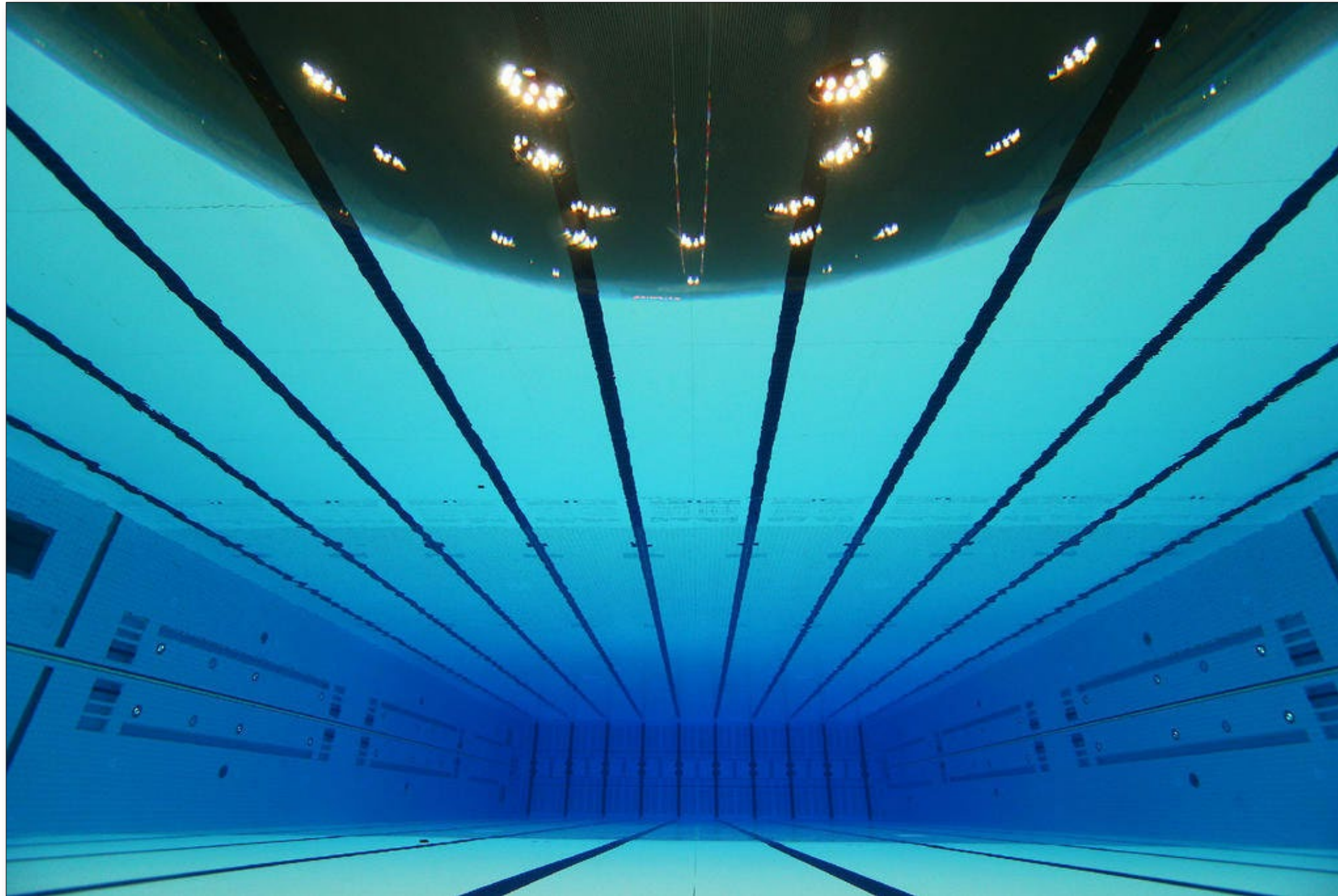
Total Internal Reflection

Total Internal Reflection
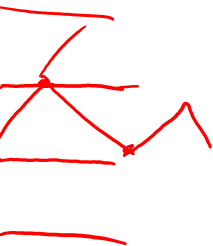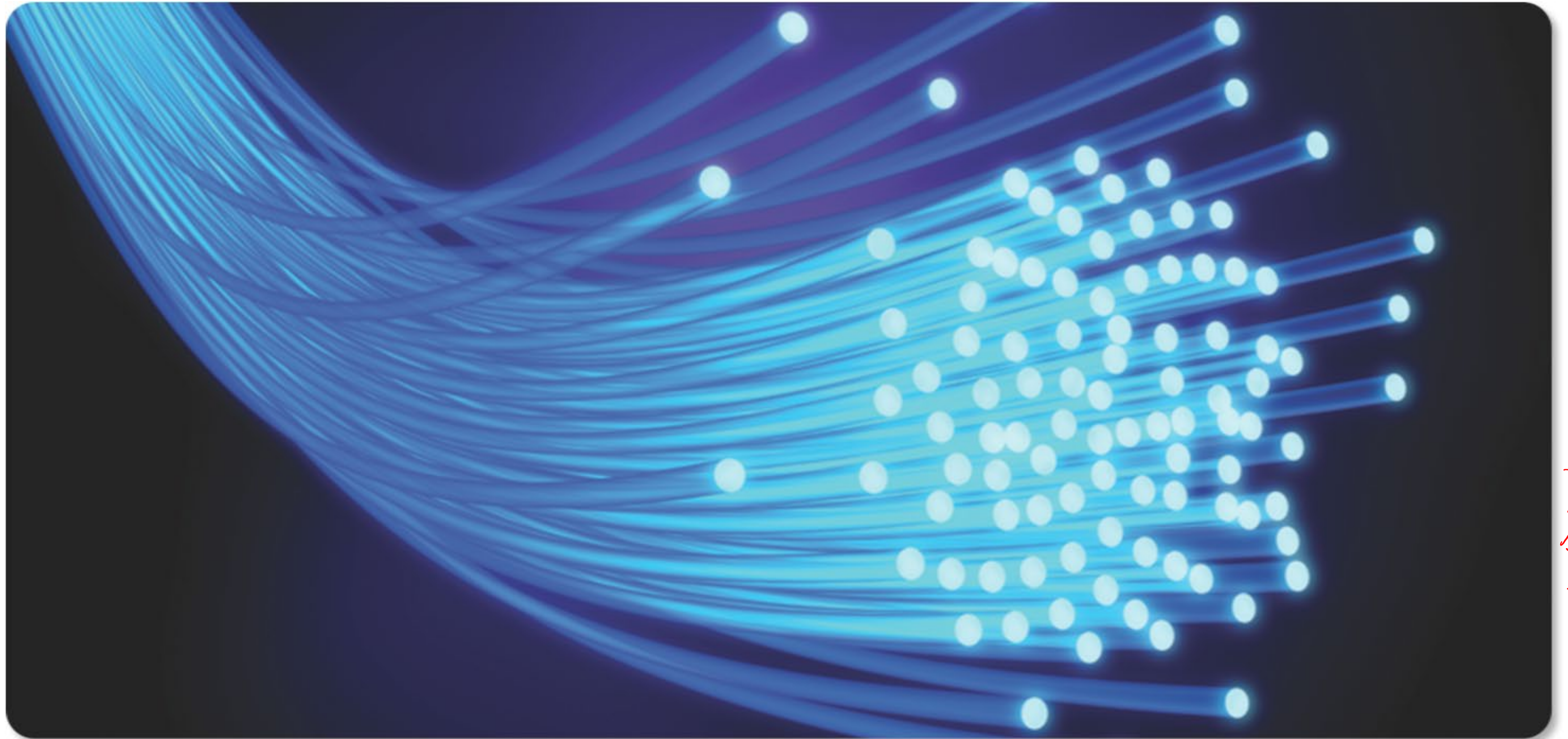
Total Internal Reflection

Reflection vs. Refraction

How much light is reflected vs. refracted?

