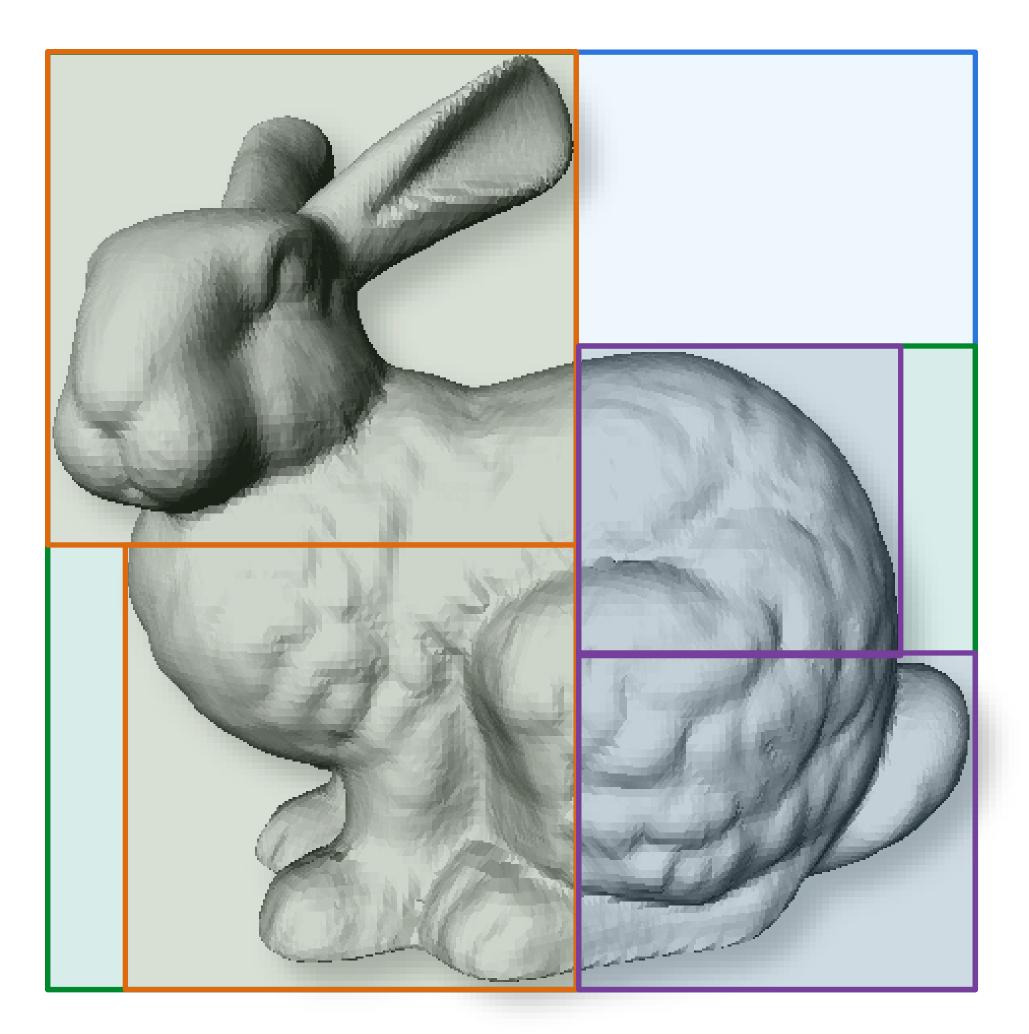
Ray tracing and geometric representations



http://graphics.cs.cmu.edu/courses/15-468

15-468, 15-668, 15-868 Physics-based Rendering Spring 2023, Lecture 2

Course announcements

- Programming assignment 1 will be posted on Friday 1/27 and will be due two weeks later.
- Take-home quiz 1 will be posted on Tuesday 1/24 and will be due a week later.
- Office hours for this week only (will finalize starting next week based on survey results): - Yannis–Thursday 3-4 pm, Smith Hall (EDSH) 225.



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Course announcements

Is anyone not on Piazza? \bullet

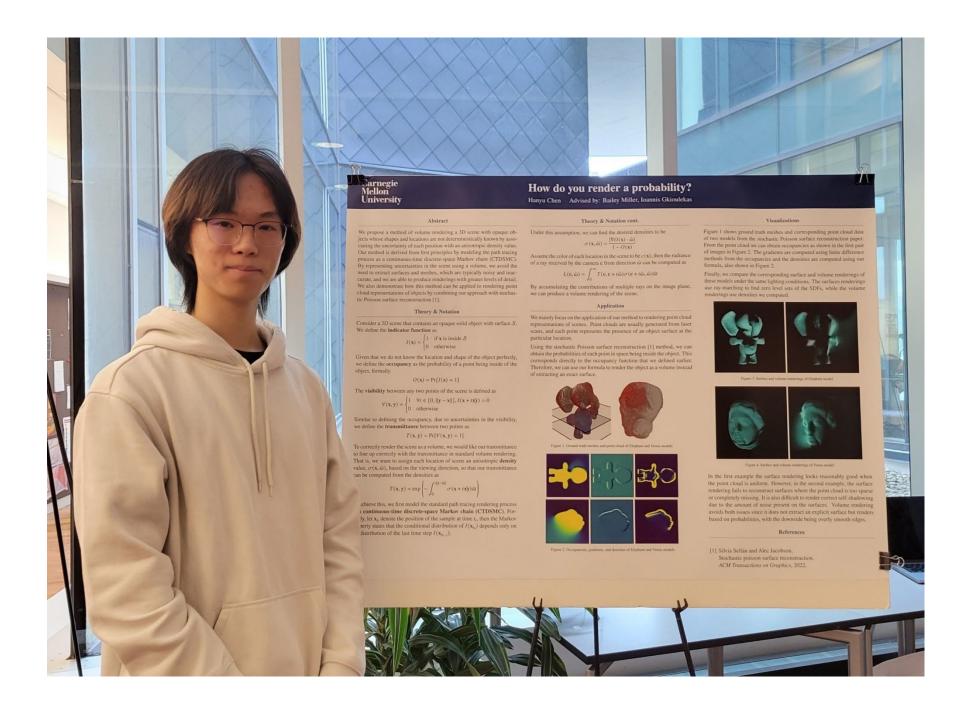
https://piazza.com/class/lctj7gng8wql4/

Is anyone not on Canvas?

Is anyone not on Slack?

https://canvas.cmu.edu/courses/33678

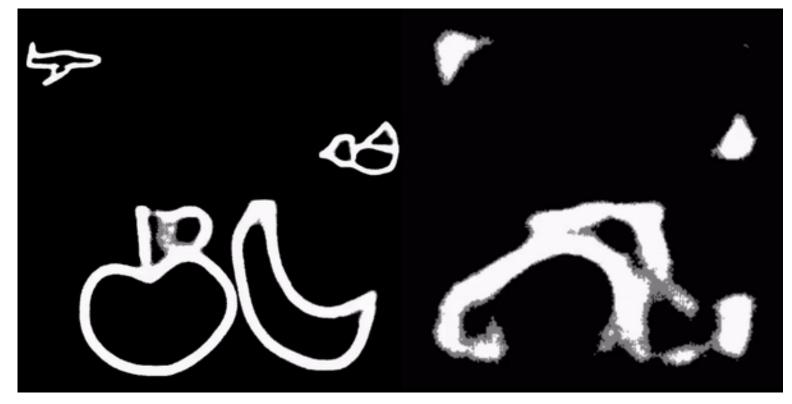




Hanyu Chen

15-468 TA, Senior in Computer Science & Math

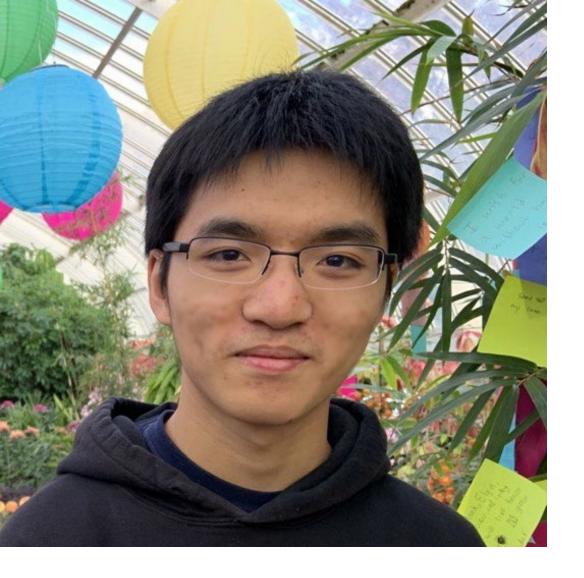
- Research interest broadly in computer vision/computer ---graphics/rendering
- Currently working with Yannis in neural rendering & surface reconstruction related research



some random computer vision related work...

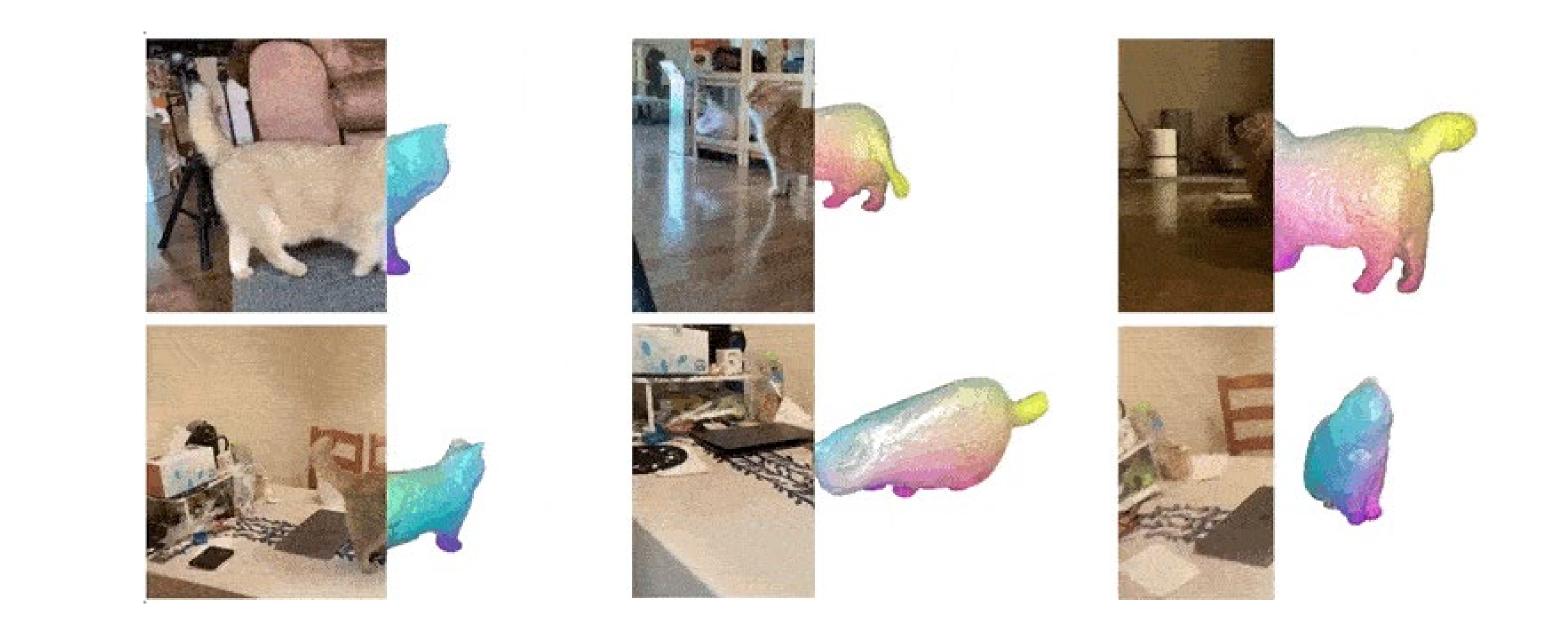


and some differentiable rendering related work...



Jeff Tan (jefftan@andrew.cmu.edu)

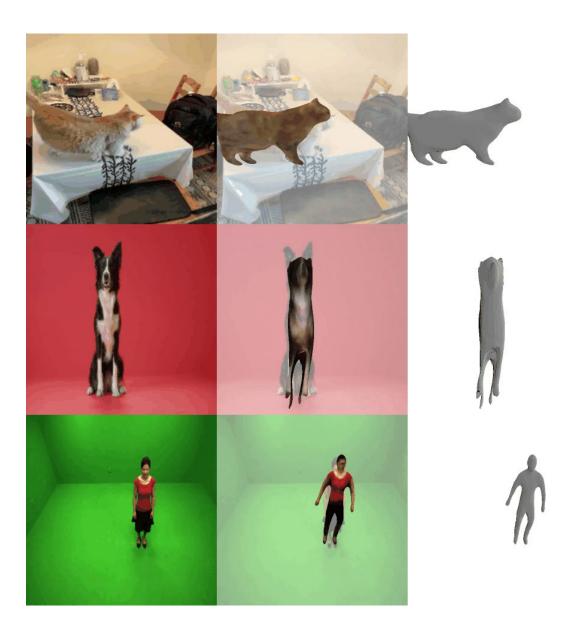
Advised by Prof. Deva Ramanan



Yang et al. (CVPR 2022)

15-468 TA and Senior in Computer Science

Research: Neural rendering for real-time dynamic 3D reconstruction



Tan et al. (in submission)



Overview of today's lecture

- Introduction to ray tracing. •
- Intersections with geometric primitives. •
- Triangular meshes.



Slide credits

Most of these slides were directly adapted from:

• Wojciech Jarosz (Dartmouth).



Two forms of 3D rendering

Rasterization: object point to image plane

- start with a 3D object point
- apply transforms
- determine the 2D image plane point it projects to

Ray tracing: image plane to object point

- start with a 2D image point
- generate a ray
- determine the visible 3D object point

Inverse processes



Two forms of 3D rendering

Rasterization

for (each triangle) for (each pixel or ray) for (each pixel) → for (each triangle) if (triangle covers pixel) if (ray hits triangle) keep closest hit keep closest hit **Triangle-centric Ray-centric**

Ray tracing





Rasterization advantages

Modern scenes are more complicated than images

- (not that much)
 - of course, if we have more than one sample per pixel this gets larger, but e.g. 4x supersampling is still a relatively comfortable ~100 MB
- Our scenes are routinely larger than this
 - This wasn't always true
- A rasterization-based renderer can *stream* over the triangles, no need to keep entire dataset around
- Allows parallelism and optimizations of memory systems

- A 1920x1080 frame (1080p) at 64-bit color and 32-bit depth per pixel is 24 MB



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Rasterization limitations

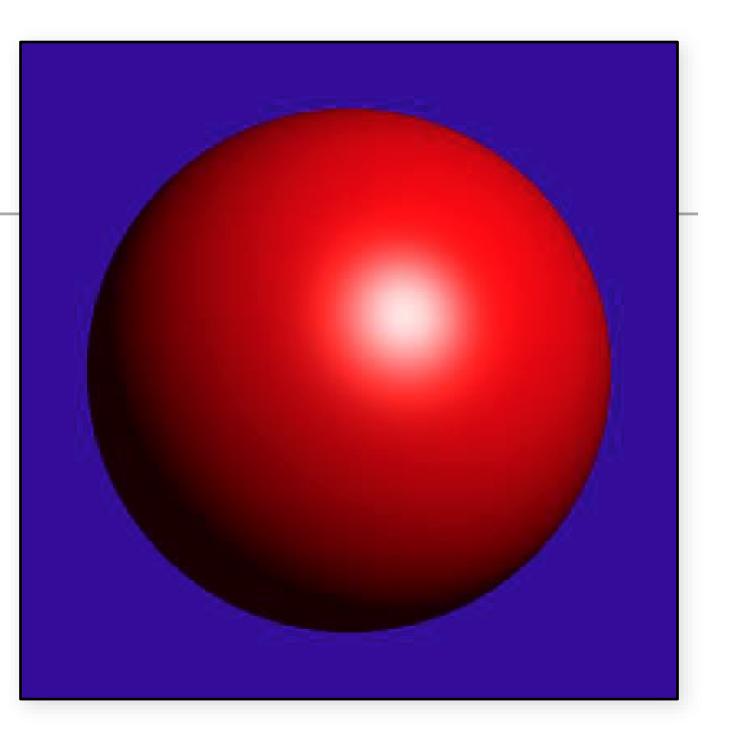
Restricted to scan-convertible primitives

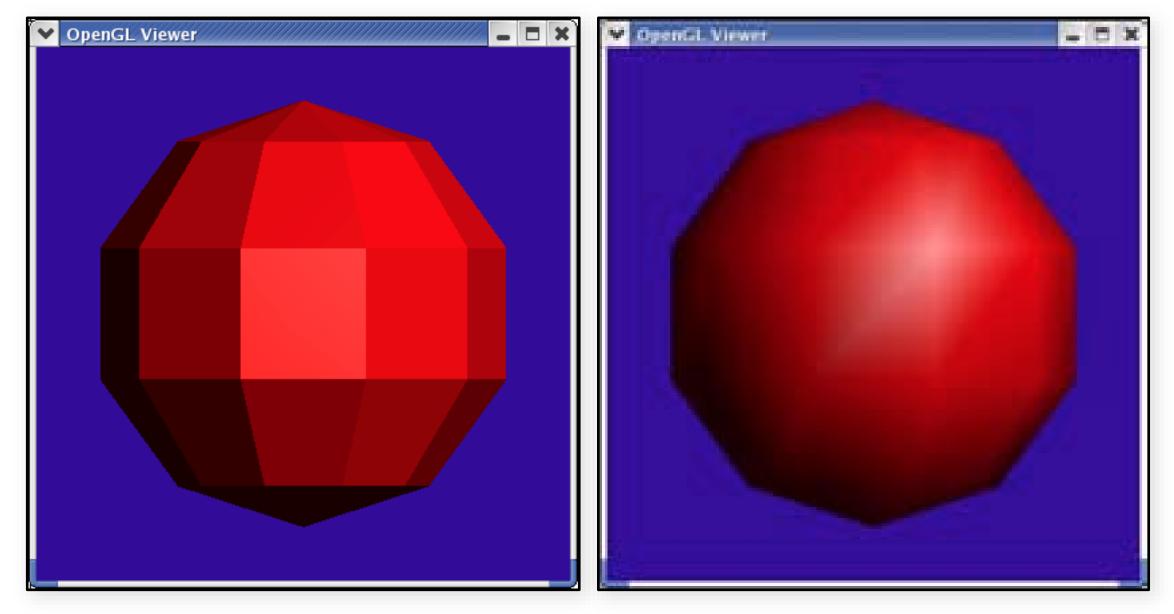
- Pretty much: triangles

Faceting, shading artifacts

- This is largely going away with programmable per-pixel shading, though

No unified handling of shadows, reflection, transparency







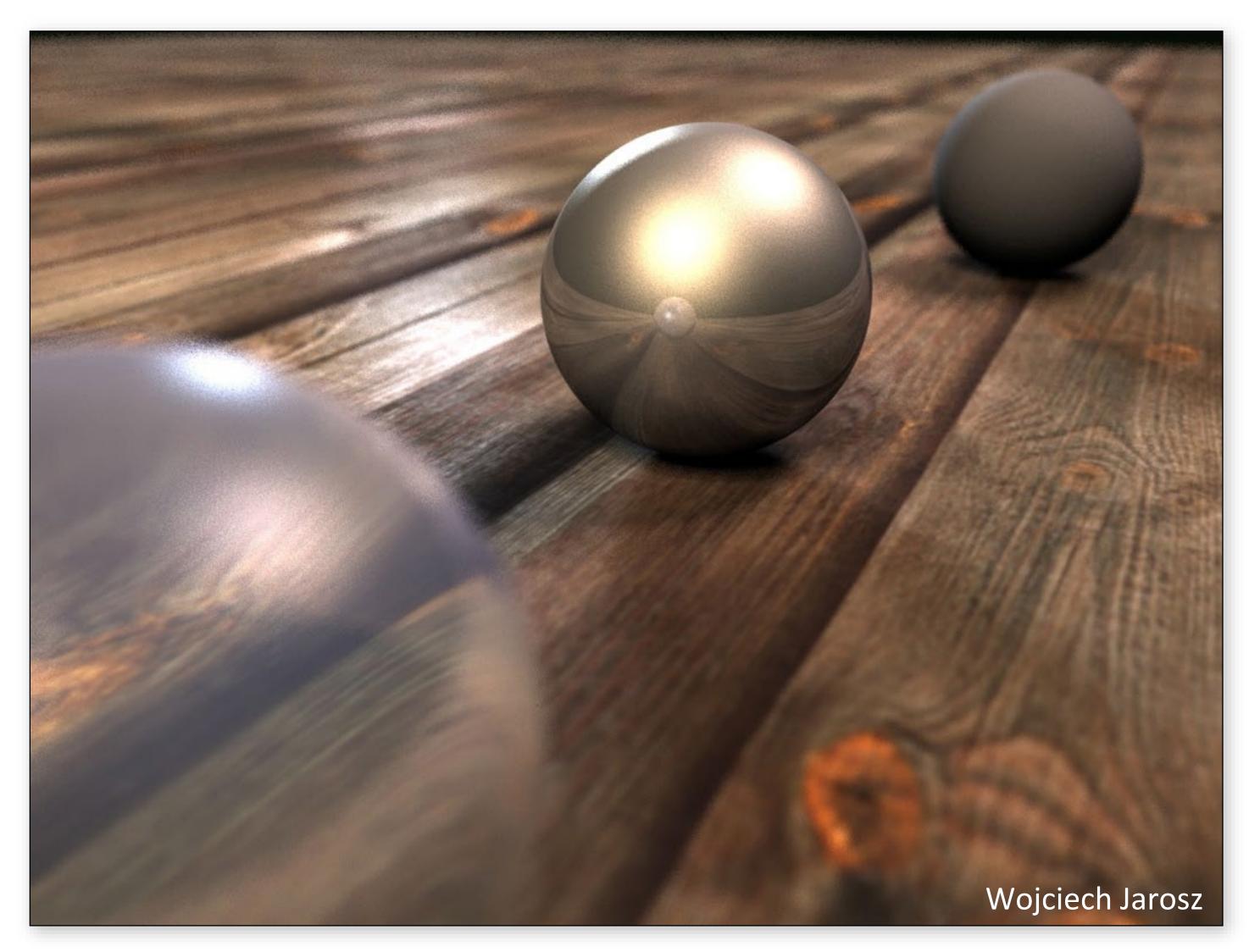
Ray/path tracing

Advantages

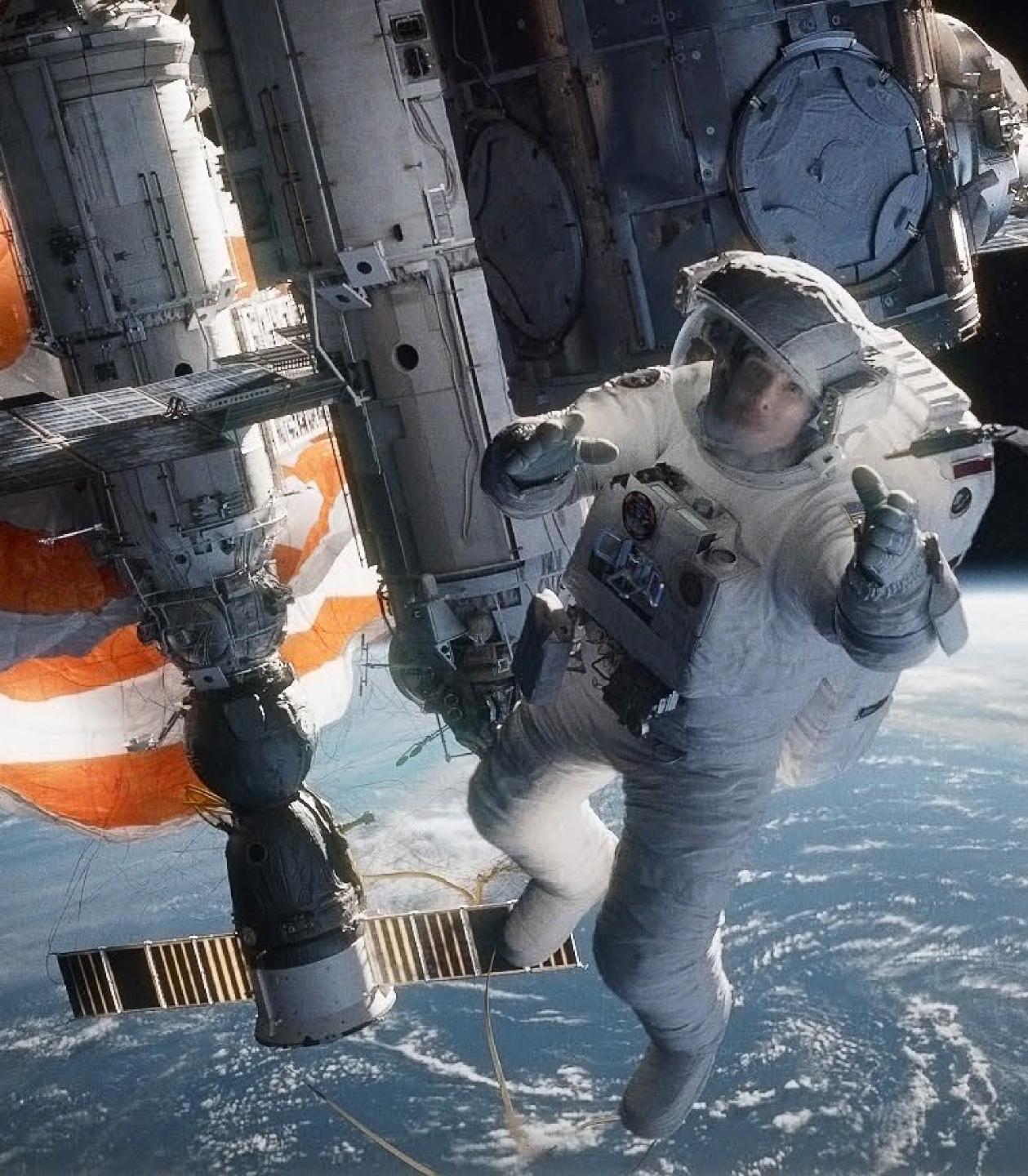
- Generality: can render anything that can be intersected with a ray - Easily allows recursion (shadows, reflections, etc.)
- Disadvantages
- Hard to implement in hardware (lacks computation coherence, must fit entire scene in memory, bad memory behavior)
 - Not such a big point anymore given general purpose GPUs
- Has traditionally been too slow for interactive applications
- Both of the above are changing rather rapidly right now!

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A ray-traced image







Ray tracing today



Rapid change in film industry

2008:

- Most CGI in films rendered using micro-polygon rasterization.
- "You'd be crazy to render a full-feature film with ray/path tracing."
- Ray/path tracing mostly interesting to academics

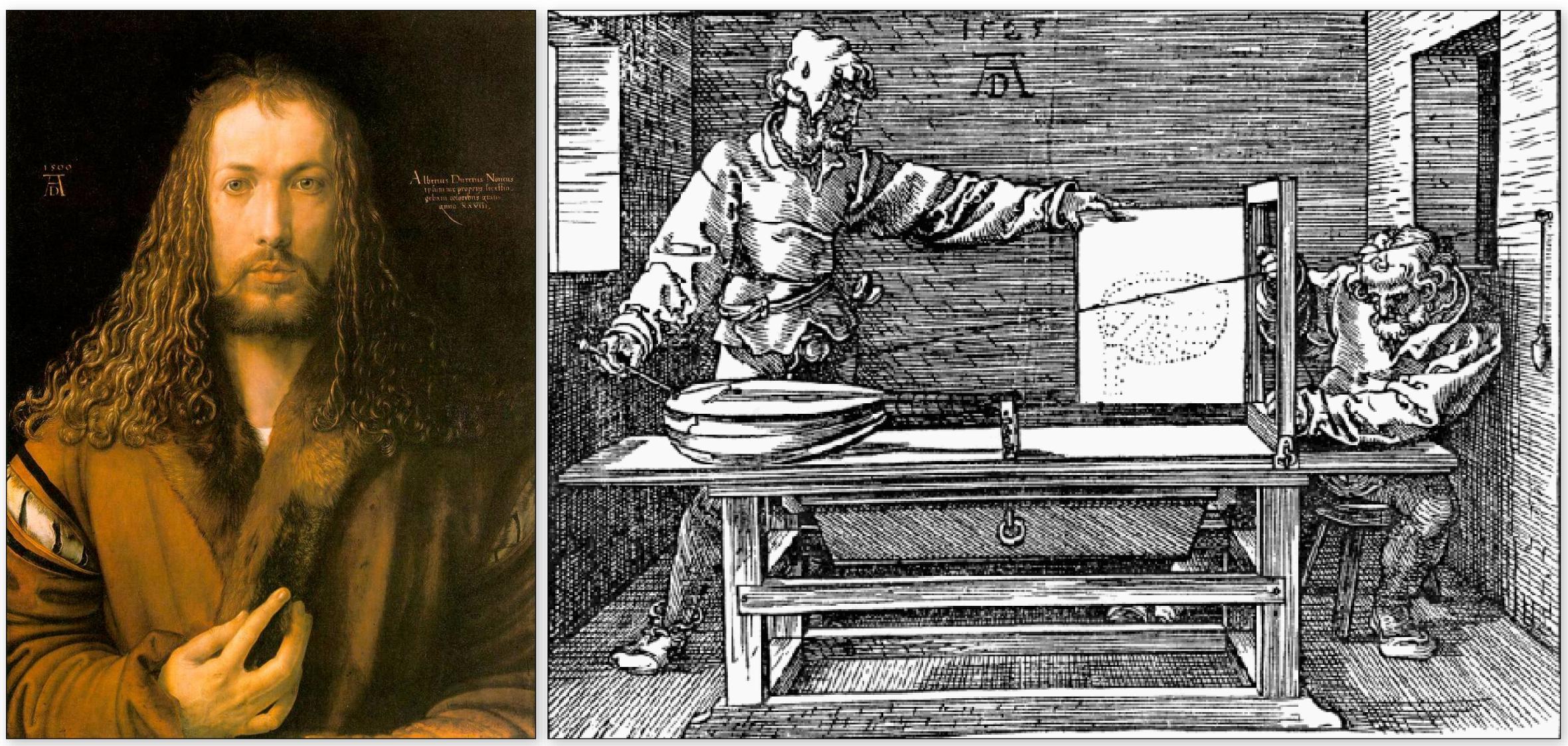
2018:

- Most major films now rendered using ray/path tracing.
- "You'd be crazy *not* to render a full-feature film using path tracing."



