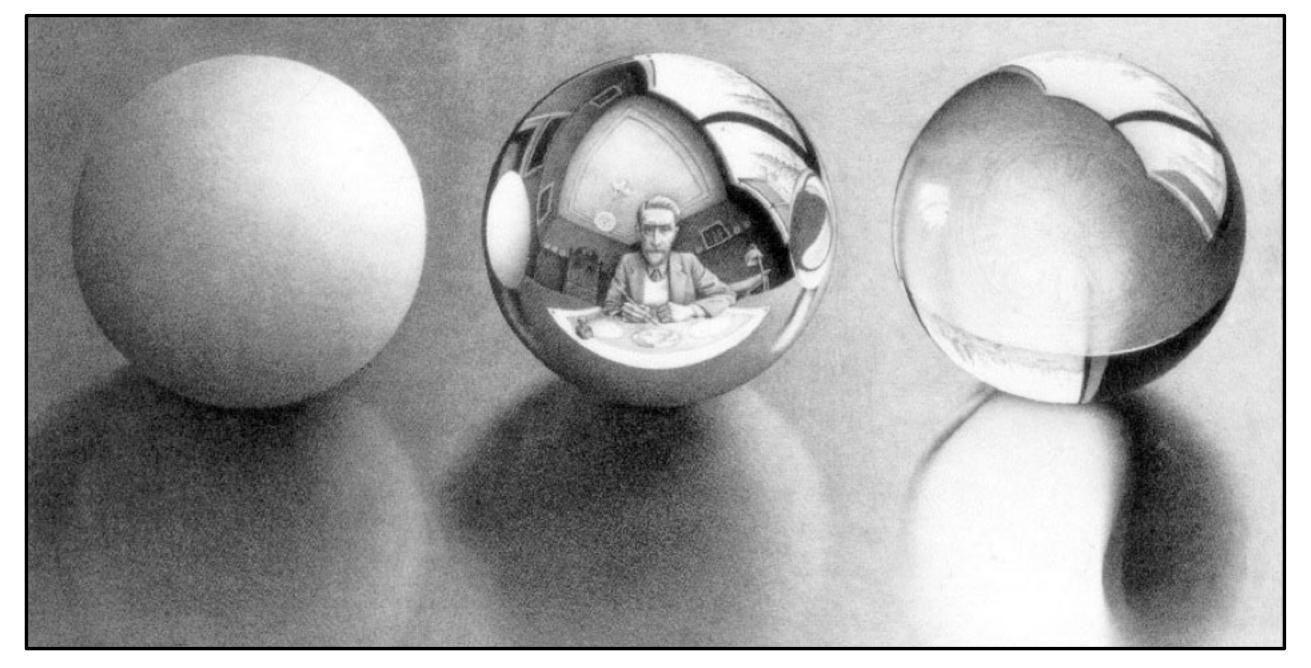
Ray tracing and simple shading



15-468, 15-668, 15-868 Physics-based Rendering Spring 2022, Lecture 3

Course announcements

- Programming assignment 0 available on Canvas.
 - Ungraded, no due date.
 - Used to set up rendering environment and github-based submission system.
 - Should take no more than 1-2 hours max.
- Programming assignment 1 will be posted on Friday 2/28, will be due two weeks later.
- Take-home quiz 1 will be posted tonight, will be due Tuesday 2/1.
- Office hours for the rest of the semester:
 - Po, Mondays 4 6 pm ET.
 - Yannis, Wednesdays 5 7 pm ET.
 - Bailey, Thursdays 5 7 pm ET.
 - For this week only, office hours are on Zoom. See Canvas for links.
 - Starting next week, office hours will be in-person at the Smith Hall graphics lounge.
 - Yannis may schedule additional office hours on Fridays.

Overview of today's lecture

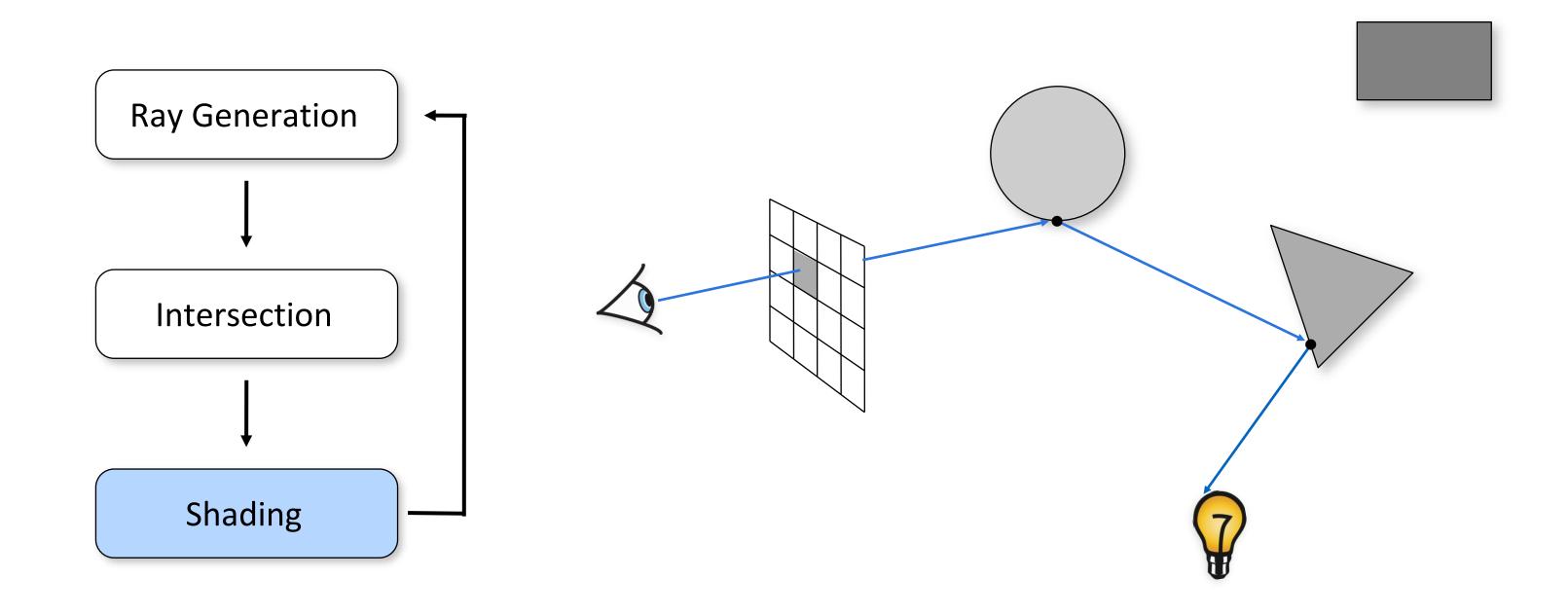
- Leftover from previous lecture: intersections, meshes, acceleration structures.
- Basics of shading.
- Basic reflection models.

Slide credits

Most of these slides were directly adapted from:

Wojciech Jarosz (Dartmouth).

Recap: Raytracing



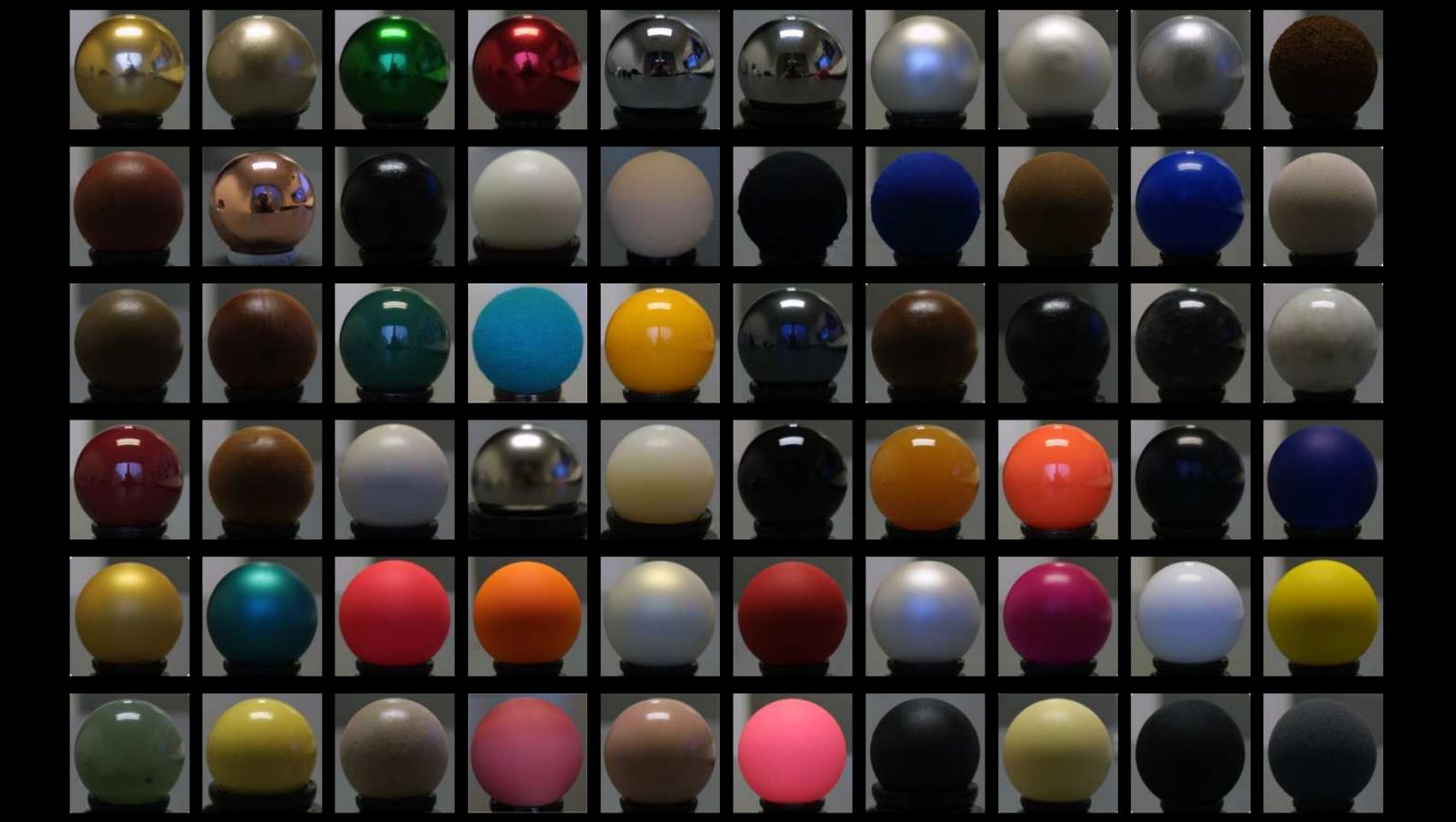
Shading

When ray hits a surface we perform lighting/shading

Determine "what color/light should we see at this location?"

Surfaces can scatter and/or emit light

- Surface emits light? just return emitted color (determined by the material)
- Surface scatters/reflects/refracts light?
 (recursively) trace a ray in a scattering direction
 (determined by the underlying material)