- in reality determined by "Fresnel equations"

Fresnel Equations

Reflection and *refraction* from smooth *dielectric* (e.g. glass) surfaces

Reflection from *conducting* (e.g. metal) surfaces
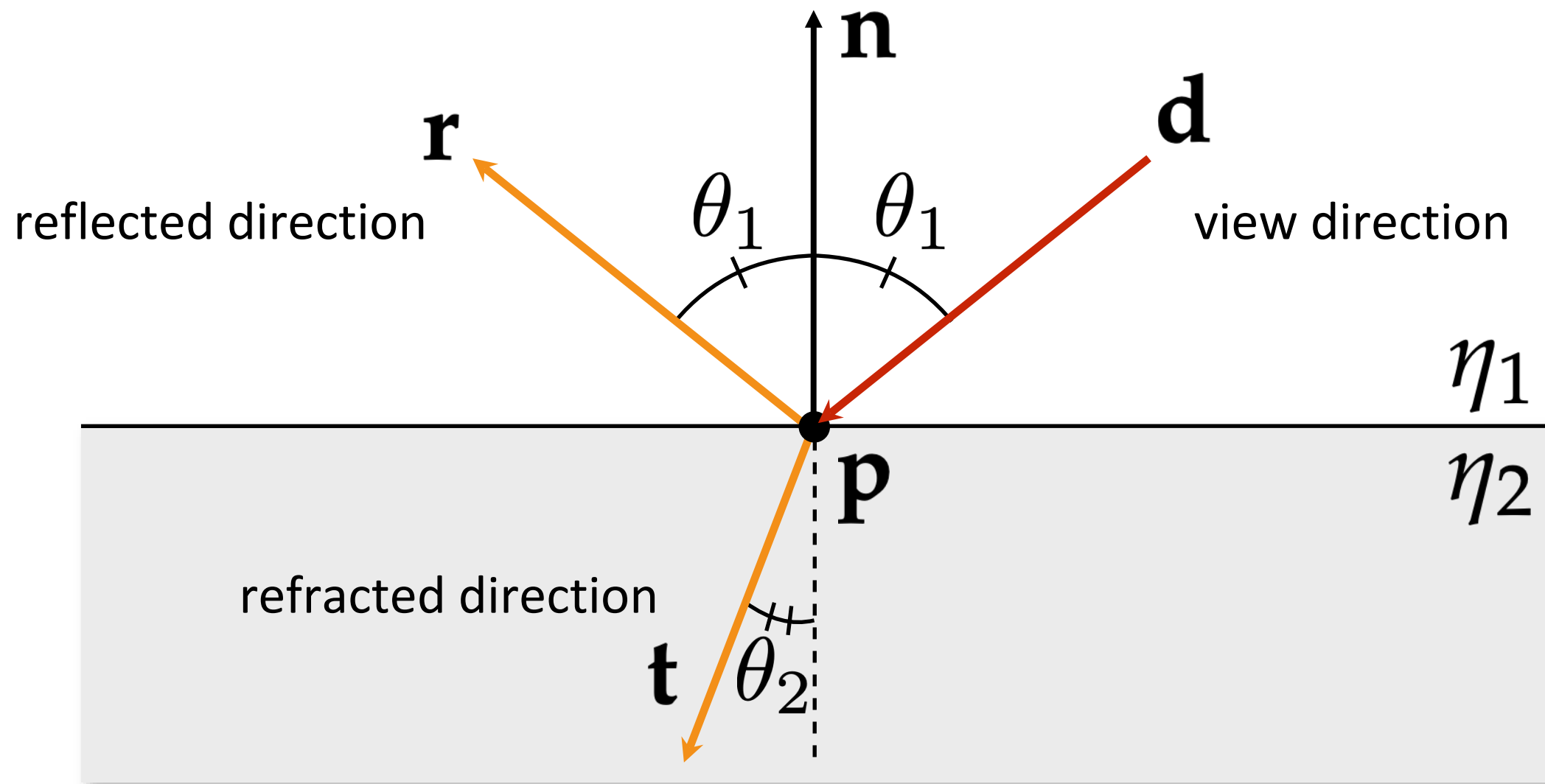
Derived from Maxwell equations

Involves polarization of the wave

Fresnel Equations for Dielectrics

Reflection of light polarized parallel and perpendicular to the plane of refraction

$$\rho_{\parallel} = \frac{\eta_2 \cos\theta_1 - \eta_1 \cos\theta_2}{\eta_2 \cos\theta_1 + \eta_1 \cos\theta_2}$$

reflected: $\quad F_r = \frac{1}{2}\left(\rho_{\parallel}^2 + \rho_{\perp}^2\right)$

$$\rho_{\perp} = \frac{\eta_1 \cos\theta_1 - \eta_2 \cos\theta_2}{\eta_1 \cos\theta_1 + \eta_2 \cos\theta_2}$$

refracted: $\quad F_t = 1 - F_r$

What's happening in this photo?