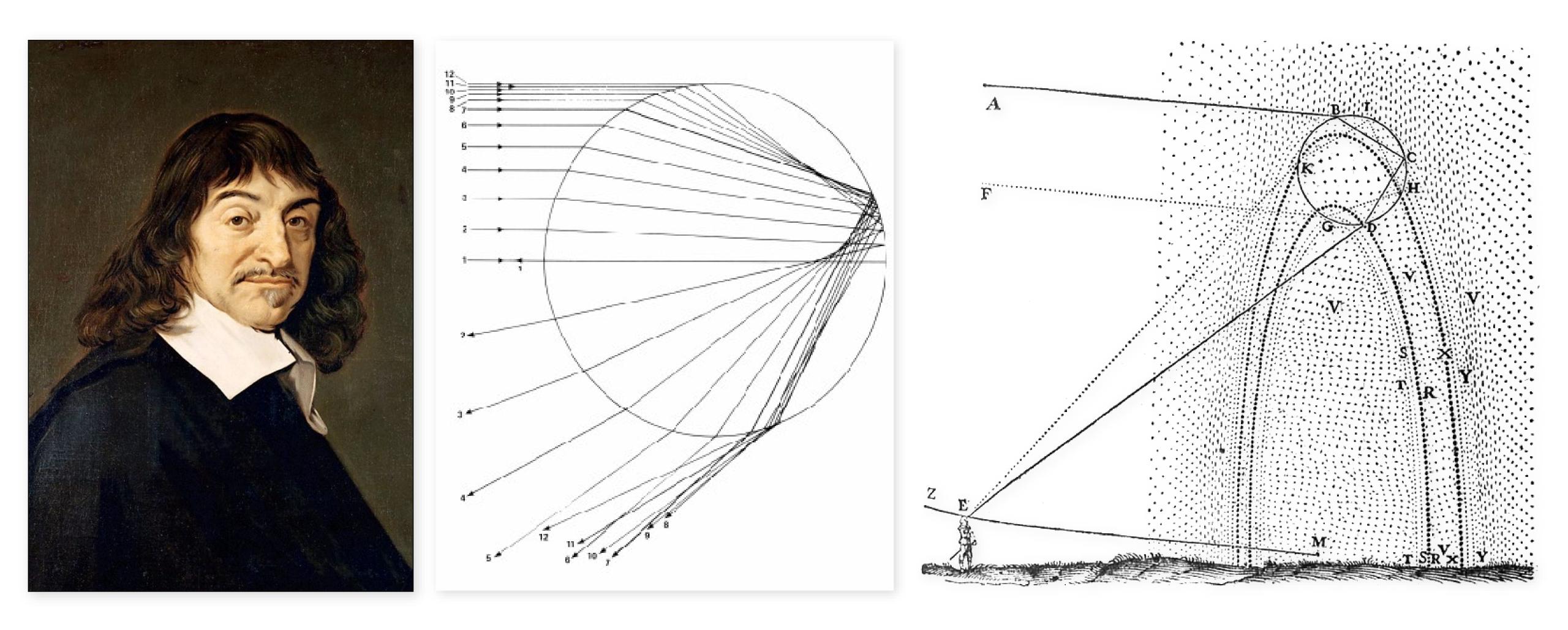
15

Albrecht Dürer (1525)

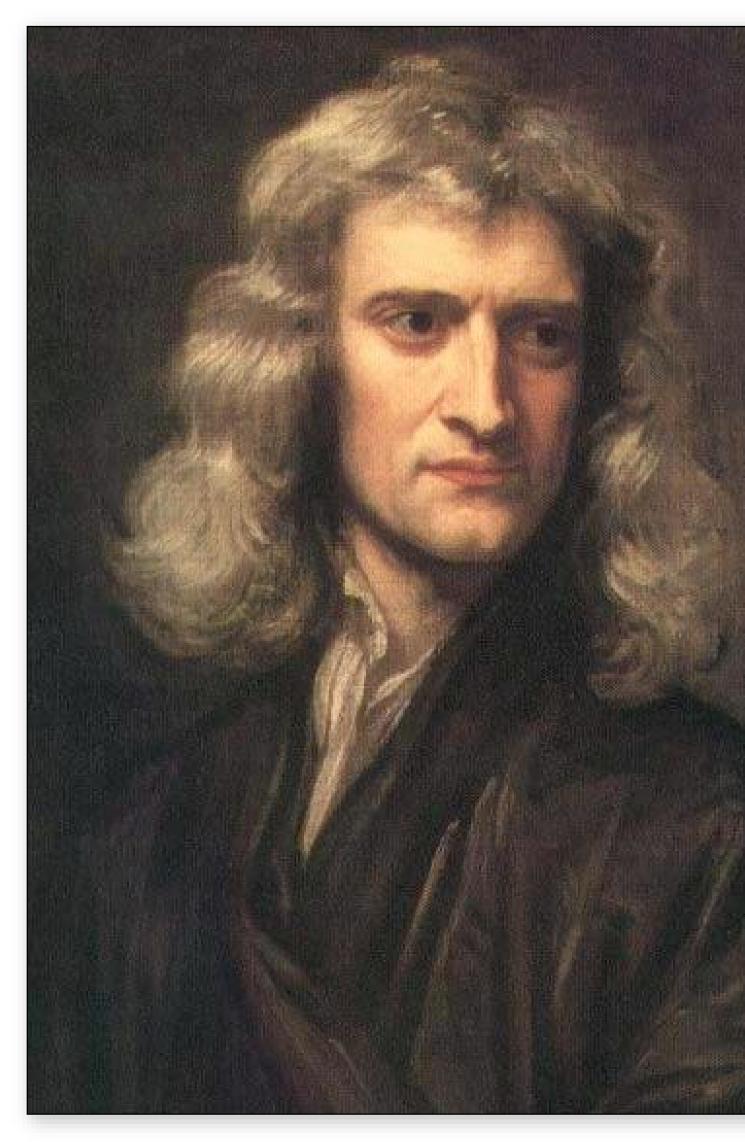


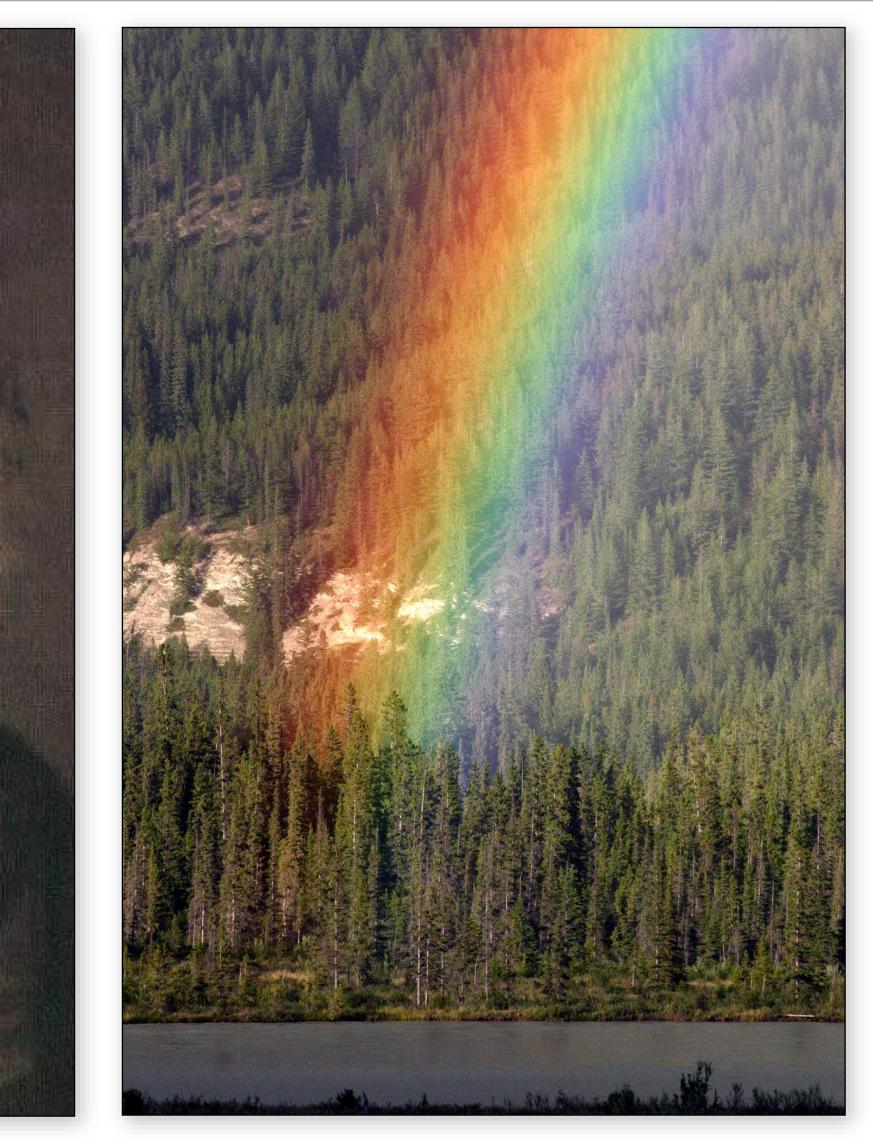


René Descartes (1650)



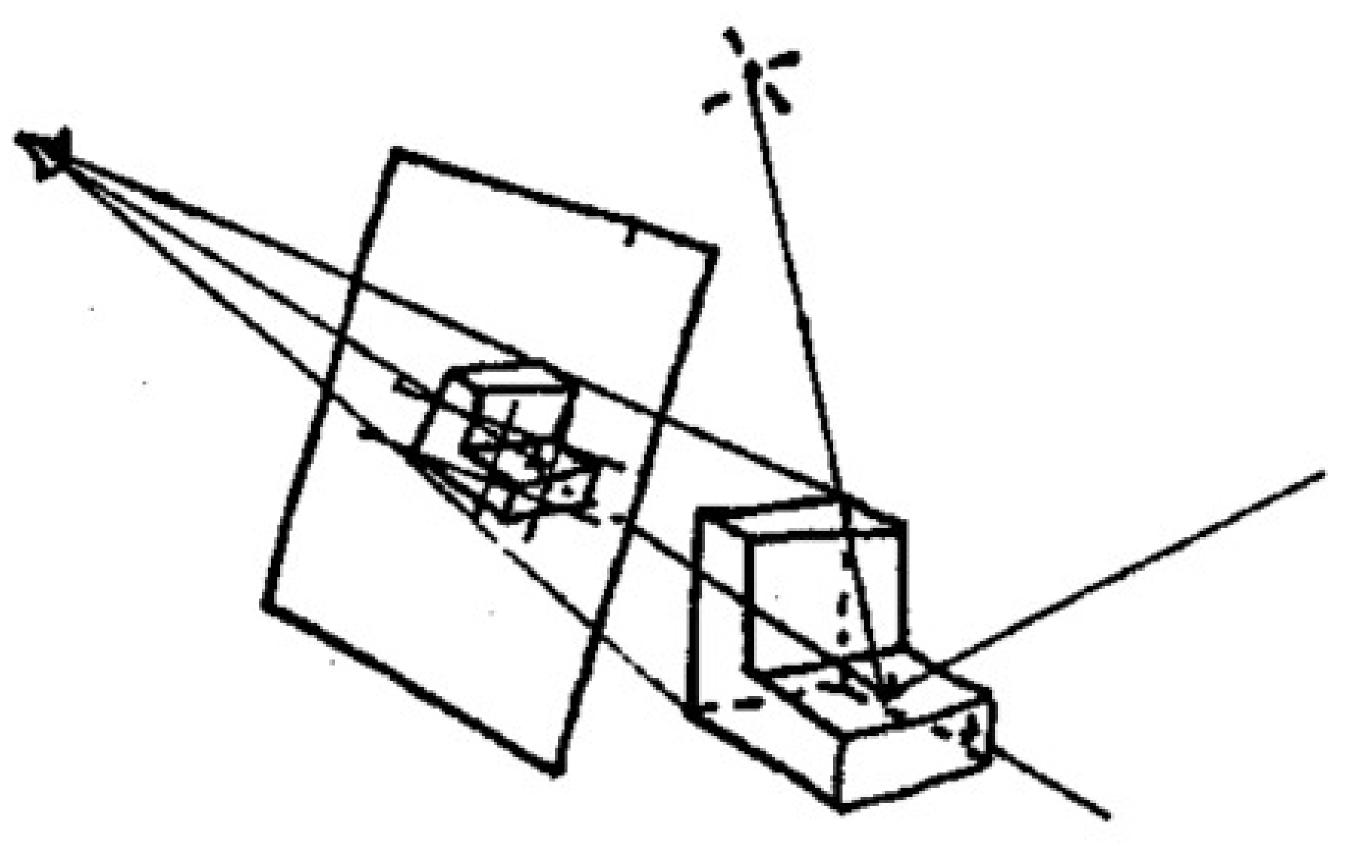
Isaac Newton (1670)







Appel (1968)

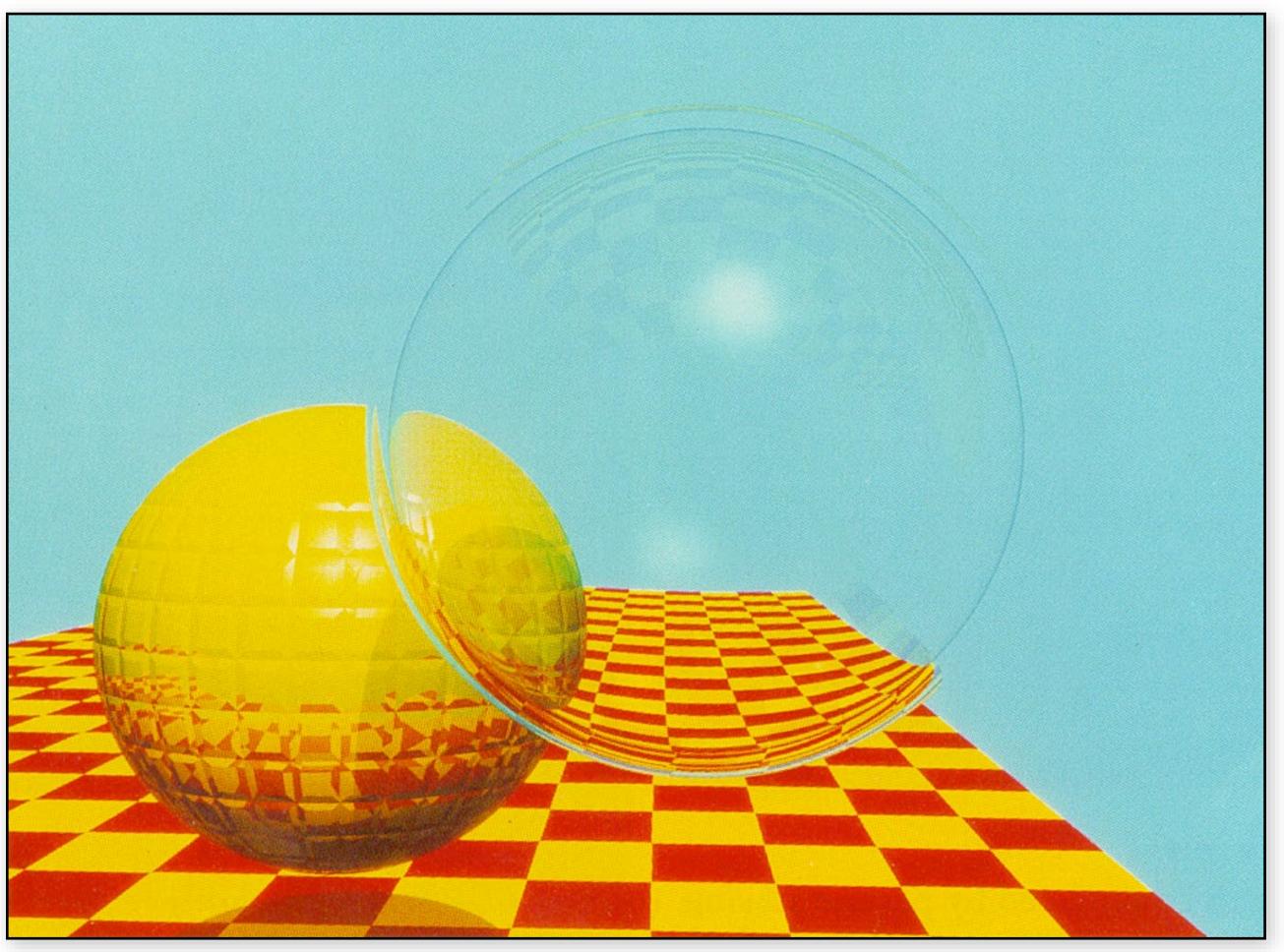


Ray casting

- Generate an image by sending one ray per pixel
- Check for shadows by sending a ray towards the light



Whitted (1979)



recursive ray tracing (reflection & refraction)



Light Transport - Assumptions

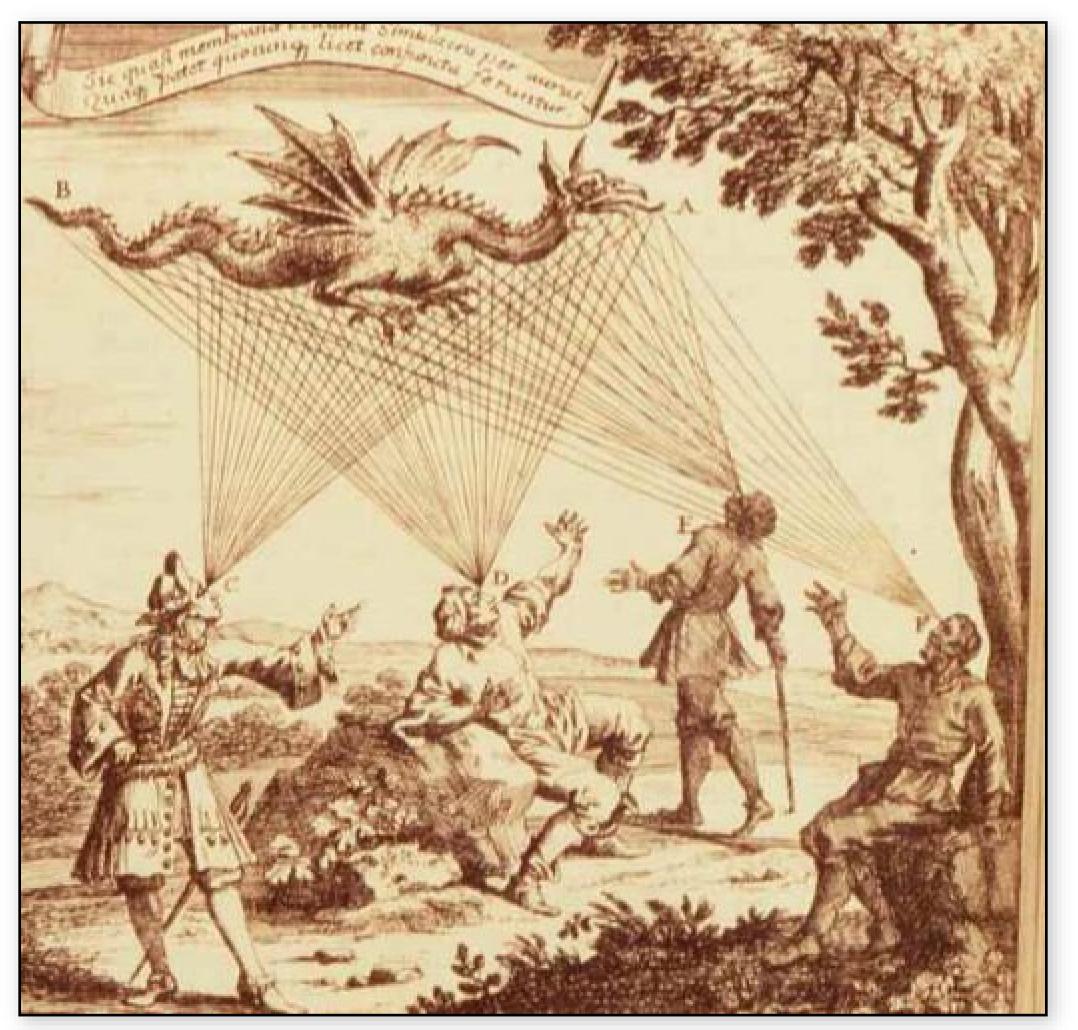
Geometric optics:

- no diffraction, no polarization, no interference
- Light travels in a straight line in a vacuum
- no atmospheric scattering or refraction
- no gravity effects

Color can be represented as three numbers: (R,G,B)

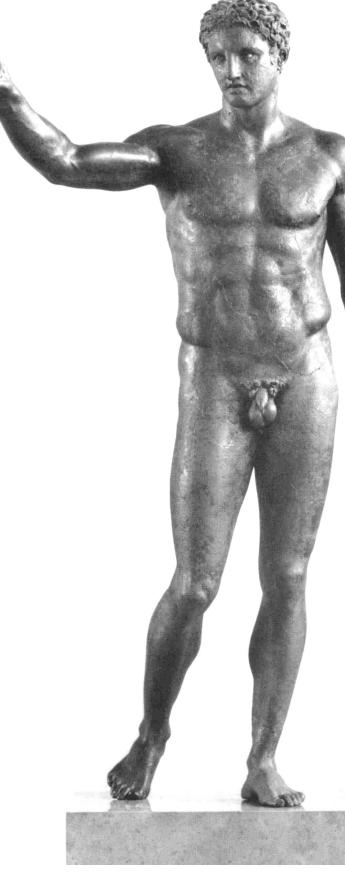


Emission theory of vision



Eyes send out "feeling rays" into the world

- Supported by:
- Ancient greeks
- 50% of US college students*

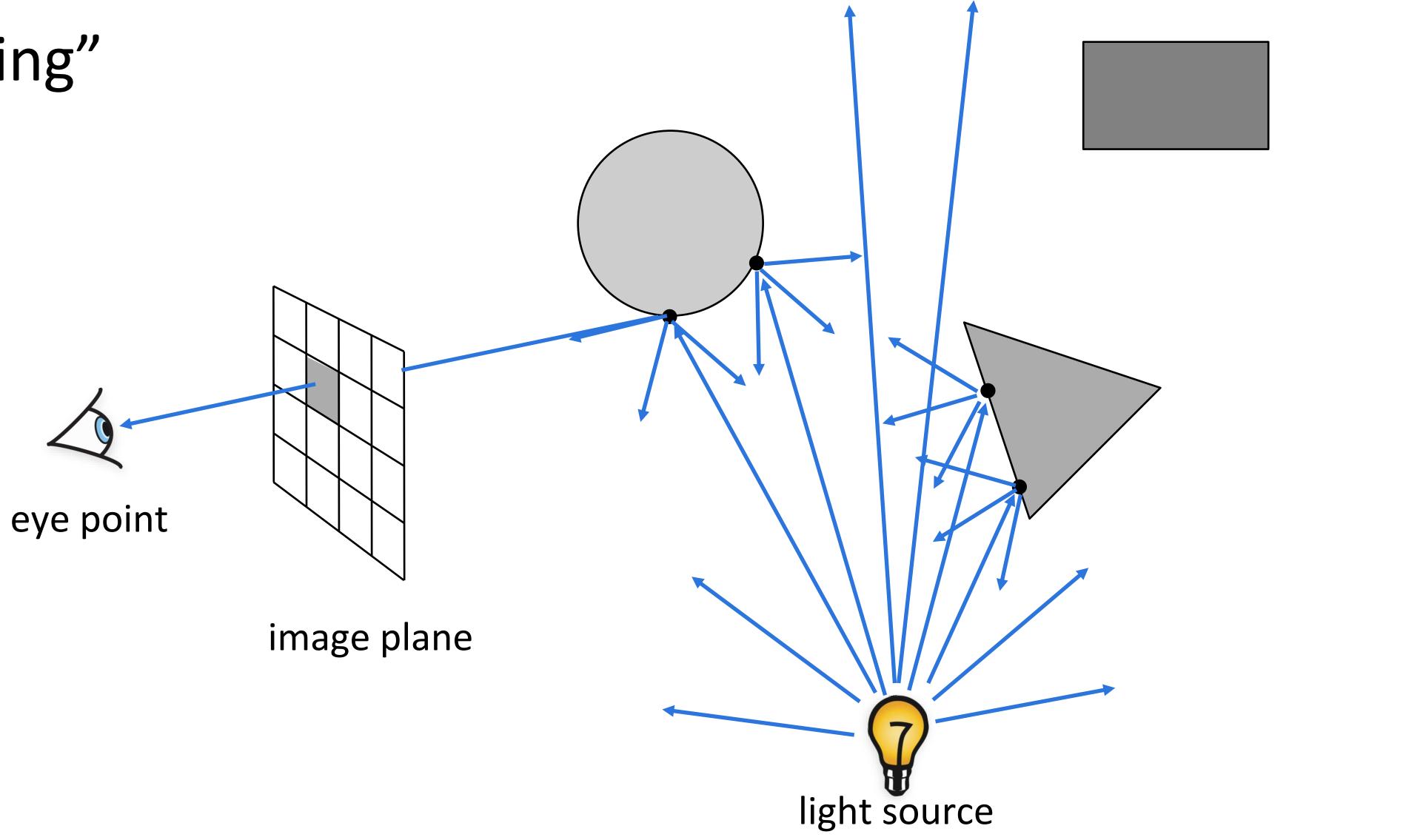






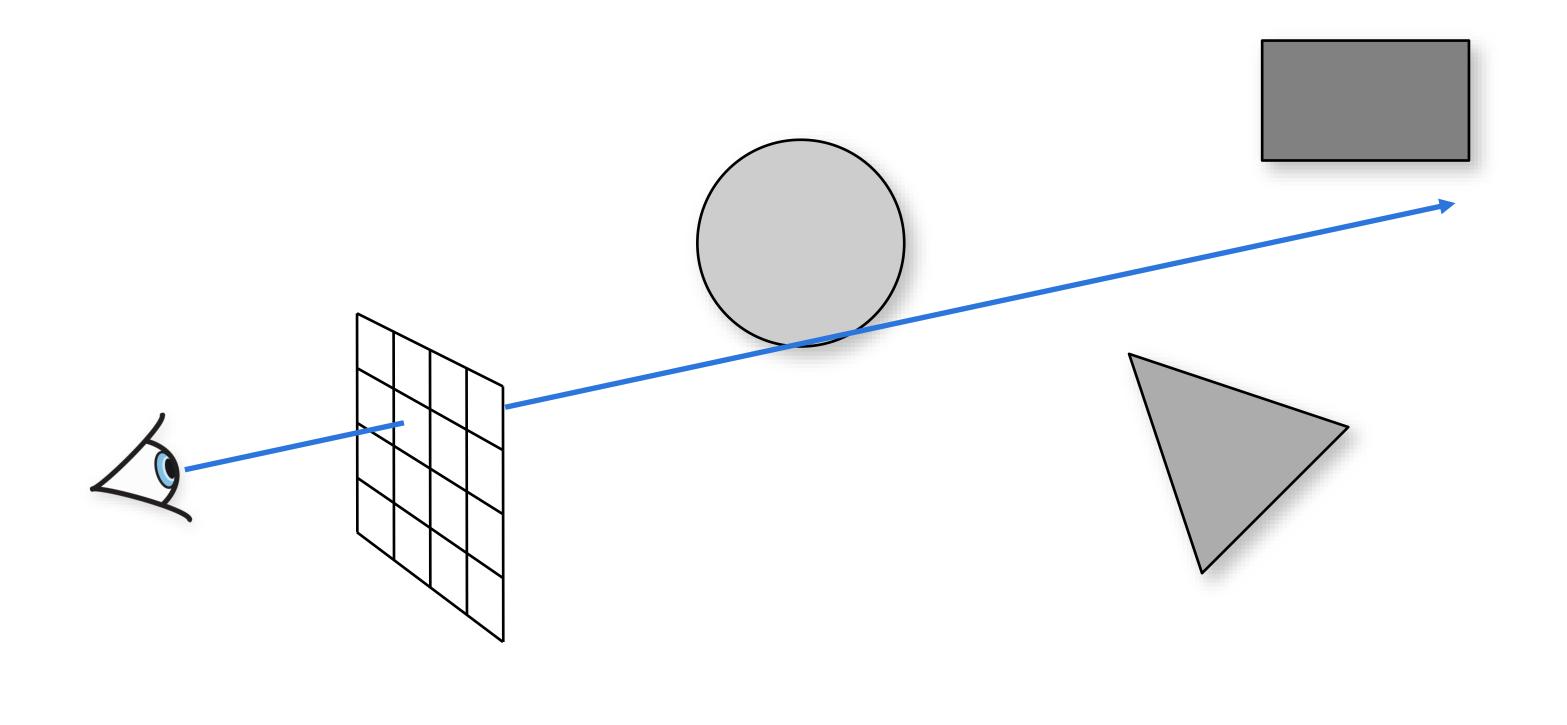
Ray Tracing - Overview

"light tracing"