Overview

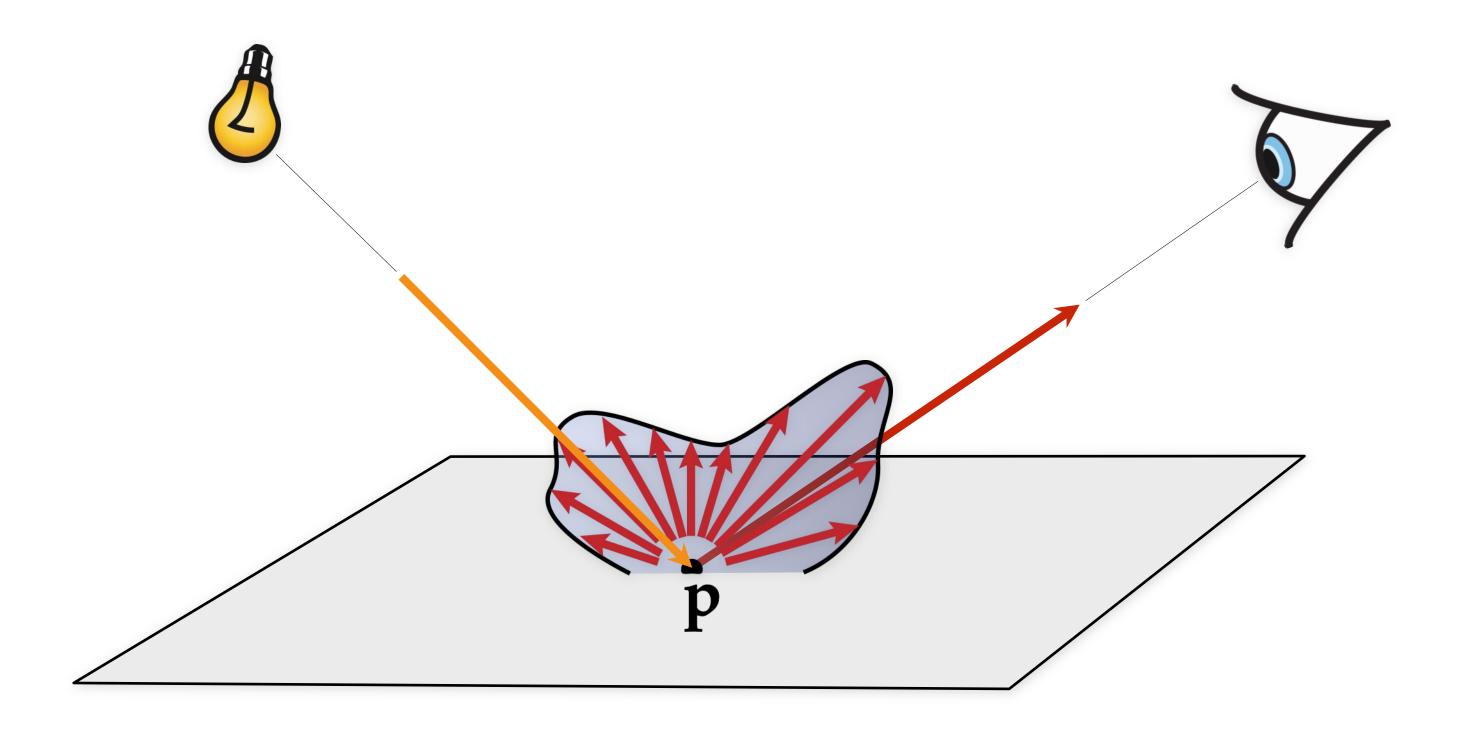
Diffuse shading

Specular reflection

Refraction

Diffuse emission

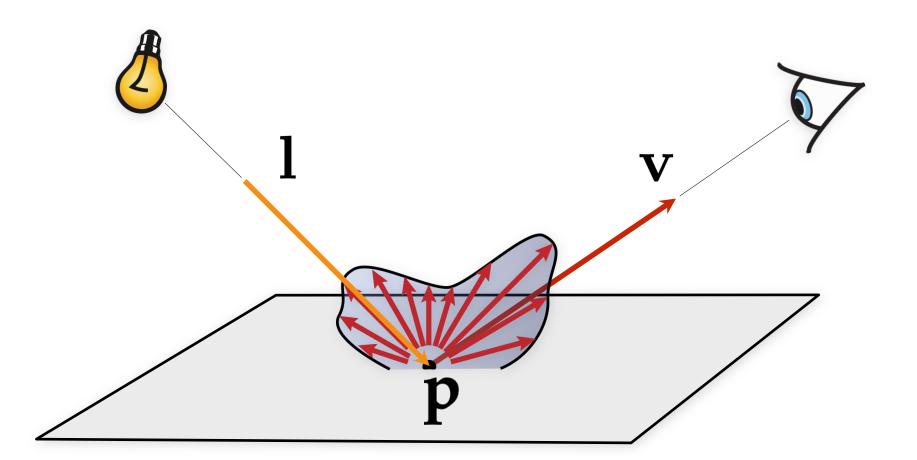
Light-material interactions



The BSDF

Bidirectional Scattering Distribution Function

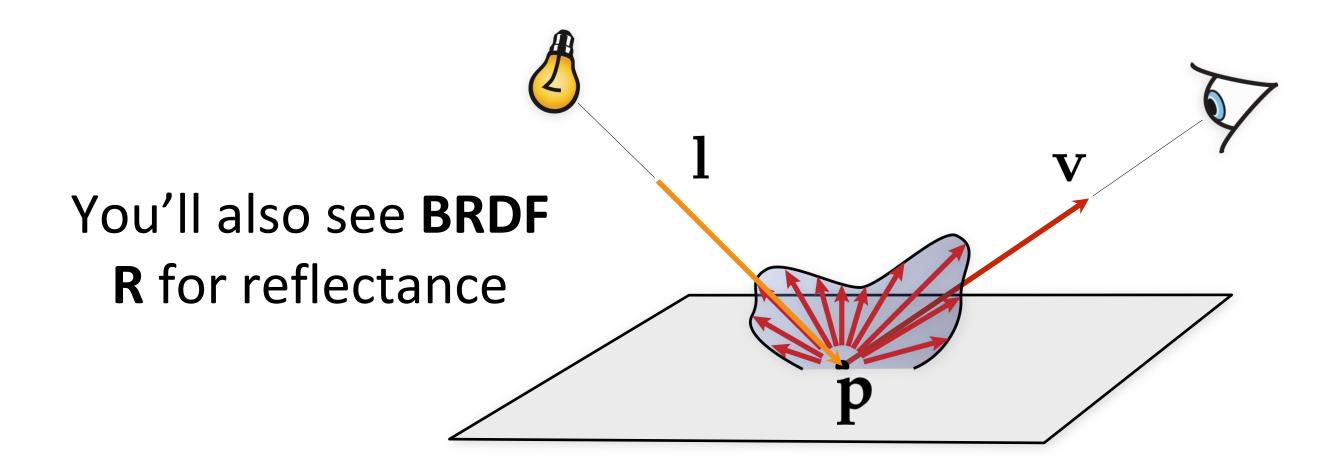
- informally: how much the material scatters light coming from one direction ${\bf l}$ into some other direction ${\bf v}$, at each point ${\bf p}$



The BSDF

Bidirectional Scattering Distribution Function

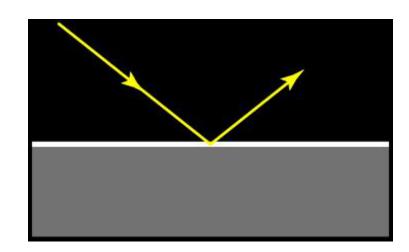
- informally: how much the material scatters light coming from one direction ${\bf l}$ into some other direction ${\bf v}$, at each point ${\bf p}$



Real-world materials

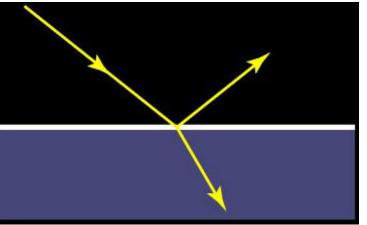
Metals





Dielectric

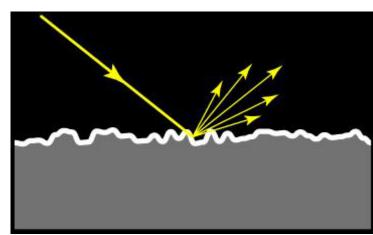




Real-world materials

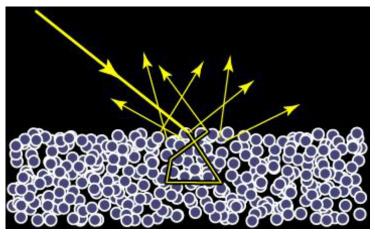
Metals





Dielectric





Idealized material models

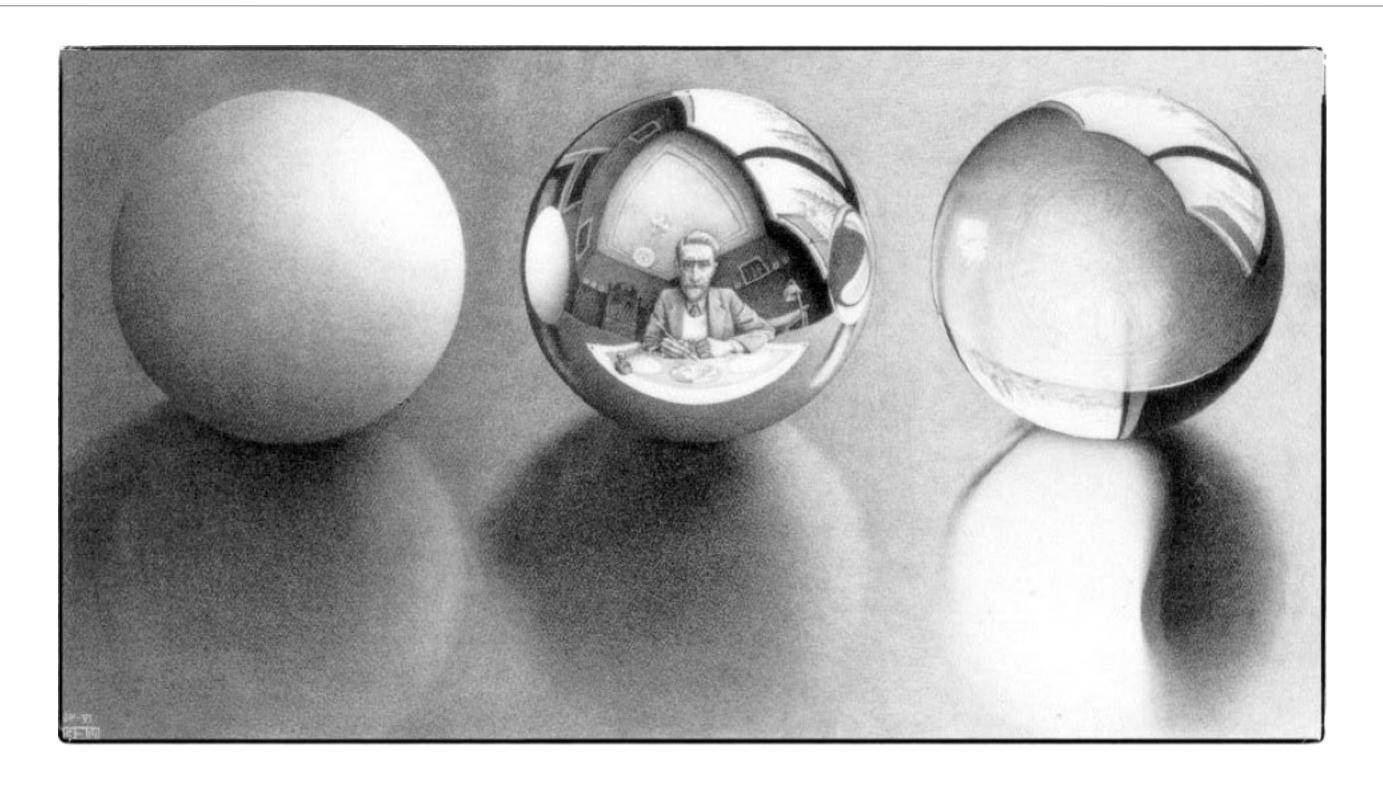
Diffuse reflection

- light is reflected in all directions
- colored by surface color

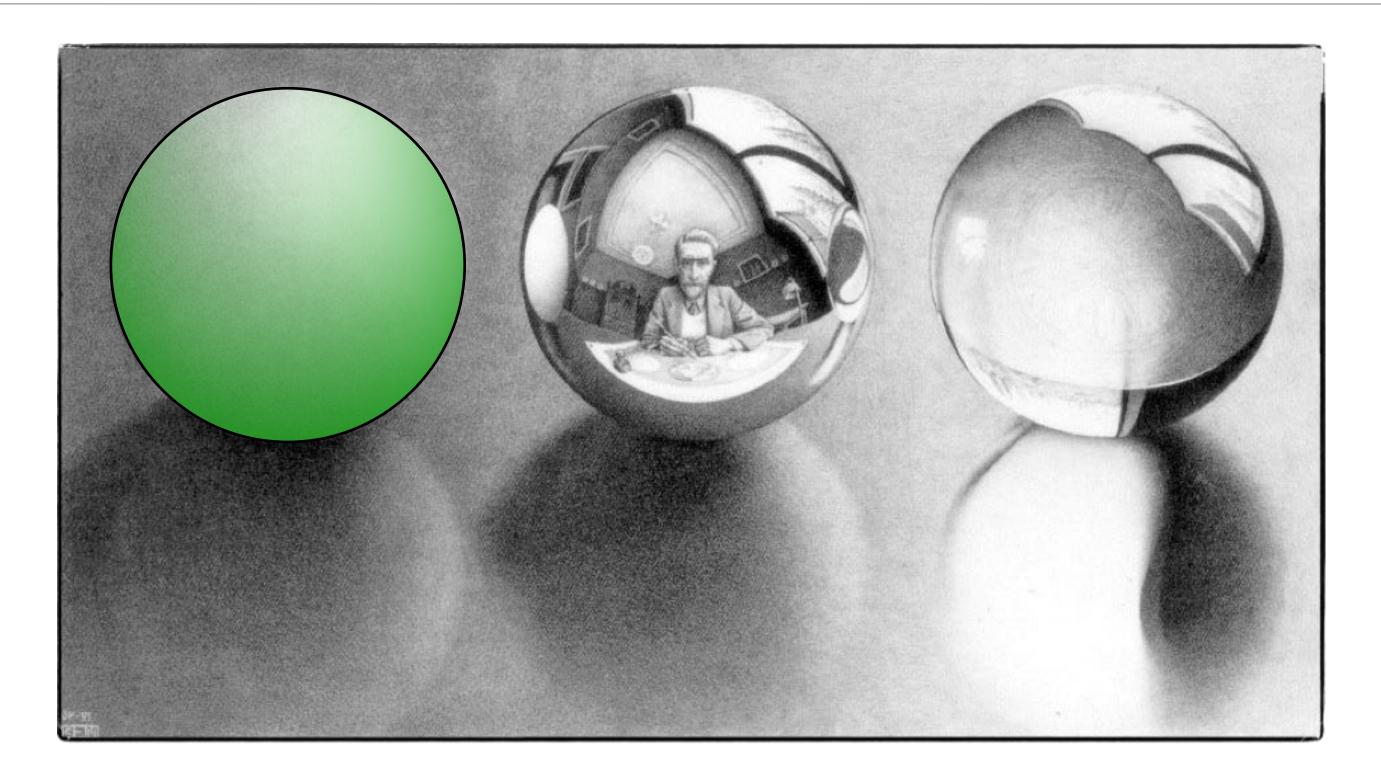
Smooth specular reflection/refraction (e.g., chrome, glass, glaze/varnish)