Polarizing Filter

Polarization

Without Polarizer

With Polarizing Filter

Polarization

Without Polarizer

With Polarizing Filter

Effect of Polarization

Effect of Polarization

Fresnel Equations for Dielectrics

Reflection of light polarized parallel and perpendicular to the plane of refraction
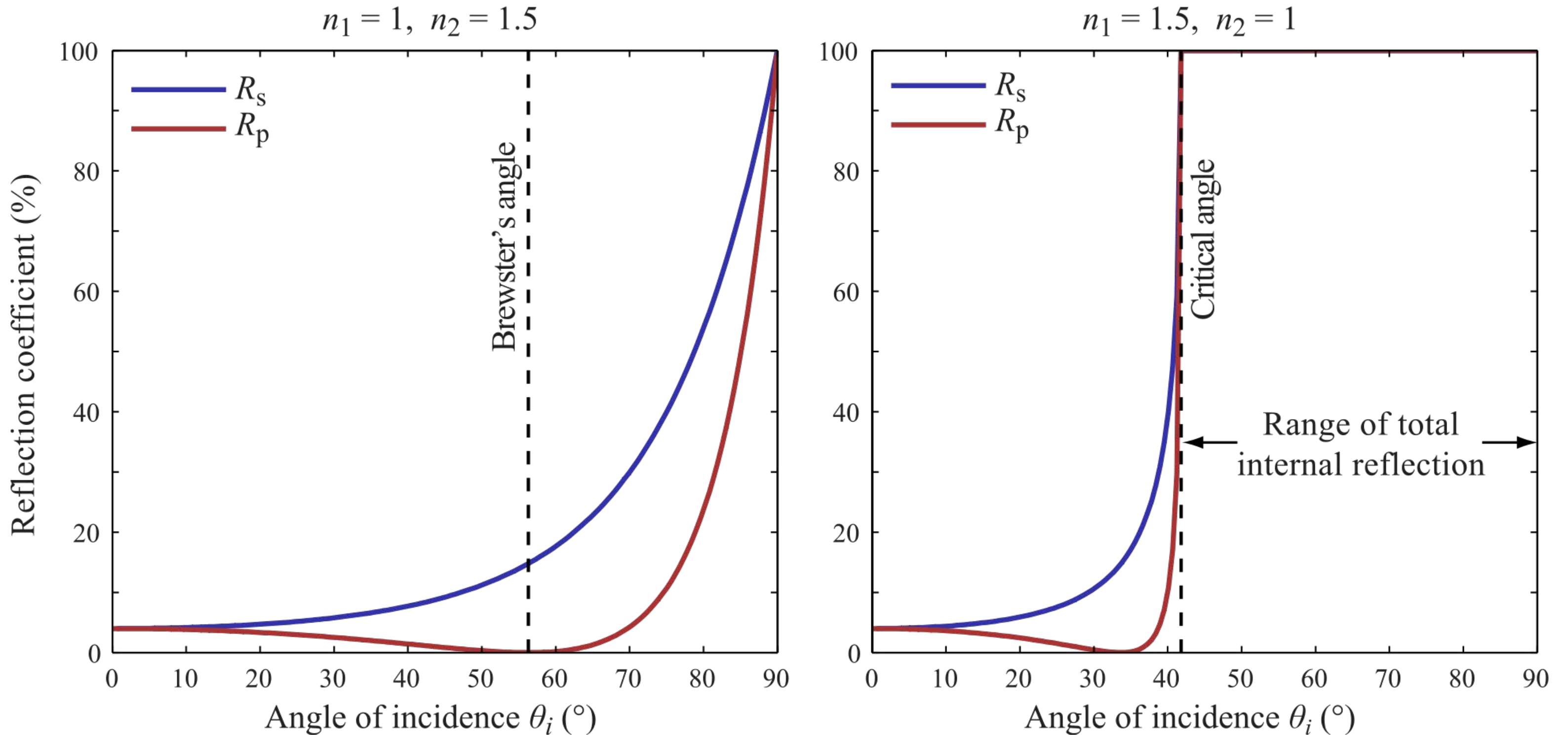
$$\rho_{\parallel} = \frac{\eta_2 \cos\theta_1 - \eta_1 \cos\theta_2}{\eta_2 \cos\theta_1 + \eta_1 \cos\theta_2}$$

reflected: $F_r = \frac{1}{2}\left(\rho_{\parallel}^2 + \rho_{\perp}^2\right)$

$$\rho_{\perp} = \frac{\eta_1 \cos\theta_1 - \eta_2 \cos\theta_2}{\eta_1 \cos\theta_1 + \eta_2 \cos\theta_2}$$
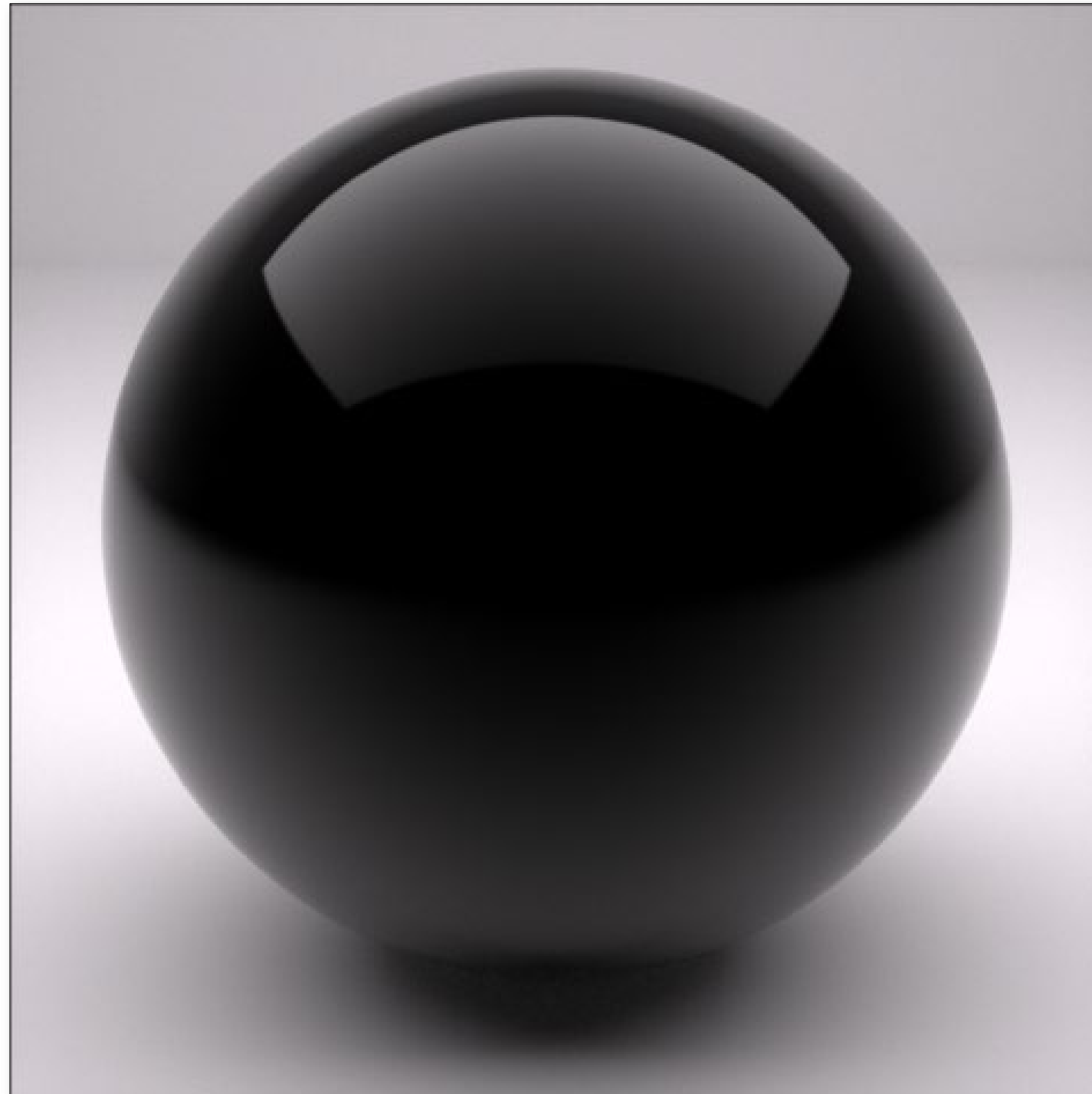
refracted: $F_t = 1 - F_r$

- The Shirley book uses a faster approximation (Schlick), but to get full accuracy you'd need to use these equations