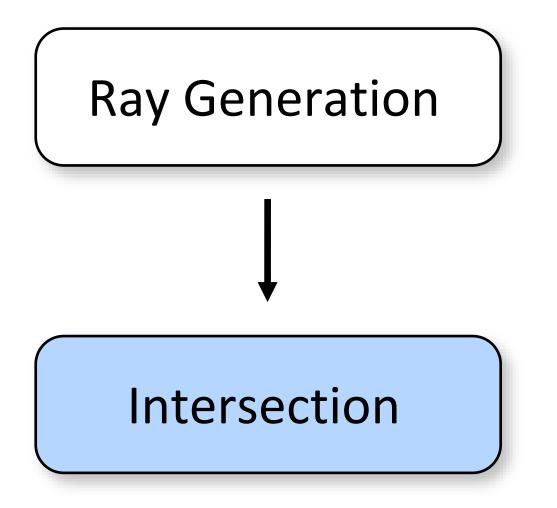


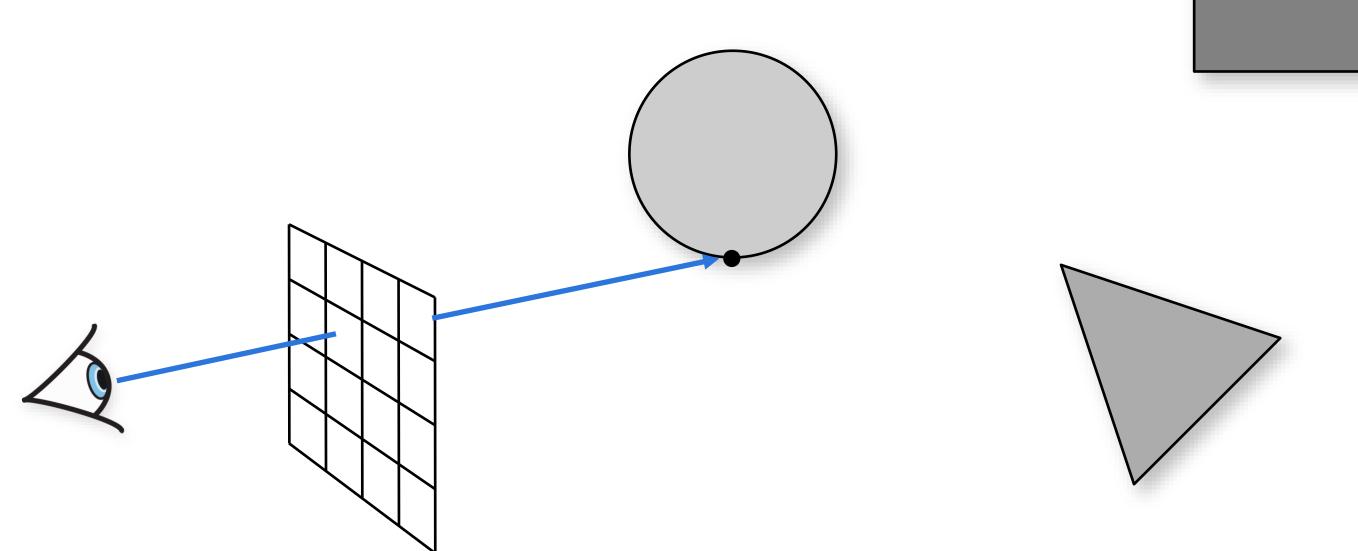
Ray Generation







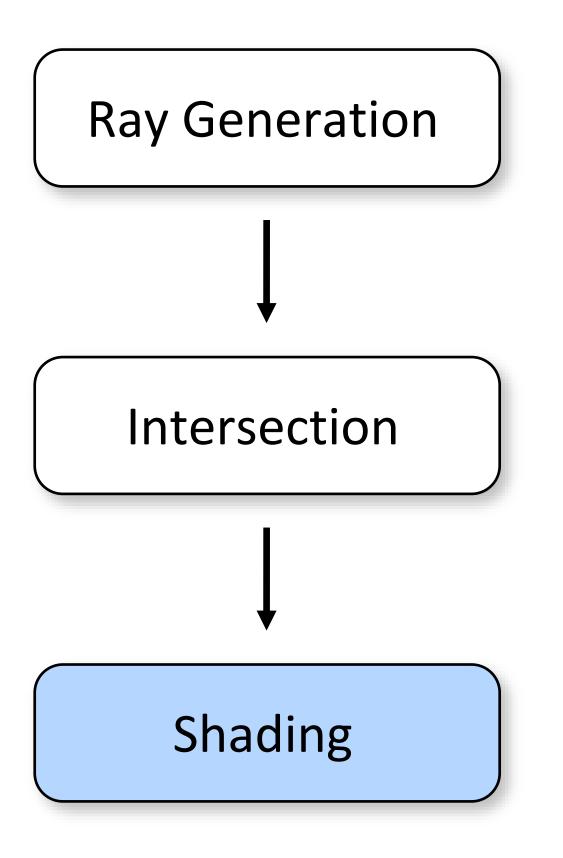


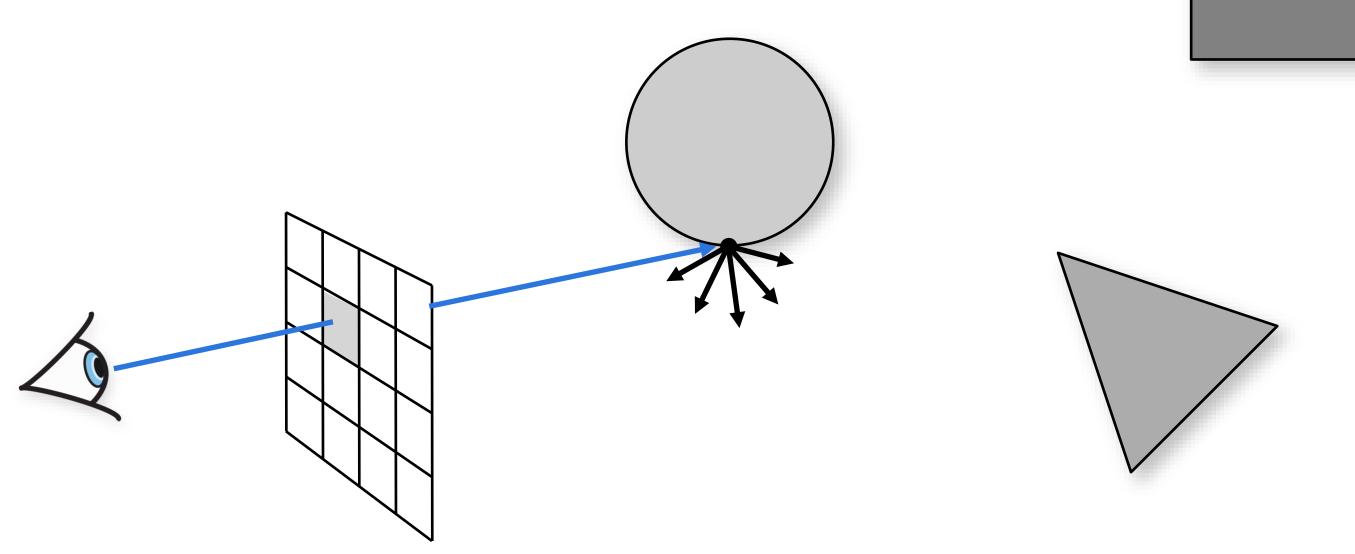








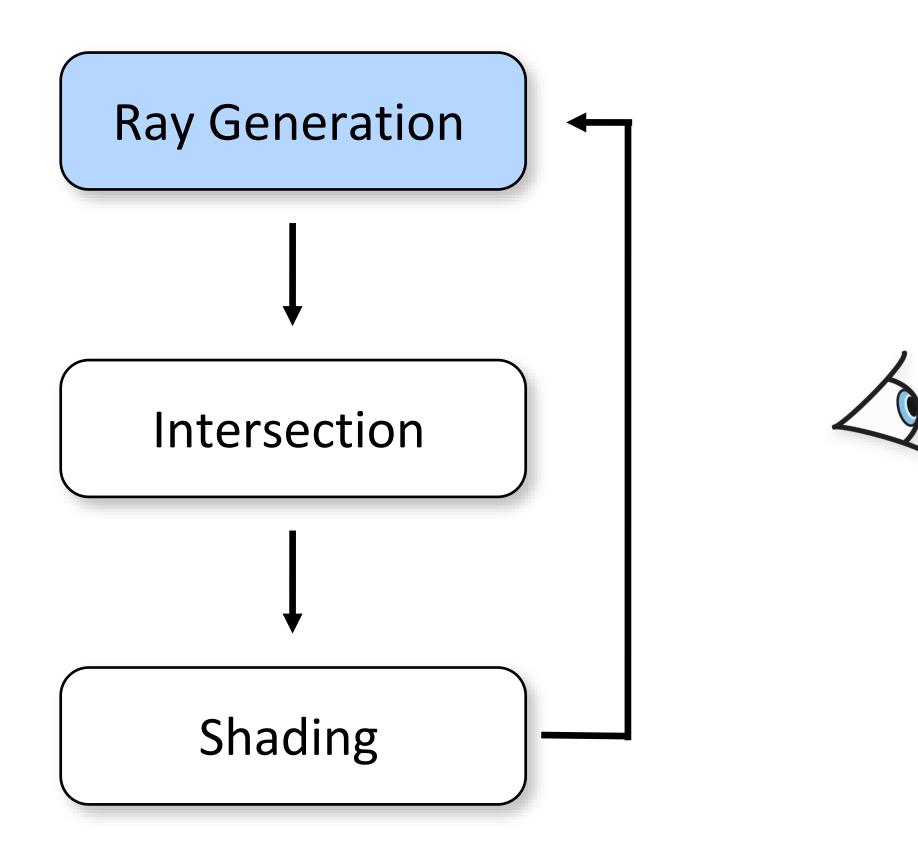


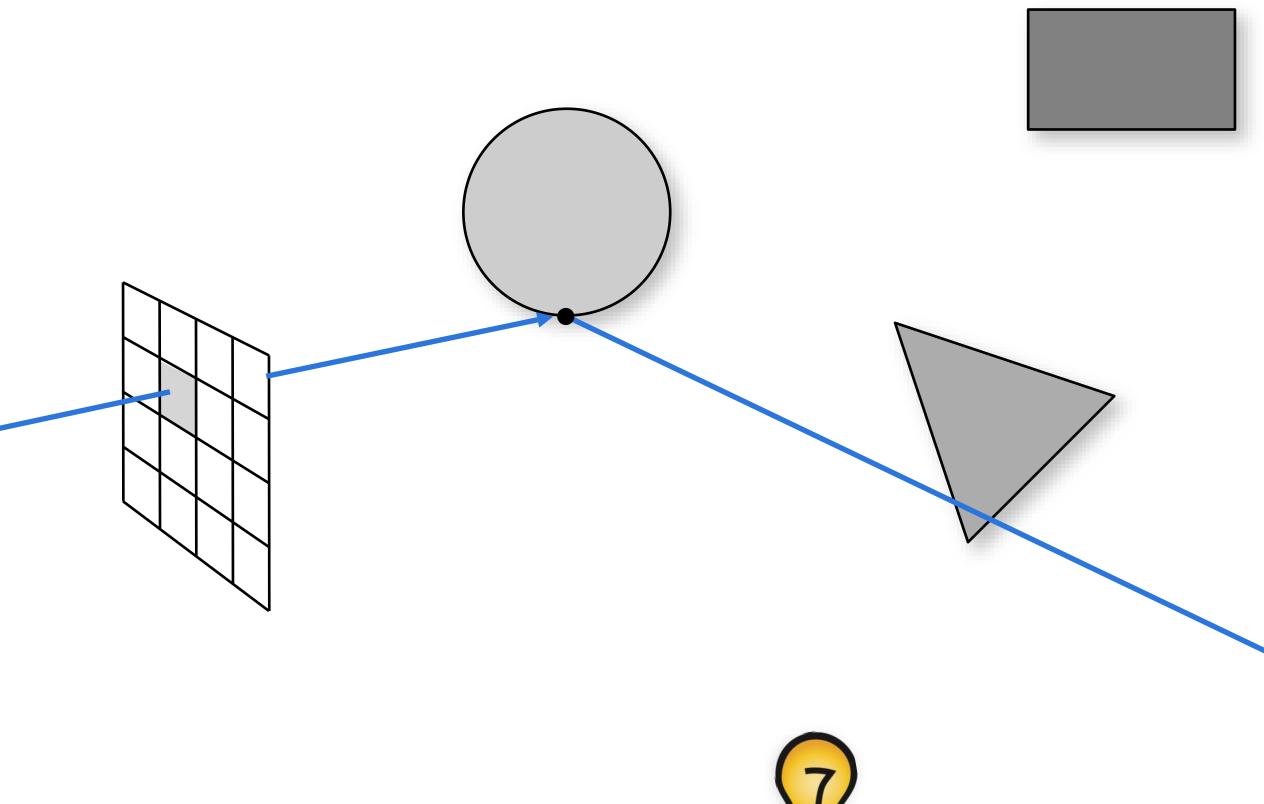






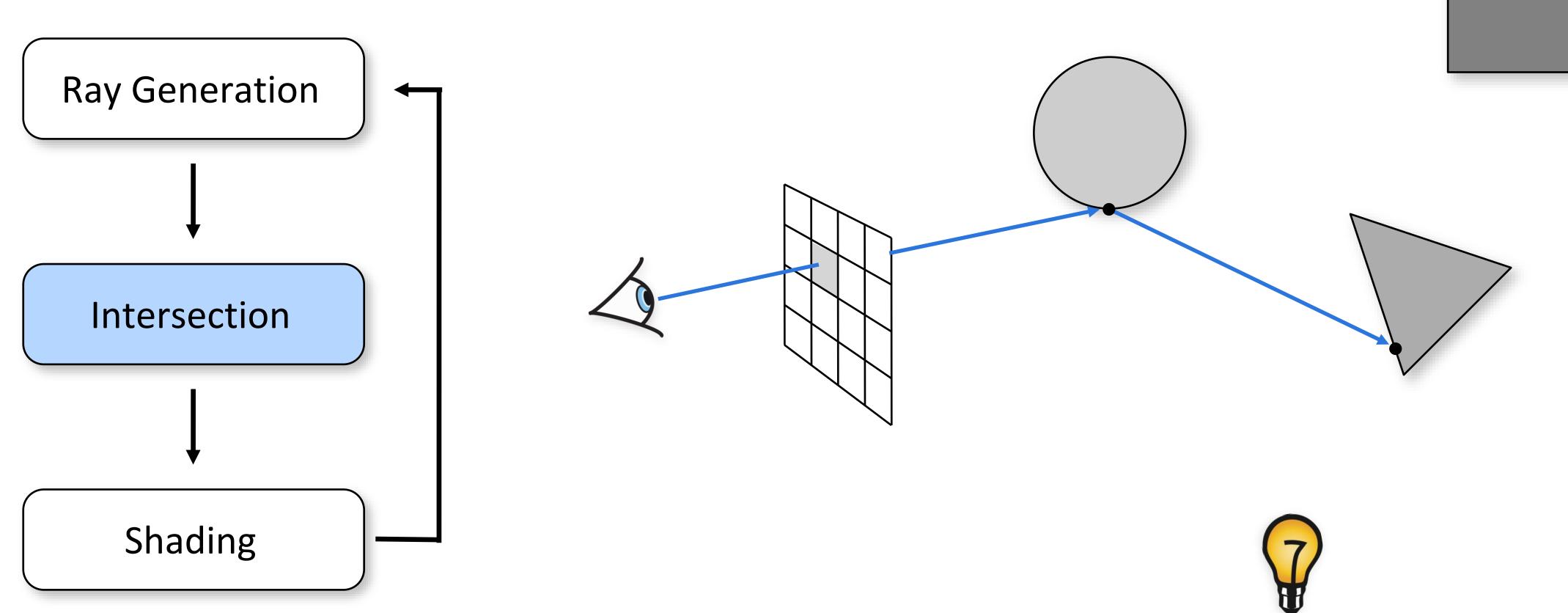






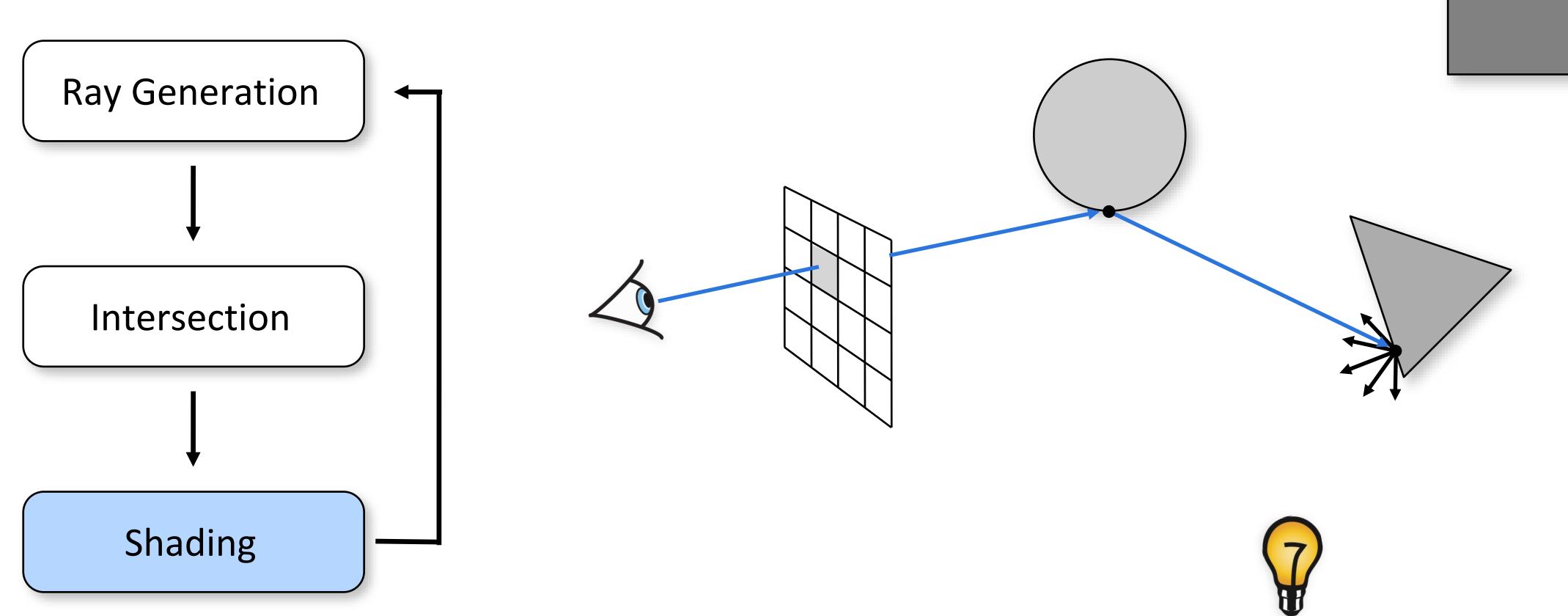






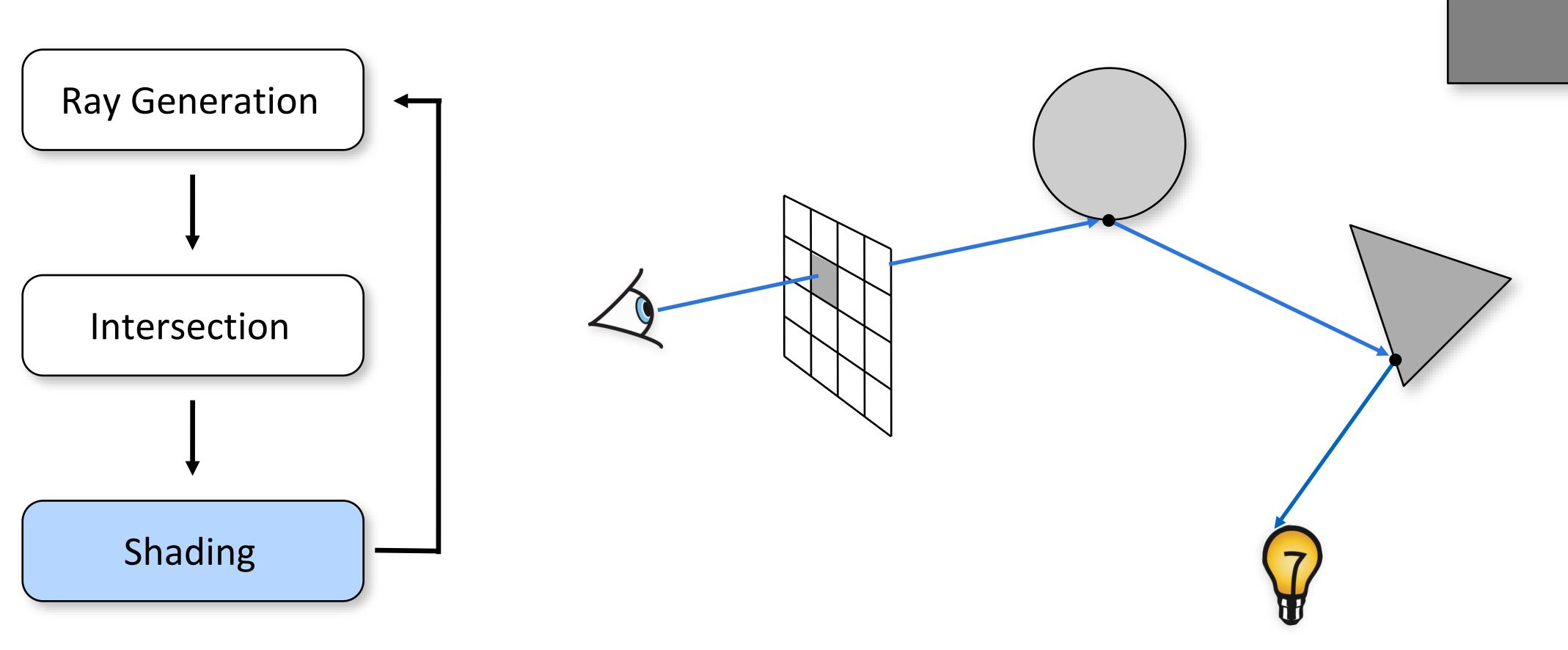
















Ray Tracing Pseudocode

rayTraceImage()

parse scene description

for each pixel ray = generateCameraRay(pixel) pixelColor = trace(ray)



Ray Tracing Pseudocode trace(ray) hit = find first intersection with scene objects color = (shade(hit)) return color might trace more rays (recursive)



Ray Tracing Pseudocode

rayTraceImage()

parse scene description

for each pixel ray = (generateCameraRay(pixel) pixelColor = trace(ray) what is a ray?

how do we generate a camera ray?

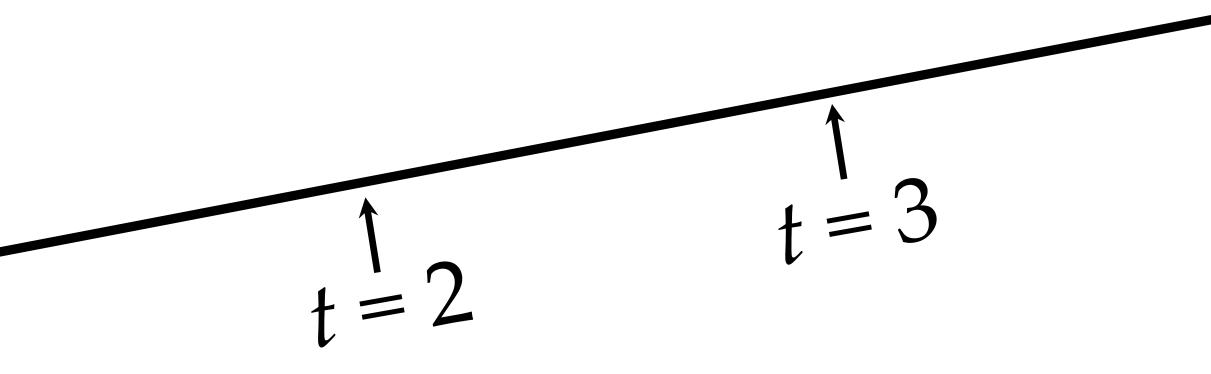


Ray: a half line

Standard representation: origin (point) o and direction d

- this is a parametric equation for the line
- lets us directly generate the points on the line
- if we restrict to t > 0 then we have a ray
- note replacing d with ad does not change ray (for a > 0)

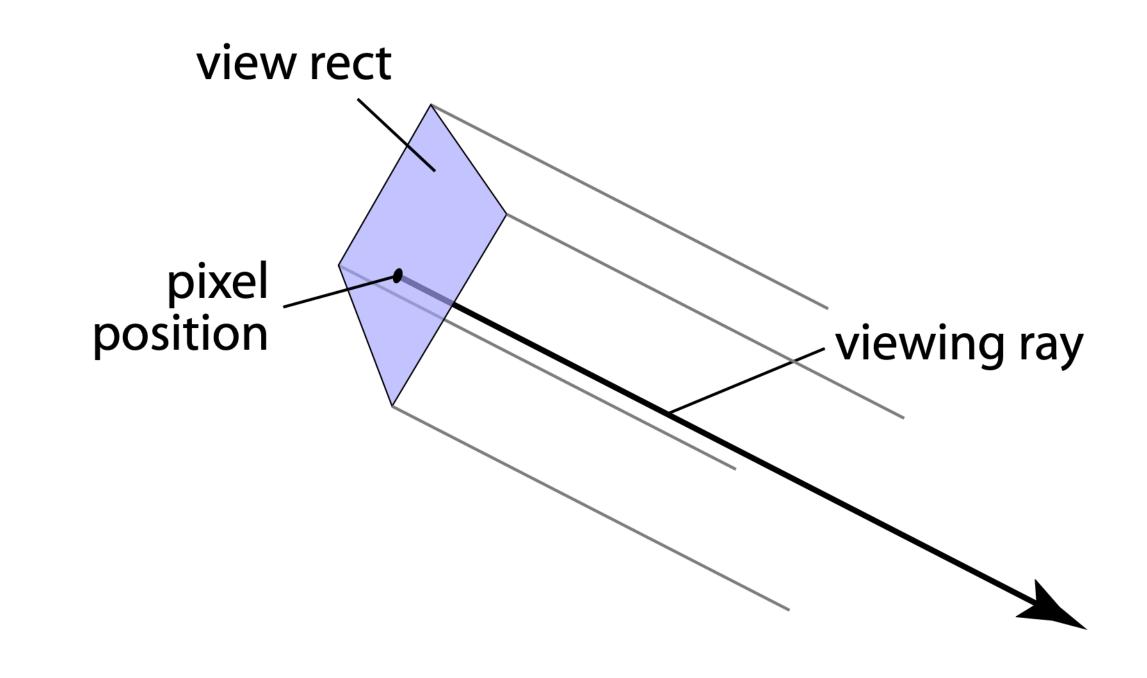
$\mathbf{r}(t) = \mathbf{o} + t\mathbf{d}$

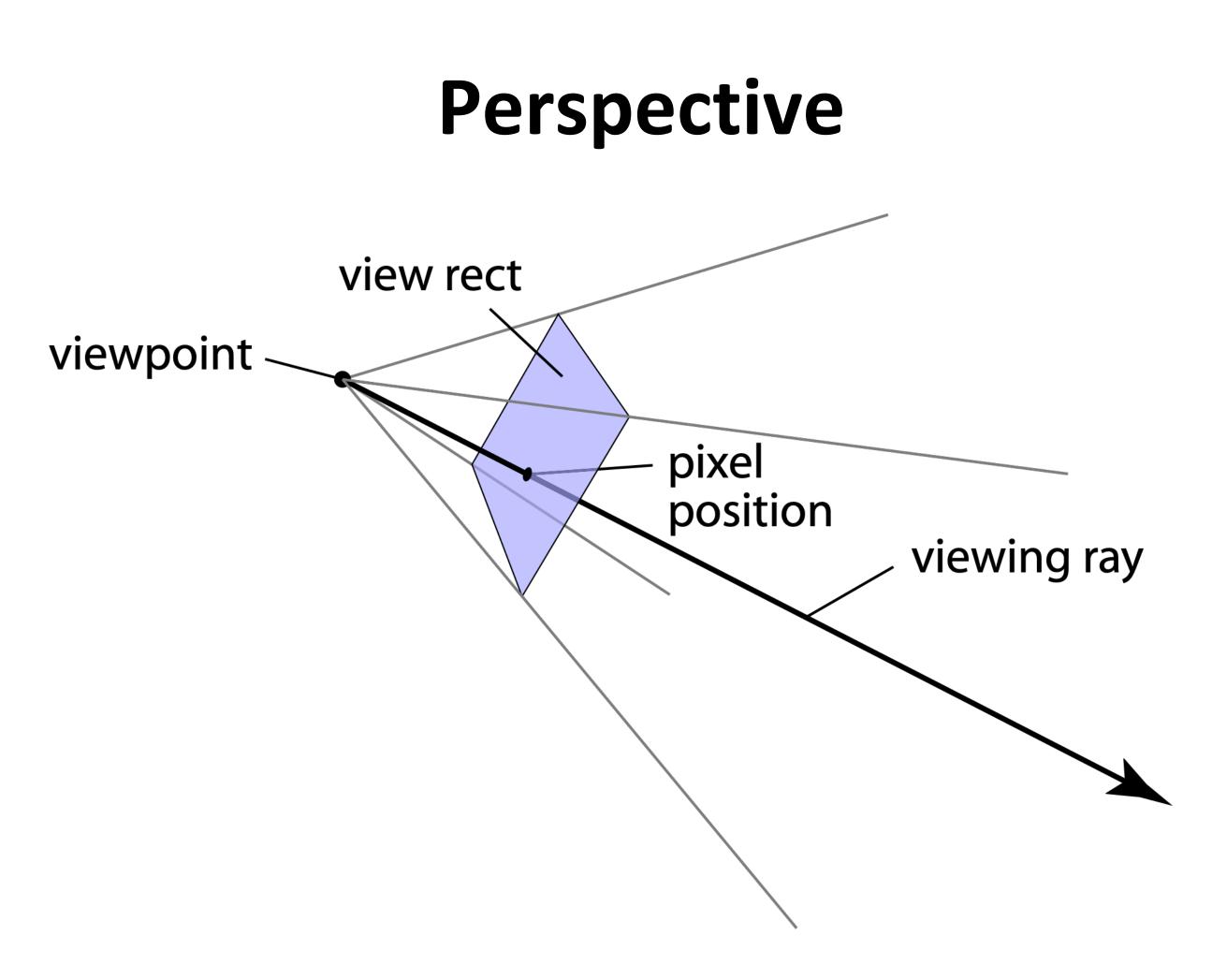




Generating eye rays

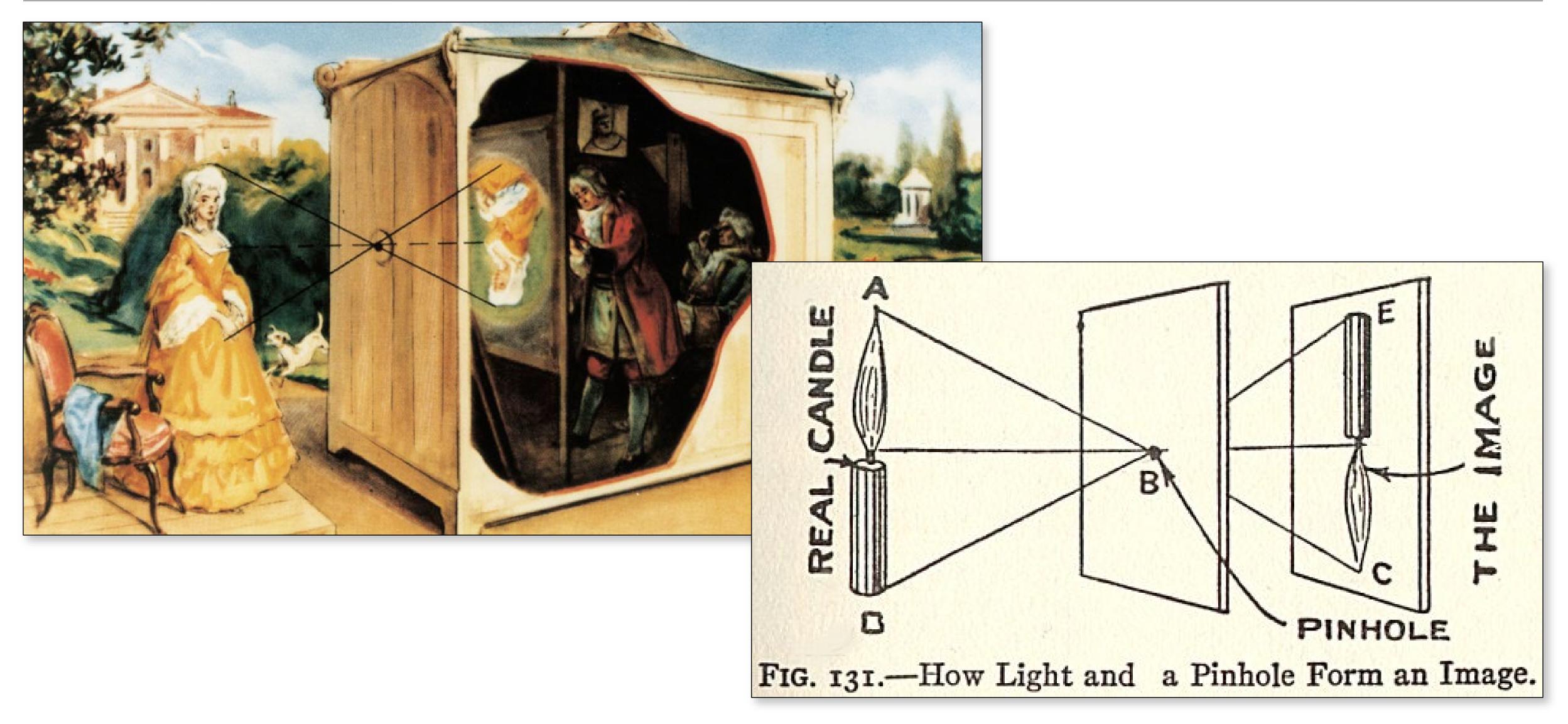
Orthographic





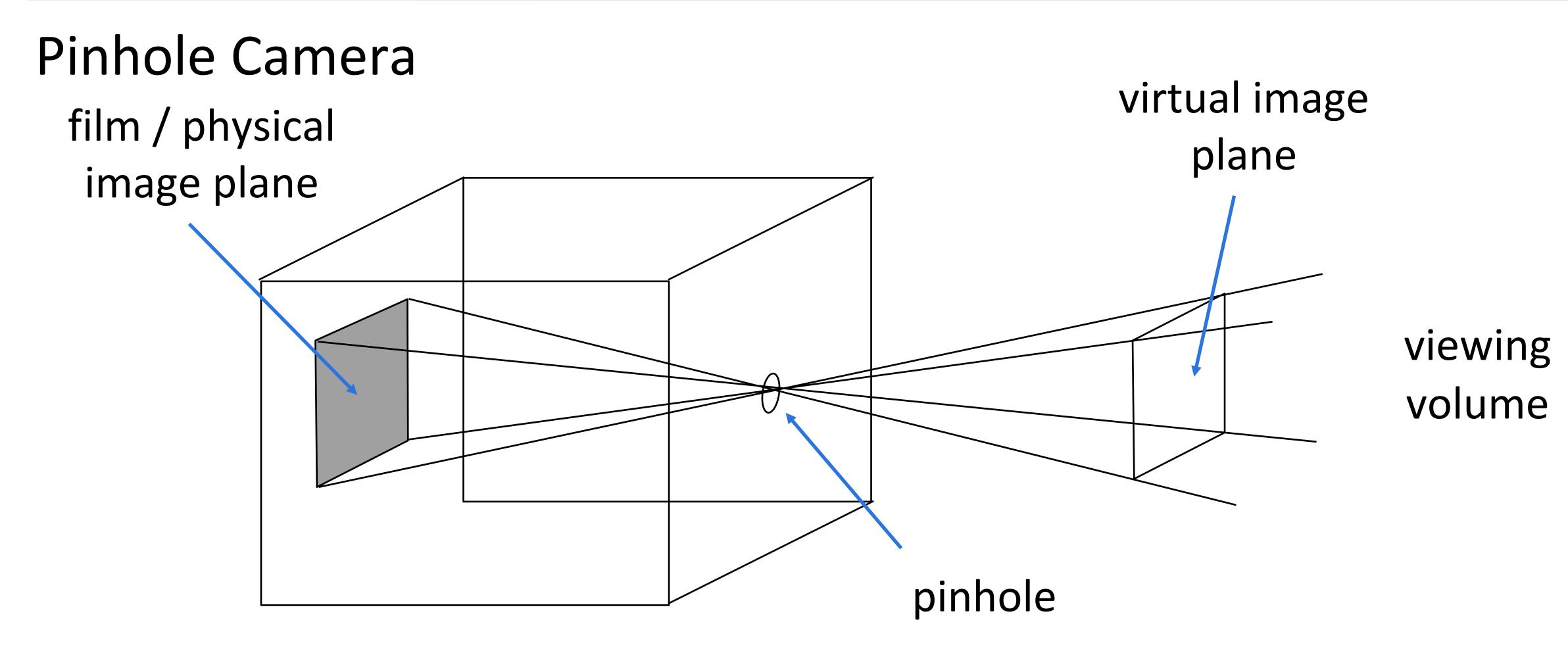


Pinhole Camera (Camera Obscura)