- light reflected/refracted only in a single direction
- colored by source color

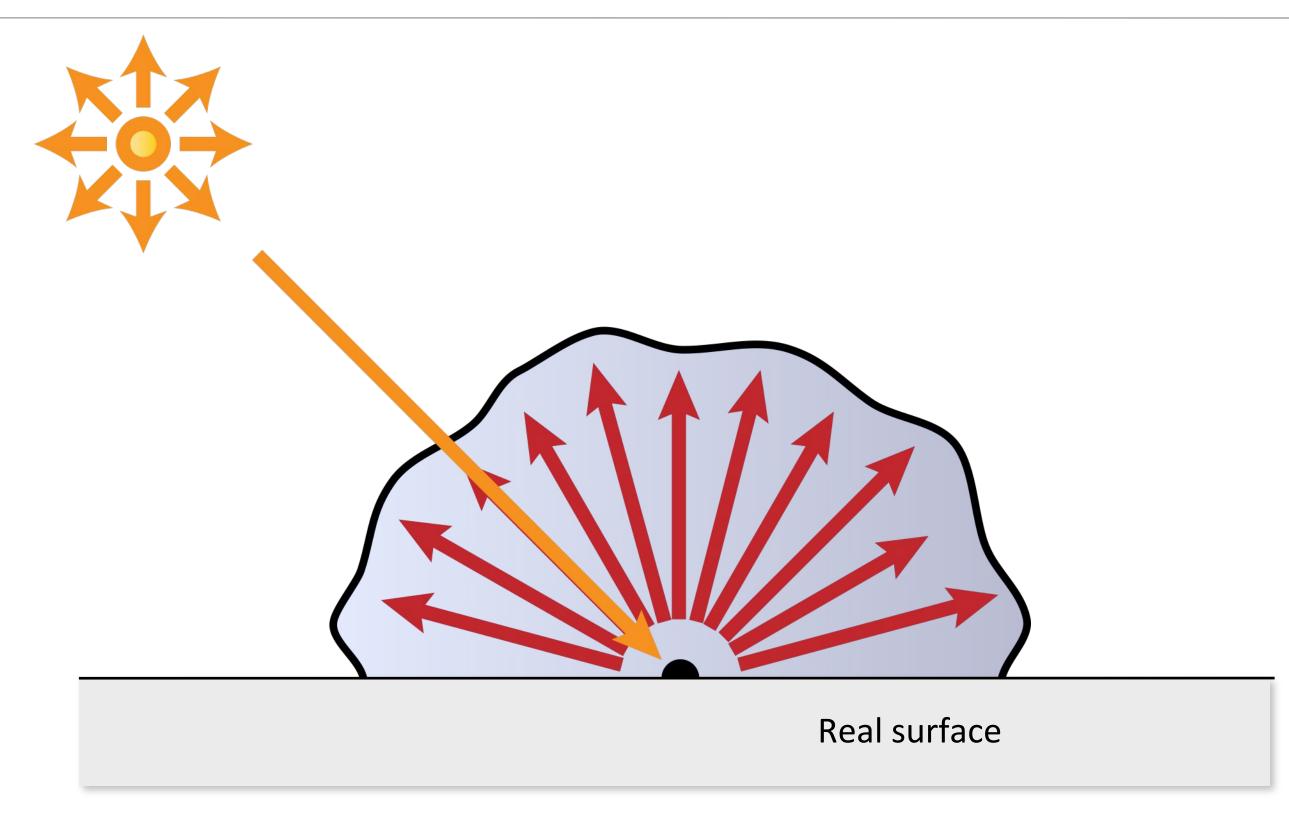
Idealized materials



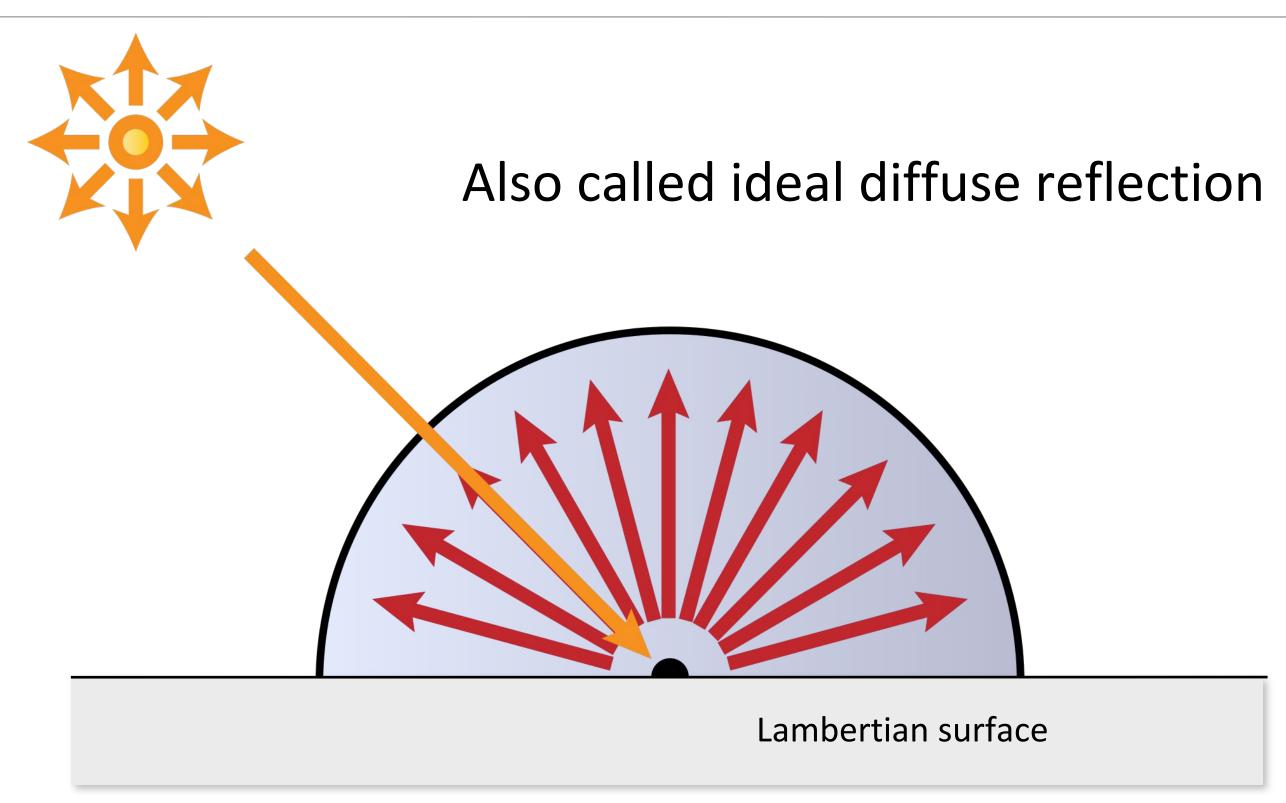
Diffuse reflection



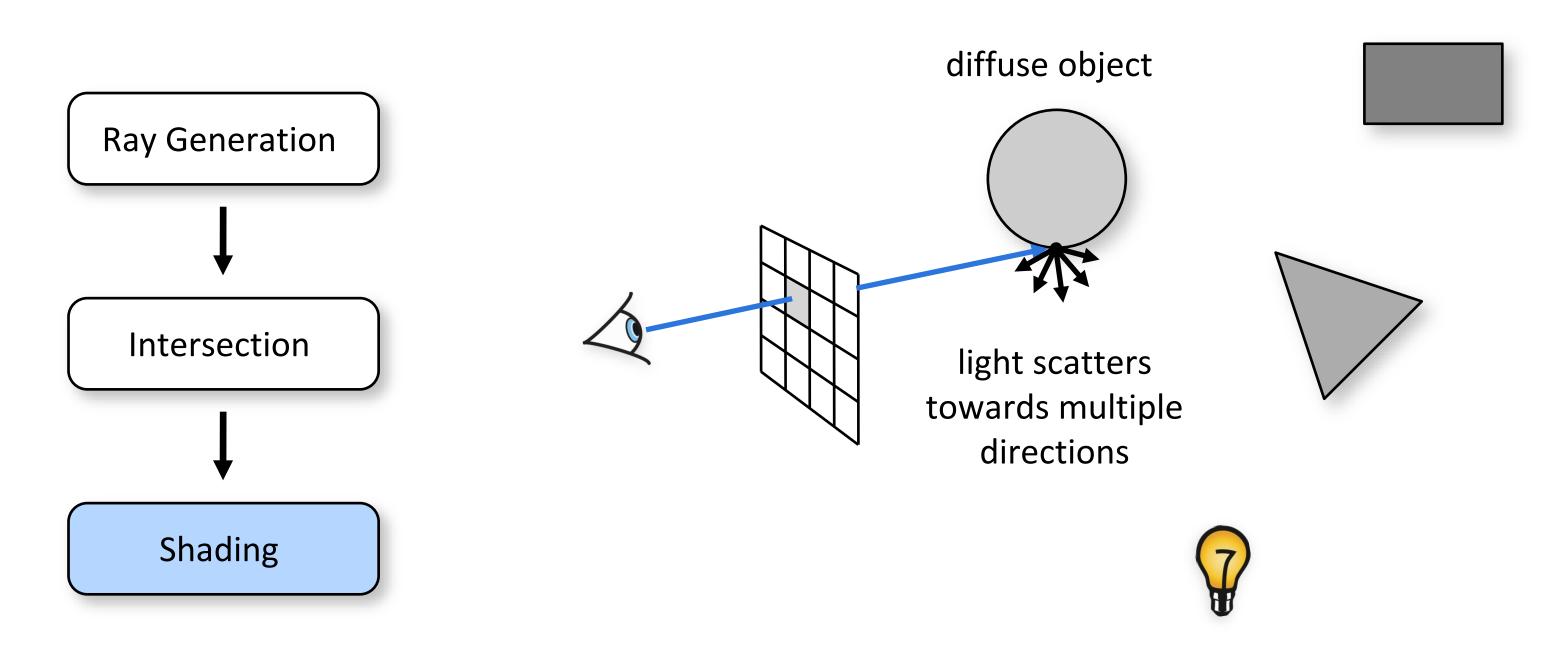
Diffuse reflection



Lambertian reflection

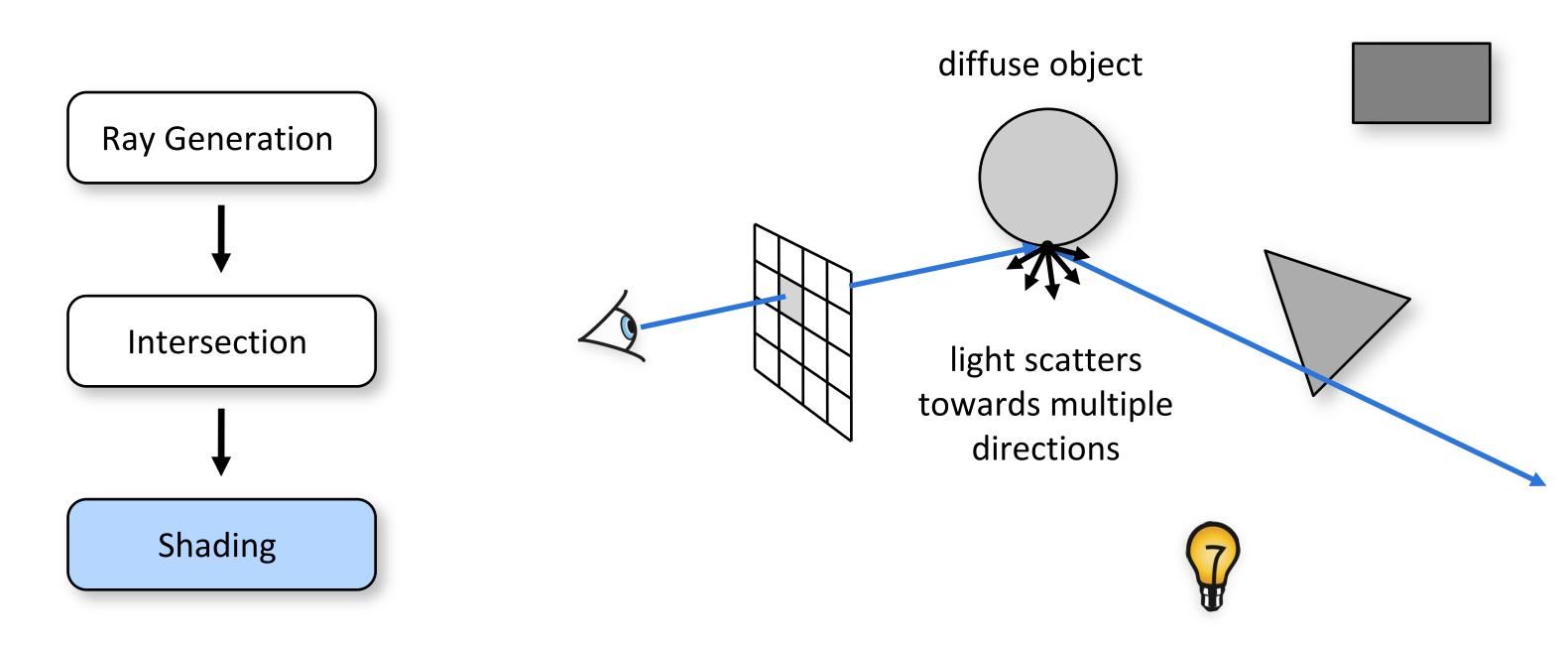


Basic Ray Tracing Pipeline



What direction should we trace a new ray towards?

Basic Ray Tracing Pipeline



What direction should we trace a new ray towards?

Pick a direction at random!

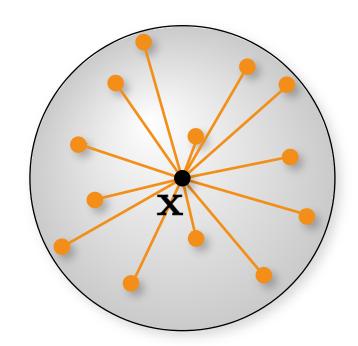
From what distribution should we sample directions?

From what distribution should we sample directions?

- Probability proportional to $\cos(\hat{n} \cdot \hat{\omega})$.
- Even though BSDF scatters to all directions uniformly, we need to account for foreshortening.

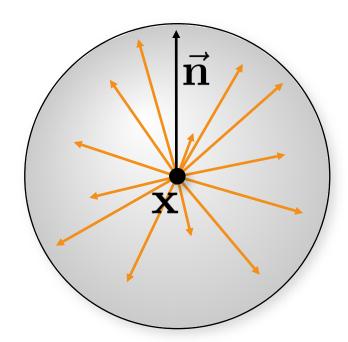
How do we sample directions based on this *cosine-weighted* distribution?