Fresnel equations for glass

$n_1 = 1, \ n_2 = 1.5$

$n_1 = 1.5, \ n_2 = 1$
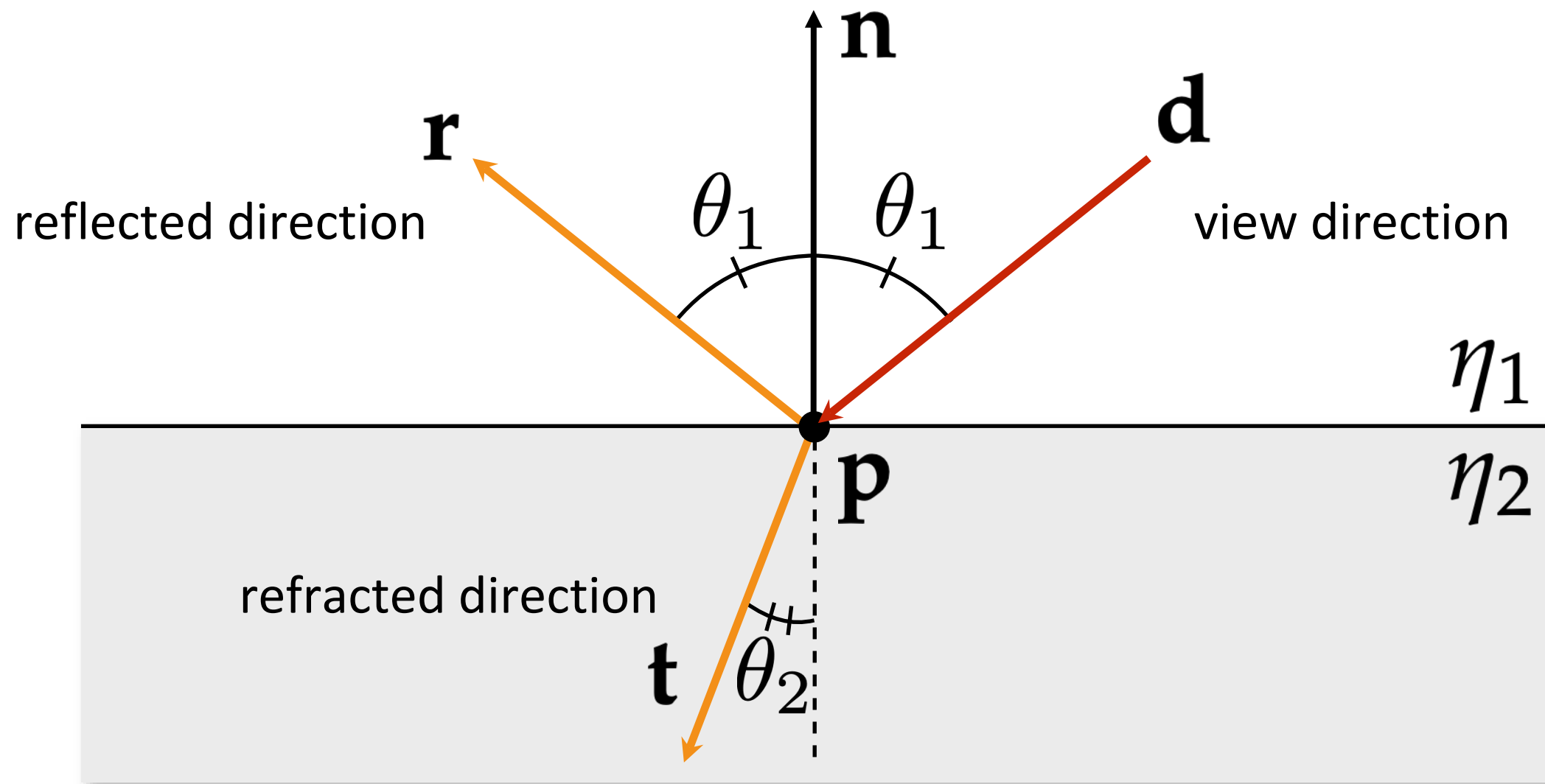
Fresnel reflection

Fresnel reflection/refraction
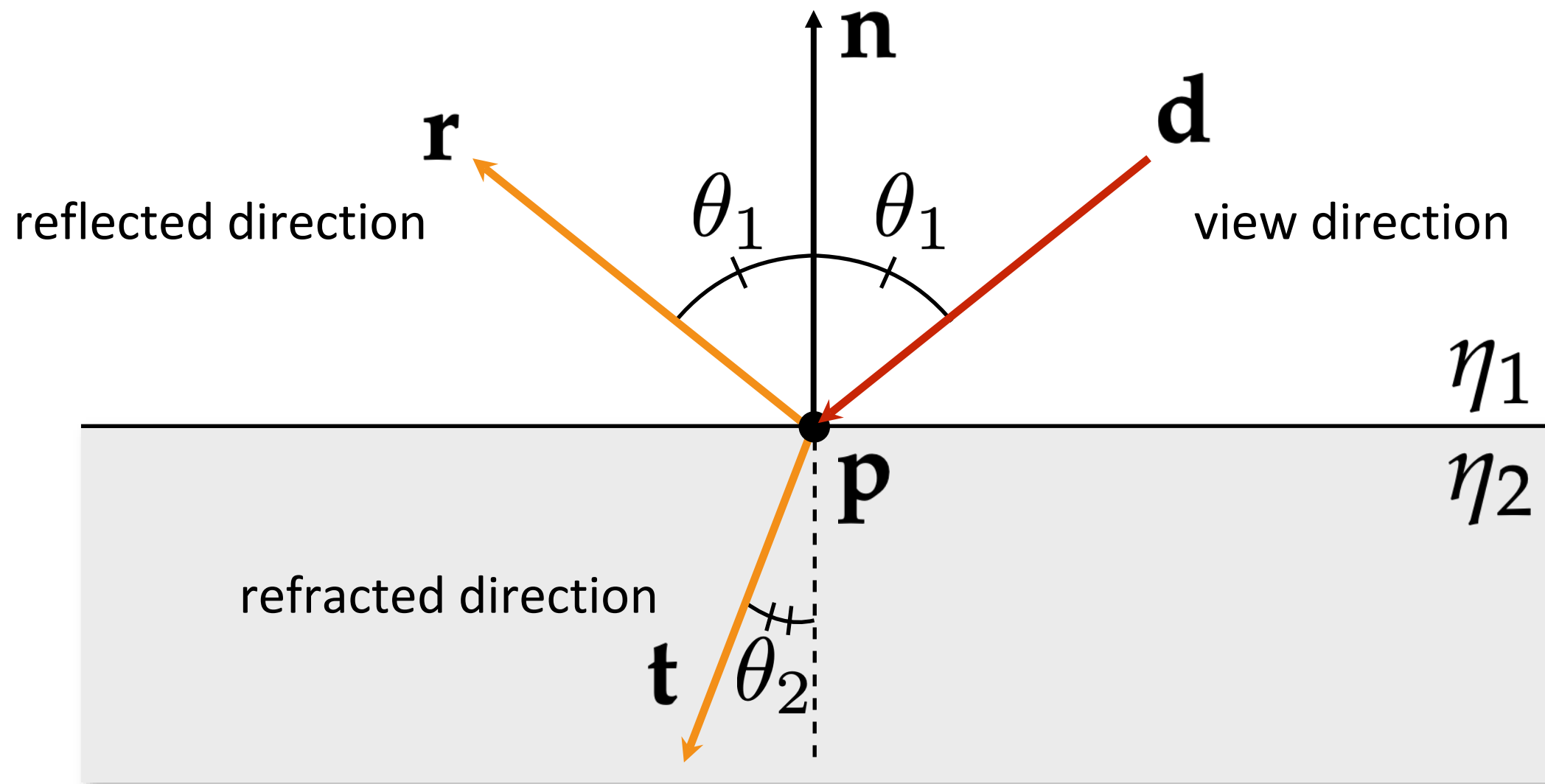
Reflection vs. Refraction