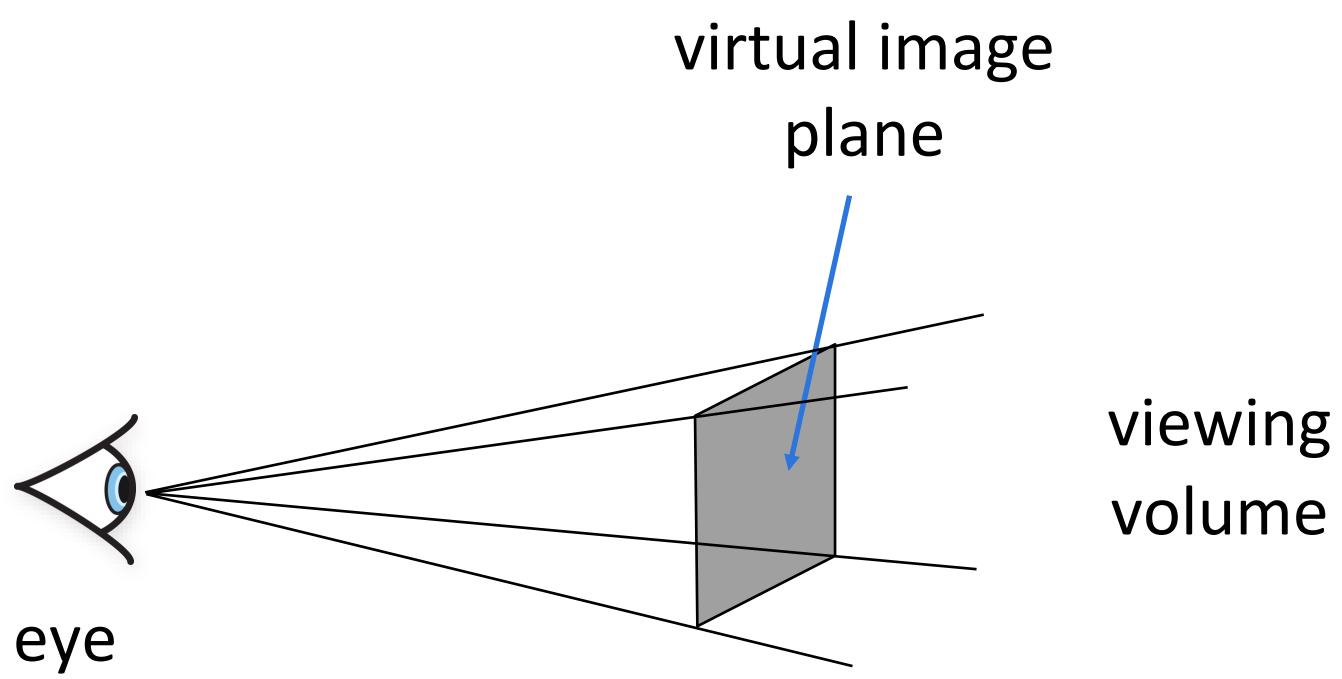
Pinhole Camera





Pinhole Camera

Pinhole Camera





Generating eye rays—perspective

Establish view rectangle in X–Y plane, specified by, e.g. - l, r, t, b

Place rectangle at z = -d

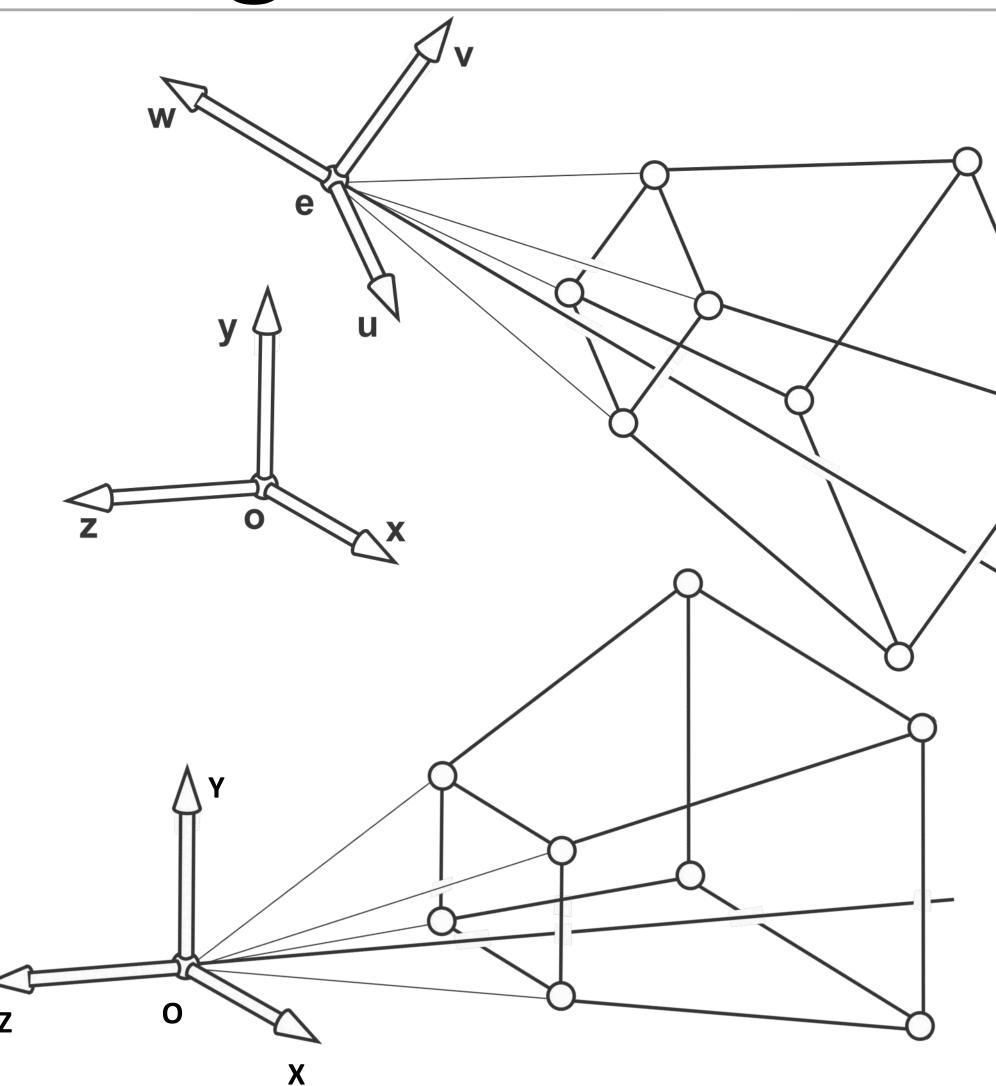
$$\mathbf{s} = [u, v, -d]^T$$
$$\mathbf{d} = \mathbf{s}$$
$$\mathbf{r}(t) = \mathbf{o} + t\mathbf{d}$$

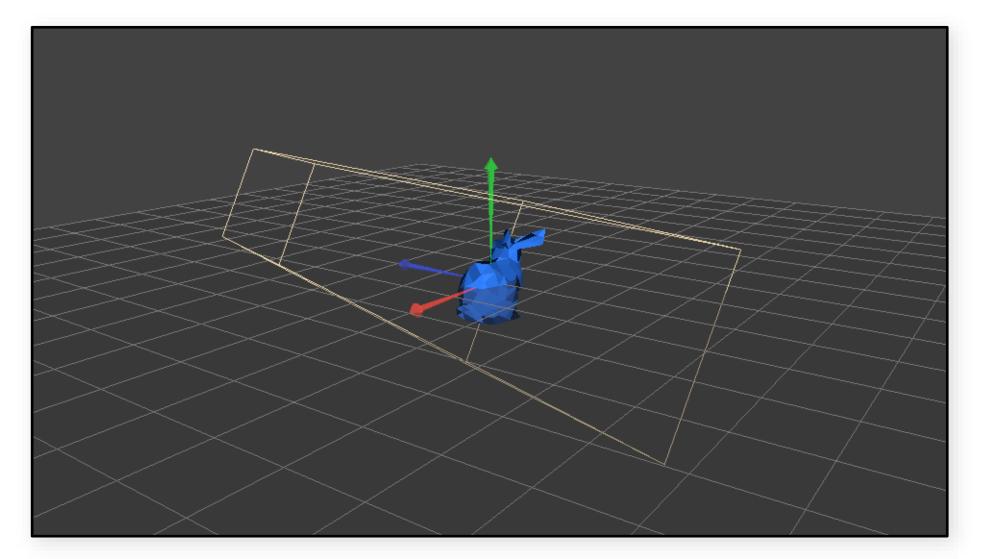
Does distance d matter?

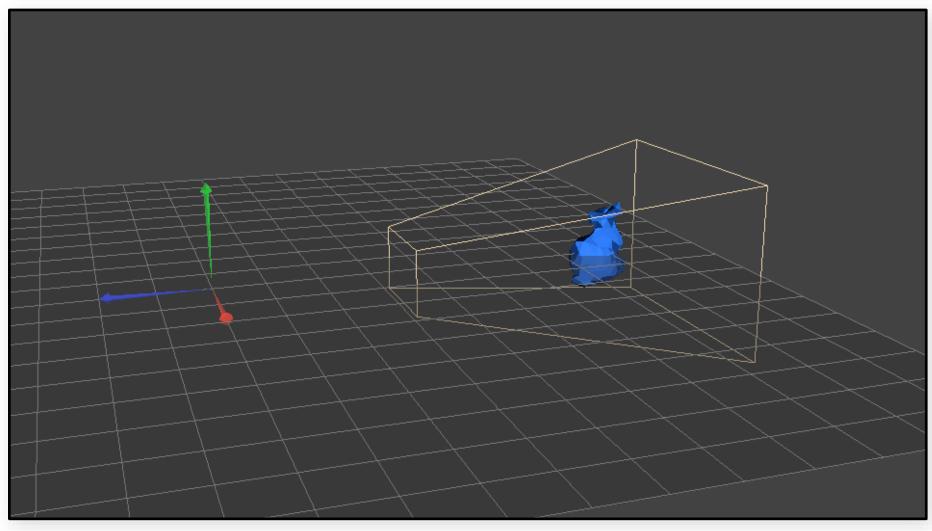
 $\vee \geq t$



Placing the camera in the scene





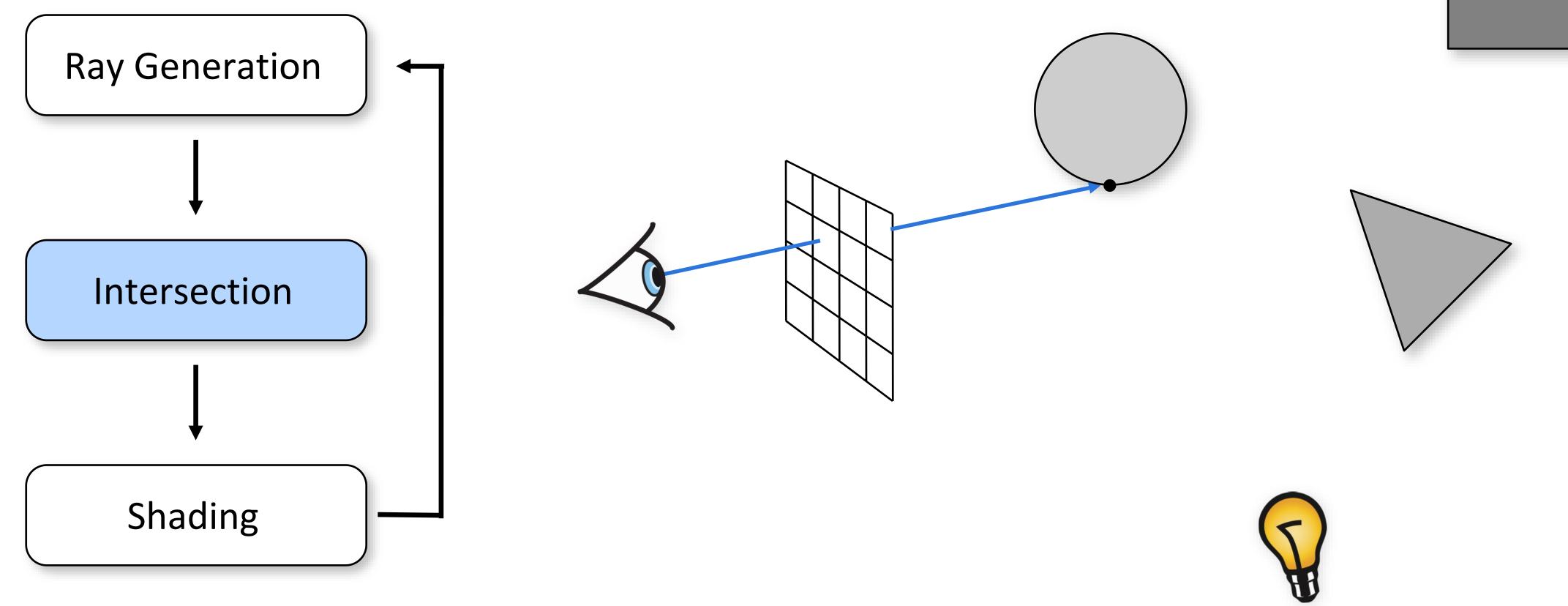


Generating eye rays—orthographic

How do you generate a ray for an orthographic camera?



Ray-Surface Intersections







Ray-Surface Intersections

Surface primitives

- spheres
- planes
- triangles
- general implicits
- etc.



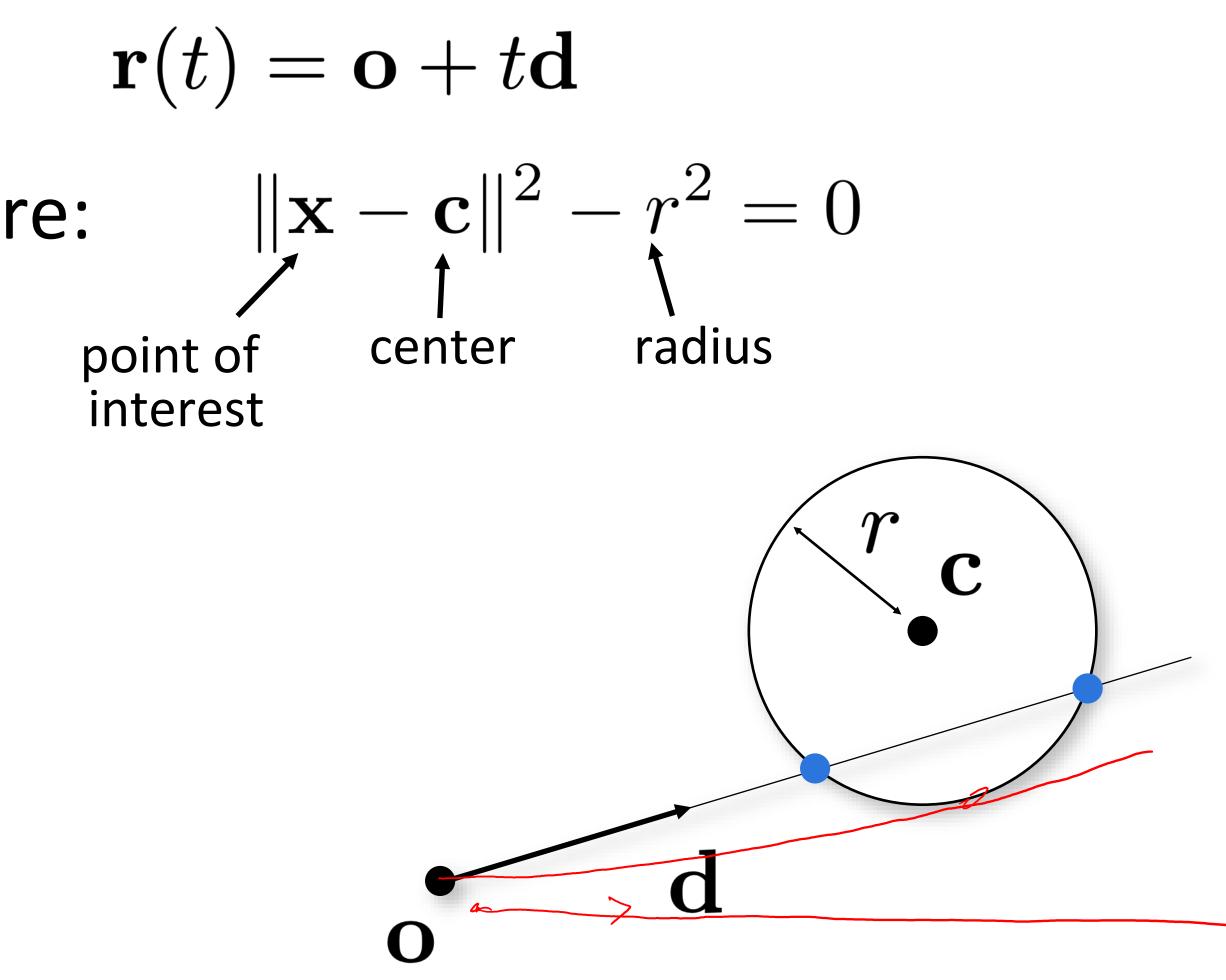
Ray-Sphere Intersection

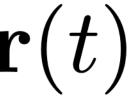
Algebraic approach:

- Condition 1: point is on ray:
- Condition 2: point is on sphere:

- substitute and solve for *t*:

$$\|\mathbf{o} + t\mathbf{d} - \mathbf{c}\|^2 - r^2 = 0$$







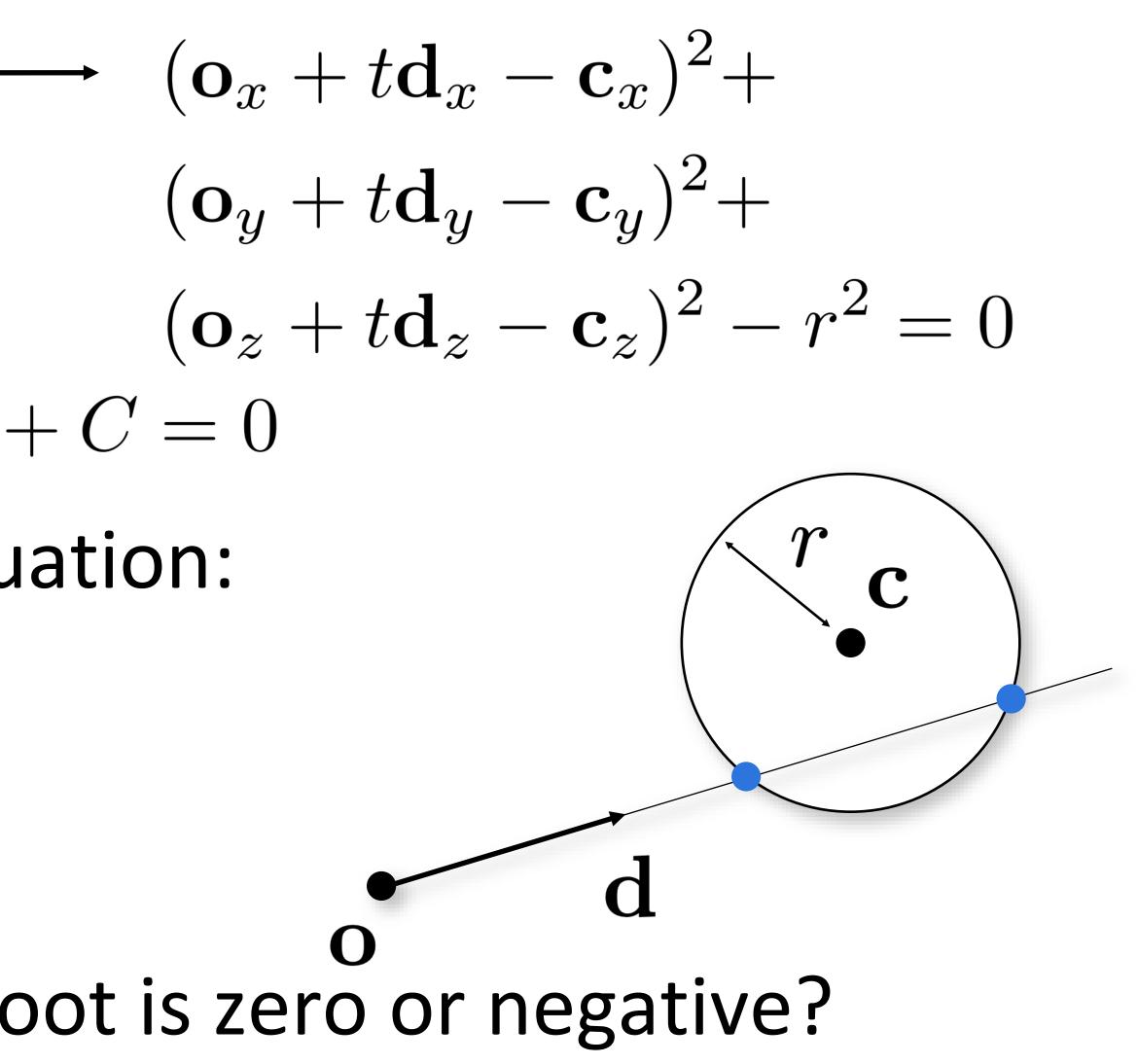
Ray-Sphere Intersection

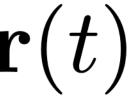
substitute and solve for t $\|\mathbf{o} + t\mathbf{d} - \mathbf{c}\|^2 - r^2 = 0 \longrightarrow (\mathbf{o}_x + t\mathbf{d}_x - \mathbf{c}_x)^2 +$

which reduces to: $At^2 + Bt + C = 0$ Solve for *t* using quadratic equation:

$$t = \frac{-B \pm \sqrt{B^2 - 4AC}}{2A}$$

What happens when square root is zero or negative?







Ray-Surface Intersections

Surface primitives

- spheres
- planes
- triangles
- general implicits
- etc.

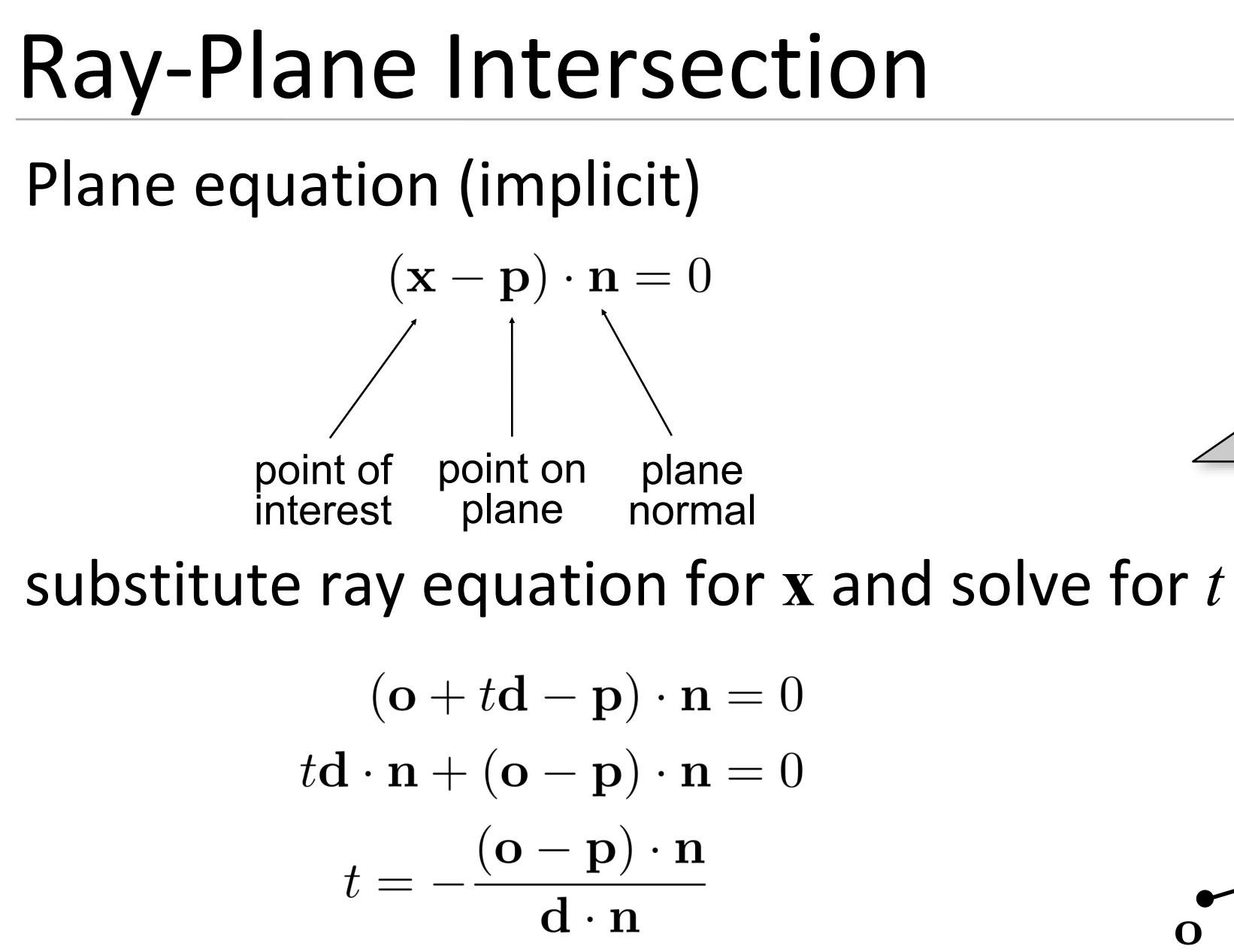


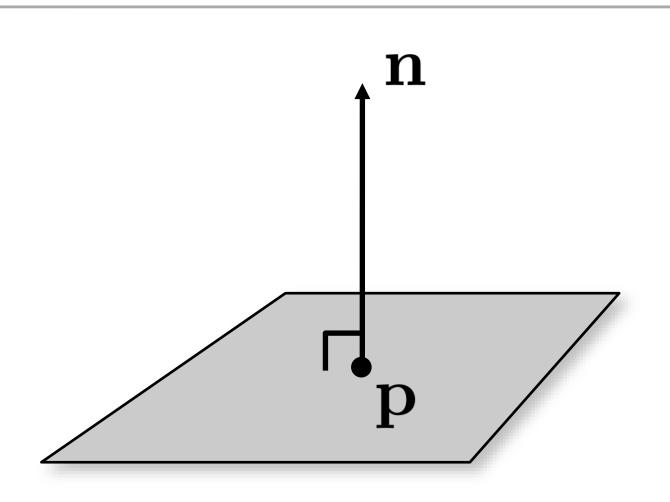
Ray-Plane Intersection Plane equation (implicit)

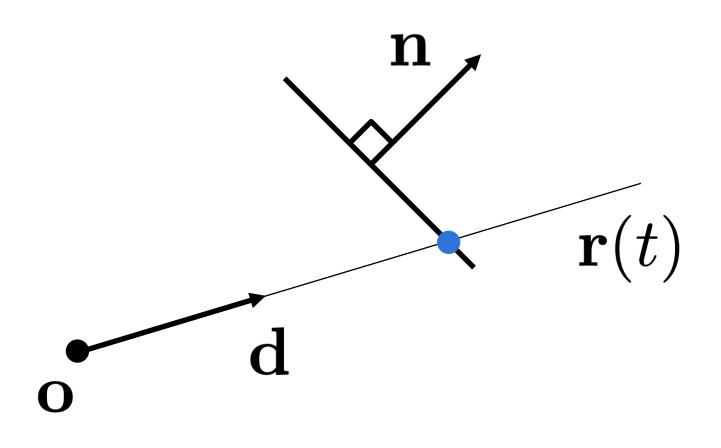
Algebraic form:

ax + by + cz + d = 0











Ray-Surface Intersections

Surface primitives

- spheres
- planes
- triangles
- general implicits
- etc.



Ray-Triangle intersection Condition 1: point is on ray: Condition 2: point is on plane: Condition 3: point is on the inside of all three edges First solve 1&2 (ray–plane intersection) for t: $(\mathbf{o} + t\mathbf{d})$ $t = -\frac{(\mathbf{o} - \mathbf{p}) \cdot}{\mathbf{d} \cdot \mathbf{n}}$

Several options for 3

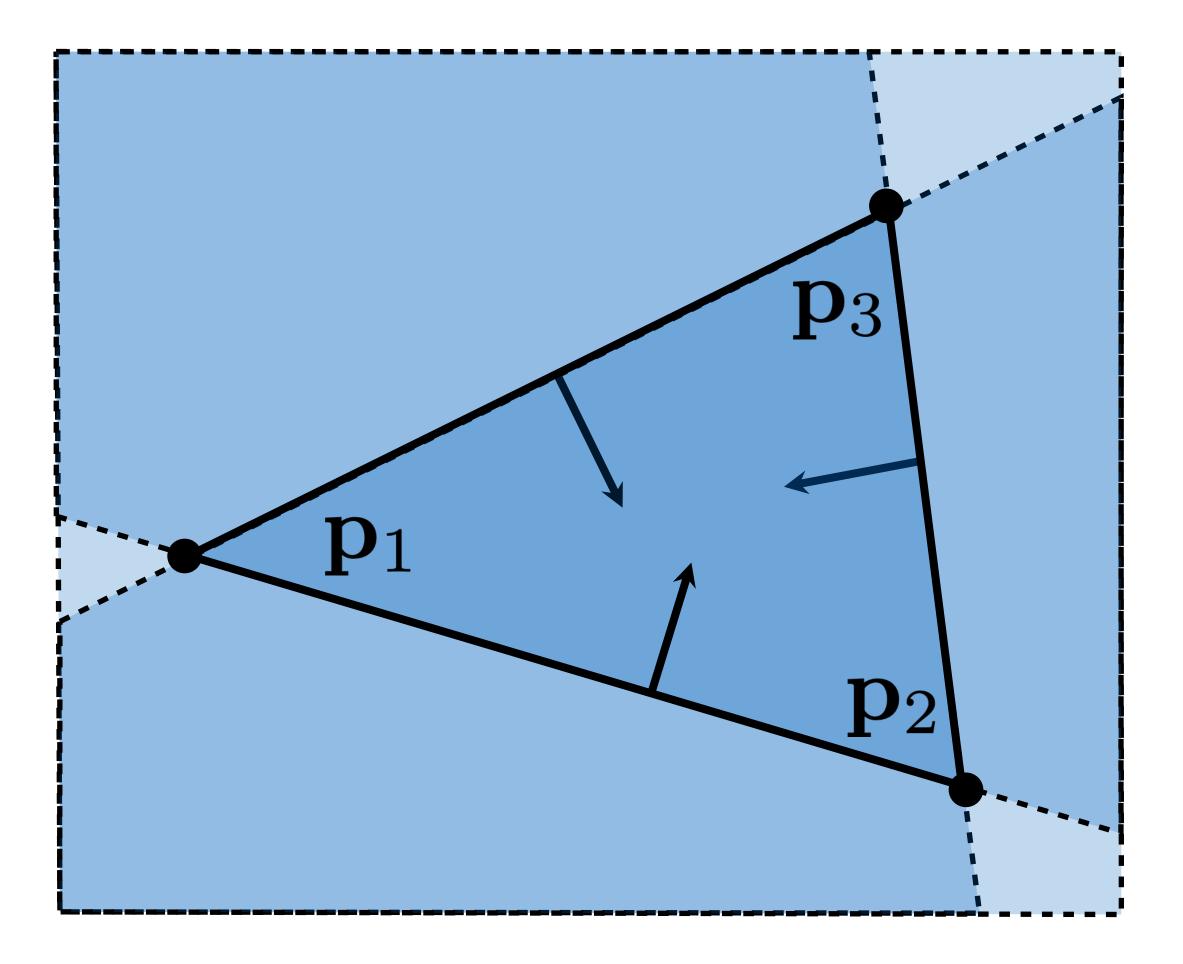
$$\mathbf{r}(t) = \mathbf{o} + t\mathbf{d}$$

$$(\mathbf{x} - \mathbf{p}) \cdot \mathbf{n} = 0$$

$$-\mathbf{p}) \cdot \mathbf{n} = 0$$
$$\mathbf{p} - \mathbf{p} \cdot \mathbf{n}$$



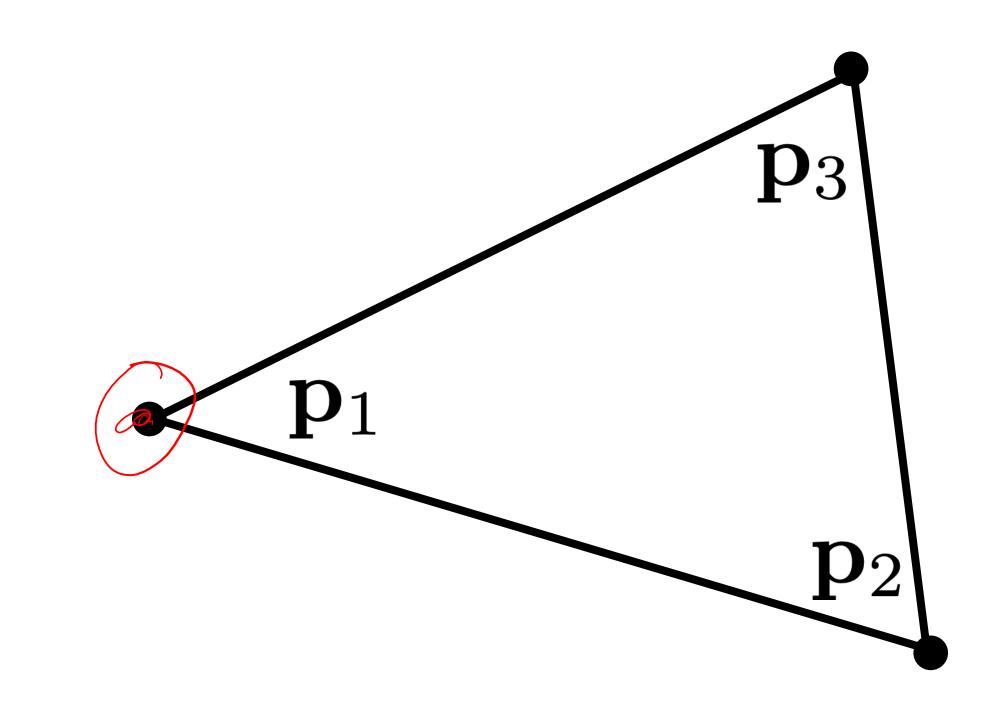
In plane, triangle is the intersection of 3 half spaces





$\mathbf{n} = (\mathbf{p}_2 - \mathbf{p}_1) \times (\mathbf{p}_3 - \mathbf{p}_1)$

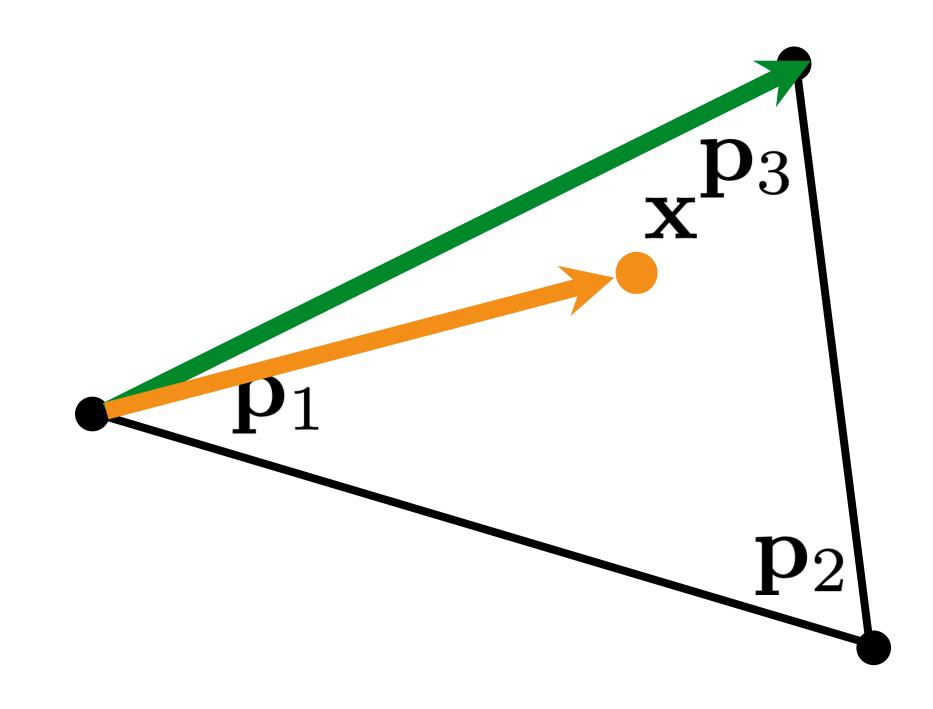
Which way does n point?