Generate points uniformly on sphere (unit directions)

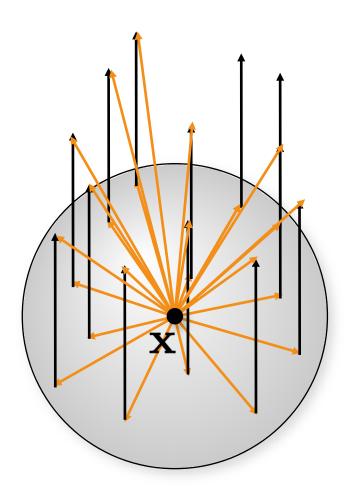


Generate points uniformly on sphere (unit directions)

unit normal



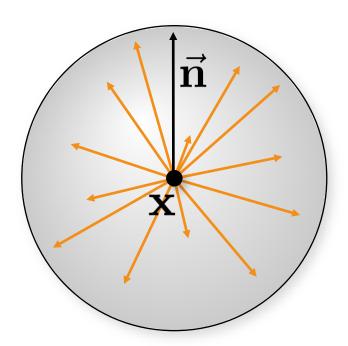
Add unit normal

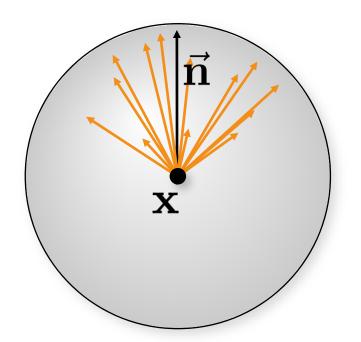


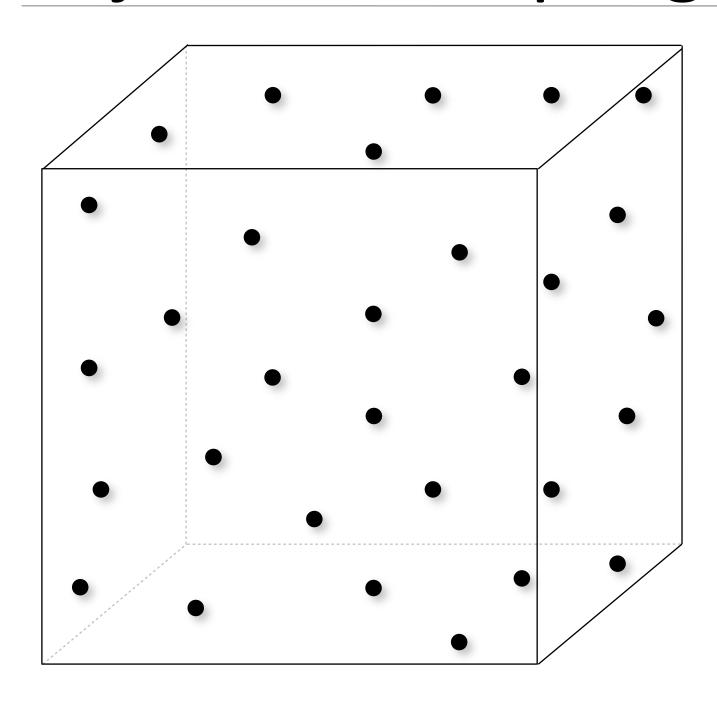
Generate points uniformly on sphere (unit directions)

Add unit normal normalize

unit normal

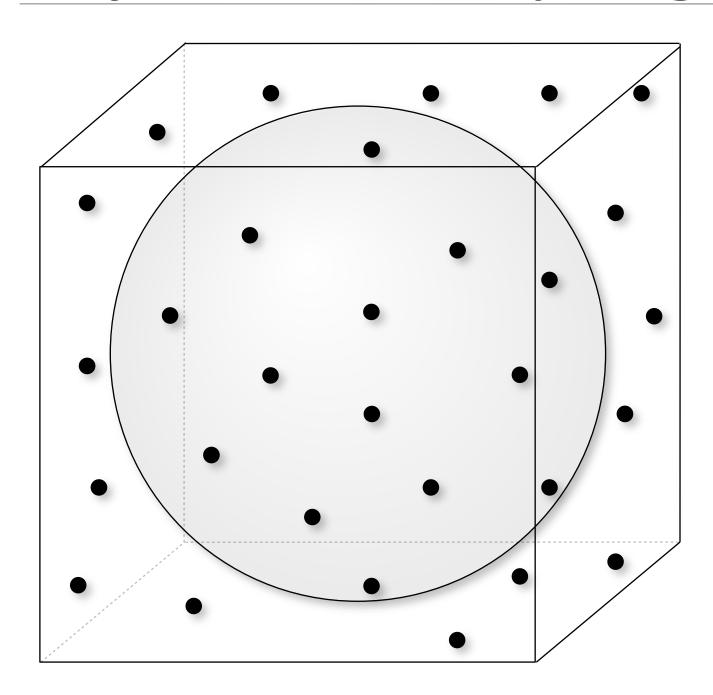




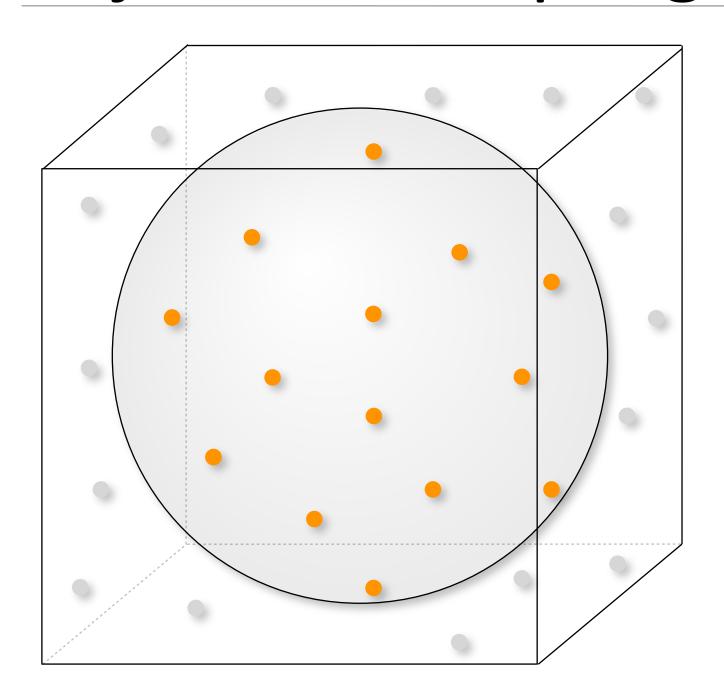


```
Vector3D v;
```

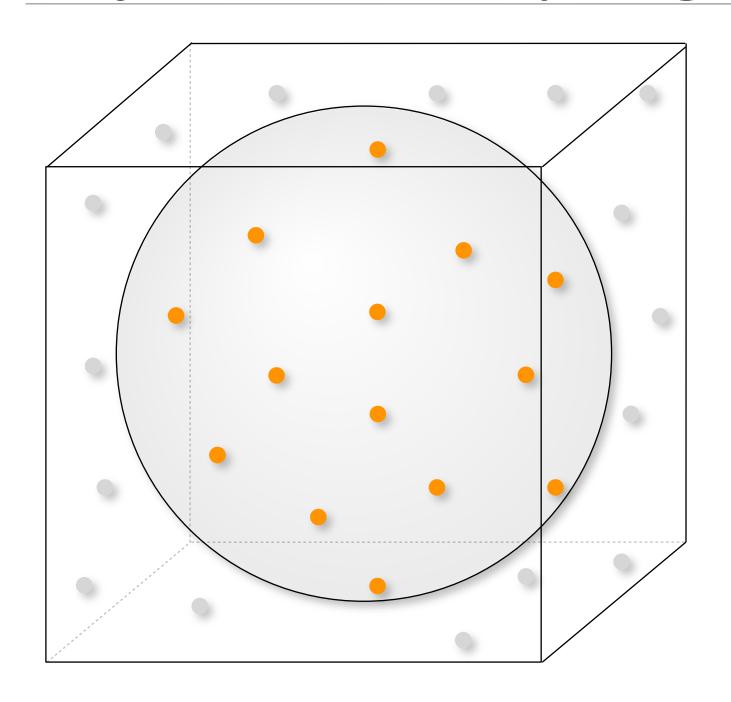
```
v.x = 1-2*randf();
v.y = 1-2*randf();
v.z = 1-2*randf();
```



```
Vector3D v;
do
{
    v.x = 1-2*randf();
    v.y = 1-2*randf();
    v.z = 1-2*randf();
} while(v.length<sup>2</sup>() > 1)
```

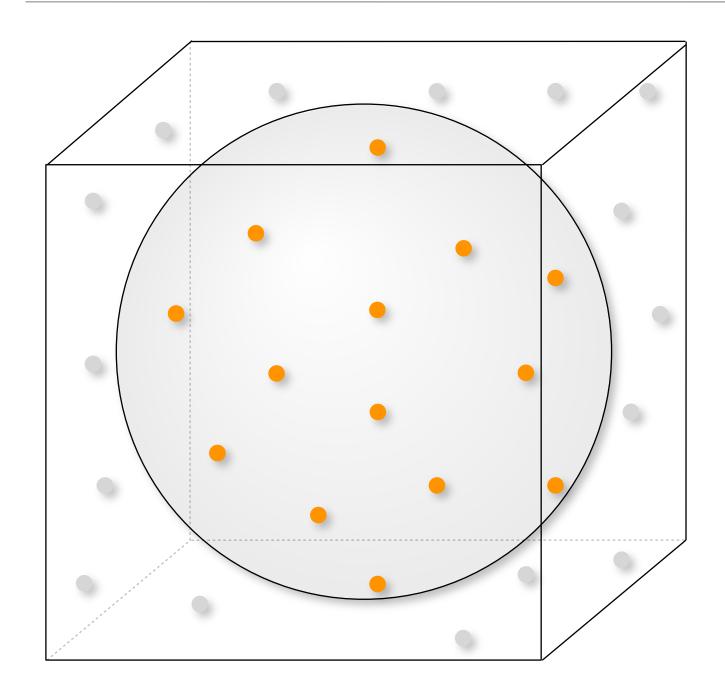


```
Vector3D v;
do
{
    v.x = 1-2*randf();
    v.y = 1-2*randf();
    v.z = 1-2*randf();
} while(v.length<sup>2</sup>() > 1)
```



```
Vector3D v;
do
   v.x = 1-2*randf();
   v.y = 1-2*randf();
   v.z = 1-2*randf();
} while(v.length<sup>2</sup>() > 1)
// Project onto sphere
v /= v.length();
```

Sampling a Sphere using normal samples



```
Vector3D v;
v.x = randnf();
v.y = randnf();
v.z = randnf();
// Project onto sphere
v /= v.length();
```

- No rejection sampling required (no while loop).
- Need to use normal, rather than uniform, samples.

Diffuse shading

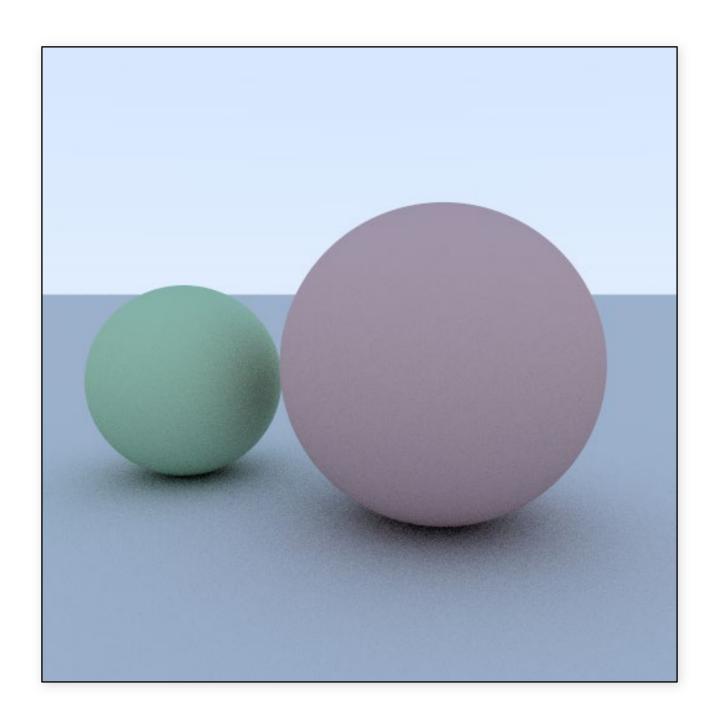
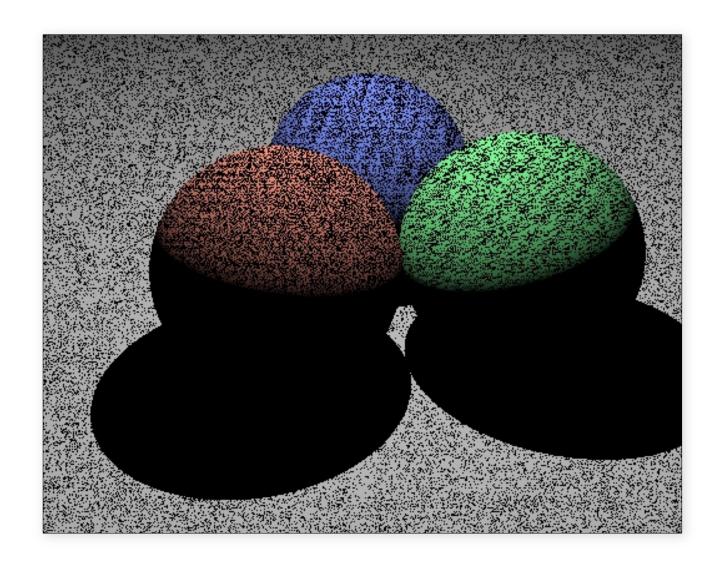


Image so far

```
Scene::trace(Ray ray)
   hit = surfaces.intersect(ray);
   if hit
      [col, sRay] = hit->mat->scatter(ray)
      return col * trace(sRay);
   else
      return backgroundColor;
```

Rounding errors

Don't fall victim to one of the classic blunders:



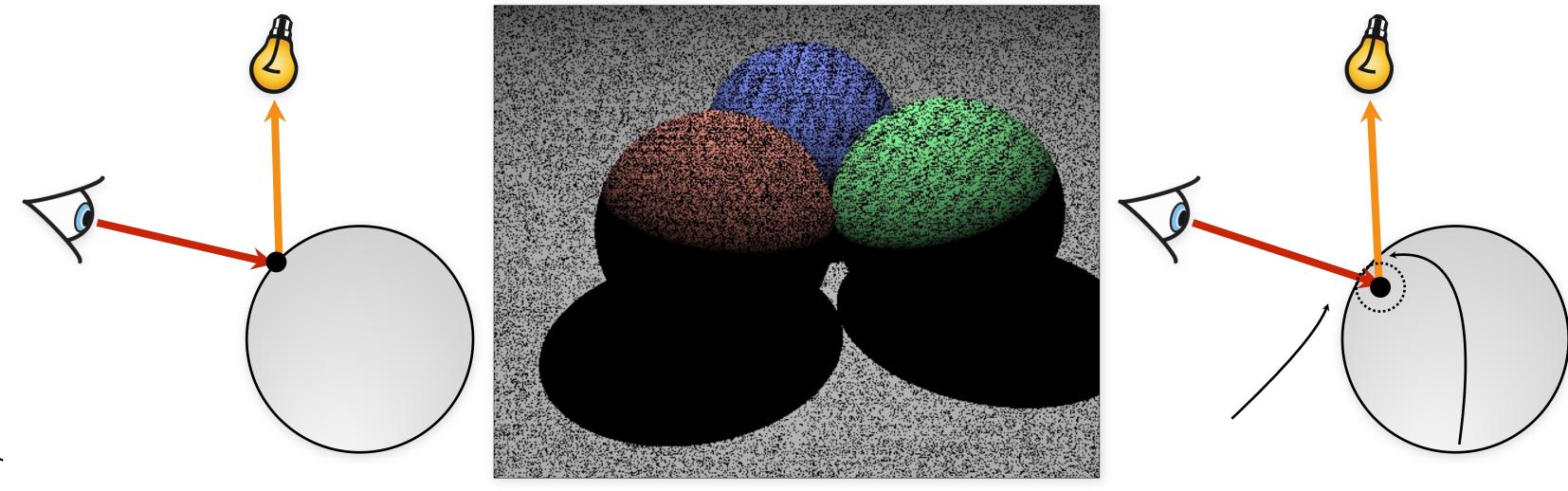
affectionately called "shadow acne"

What's going on?