During ray tracing, how do we decide whether to reflect or refract?
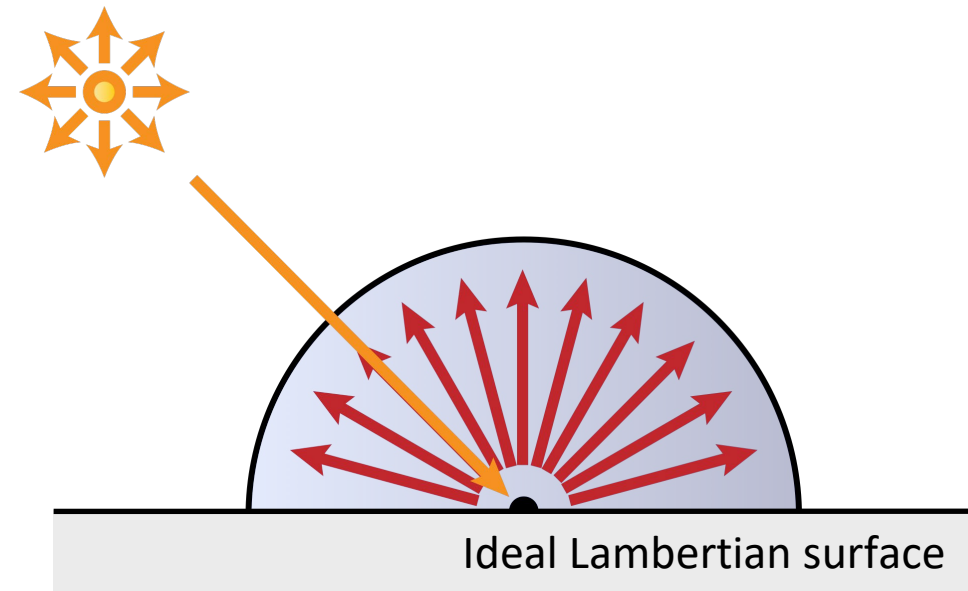
Reflection vs. Refraction

During ray tracing, how do we decide whether to reflect or refract?

- Randomly! Using Fresnel coefficients as probabilities.