$\mathbf{n} = (\mathbf{p}_2 - \mathbf{p}_1) \times (\mathbf{p}_3 - \mathbf{p}_1)$ $\mathbf{n}_{\mathbf{x}13} = (\mathbf{x} - \mathbf{p}_1) \times (\mathbf{p}_3 - \mathbf{p}_1)$ Which way does **n** point?

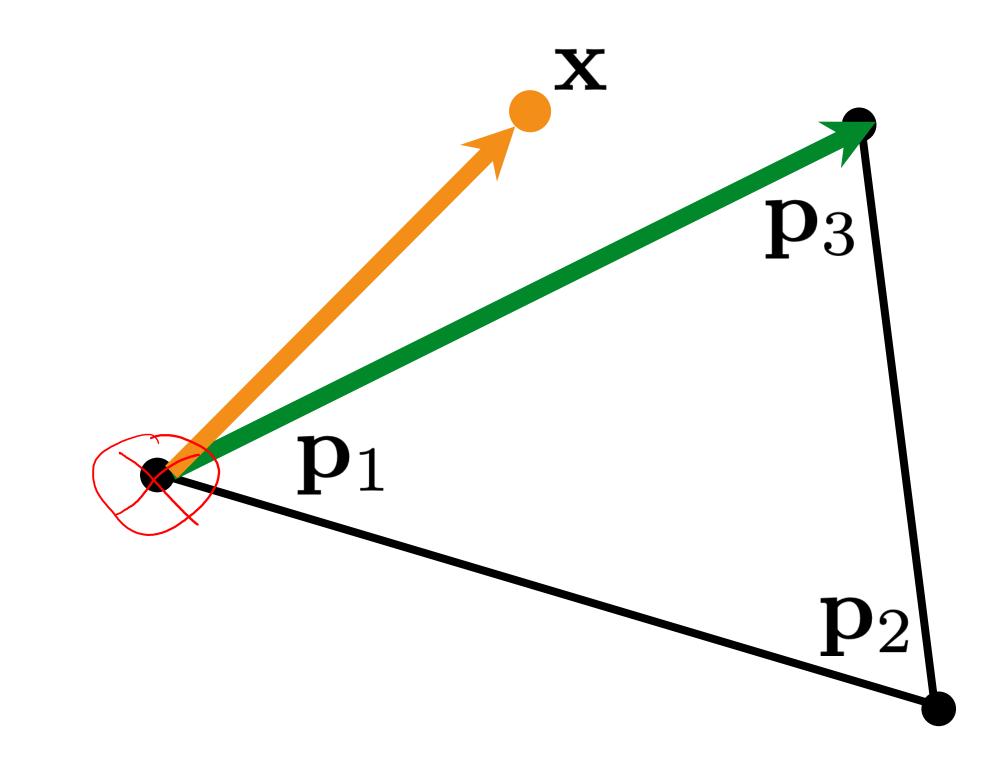
What about n_{x13} ?





$\mathbf{n} = (\mathbf{p}_2 - \mathbf{p}_1) \times (\mathbf{p}_3 - \mathbf{p}_1)$ $\mathbf{n}_{\mathbf{x}13} = (\mathbf{x} - \mathbf{p}_1) \times (\mathbf{p}_3 - \mathbf{p}_1)$

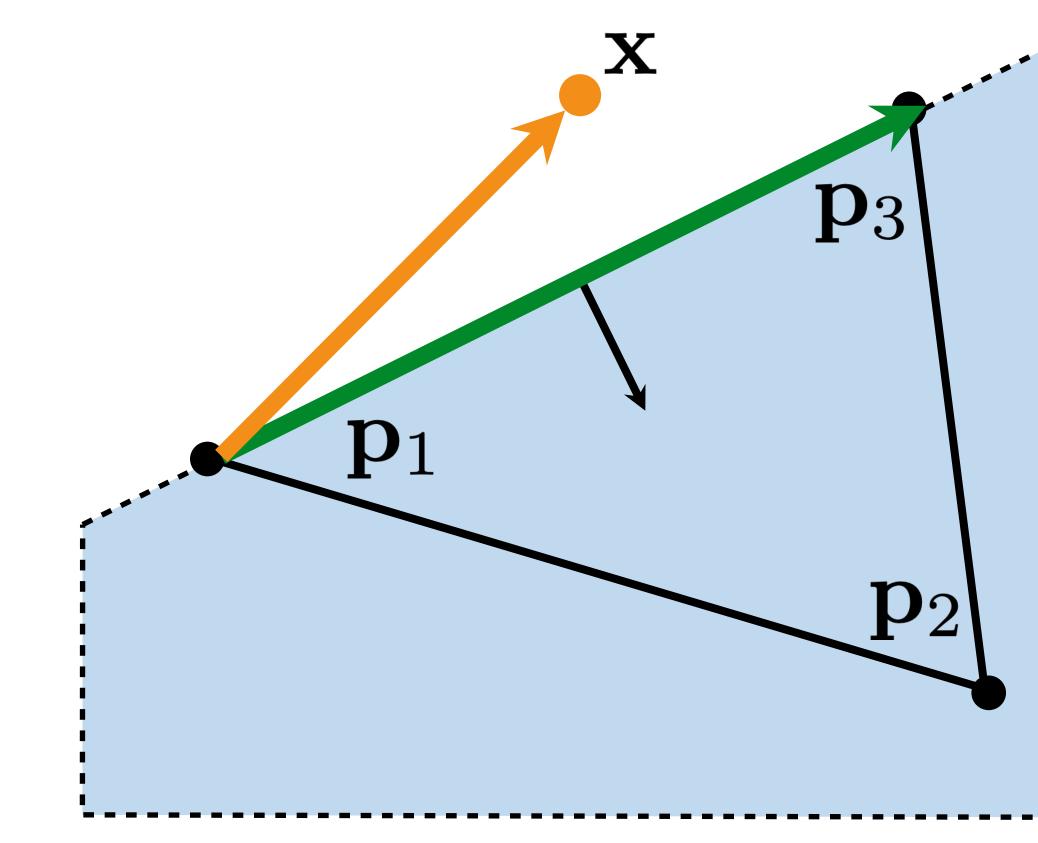
- Which way does n point?
- What about nx13?
- How about now?





$\mathbf{n} = (\mathbf{p}_2 - \mathbf{p}_1) \times (\mathbf{p}_3 - \mathbf{p}_1)$ $\mathbf{n}_{\mathbf{x}13} = (\mathbf{x} - \mathbf{p}_1) \times (\mathbf{p}_3 - \mathbf{p}_1)$

- Which way does n point?
- What about n_{x13} ?
- How about now?
- Edge test: $(\mathbf{n}_{\mathbf{x}13} \cdot \mathbf{n}) < 0$

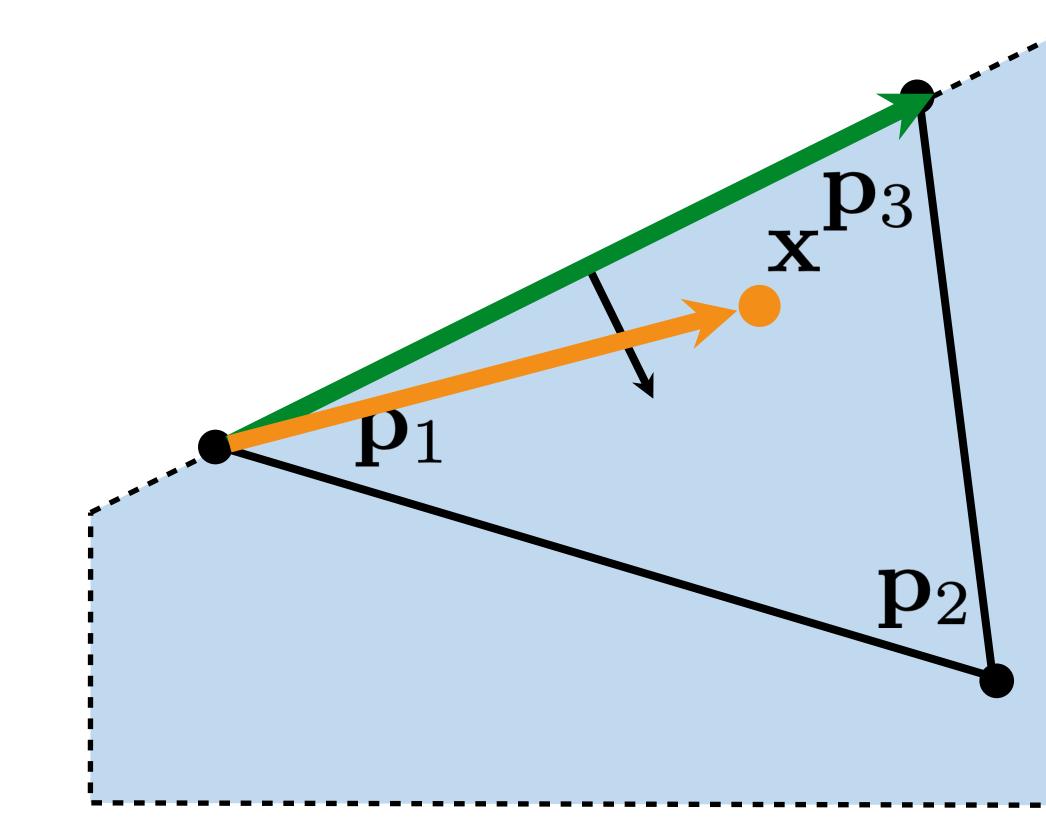






$\mathbf{n} = (\mathbf{p}_2 - \mathbf{p}_1) \times (\mathbf{p}_3 - \mathbf{p}_1)$ $\mathbf{n}_{\mathbf{x}13} = (\mathbf{x} - \mathbf{p}_1) \times (\mathbf{p}_3 - \mathbf{p}_1)$

- Which way does n point?
- What about n_{x13} ?
- How about now?
- Edge test: $(\mathbf{n}_{\mathbf{x}13} \cdot \mathbf{n}) < 0$







Intersect ray with triangle's plane

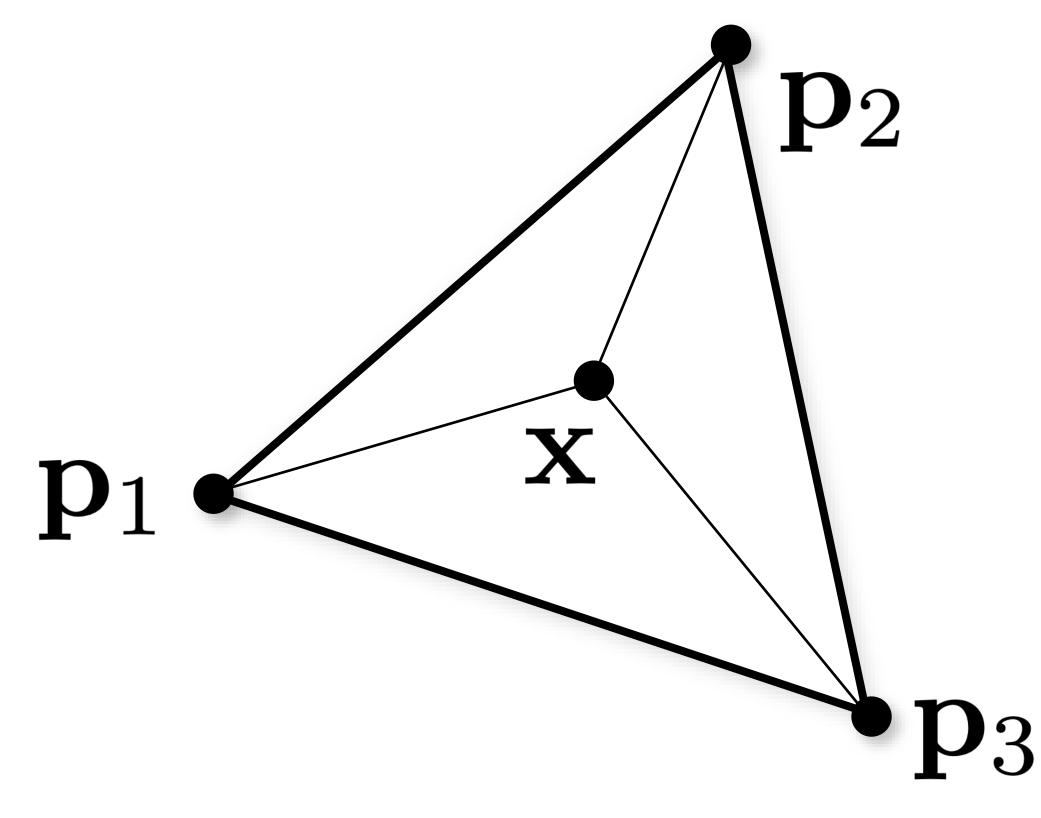
Test whether hit-point is within triangle

- compute sub-triangle areas α, β, γ
- test inside triangle conditions



Barycentric coordinates

- Barycentric coordinates:
- Inside triangle conditions:

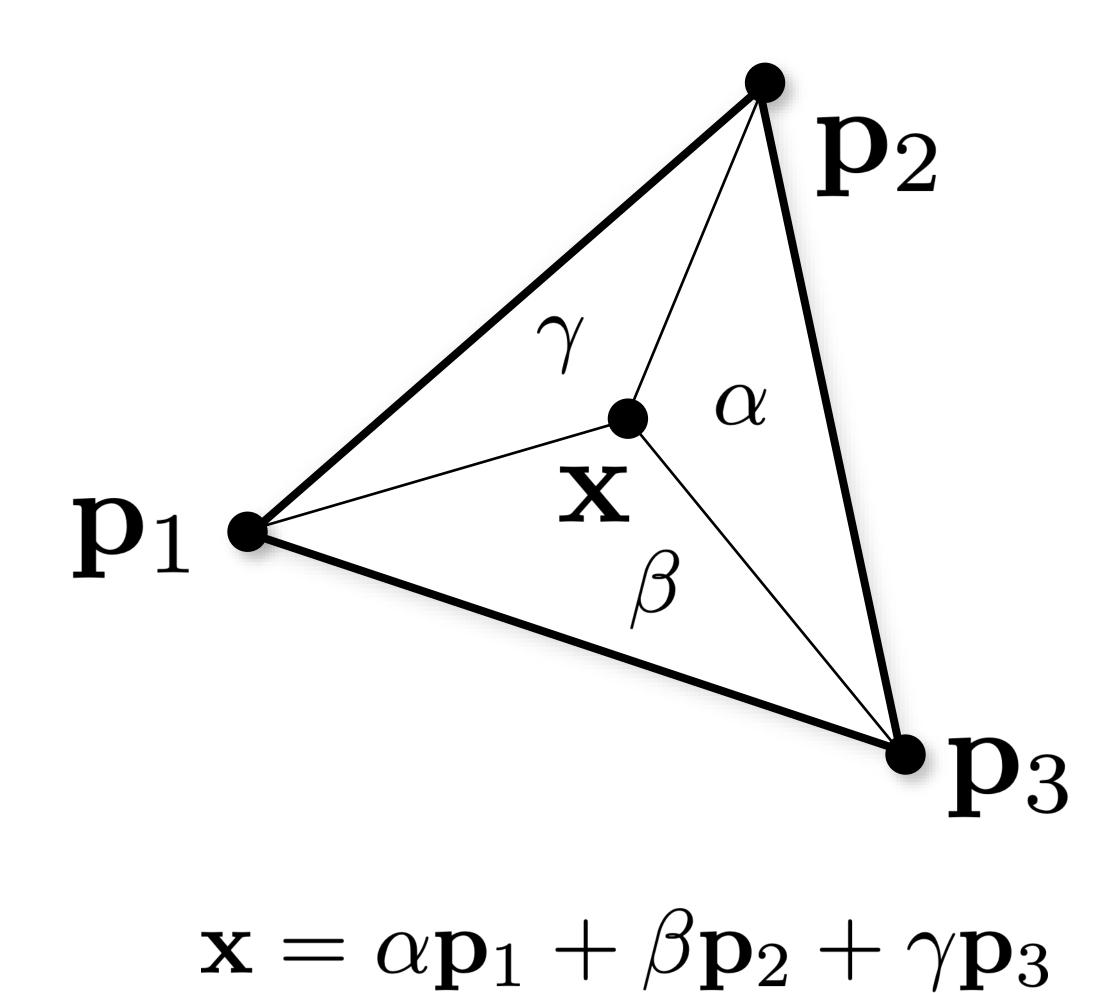


 $\mathbf{x}(\alpha, \beta, \gamma) = \alpha \mathbf{p}_1 + \beta \mathbf{p}_2 + \gamma \mathbf{p}_3$ $\alpha + \beta + \gamma = 1 \quad 0 \le \alpha \le 1$ $\gamma = 1 - \alpha - \beta \quad 0 \le \beta \le 1$ $0 \le \gamma \le 1$



Interpretations of barycentric coords

Sub-triangle areas



 $\alpha = |\Delta \mathbf{p}_2 \mathbf{p}_3 \mathbf{x}| / |\Delta \mathbf{p}_1 \mathbf{p}_2 \mathbf{p}_3|$ $\beta = |\Delta \mathbf{p}_1 \mathbf{p}_3 \mathbf{x}| / |\Delta \mathbf{p}_1 \mathbf{p}_2 \mathbf{p}_3|$ $\gamma = |\Delta \mathbf{p}_1 \mathbf{p}_2 \mathbf{x}| / |\Delta \mathbf{p}_1 \mathbf{p}_2 \mathbf{p}_3|$

Ray-Triangle Intersection (Approach 3) $\alpha \mathbf{p}_1 + \beta \mathbf{p}_2 + (1 - \alpha - \beta)\mathbf{p}_3 = \mathbf{o} + t\mathbf{d}$ Insert ray equation: $\alpha(\mathbf{p}_1 - \mathbf{p}_3) + \beta(\mathbf{p}_2 - \mathbf{p}_3) + \mathbf{p}_3 = \mathbf{o} + t\mathbf{d}$ $\alpha(\mathbf{p}_1 - \mathbf{p}_3) + \beta(\mathbf{p}_2 - \mathbf{p}_3) - t\mathbf{d} = \mathbf{o} - \mathbf{p}_3$ $\alpha \mathbf{a} + \beta \mathbf{b} - t\mathbf{d} = \mathbf{e}$ $\begin{bmatrix} -\mathbf{d} & \mathbf{a} & \mathbf{b} \end{bmatrix} \begin{bmatrix} t \\ \alpha \\ \beta \end{bmatrix} = \mathbf{e}$ Solve directly Can be much faster!





Ray-Surface Intersections

Other primitives

- cylinder
- cone, paraboloid, hyperboloid
- torus
- disk
- general polygons, meshes
- etc.



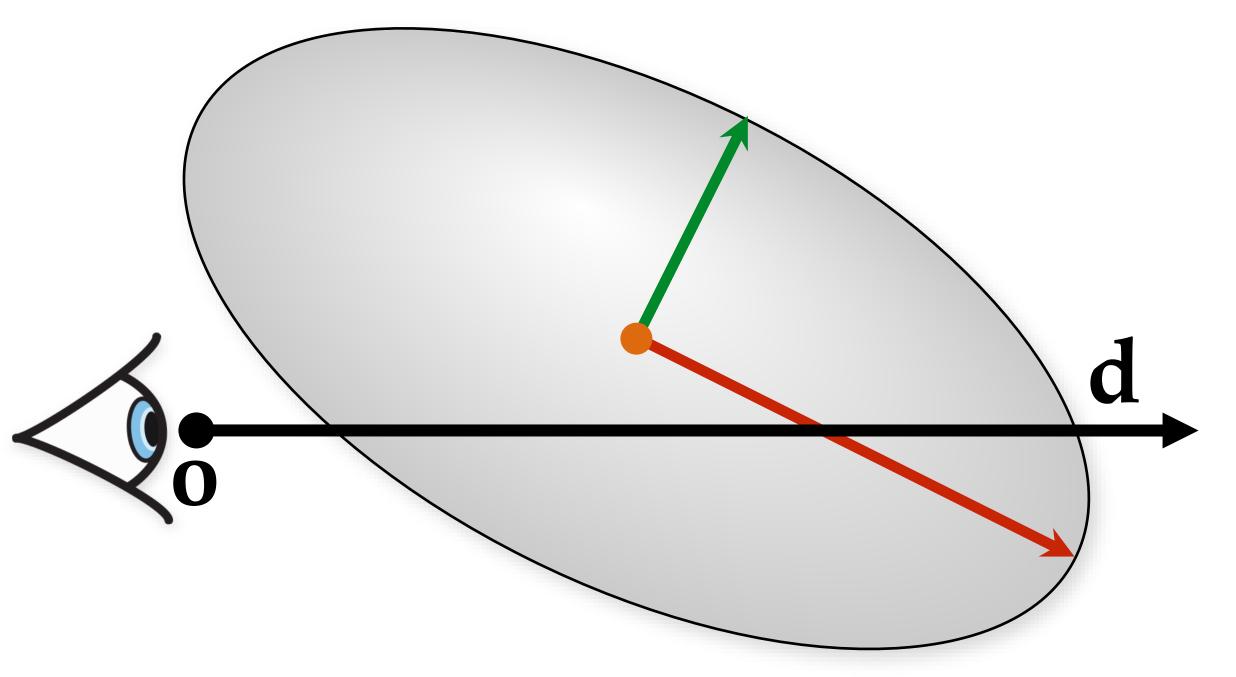
Intersecting transformed primitive?

Option 1: Transform the primitive

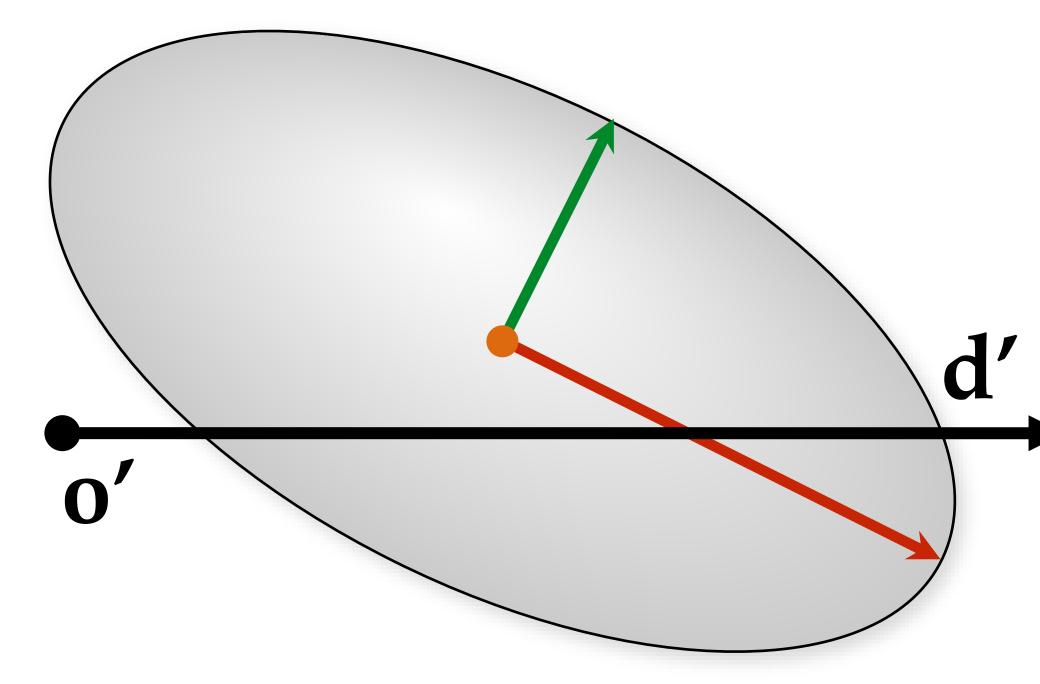
- simple for triangles, since they transform to triangles
- other primitives get more complicated (e.g. sphere \rightarrow ellipsoid)
- Option 2: Transform the ray (by the inverse transform)
- more elegant; works on any primitive
- allows simpler intersection tests (e.g., just use existing sphere-intersection routine)