After a slide by Steve Marschner

Rounding errors

Don't fall victim to one of the classic blunders:

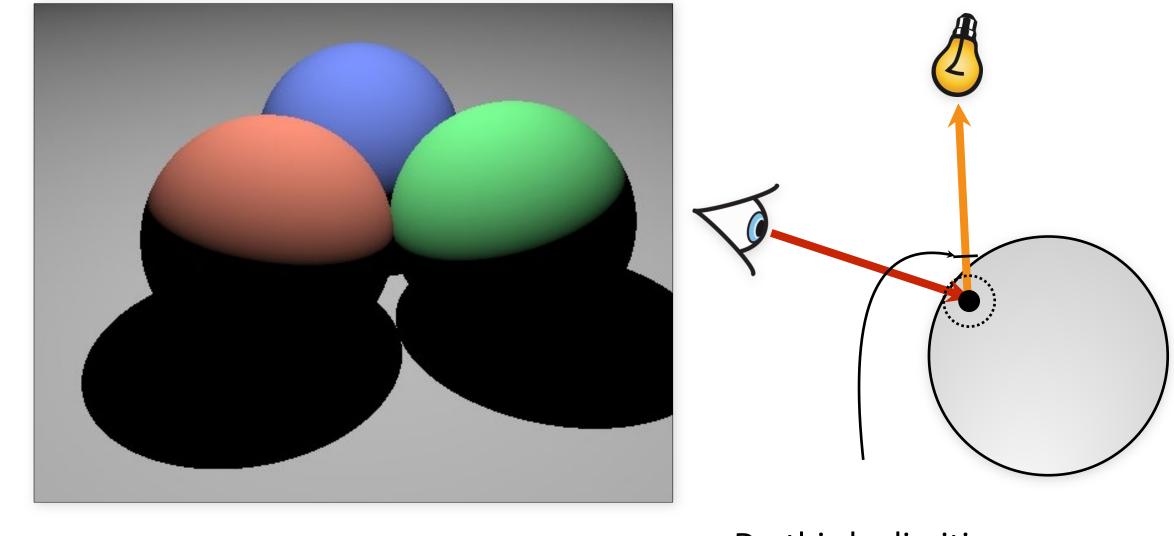


intersection inside due to floating point error

ray blocked by self-intersection

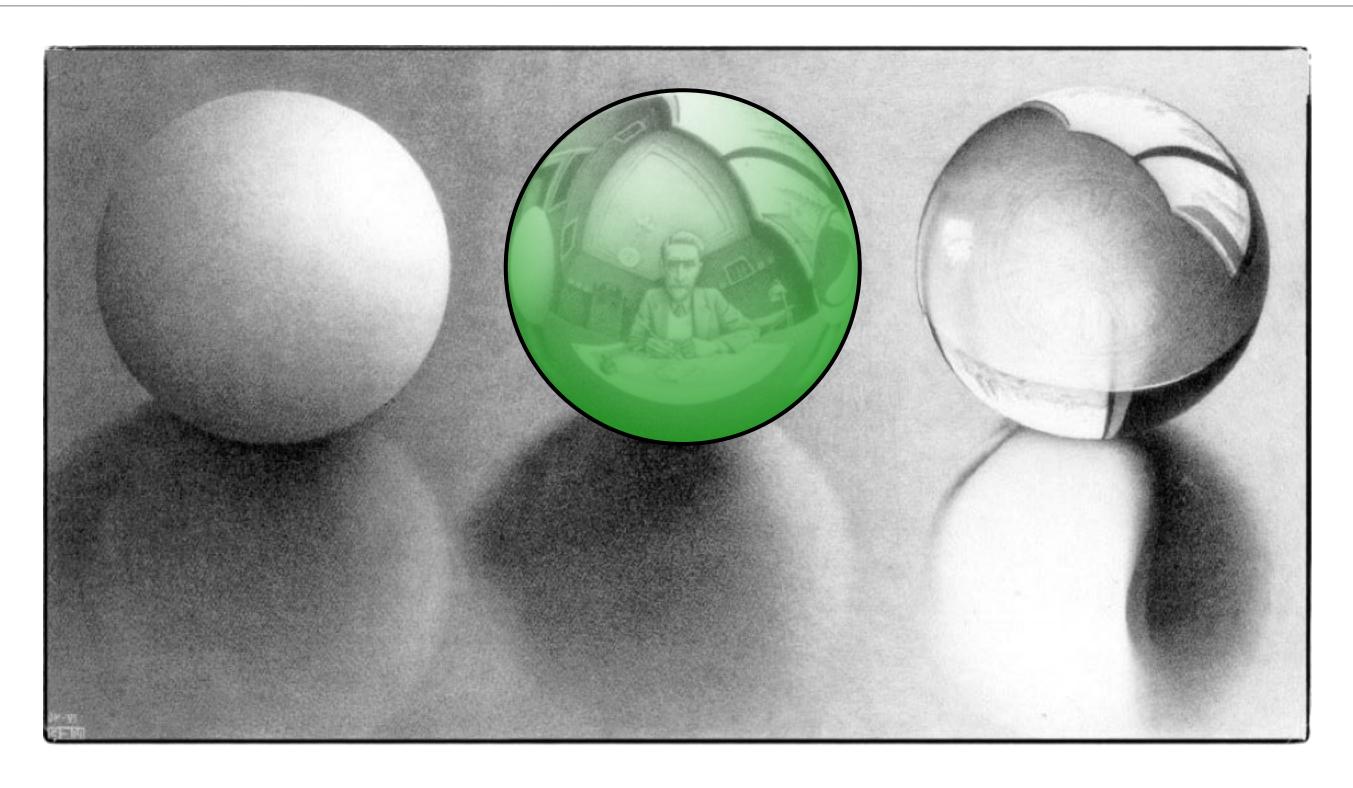
Shadow rounding errors

Solution: recursive rays start a tiny distance from the surface

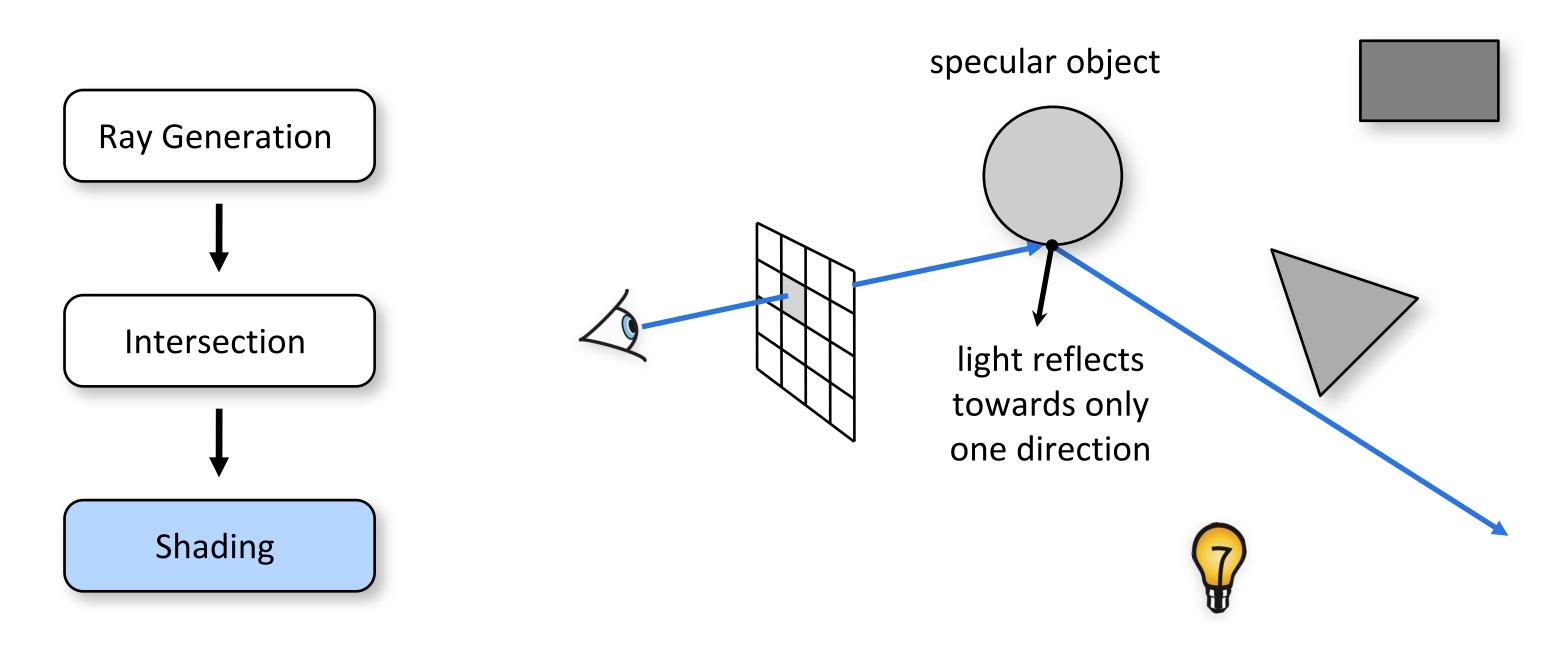


Do this by limiting the *t* range

Specular/Mirror reflection

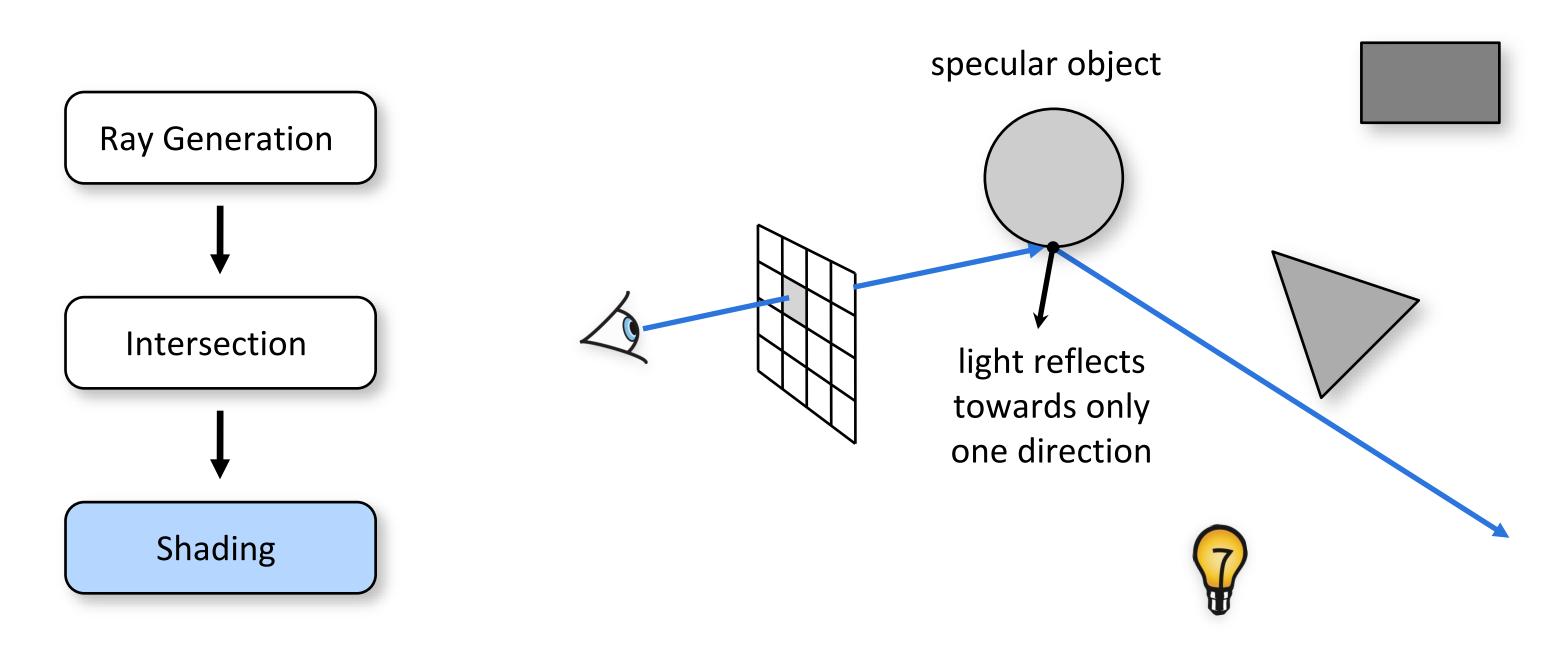


Basic Ray Tracing Pipeline



What direction should we trace a new ray towards?

Basic Ray Tracing Pipeline



What direction should we trace a new ray towards?

Just use law of mirror reflection, no need for random selection!