So Far: Idealized BRDF Models
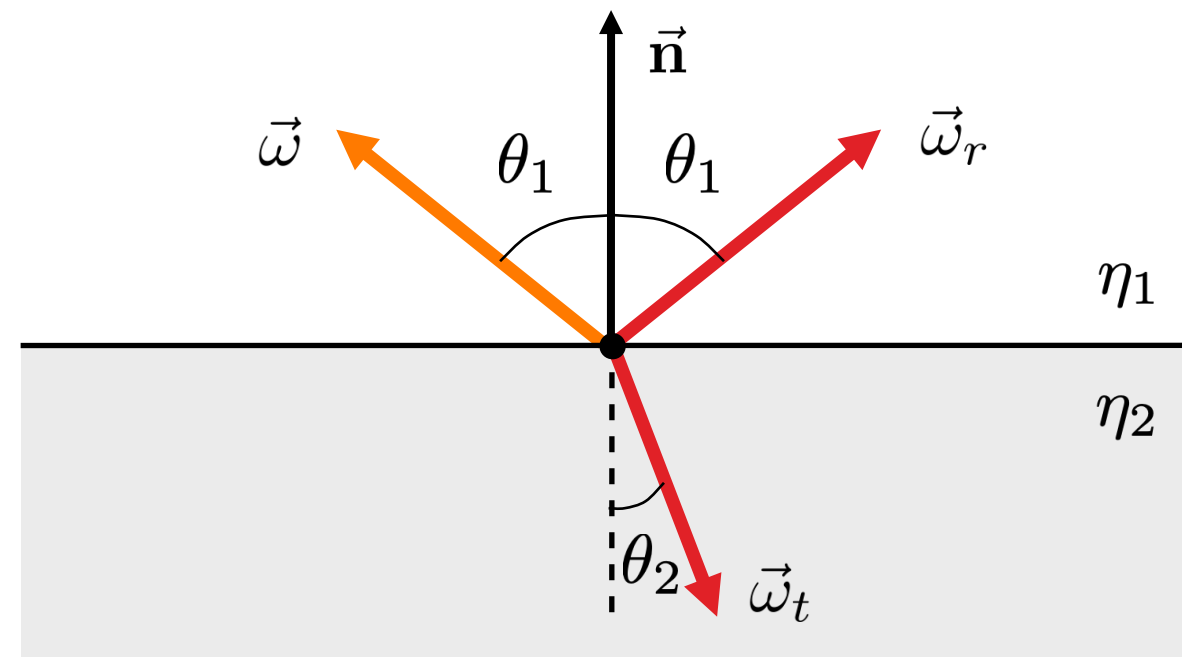
Diffuse

Ideal Lambertian surface

Specular Reflection and Refraction

$\vec{\mathbf{n}}$

$\vec{\omega}$ θ_1 θ_1 $\vec{\omega}_r$

η_1

η_2

θ_2 $\vec{\omega}_t$

Real materials are more complex

Rough materials

In reality, most materials are neither perfectly diffuse nor specular, but somewhere in between
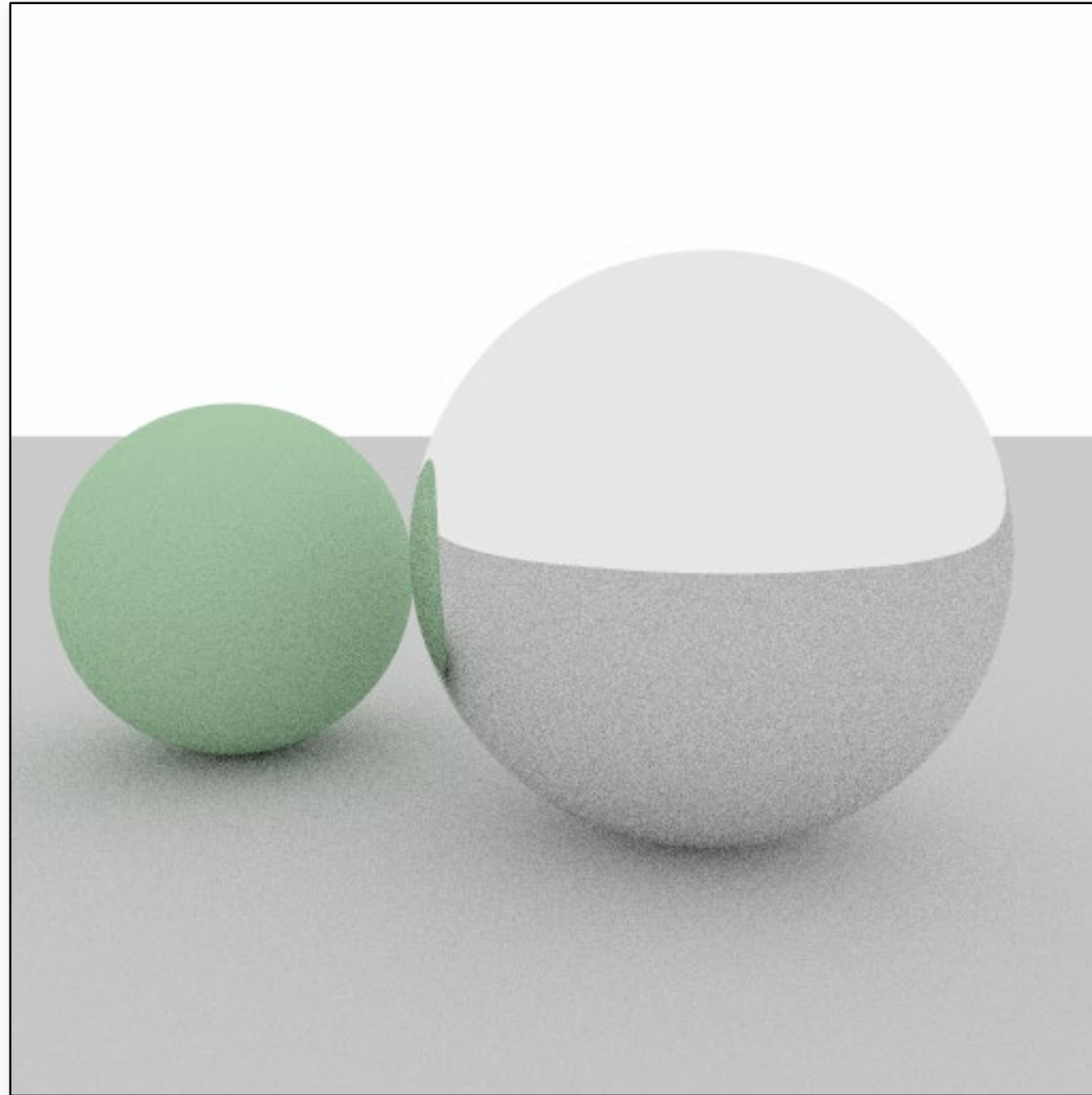
- Imagine a shiny surface scratched up at a microscopic level

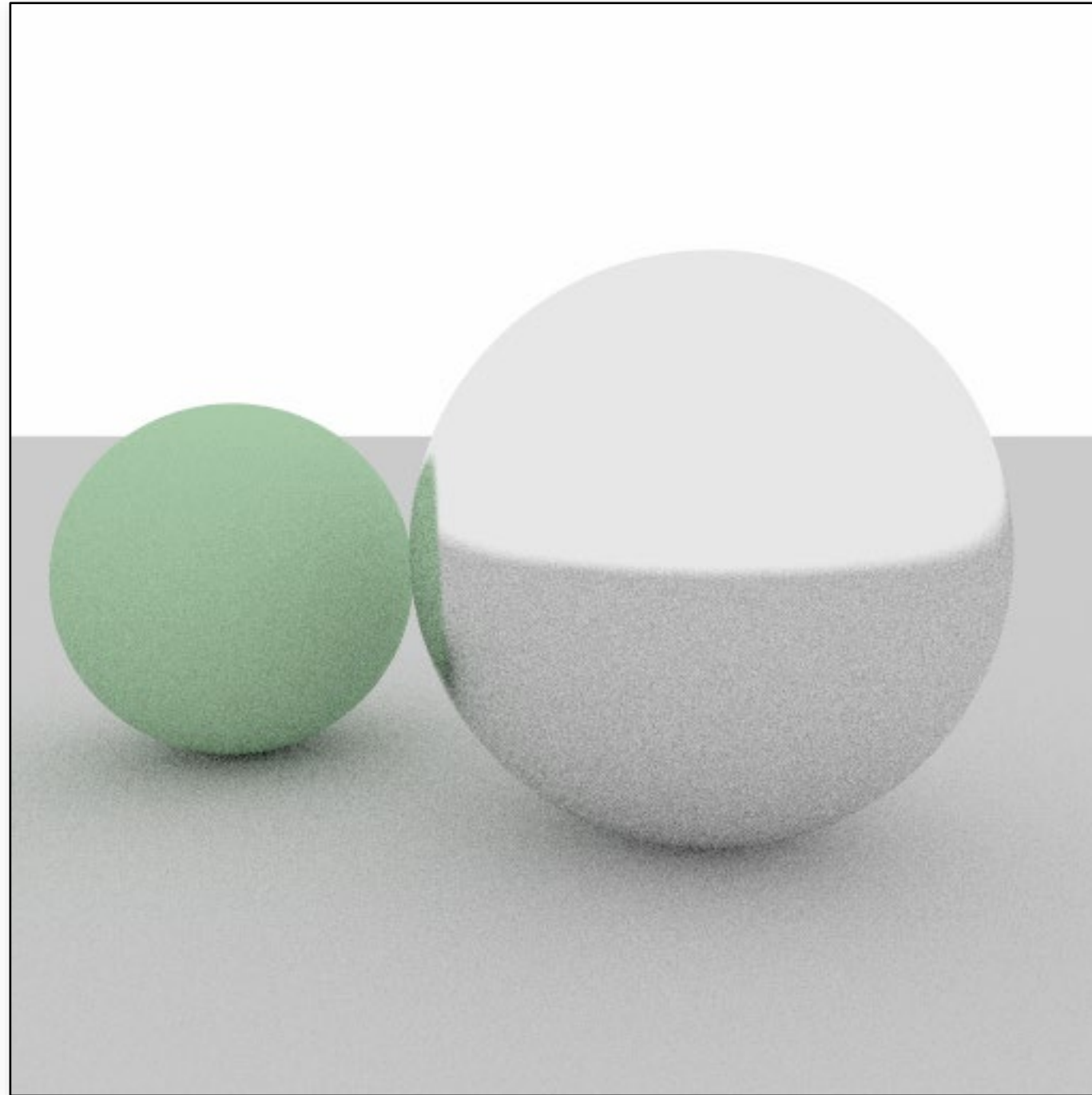We will look at a more principled way to handle this later.