World space

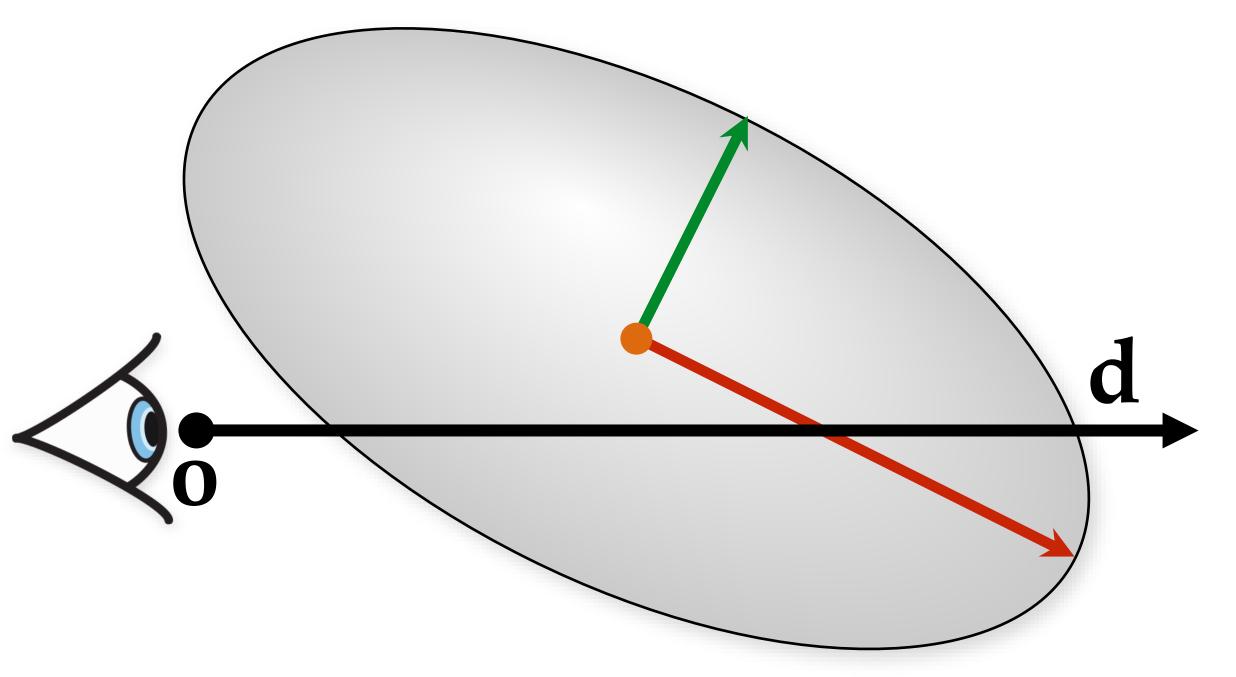


Local space

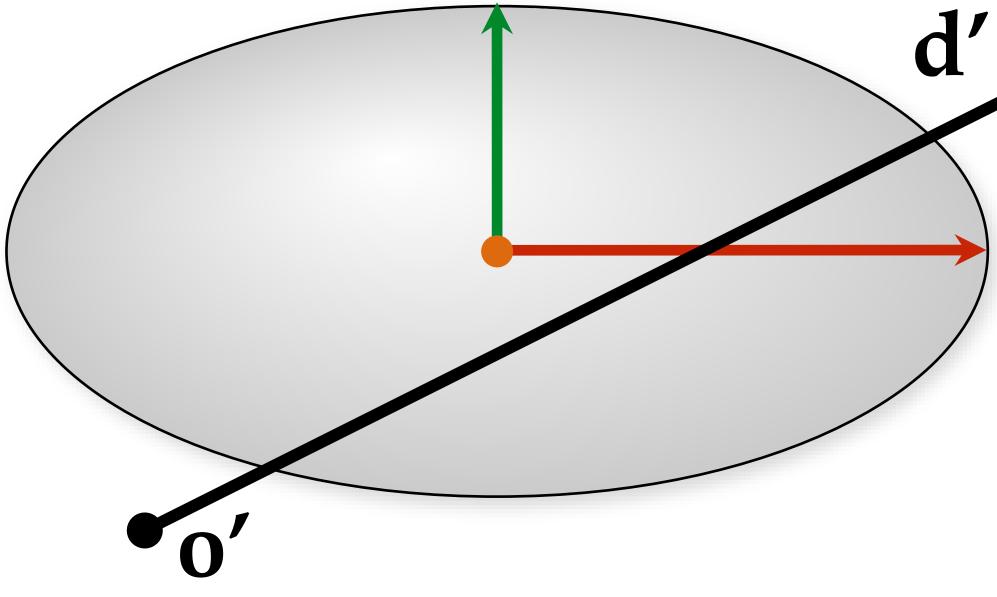




World space

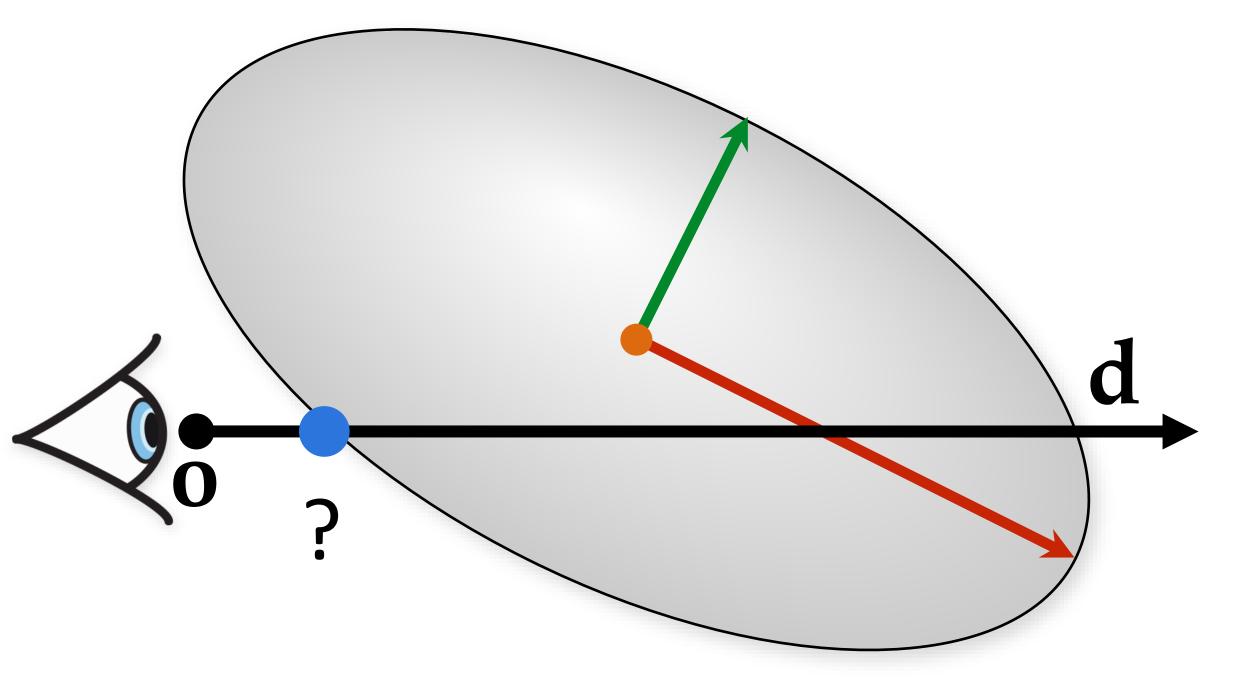


Local space

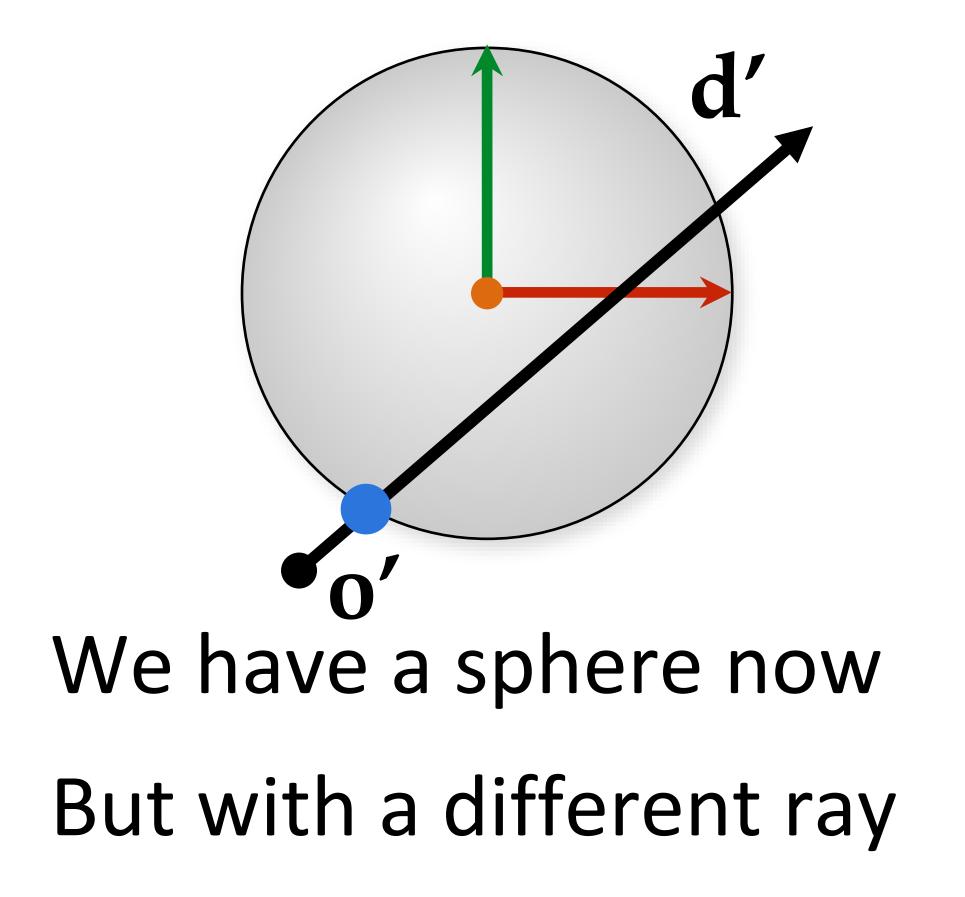




World space



Local space





Transformations in homogeneous coords

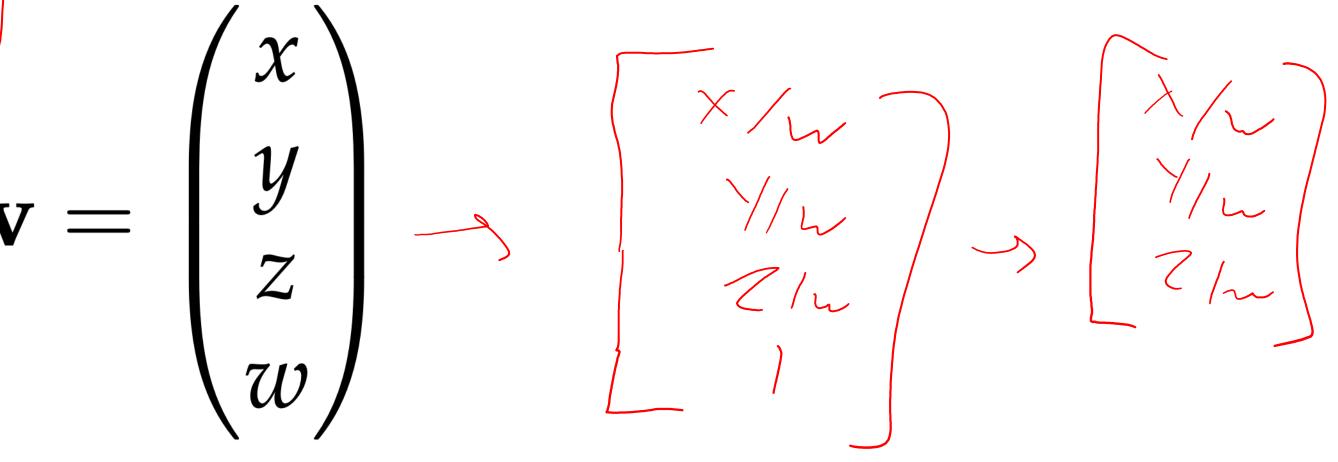
A 3D transformation matrix:

A 3D homogenous vector:

A position has $w \neq 0$, and a direction has w = 0

 $\begin{bmatrix}
\cdot & \cdot & \cdot \\
\cdot & \\
\cdot & \cdot \\$

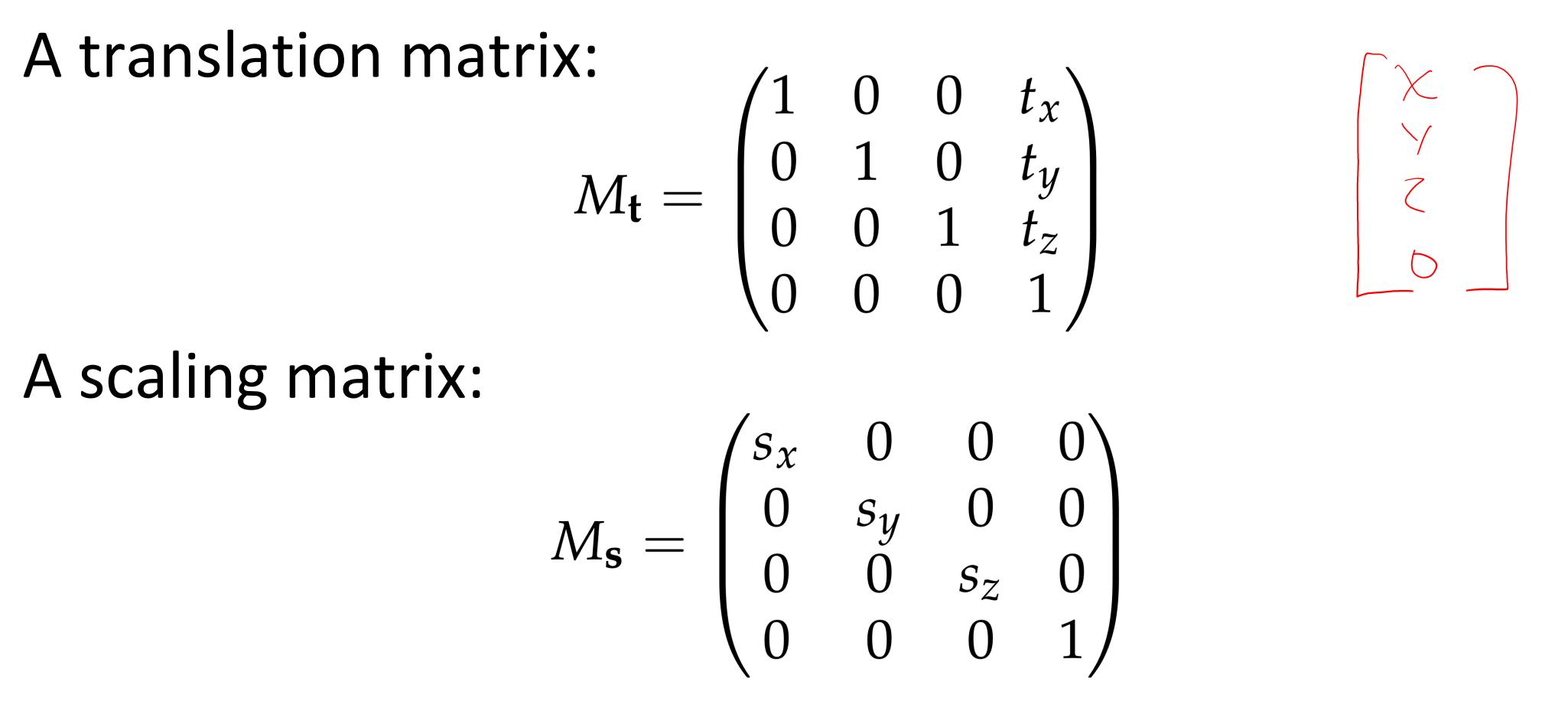
 $\begin{pmatrix} m_{11} & m_{12} & m_{13} & m_{14} \\ m_{21} & m_{22} & m_{24} & m_{24} \\ m_{31} & m_{32} & m_{33} & m_{34} \\ m_{41} & m_{42} & m_{43} & m_{44} \end{pmatrix}$

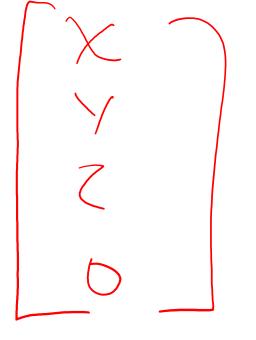




Transformations

Matrix-vector multiplication, Mv, transforms the vector







Have a transform M, a ray $\mathbf{r}(t)$, and a surface S

- To intersect:
- 1. Transform ray to local coords (by inverse of M)
- 2. Call surface intersection
- 3. Transform hit data back to global coords (by M)
- How to transform a ray $\mathbf{r}(t) = \mathbf{p} + t\mathbf{d}$ by M^{-1} ?
- $\mathbf{r'}(t) = M^{-1}\mathbf{p} + tM^{-1}\mathbf{d}$
- Remember: p forms as a point, d as a direction!



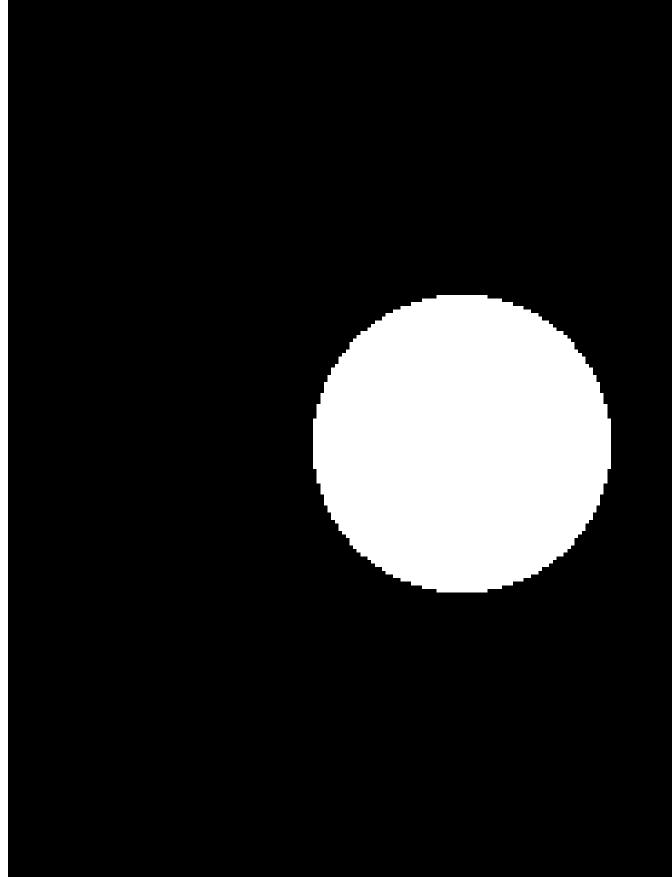
Ray-Surface Intersections

Other primitives

- cylinder
- cone, paraboloid, hyperboloid
- torus
- disk
- general polygons, meshes
- etc.



Image so far With eye ray generation and sphere intersection parse scene description for each pixel: ray = camera.getRay(pixel); hit = s.intersect(ray, 0, +inf); if hit: image.set(pixel, white);





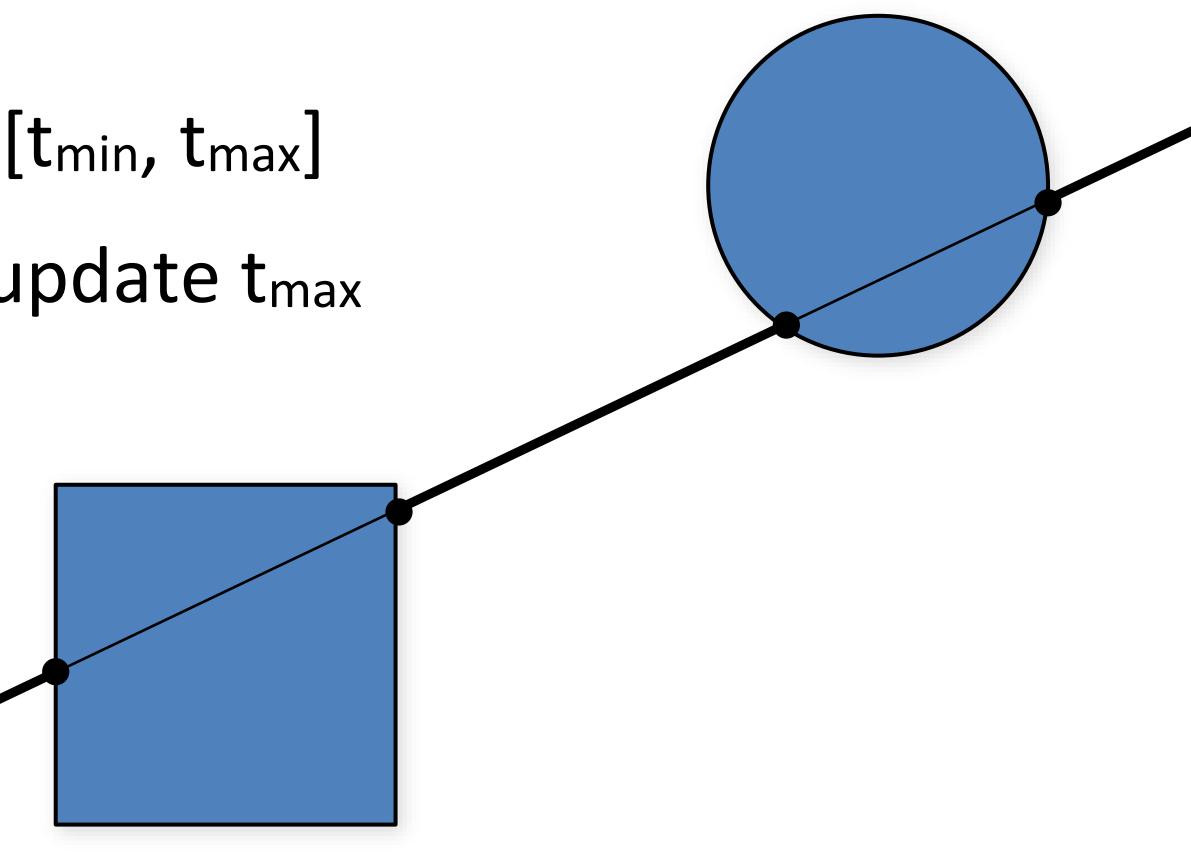


Intersecting many shapes

Intersect each primitive

Pick closest intersection

- Only within considered range [t_{min}, t_{max}]
- After each valid intersection, update t_{max}
- Essentially a line search







Intersection against many shapes

The basic idea is:

Surfaces::intersect(ray, tMin, tMax): tBest = +inf; firstHit = null; for s in surfaces: hit = s.intersect(ray, tMin, tBest); if hit: tBest = hit.t; firstHit = hit; return firstHit;

(acceleration structures)

- this is linear in number of surfaces but there are sublinear methods

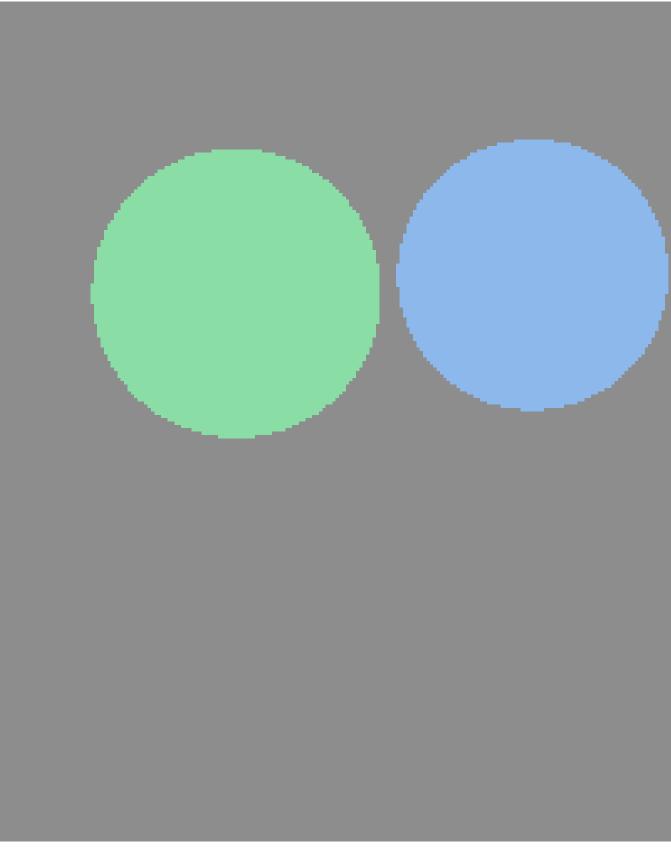


Image so far

With eye ray generation and scene intersection

```
for each pixel:
   ray = camera.getRay(pixel);
   c = scene.trace(ray, 0, +inf);
   image.set(pixel, c);
```

```
Scene::trace(ray, tMin, tMax):
   hit = surfaces.intersect(ray, tMin, tMax);
   if (hit)
      return hit.color();
   else
      return backgroundColor;
```







Ray-Surface Intersections

Other primitives

- cylinder
- cone, paraboloid, hyperboloid
- torus
- disk
- general polygons, meshes
- etc.



How should we represent complex geometry?

How are they obtained?

- modeled by hand
- scanned

What operations must we support?

- modeling/editing
- animating
- texturing
- rendering

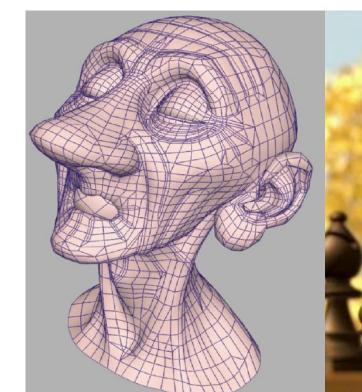


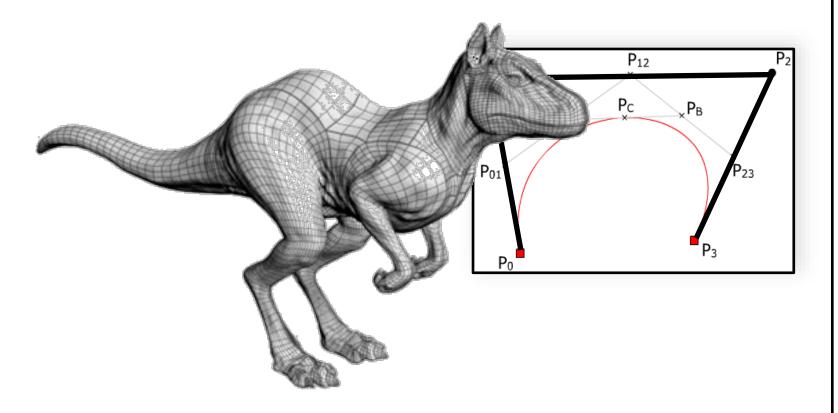




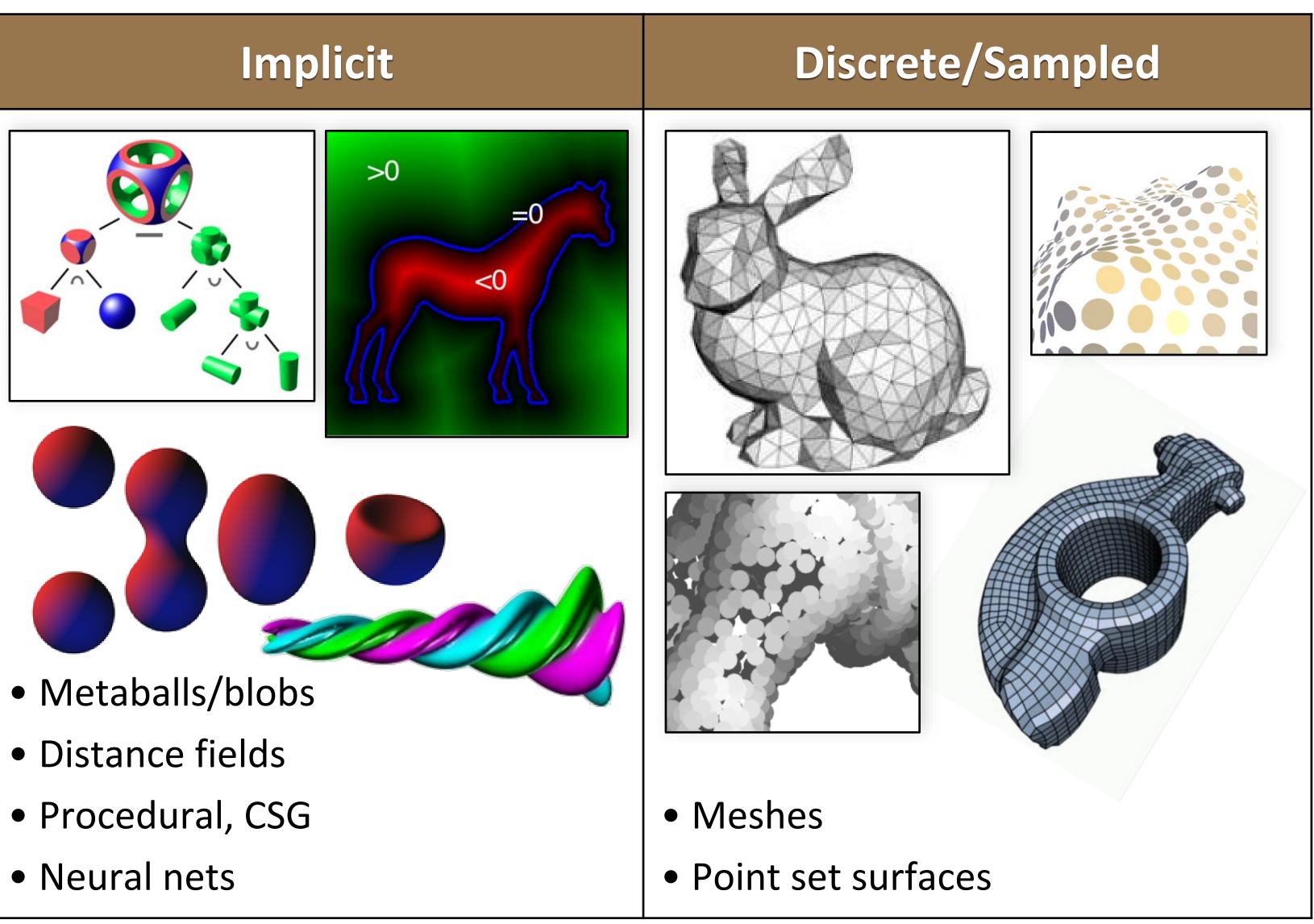
Surface representation zoo!