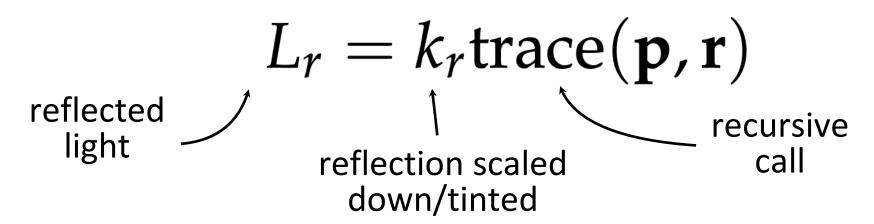
Consider perfectly shiny surface

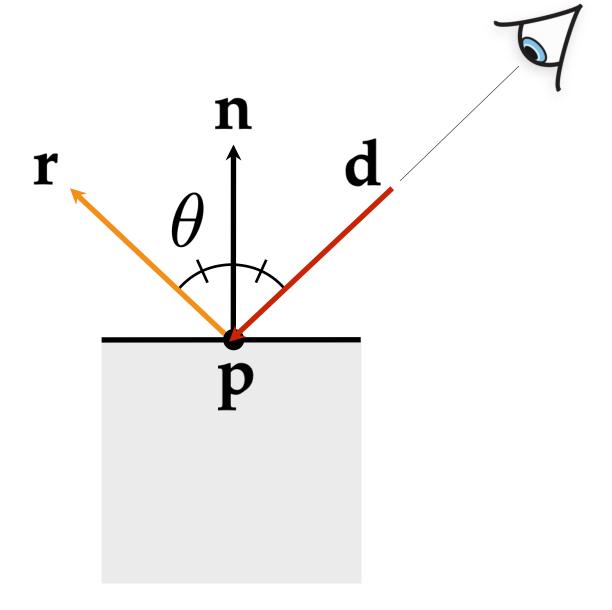
- there's a reflection of other objects

Can render this using recursive ray tracing

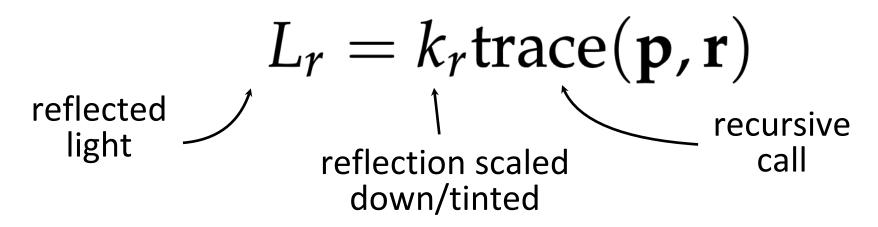
- to find out mirror reflection color ask: "what color is seen from surface point in reflection direction?"

Evaluated by tracing a new ray:



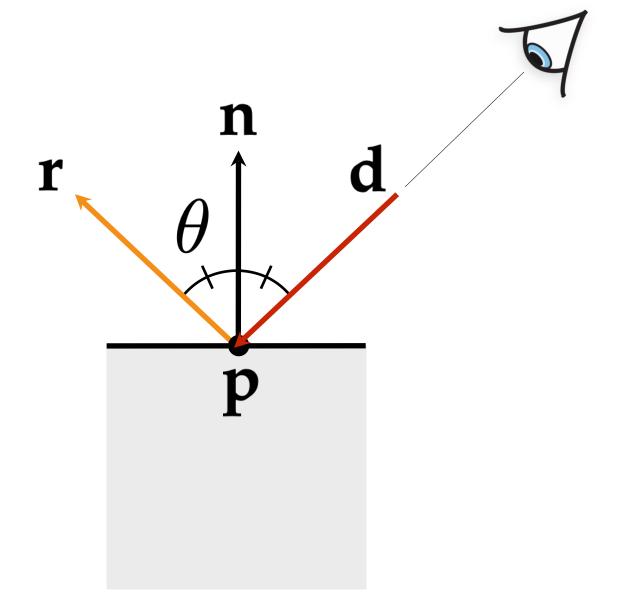


Evaluated by tracing a new ray:



Implementation details:

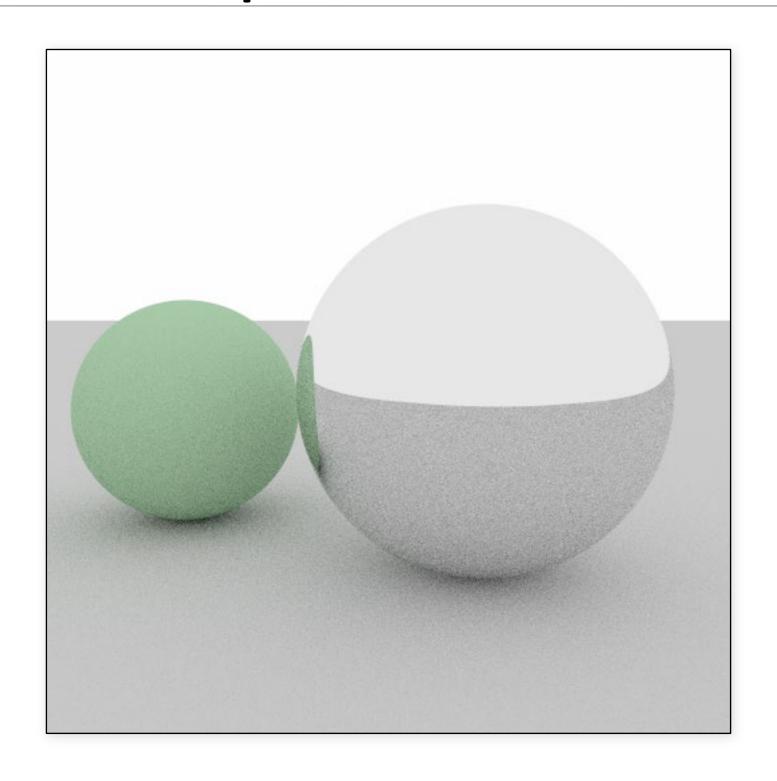
- don't self-intersect ($t_{min} > \epsilon$)
- don't recurse indefinitely

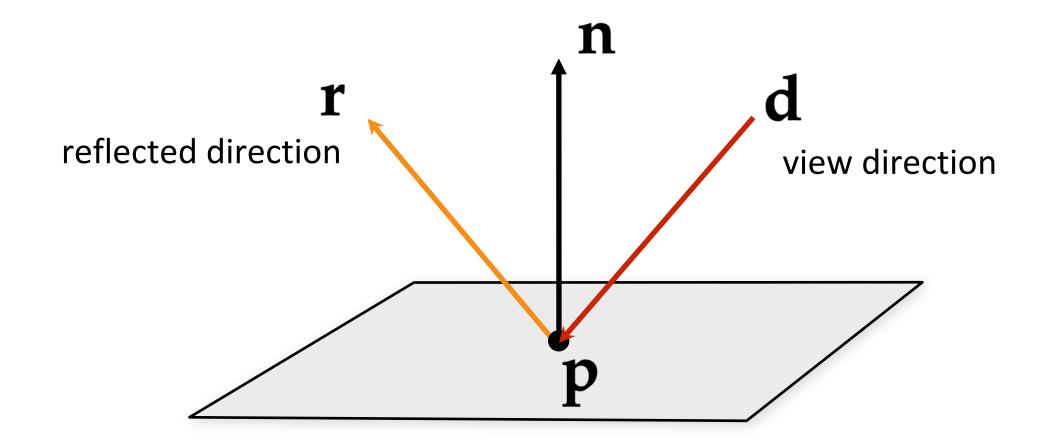


Same pseudo-code

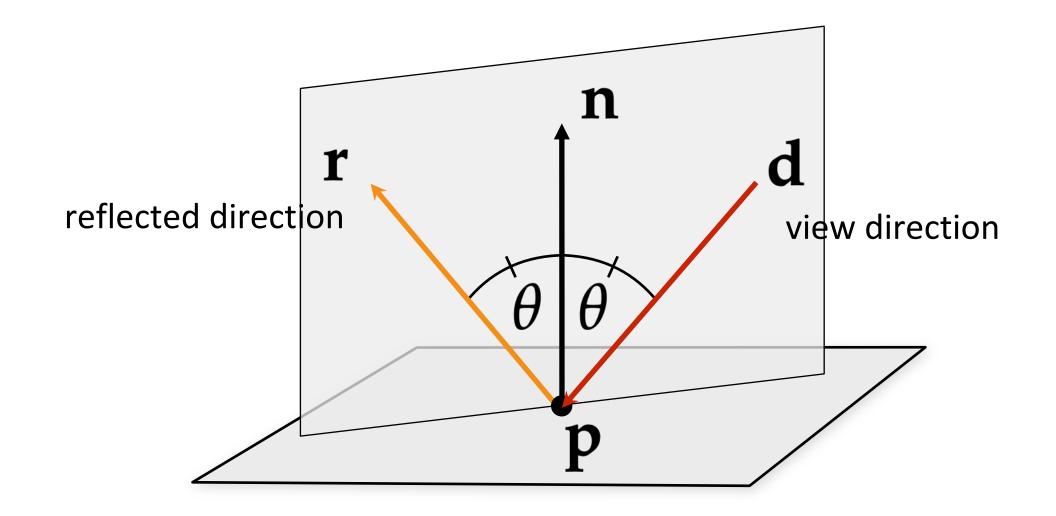
```
Scene::trace(Ray ray)
   hit = surfaces.intersect(ray);
   if hit
      [col, sRay] = hit->mat->scatter(ray)
      return col * trace(sRay);
   else
      return backgroundColor;
```

Diffuse & mirror spheres



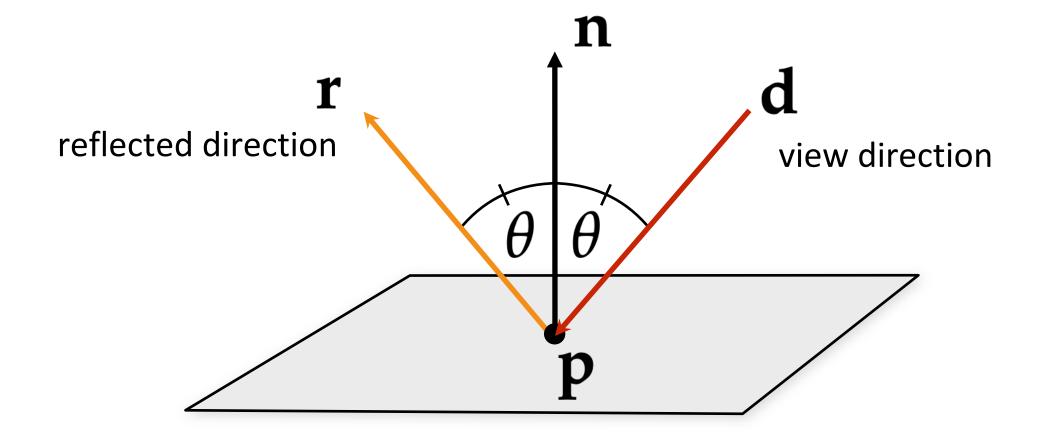


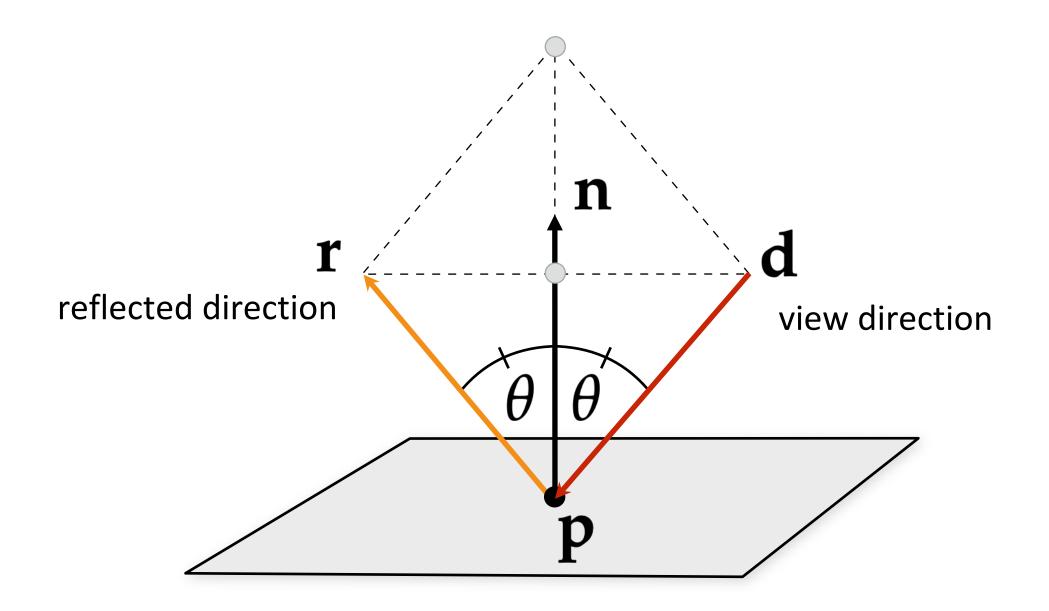
What two properties defined reflection direction?