For now, we can easily approximate one important characteristic: blurred reflections

- Compute reflection direction, then add a random offset to it

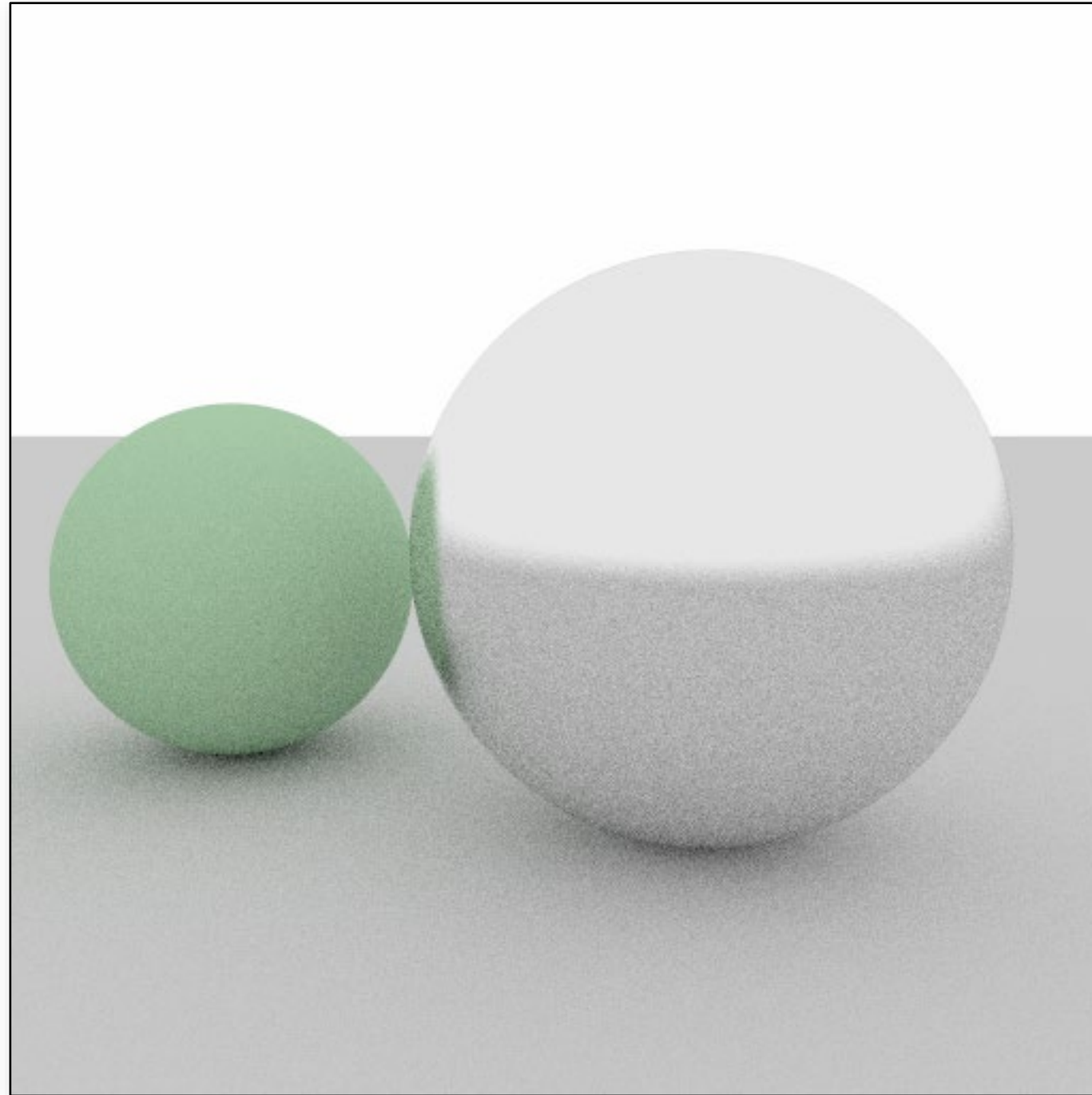- Sample random offset from sphere. Scale it to increase/decrease fuzziness
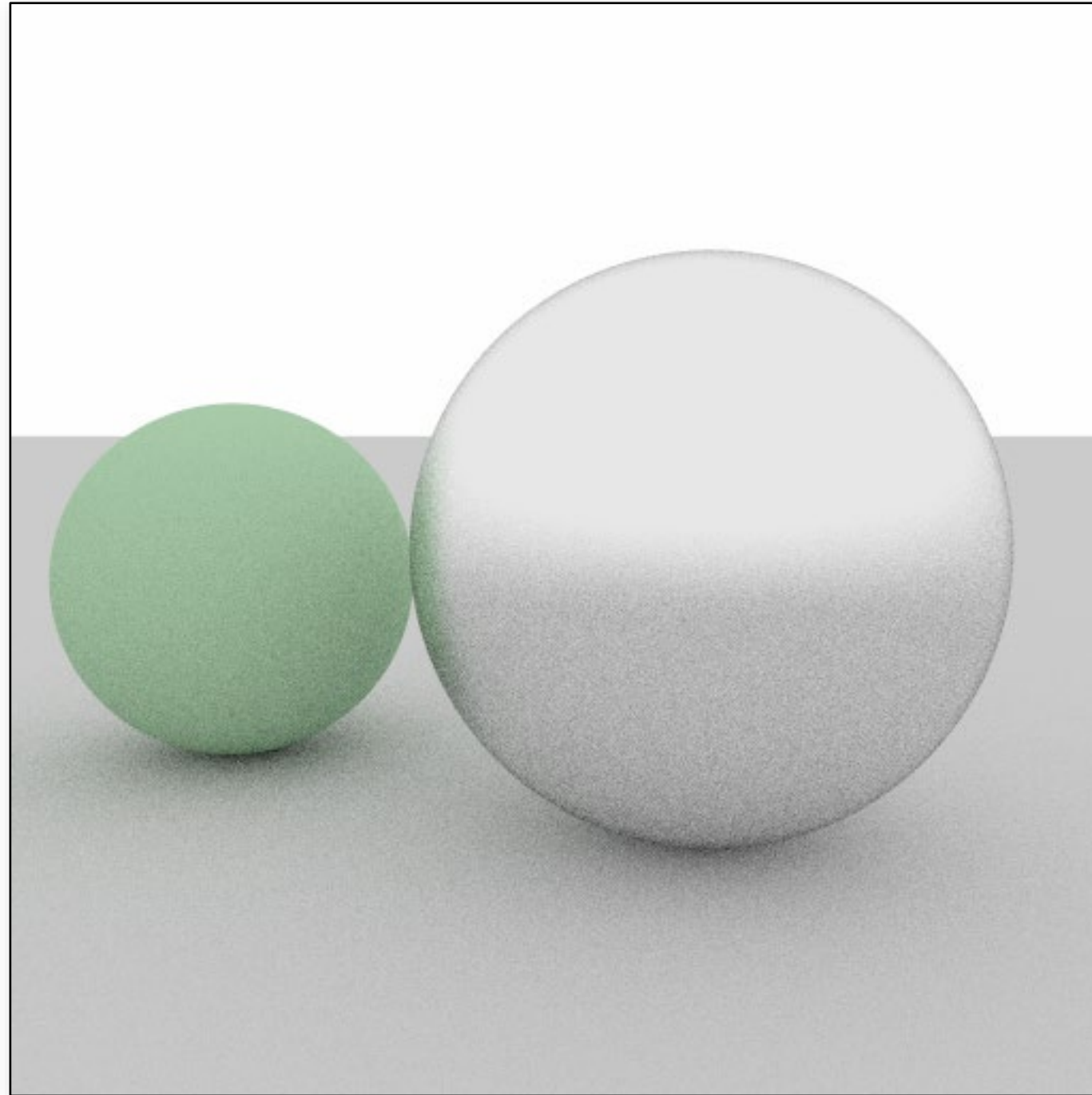
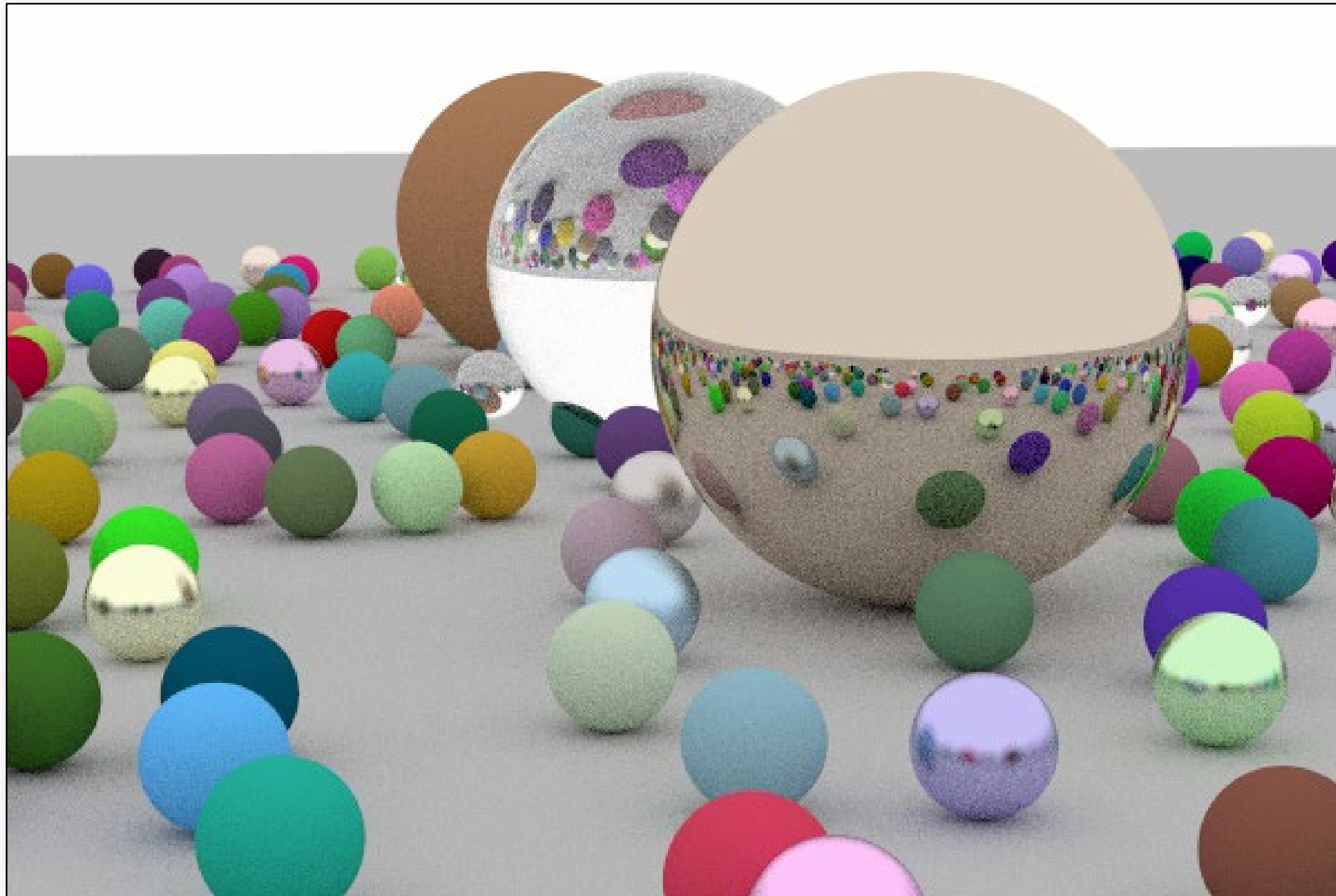# Diffuse & mirror spheres