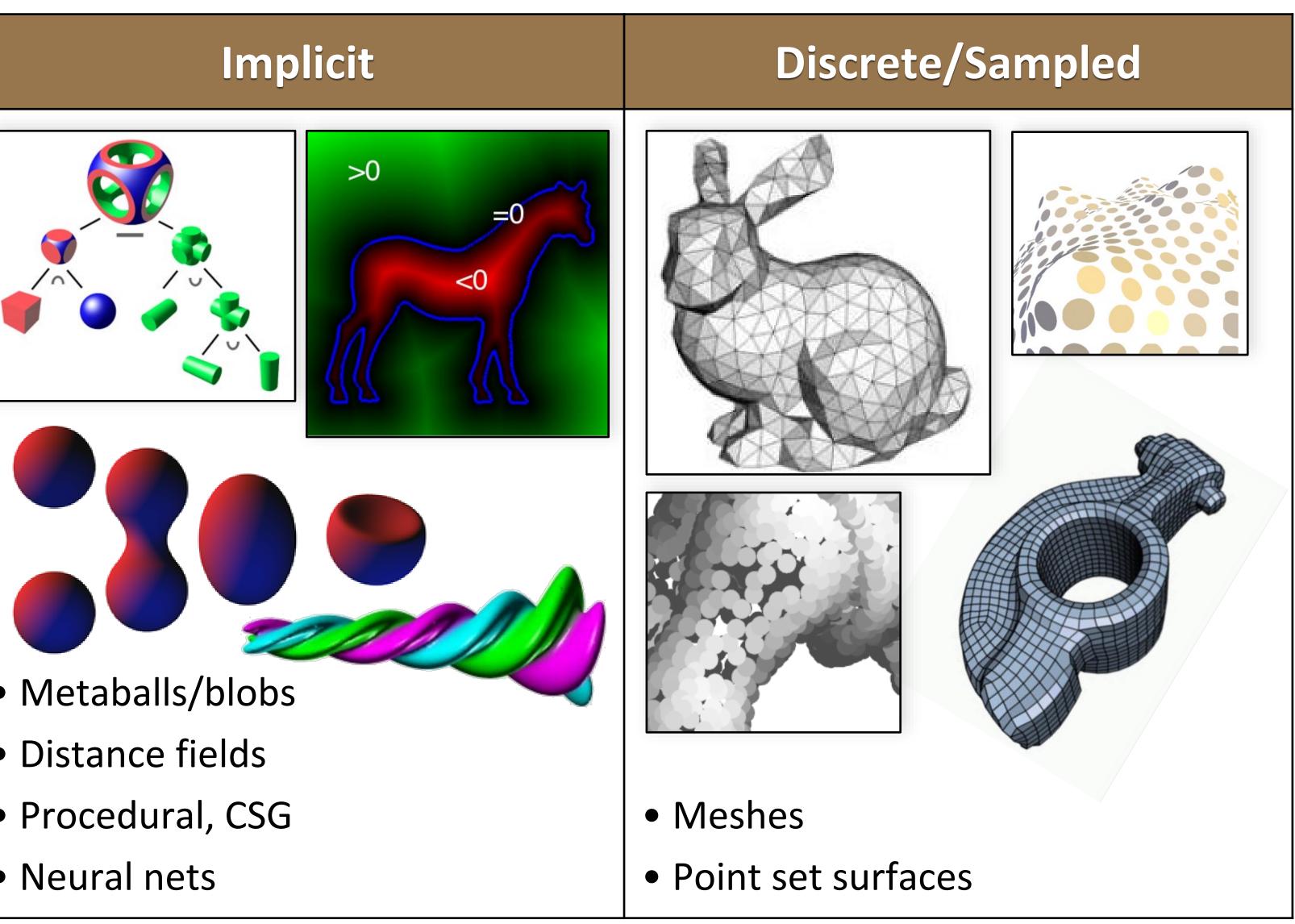
Parametric





- Splines, tensor-product surfaces
- Subdivision surfaces

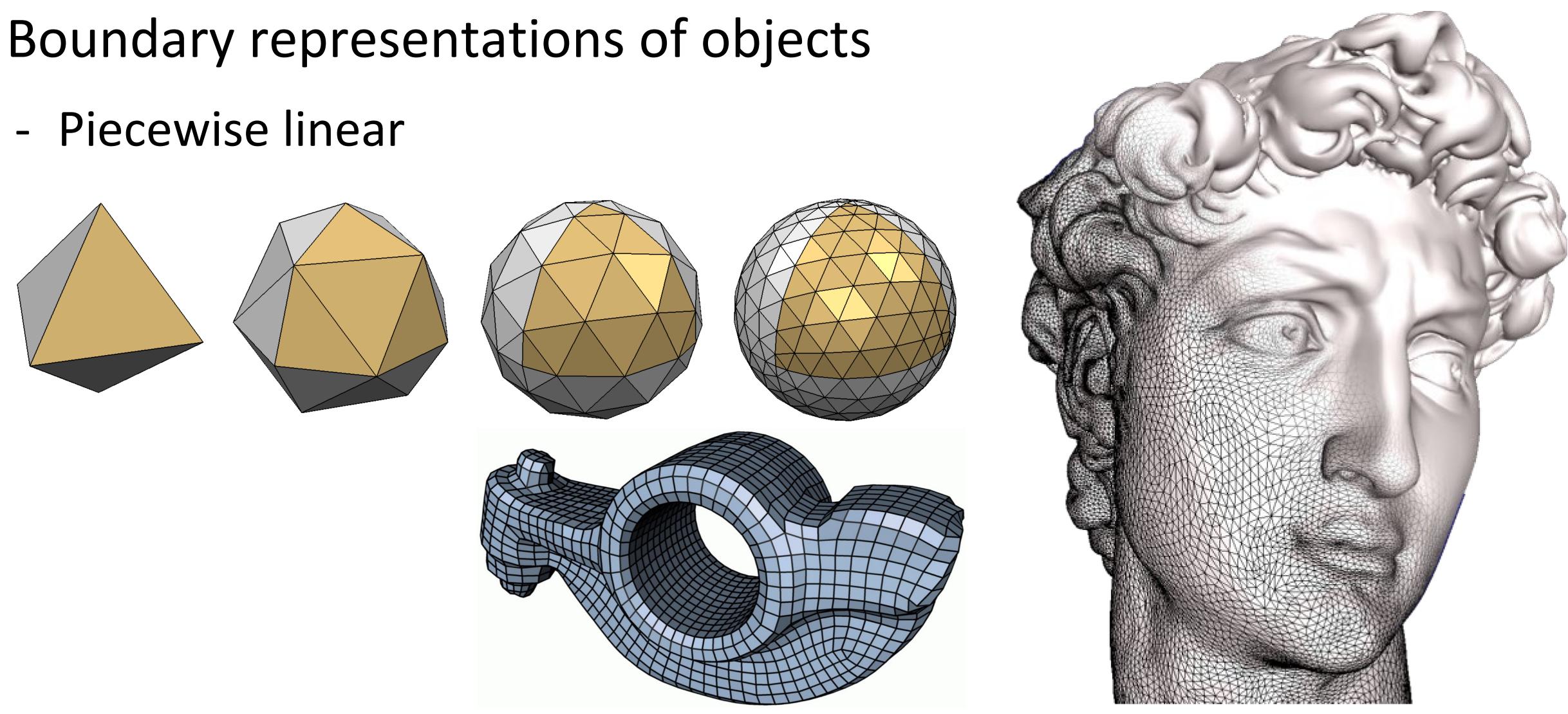




After a slide by Olga Sorkine-Hornung

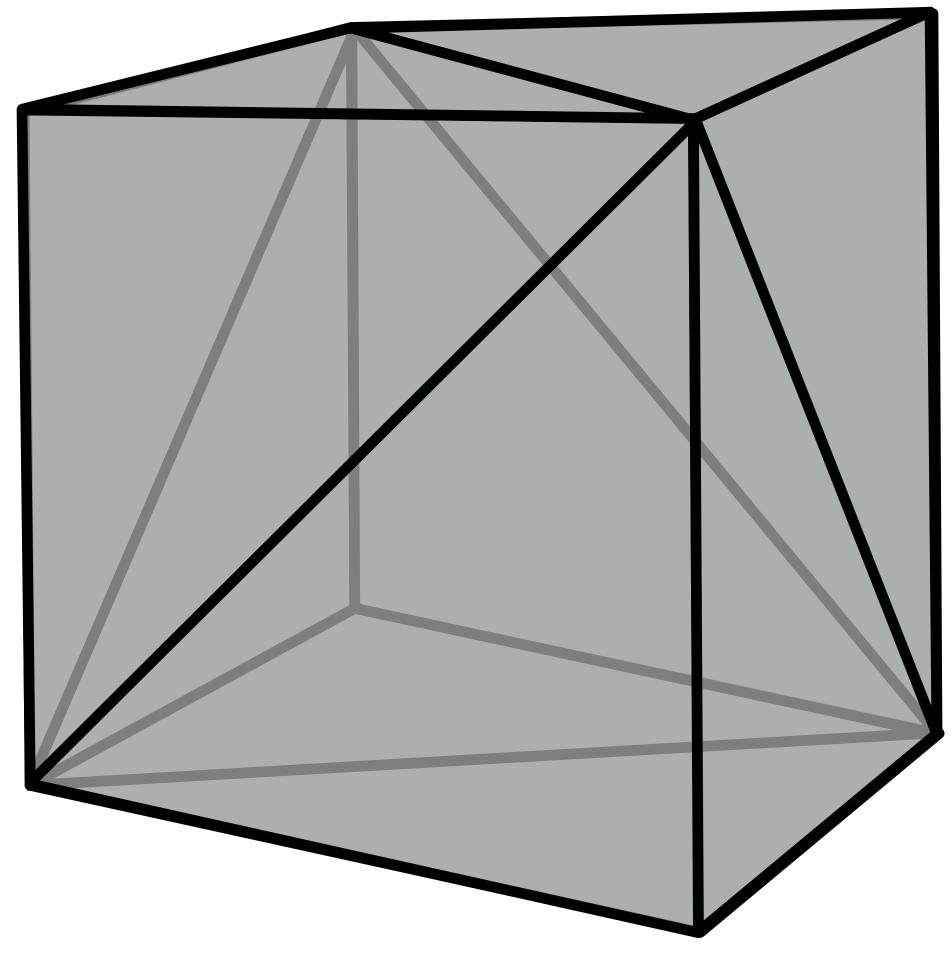


Polygonal Meshes





A small triangle mesh



lide by Steve Marschner S After a

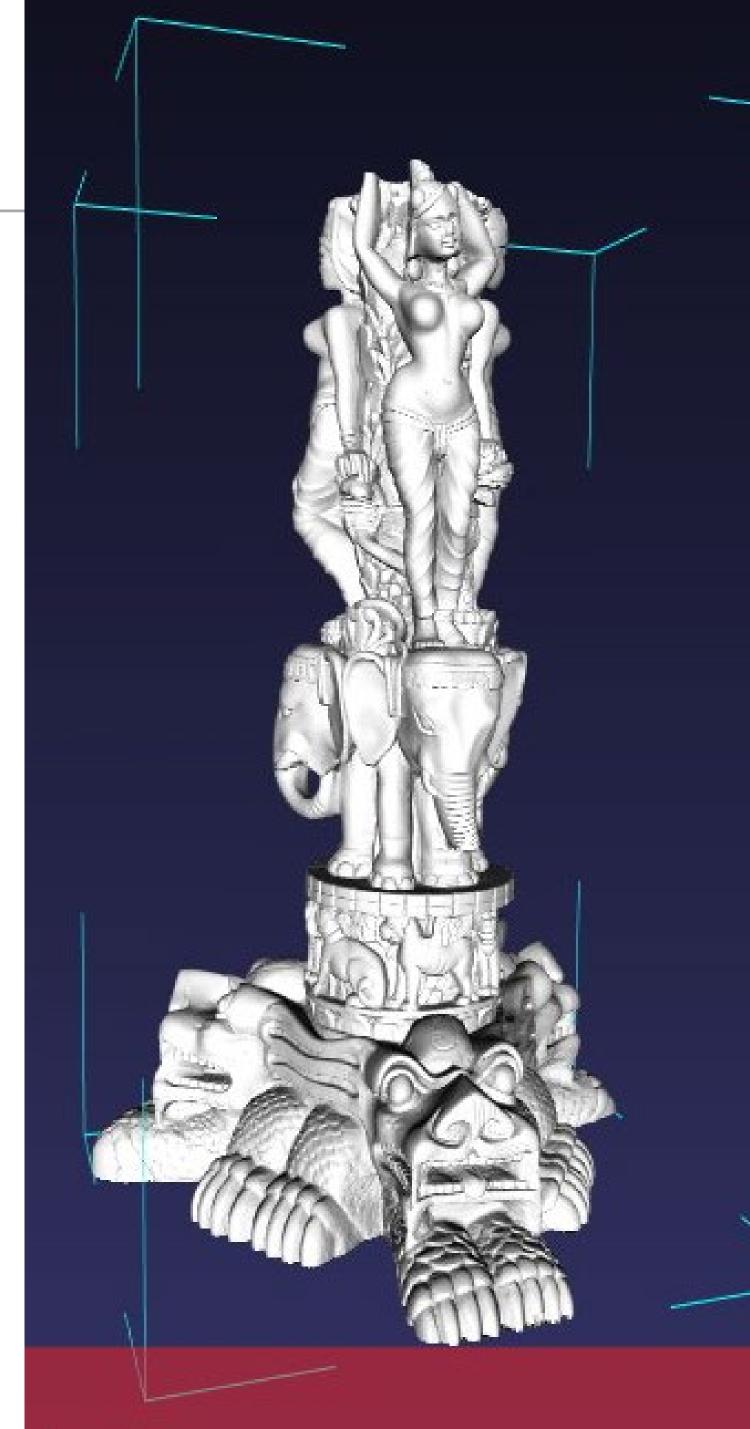
12 triangles, 8 vertices



A large mesh

10 million triangles from a highresolution 3D scan







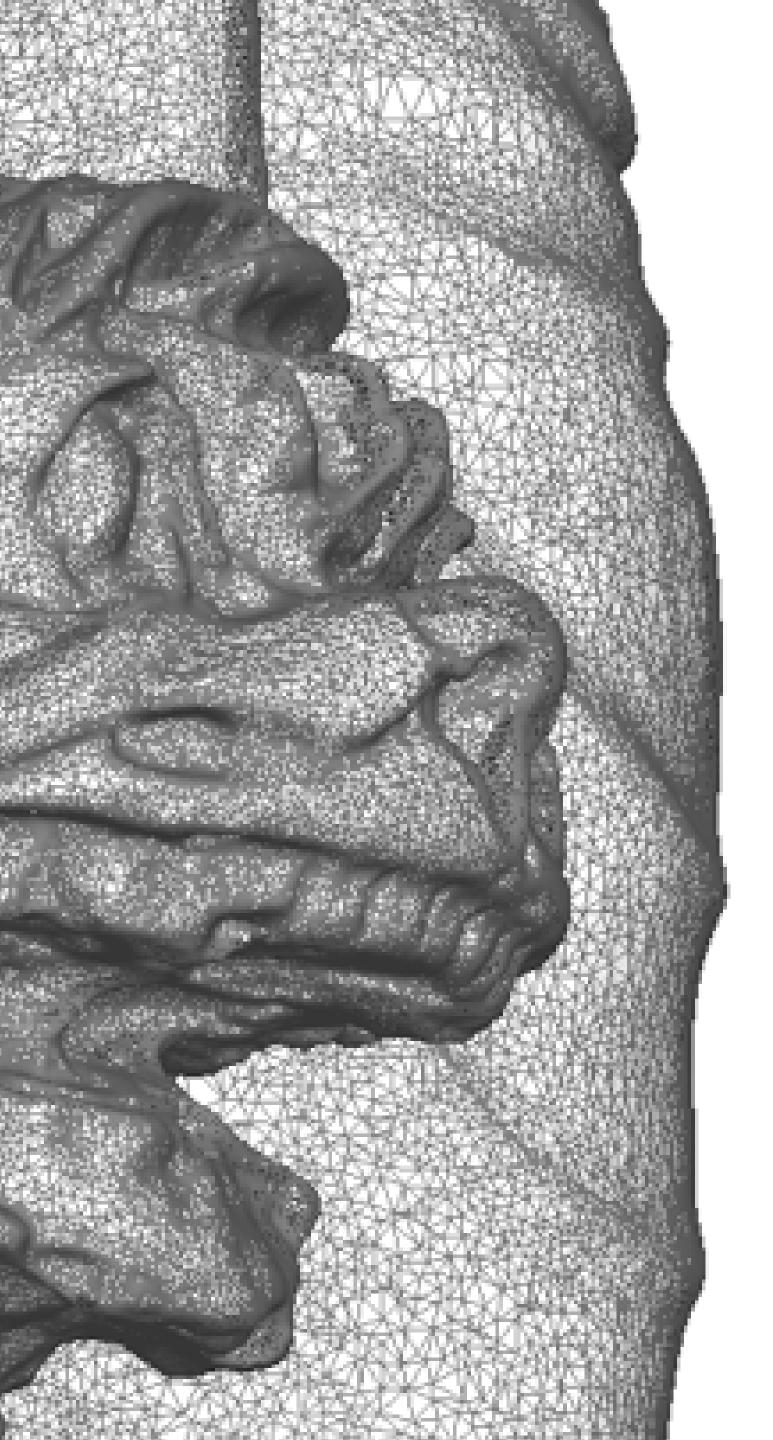


After a slide by Steve Marschner









spheres



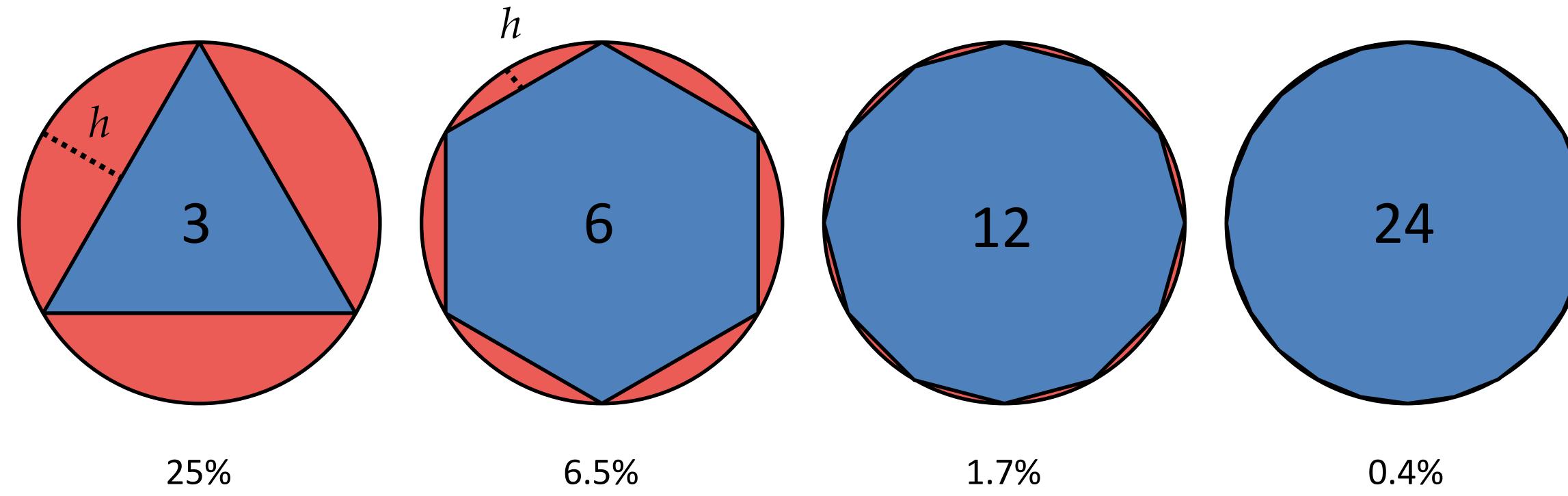
approximate sphere

Rineau & Yvinec CGAL manual



Meshes as Approx. of Smooth Surfaces

Piecewise linear approximation - Error is $O(h^2)$



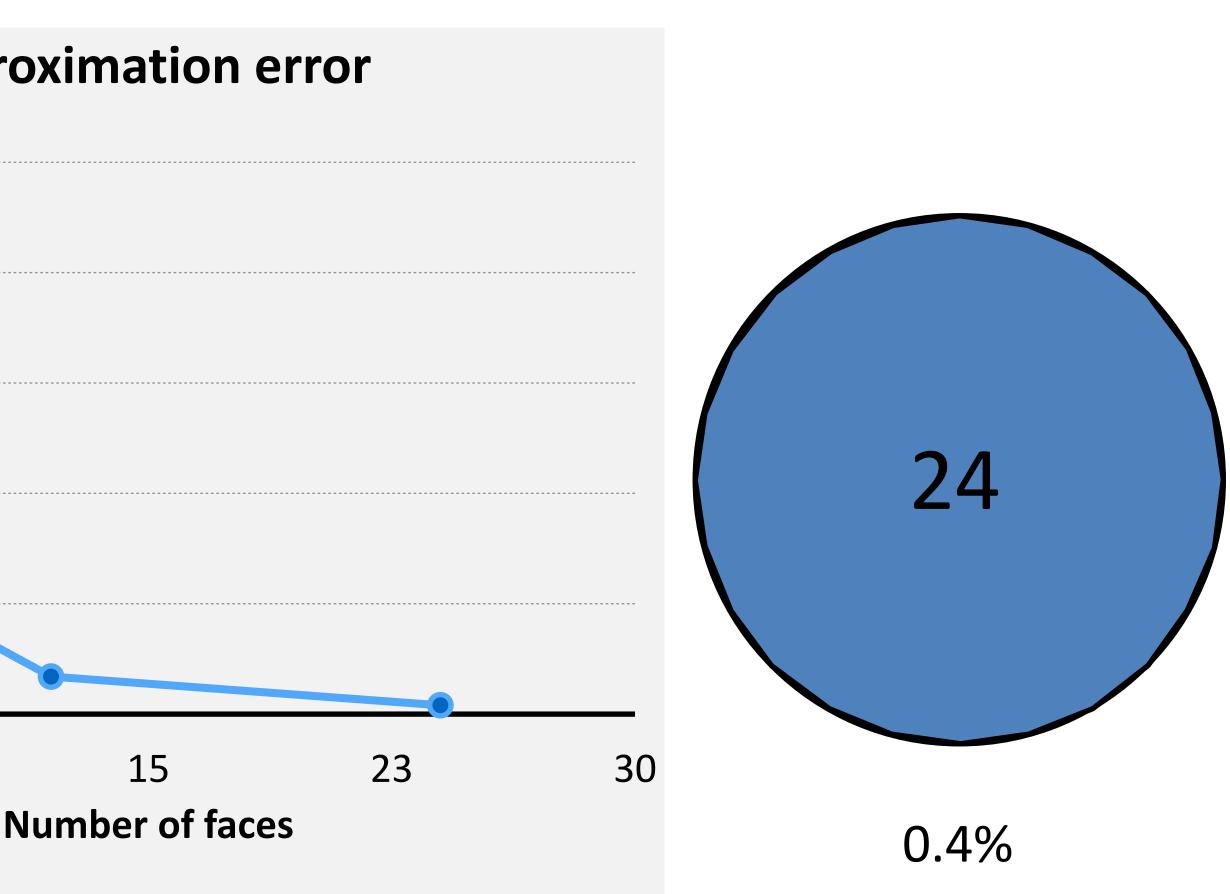
lide by Olga Sorkine-Hornung S After a





Meshes as Approx. of Smooth Surfaces **Piecewise linear approximation** - Error is $O(h^2)$ #faces vs. approximation error 25. 20. Approximation error 15. 3 10. 5. 0. 23 8 15 0 30 Number of faces 25%

lide by Olga Sorkine-Hornung S σ After

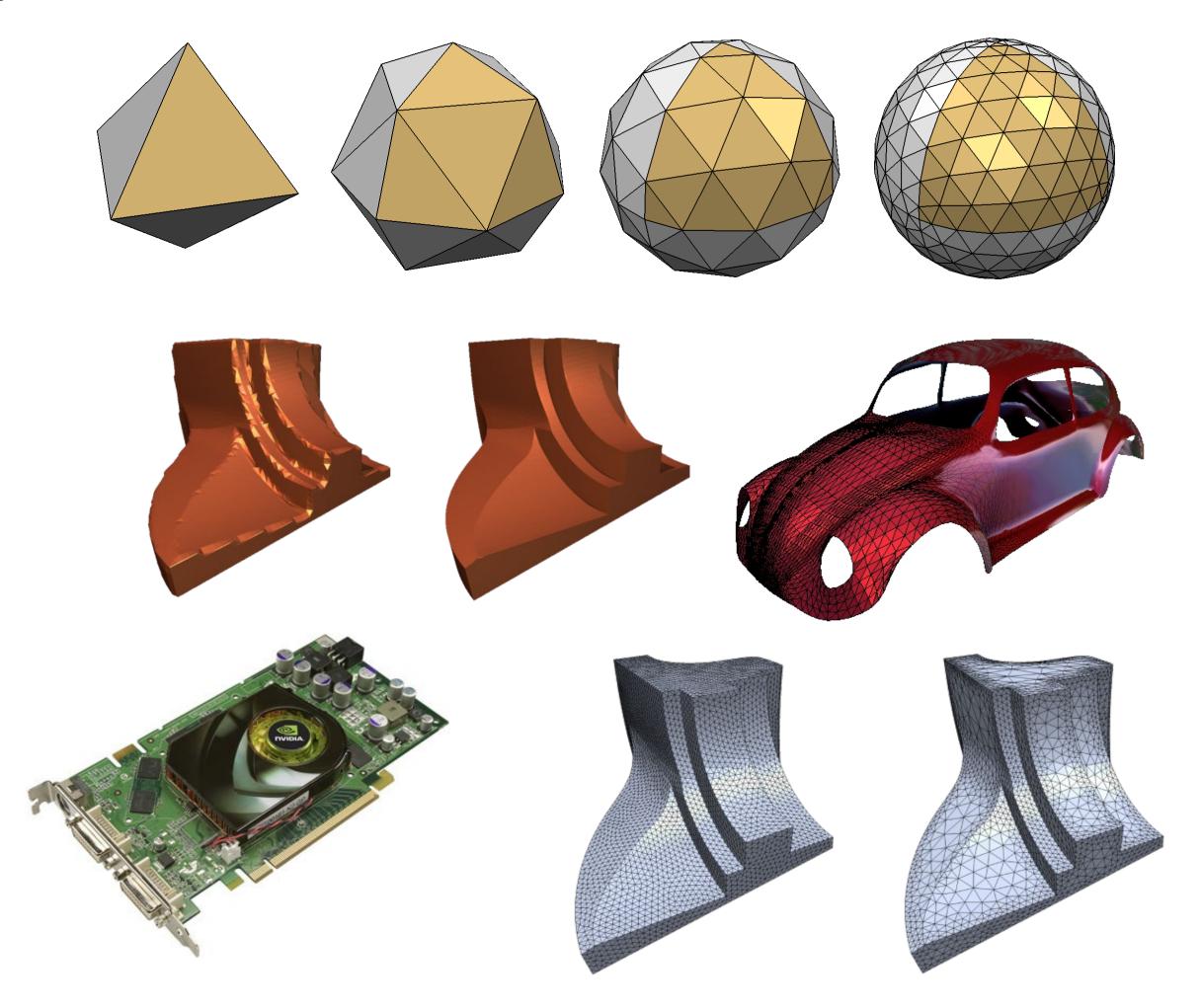




Polygonal Meshes

Polygonal meshes are a good representation

- approximation $O(h^2)$
- arbitrary topology
- piecewise smooth surfaces
- adaptive refinement
- efficient rendering





Data Structures: What should be stored?



- Attributes
- Normal, color, texture coordinates
- Per vertex, face, edge
- Connectivity
- Adjacency relationships

Geometry: 3D coordinates



Separate Triangle List or Face Set (STL)

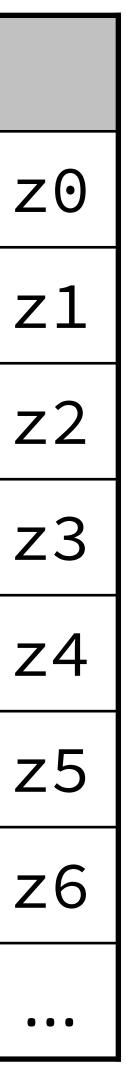
Face: 3 vertex positions

Storage:

- 4 Bytes/coordinate (using 32-bit floats)
- 36 Bytes/face

Wastes space

Triangles					
0	x0	y0			
1	x1	y1			
2	x2	y2			
3	х3	уЗ			
4	x4	y4			
5	x5	y5			
6	x6	y6			
• • •	• • •	• • •			





Indexed Face Set (OBJ, OFF, WRL)

Vertex: position

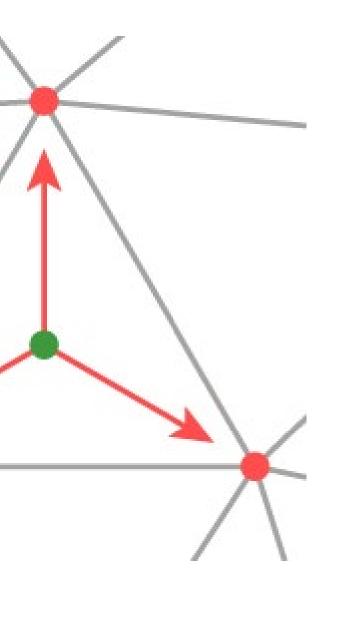
Face: vertex indices

Storage:

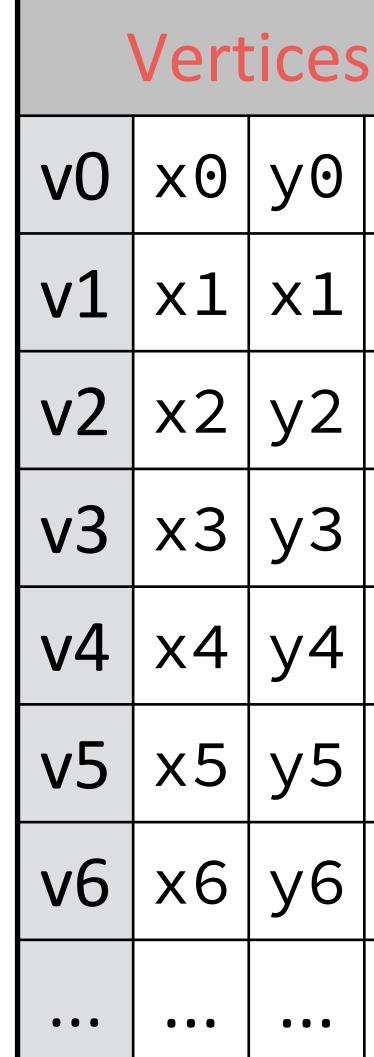
- 12 Bytes/vertex
- 12 Bytes/face

Reduces wasted space

Even better with per-vertex attributes



Triangles				
t0	V0	v1	v2	
t1	V0	v1	v3	
t2	v2	v4	v3	
t3	v5	v2	v6	
• • •	• • •	•••	•••	







Data on meshes

geometry

Can store additional data at faces, vertices, or edges Examples

- colors stored on faces, for faceted objects
- information about sharp creases stored at edges
- any quantity that varies continuously (without sudden changes, or *discontinuities*) gets stored at vertices

Often need to store additional information besides just the



Key types of vertex data

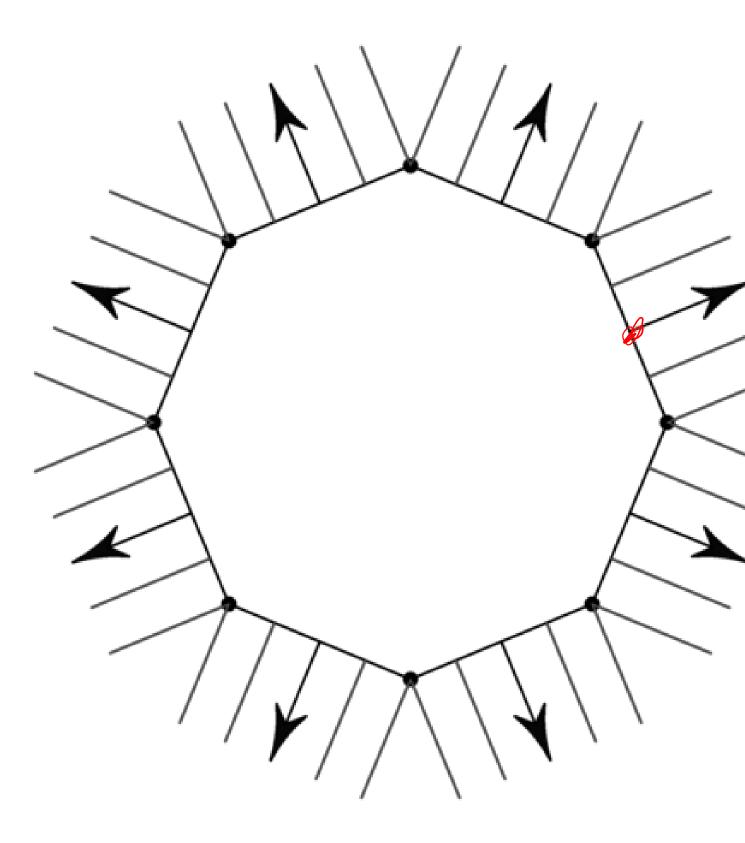
- Surface normals
- vertices
- **Texture coordinates**
- 2D coordinates that tell you how to paste images on the surface
- Positions
- at some level this is just another piece of data

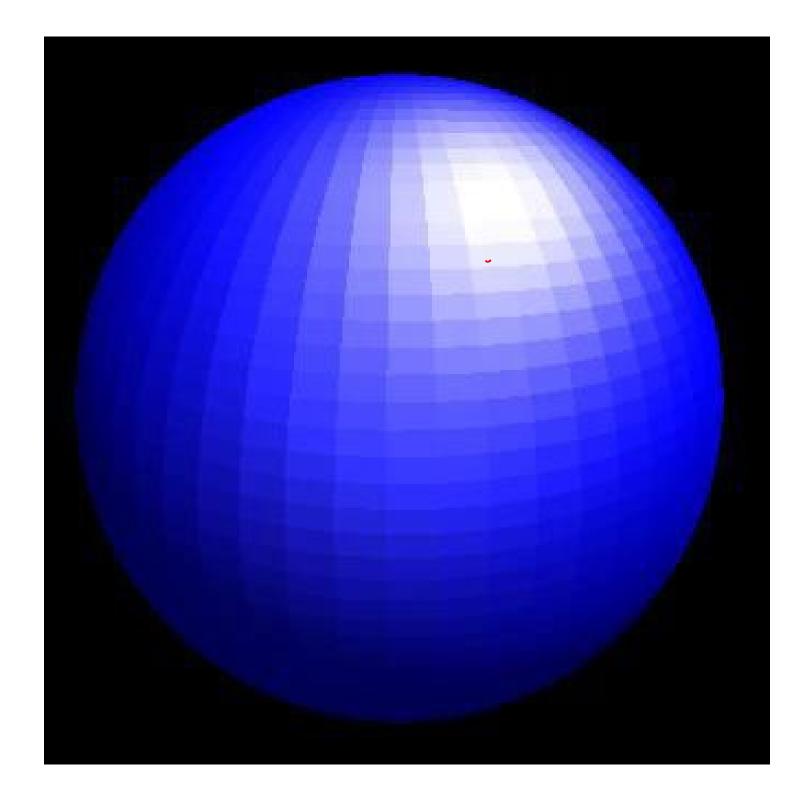
- when a mesh is approximating a curved surface, store normals at



Defining normals

Face normals: same normal for all points in face - geometrically correct, but faceted look







Problems with face normals

Piecewise planar approximation converges pretty quickly to the smooth geometry as the number of triangles increases

- error is $O(h^2)$

But the surface normals don't converge so well

- normal is constant over each trian edges
- error is only O(h)

- normal is constant over each triangle, with discontinuous jumps across

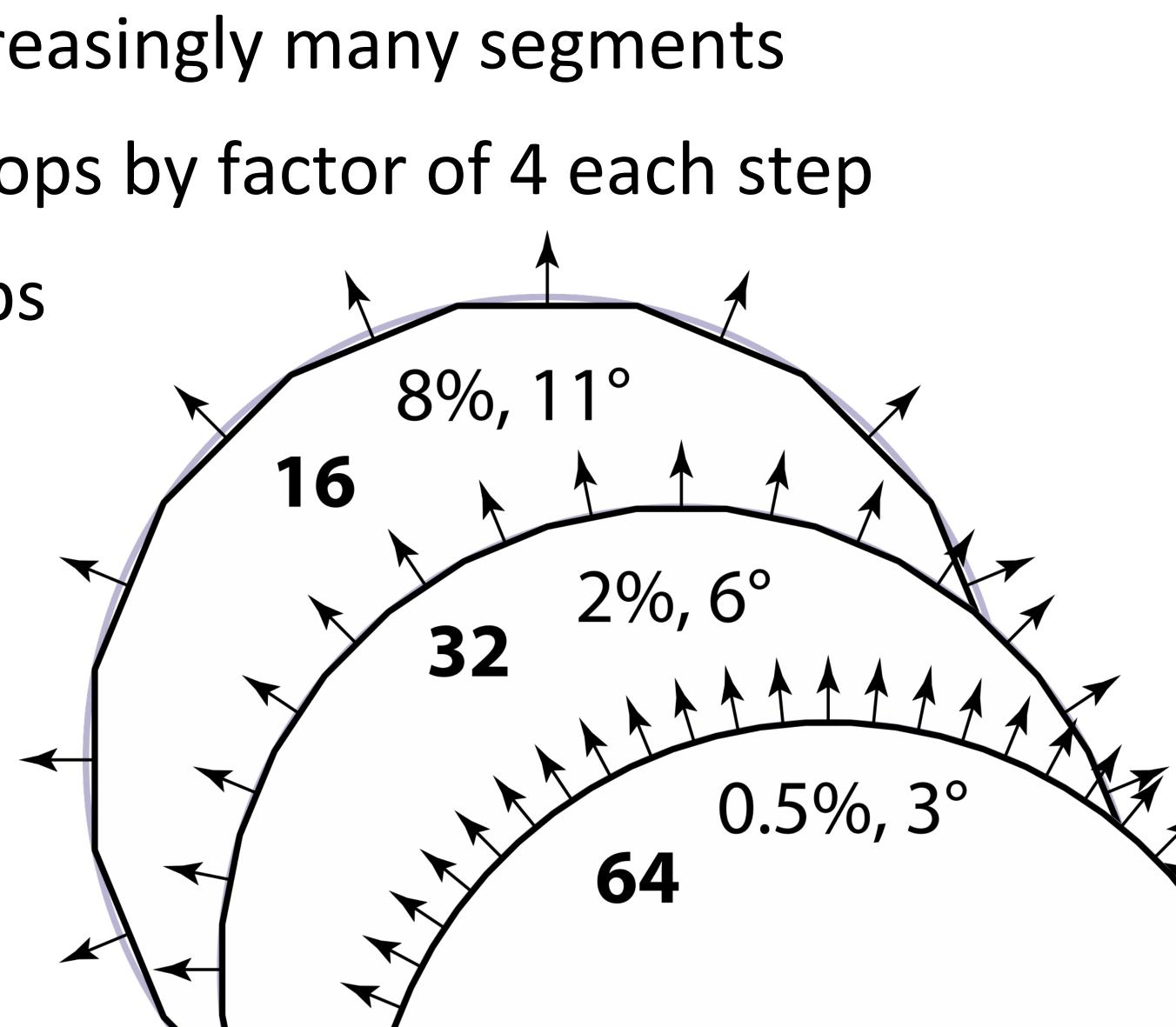


Problems with face normals—2D example

Approximating circle with increasingly many segments

Max error in position error drops by factor of 4 each step

Max error in normal only drops by factor of 2



Problems with face normals—solution

Piecewise planar approximation converges pretty quickly to the smooth geometry as the number of triangles increases

- for mathematicians: error is $O(h^2)$
- But the surface normals don't converge so well
- normal is constant over each triangle, with discontinuous jumps across edges
- for mathematicians: error is only O(h)