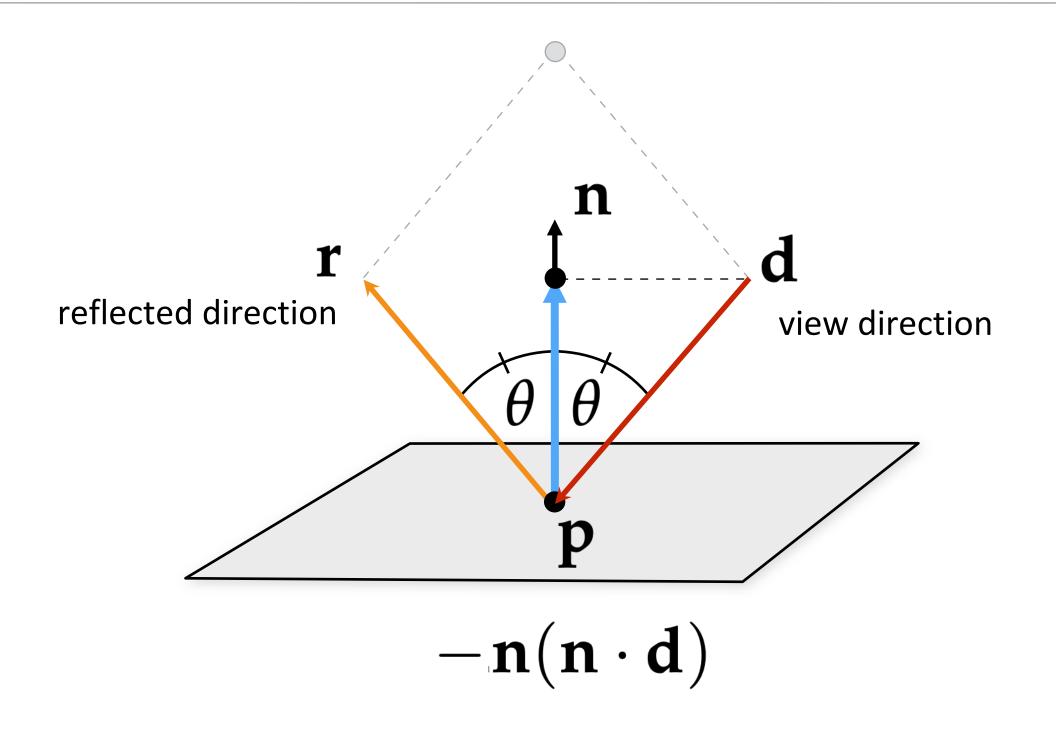


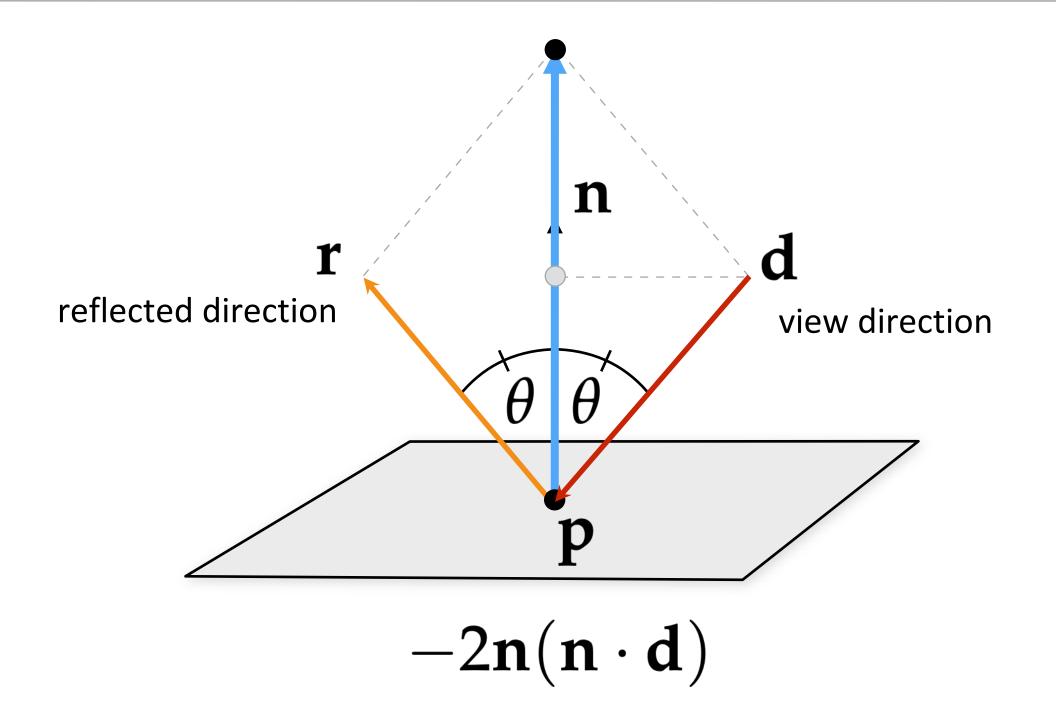
What two properties defined reflection direction?

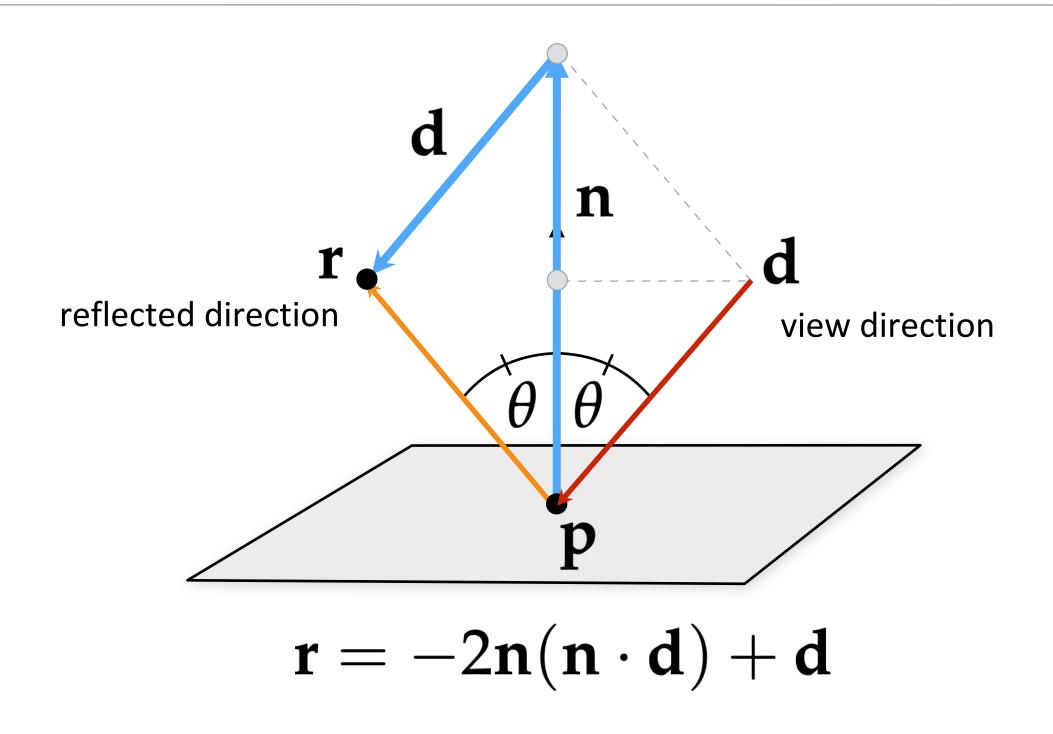
- co-planar view direction, reflected direction, and normal direction
- equal angles between normal-view directions, and normal-reflected directions



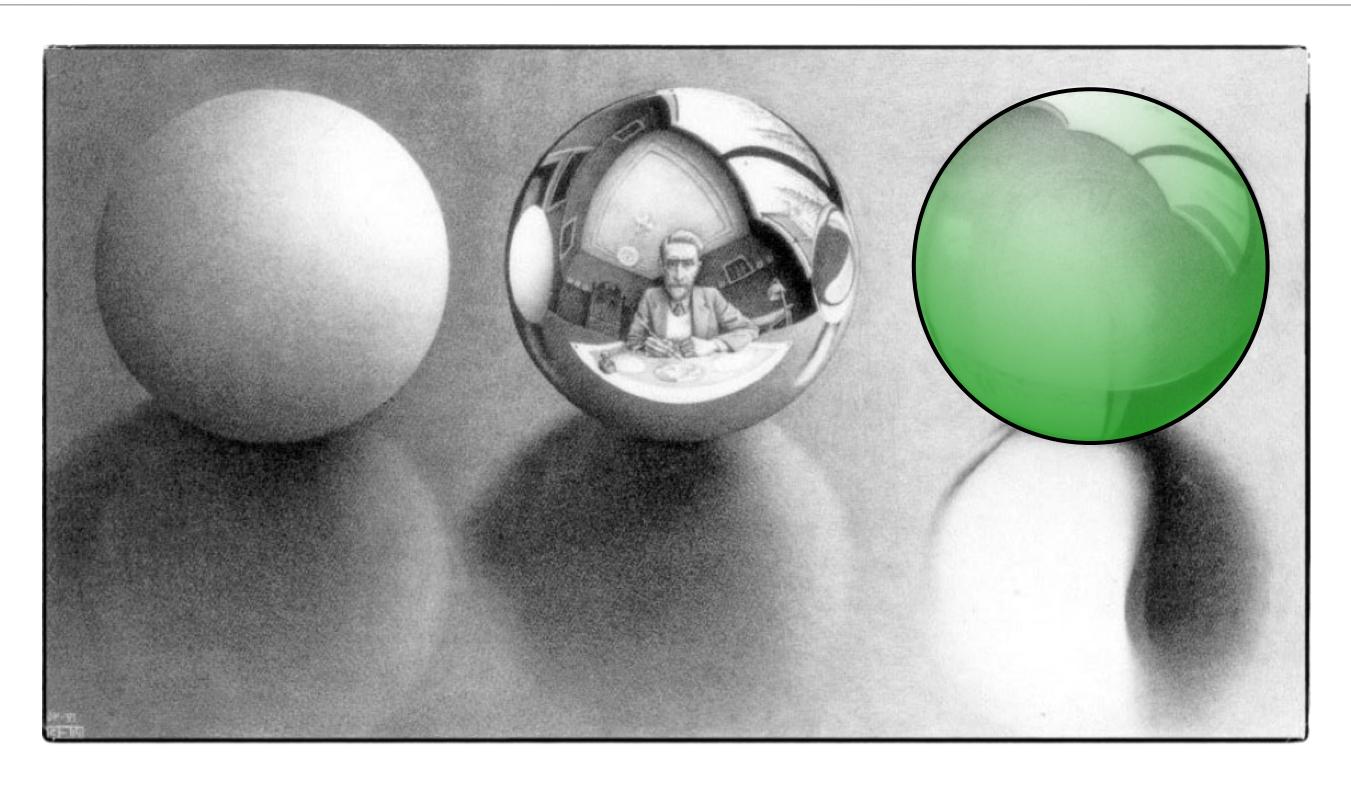








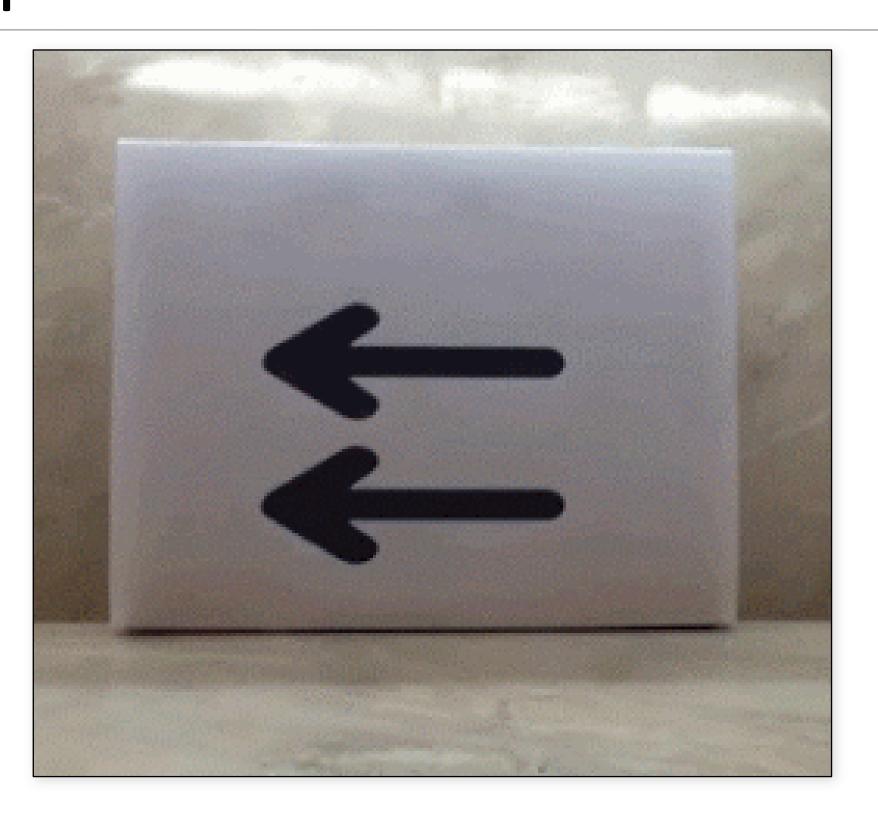
Specular refraction



Refraction



Refraction



Index of Refraction

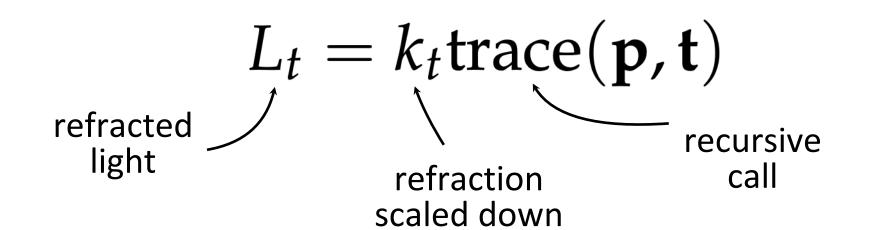
Speed of light in vacuum / speed of light in medium

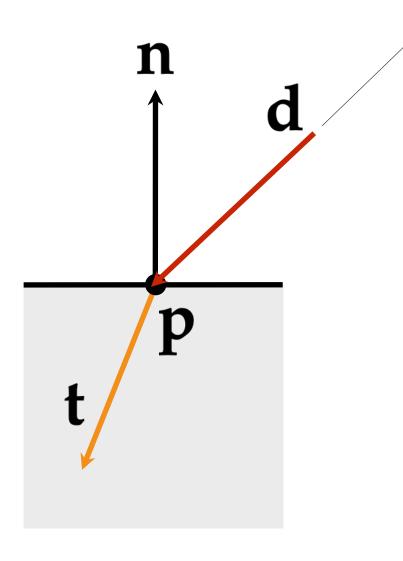
Some values of η	
Vacuum	1
Air at STP	1.00029
Ice	1.31
Water	1.33
Crown glass	1.52 - 1.65
Diamond	2.417

Specular transmission/refraction

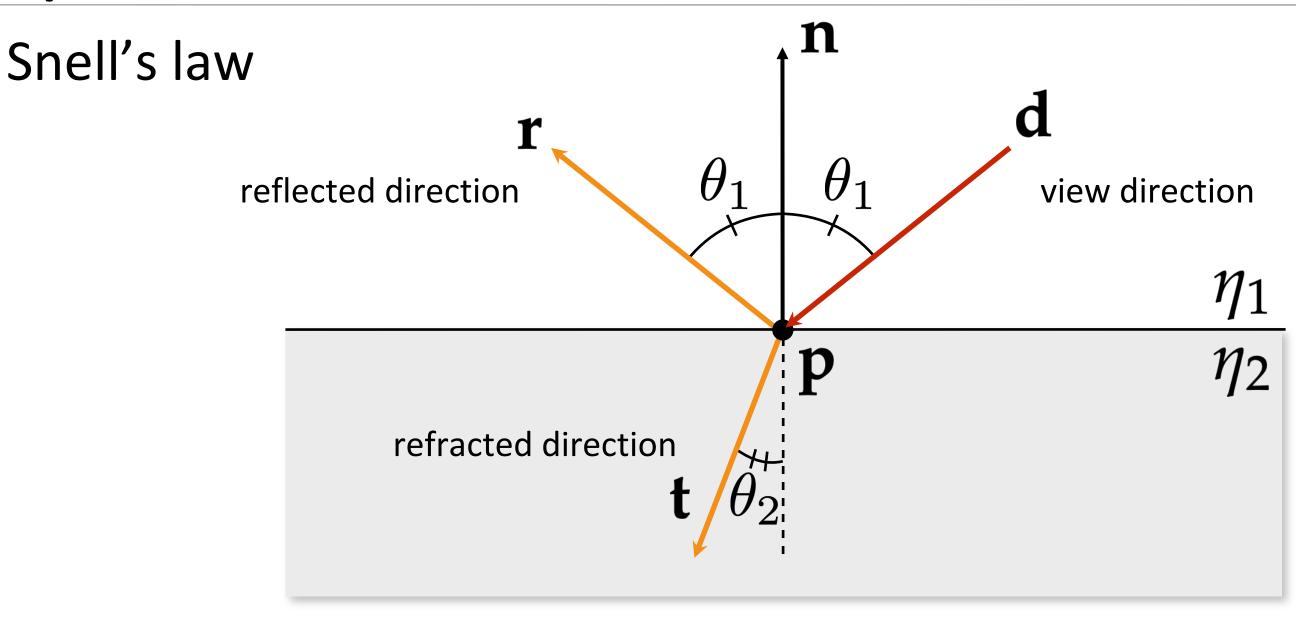
Materials like water, glass, etc., also refract/bend light