Diffuse & rough mirror spheres

Diffuse & rough mirror spheres

Diffuse & rough mirror spheres
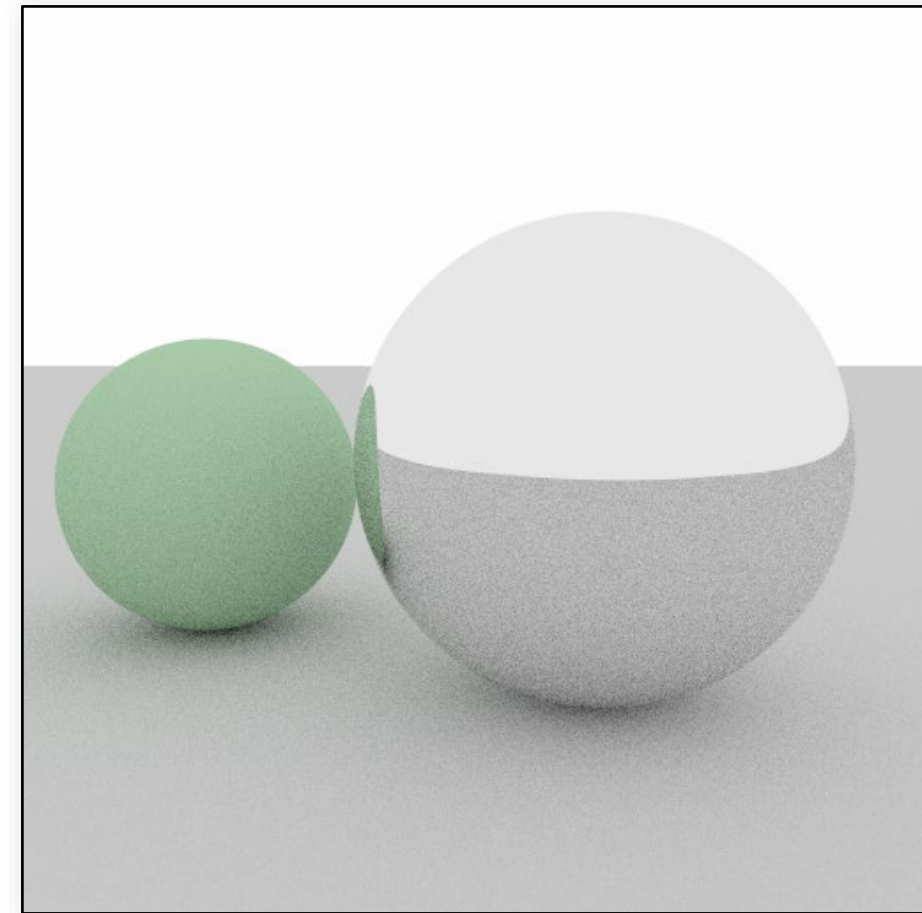
Putting it together

Lighting

Lighting

So far, the sky or background has been the only source of emitted light

But we can easily make any surface a light source!

- Just return an emitted color when a ray hits that surface

- Add a function to material that returns emitted color

    • Returns black (all zeros) for regular (non-emissive) surfaces

    • Color will often be greater than (1,1,1)

- Also possible for surfaces to emit & scatter (but not common)

Pseudo-code

```
Scene::trace(Ray ray)
   hit = surfaces.intersect(ray);
   if hit
      [col, sRay] = hit->mat->scatter(ray)
      return col * trace(sRay);
   else
      return backgroundColor;
```

Pseudo-code

```
Scene::trace(Ray ray)
  hit = surfaces.intersect(ray);
  if hit
      emit = hit->mat->emit(ray)
      [col, sRay] = hit->mat->scatter(ray)
      return emit + col * trace(sRay);
  else
      return backgroundColor;
```