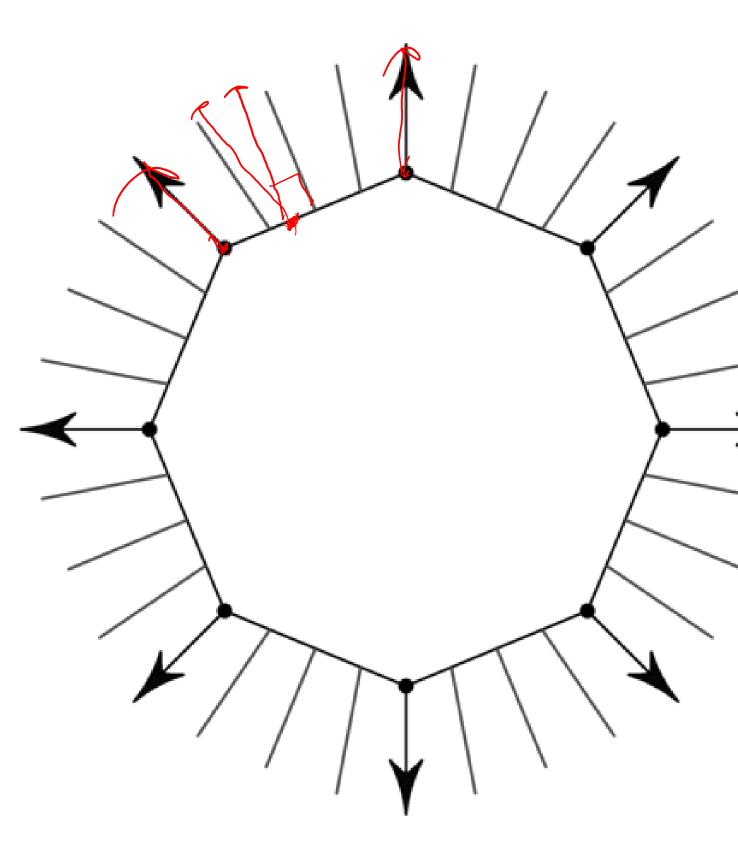
normals that vary gradually across triangles

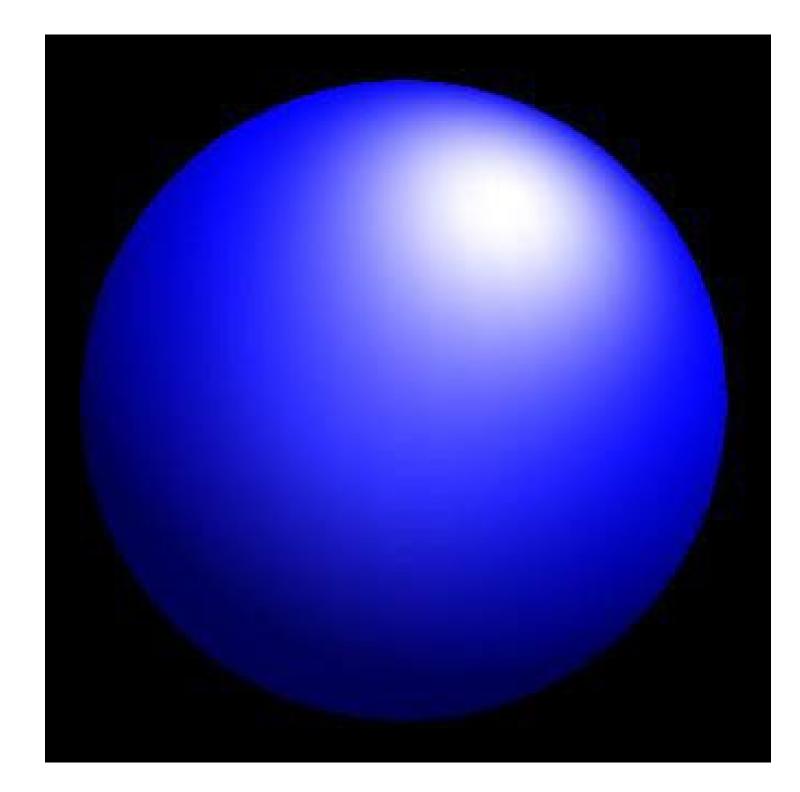
- Better: store the "real" normal at each vertex, and interpolate to get



Defining normals

Vertex normals: store normal at vertices, interpolate in face - geometrically "inconsistent", but smooth look

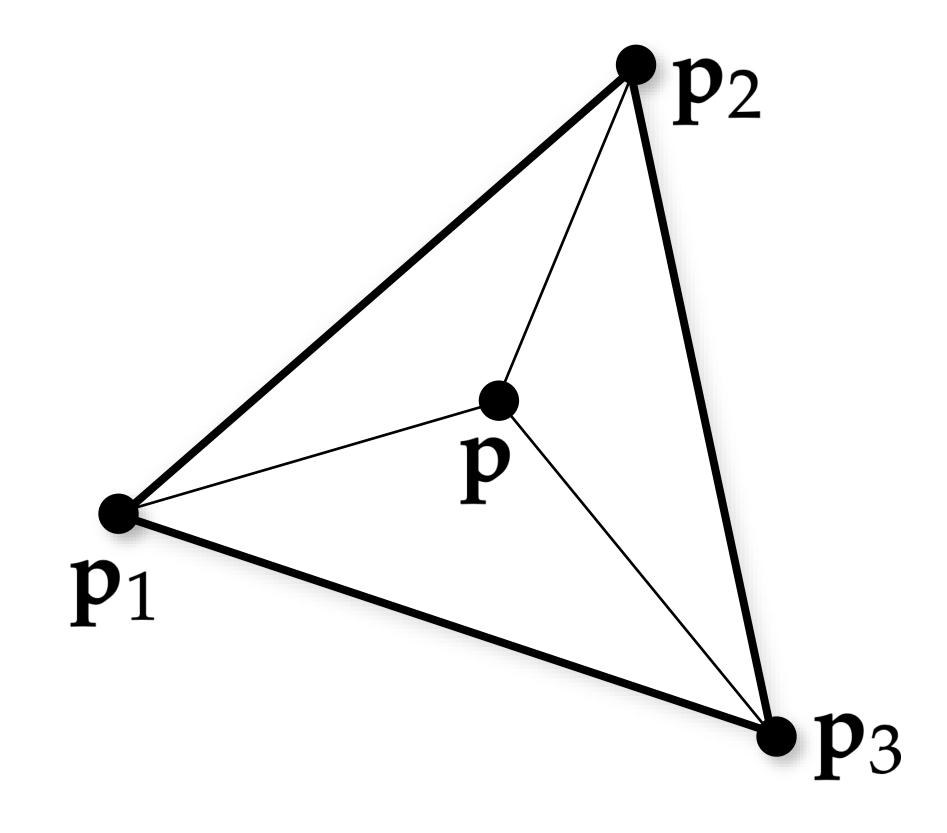






Barycentric coordinates

Barycentric interpolation:



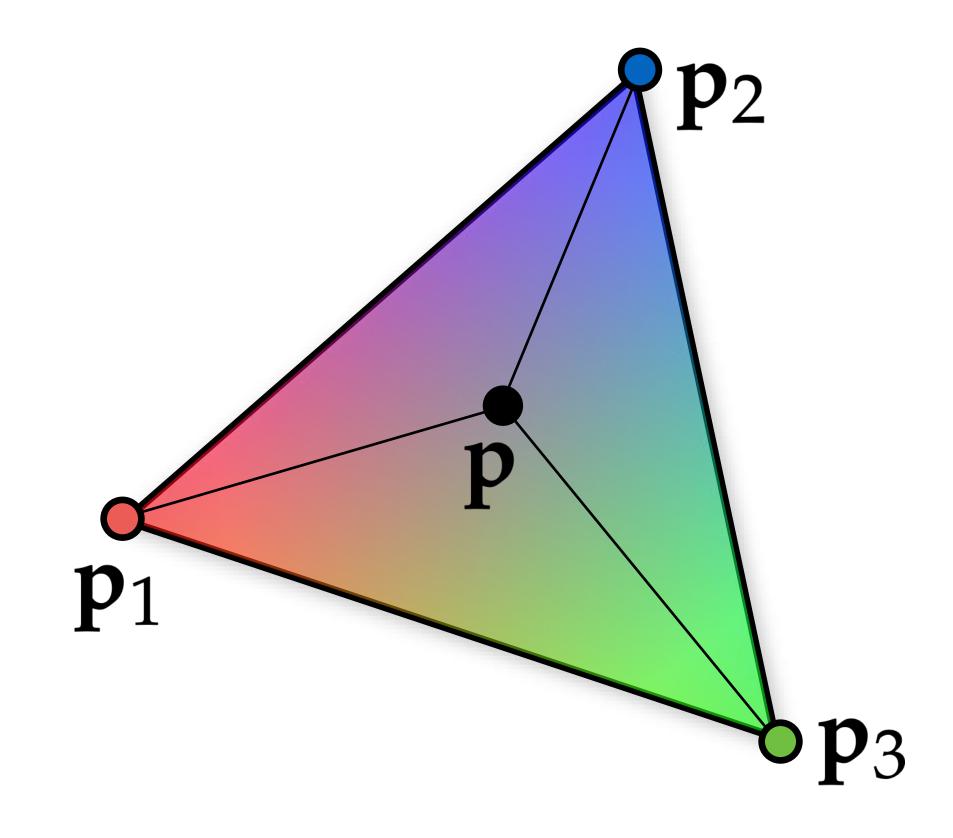
 $\mathbf{p}(\alpha,\beta,\gamma) = \alpha \mathbf{p}_1 + \beta \mathbf{p}_2 + \gamma \mathbf{p}_3$

Can use this eqn. to interpolate any vertex quantity across triangle!



Barycentric coordinates

Barycentric interpolation:



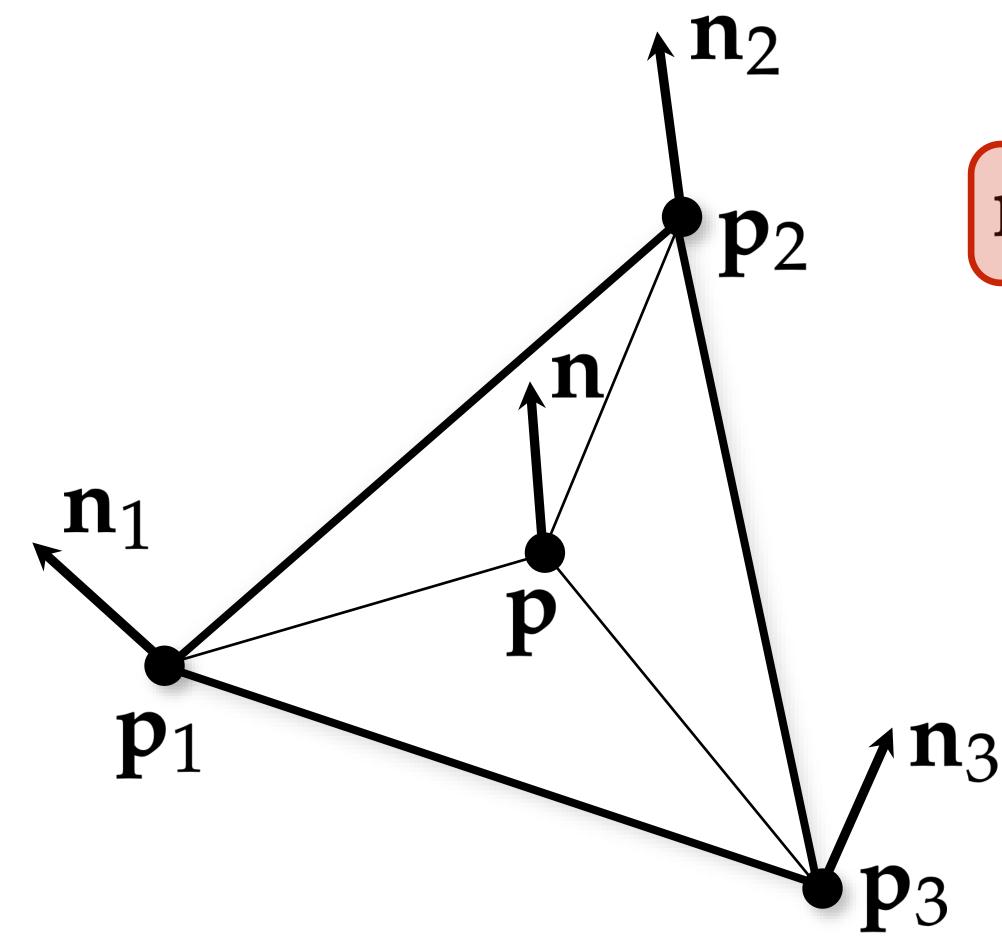
$\mathbf{p}(\alpha, \beta, \gamma) = \alpha \mathbf{p}_1 + \beta \mathbf{p}_2 + \gamma \mathbf{p}_3$ $\mathbf{c}(\alpha, \beta, \gamma) = \alpha \mathbf{c}_1 + \beta \mathbf{c}_2 + \gamma \mathbf{c}_3$

Can use this eqn. to interpolate any vertex quantity across triangle!



Barycentric coordinates

Barycentric interpolation:



 $\mathbf{p}(\alpha,\beta,\gamma) = \alpha \mathbf{p}_1 + \beta \mathbf{p}_2 + \gamma \mathbf{p}_3$ $\mathbf{c}(\alpha,\beta,\gamma) = \alpha \mathbf{c}_1 + \beta \mathbf{c}_2 + \gamma \mathbf{c}_3$ $\mathbf{n}(\alpha,\beta,\gamma) = \alpha \mathbf{n}_1 + \beta \mathbf{n}_2 + \gamma \mathbf{n}_3$

not guaranteed to be unit length

Can use this eqn. to interpolate any vertex quantity across triangle!



Realism through geometric complexity

DIDDDDDDDDDDDDDD

Andreas Byström

2000000000000000



Ray Tracing Acceleration

Ray-surface intersection is at the core of every ray tracing algorithm

Brute force approach:

- intersect every ray with every primitive
- many unnecessary raysurface intersection tests





Ray Tracing Cost

over 95 percent" [Whitted 1980]

 $Cost = O(n_x \cdot n_y \cdot n_o)$

- (number of pixels) · (number of objects)
- Assumes 1 ray per pixel

Example: 1024 x 1024 image of a scene with 1000 triangles

- Cost is (at least) 10⁹ ray-triangle intersections

Typically measured per ray:

- Naive: $O(n_o)$ - linear with number of objects

"the time required to compute the intersections of rays and surfaces is





O(n_o) Ray Tracing (The Problem)



8 primitives \rightarrow 3 seconds

50K trees each with 1M polygons = 50B polygons

 \rightarrow 594 years!



Sub-linear Ray Tracing



50K trees each with 1M polygons = 50B polygons \rightarrow **11 minutes 300,000,000x speedup!**

The solution

Improve efficiency of ray-surfaceleration structures.

- A spatial organization of objects in a scene to minimize the necessary number of ray-object intersection tests.
- Spatial sorting/subdivision (e.g. grid, kd-tree, ochre)
- Decompose space into disjoint regions & assign objects to regions
- Object sorting/subdivision (bounding volume hierarchy)
- Decompose objects into disjoint sets & bound using simple volumes for fast rejection

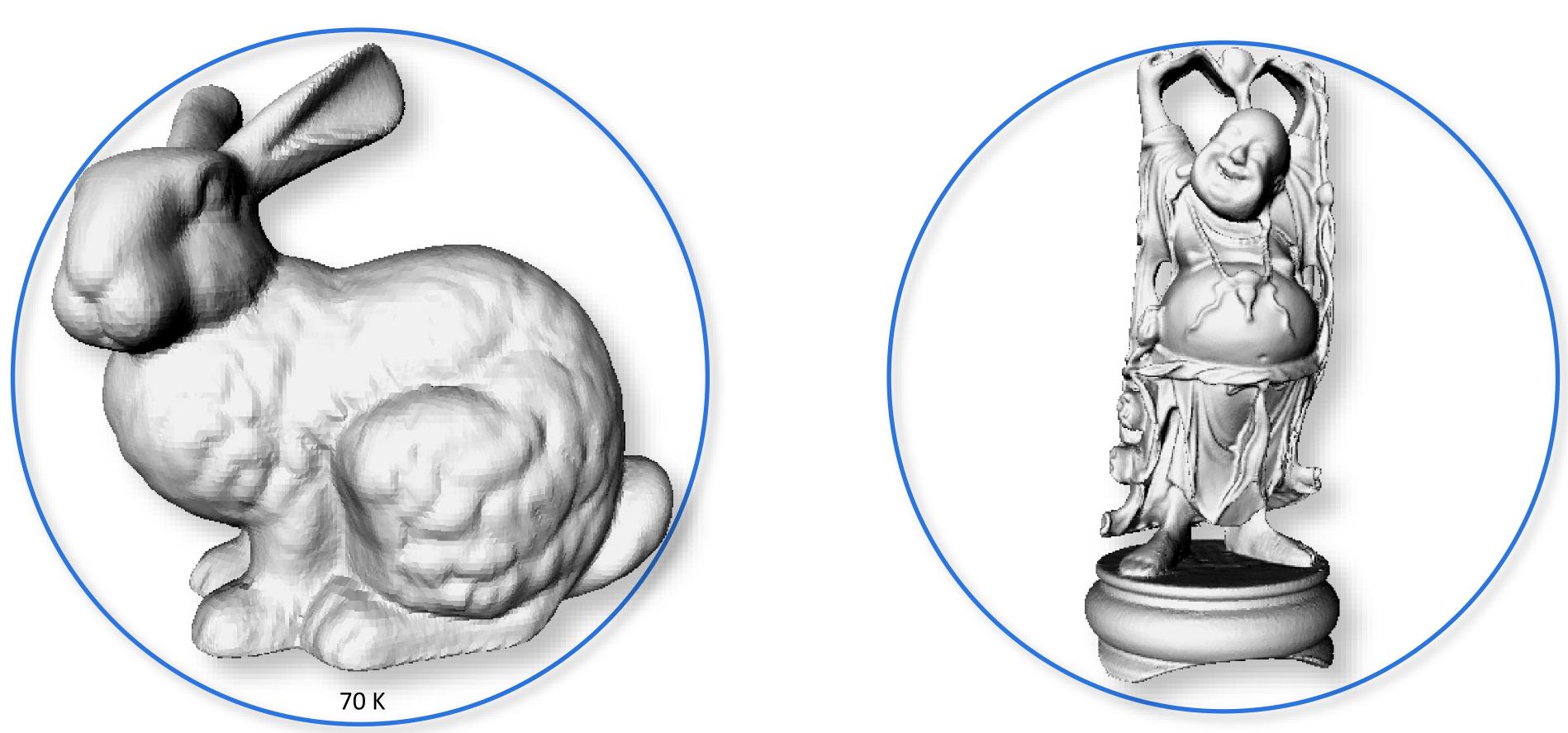
Improve efficiency of ray-surface intersections by constructing





Bounding Volumes

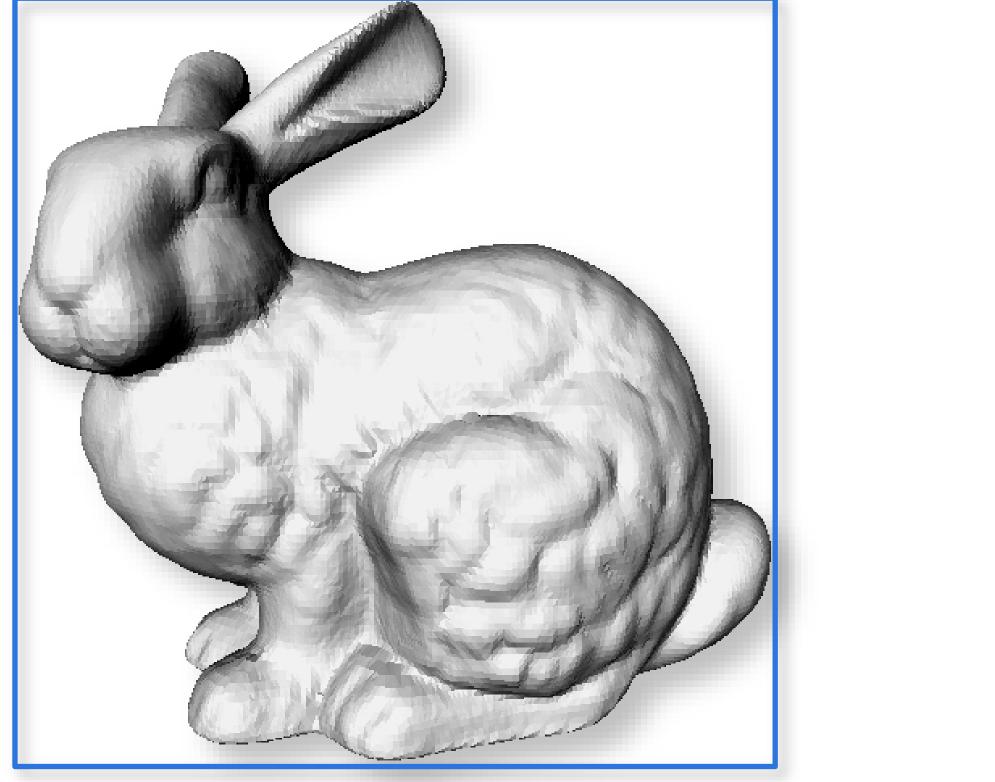
Spheres





Bounding Volumes

Axis-aligned bounding boxes (most common)

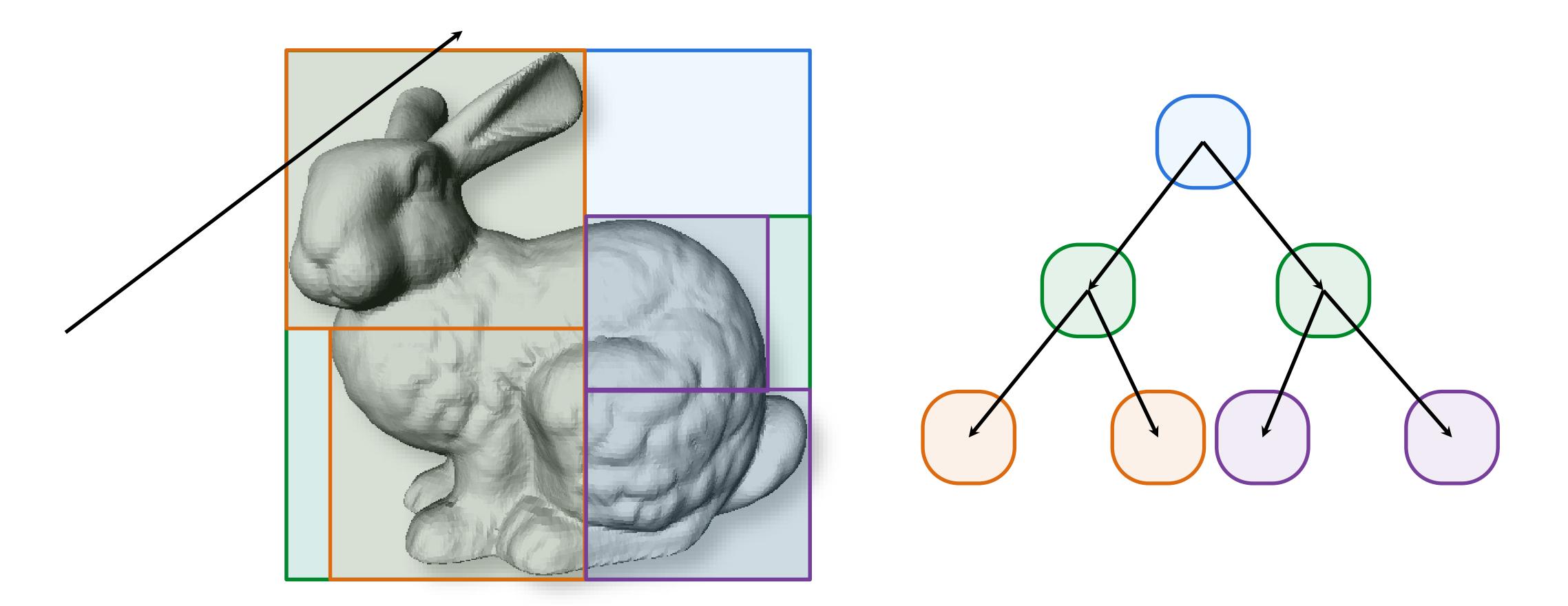






Bounding Volumes Hierarchies

Now do this hierarchically!





BVH Traversal

void BVHNode::intersectBVH(ray, &hit): if (bound.hit(ray)): if (leaf): else:

- leaf.intersect(ray, hit);
- leftChild.intersectBVH(ray, hit); rightChild.intersectBVH(ray, hit);



Constructing BVHs

Top-down:

- partition objects along an axis and create two sub-sets

Bottom-up:

- recursively group nearby objects together



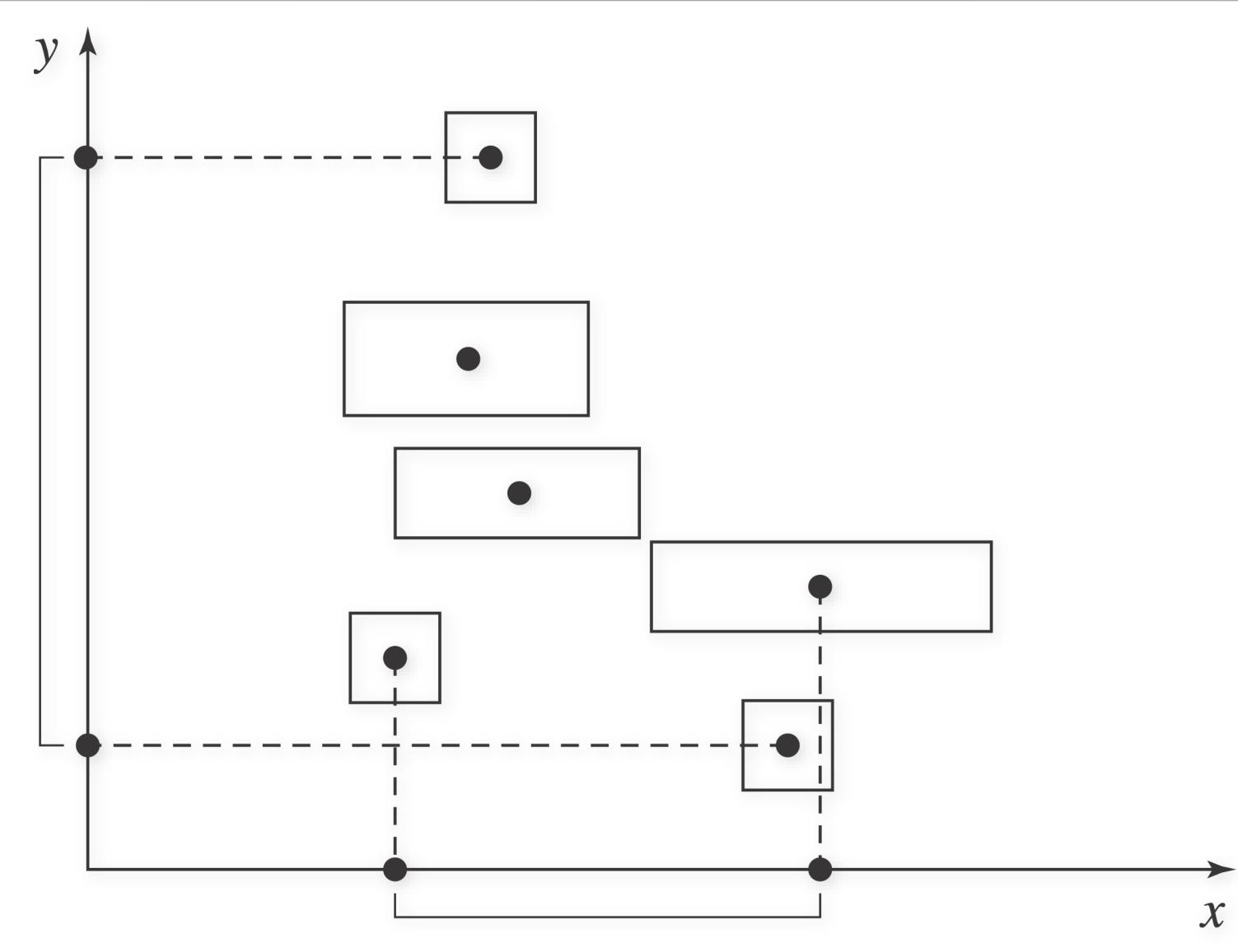
Divisive (top-down) BBH construction

- 1. Choose split axis
- 2. Choose split plane location
- 3. Choose whether to create leaf or split + repeat
- Many strategies for each of these steps

leaf or split + repeat Tese steps



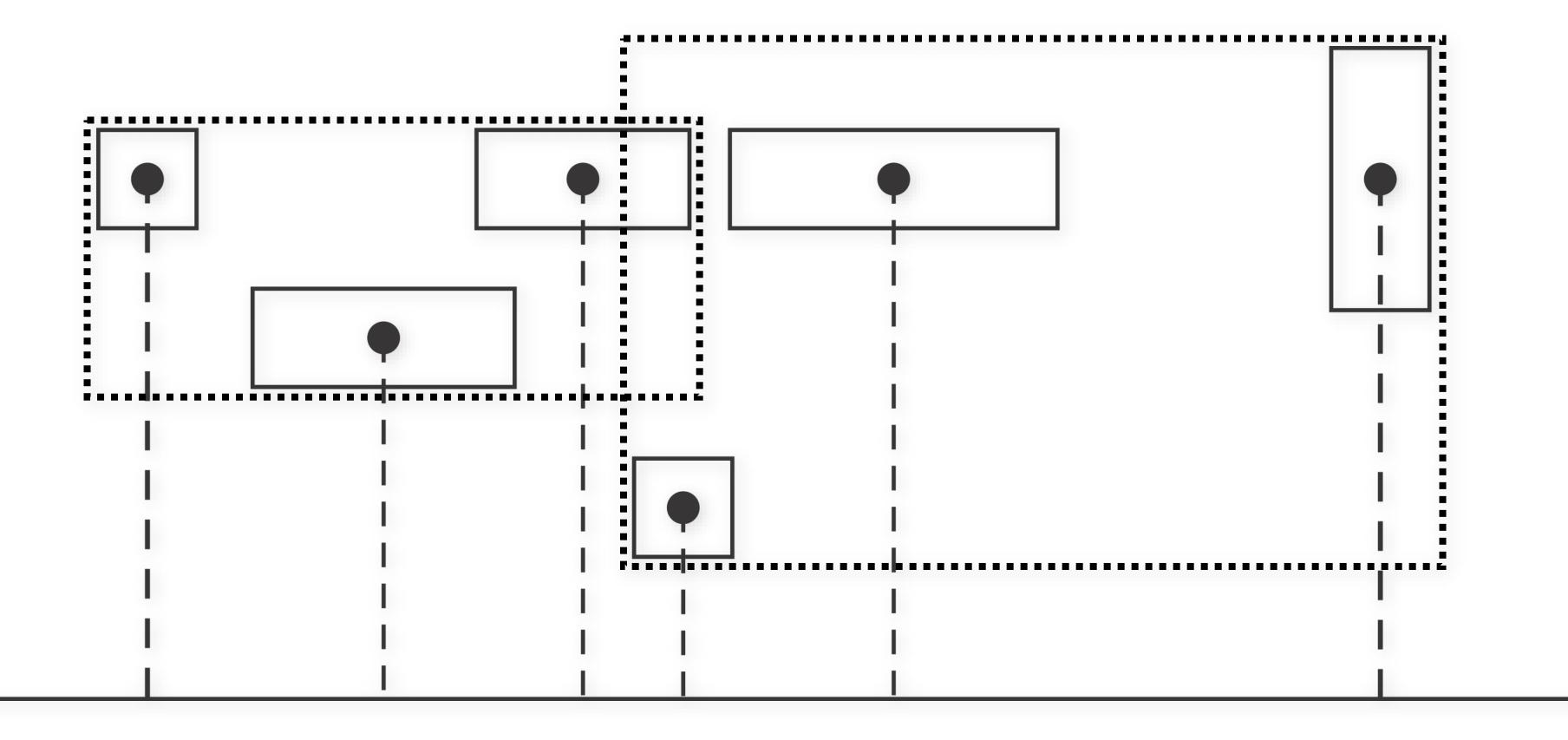
Choosing axis based on centroid extents



PBRe2 fig. 4.8 111

Object-median splitting

- 1. Sort bbox centroids along split axis
- 2. Take take first half as left child, second half as right



split axis hild, second half as right



112