Trace a recursive ray in the refraction direction



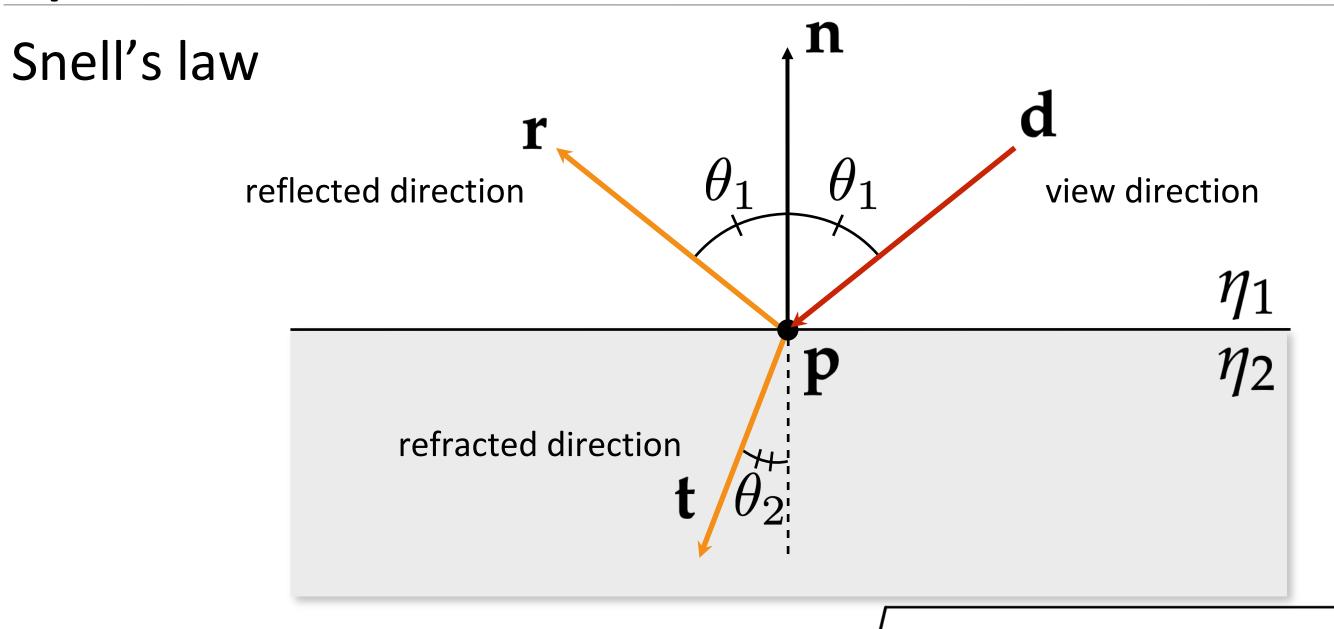


Specular transmission/refraction



$$\eta_1 \sin \theta_1 = \eta_2 \sin \theta_2$$

Specular transmission/refraction



$$\mathbf{t} = \eta_1/\eta_2 \left(\mathbf{d} - \left(\mathbf{d} \cdot \mathbf{n} \right) \mathbf{n} \right) - \mathbf{n} \sqrt{1 - \eta_1^2/\eta_2^2 \left(1 - \left(\mathbf{d} \cdot \mathbf{n} \right)^2 \right)}$$

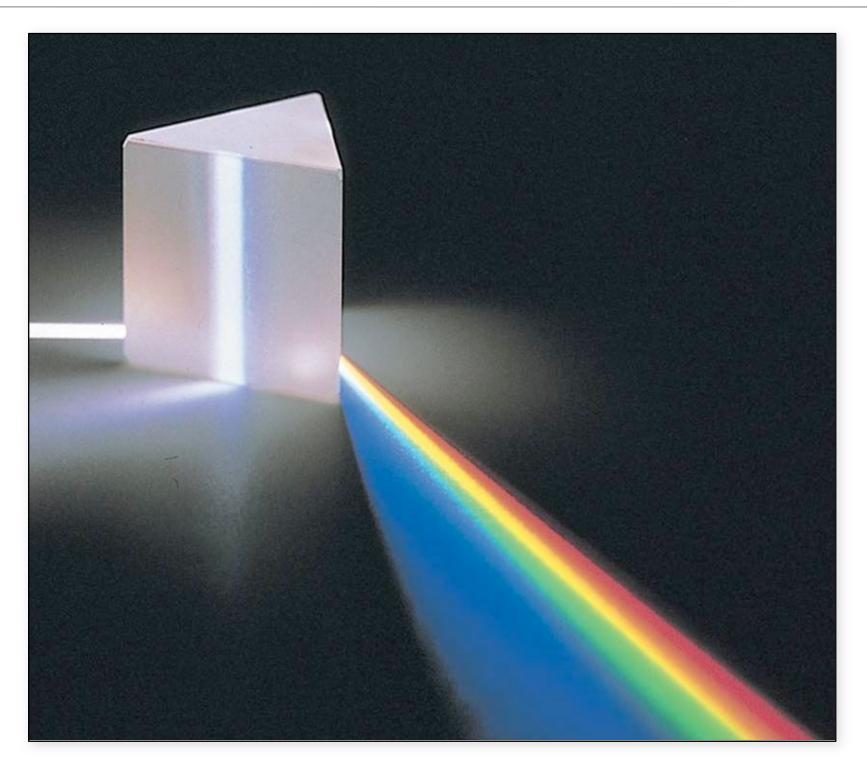
Index of Refraction

Speed of light in vacuum / speed of light in medium

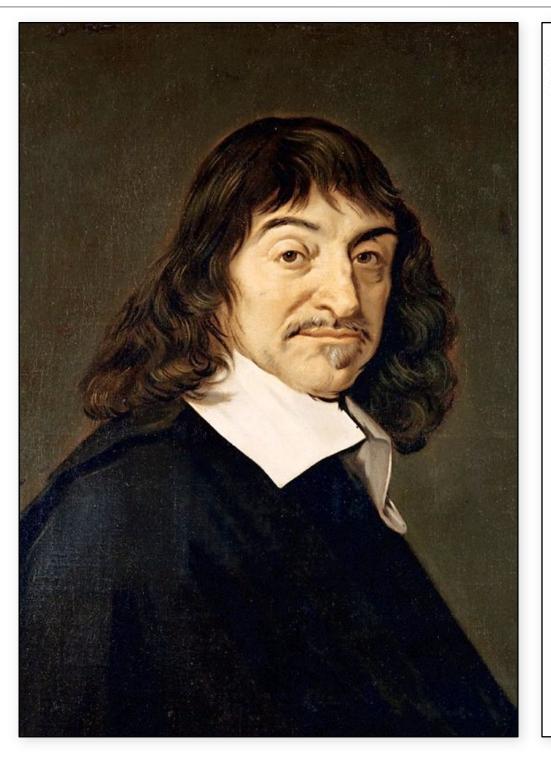
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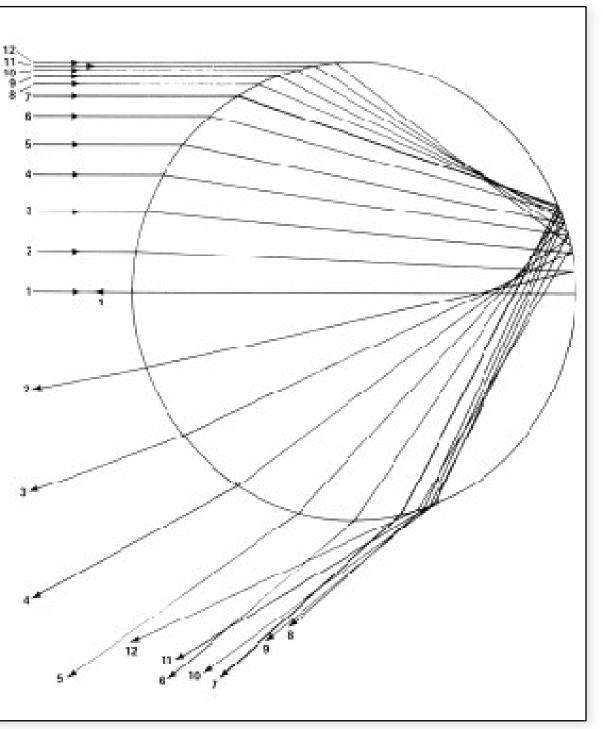
These are actually wavelength dependent!

Dispersion



Refraction in a Waterdrop





Double rainbow all the way across the sky!

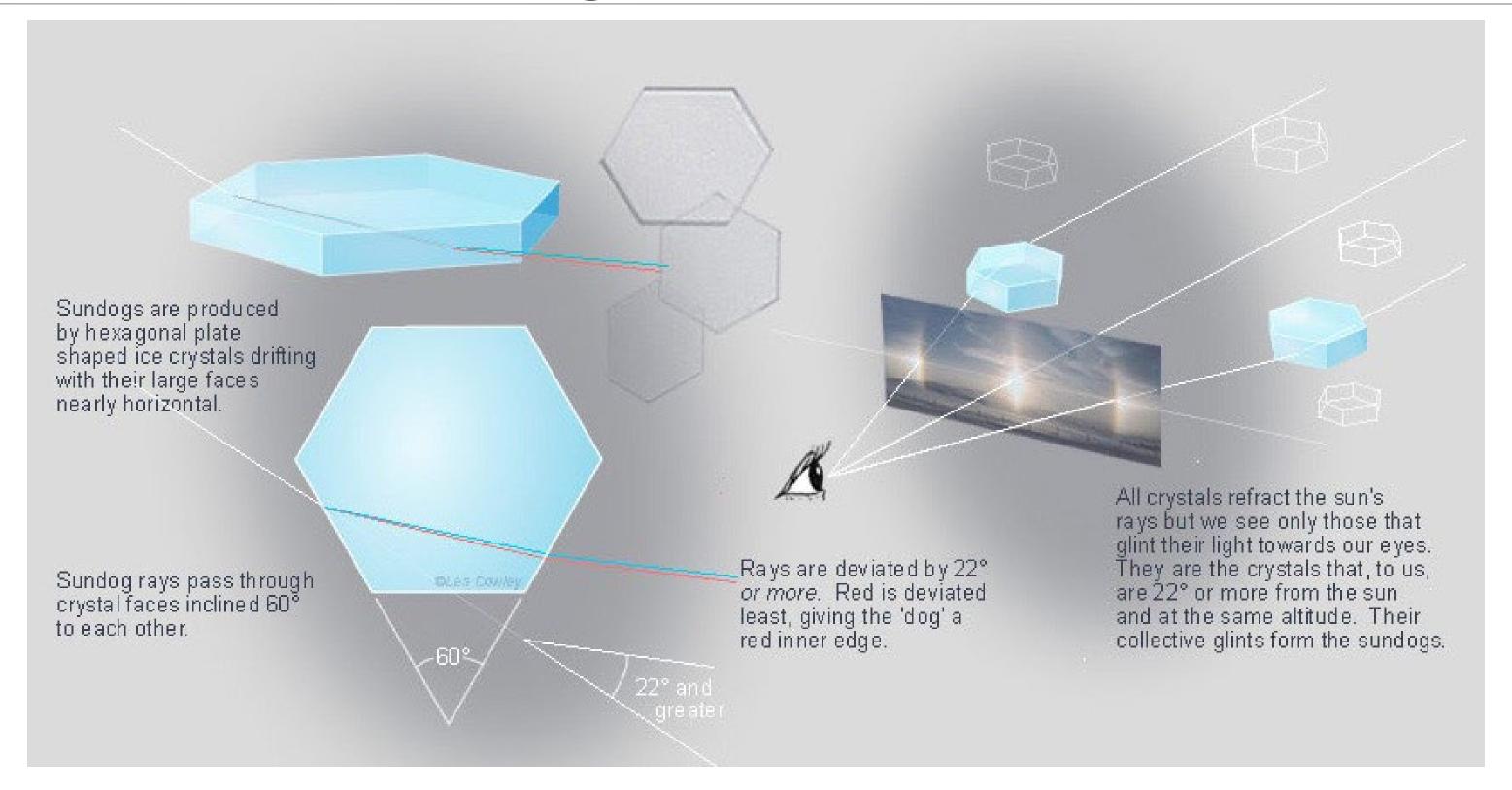


Dispersion: "Halos" and "Sun dogs"



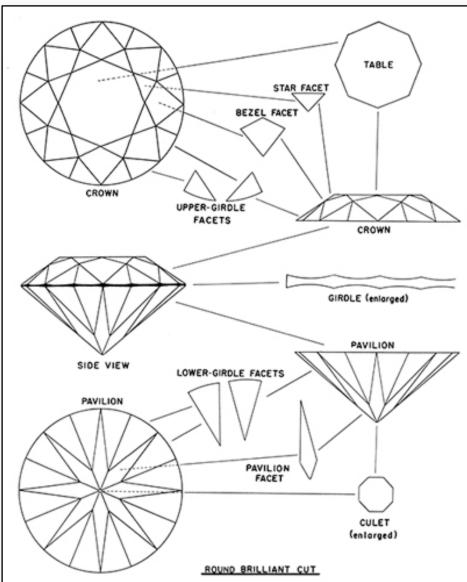


Halos and Sundogs

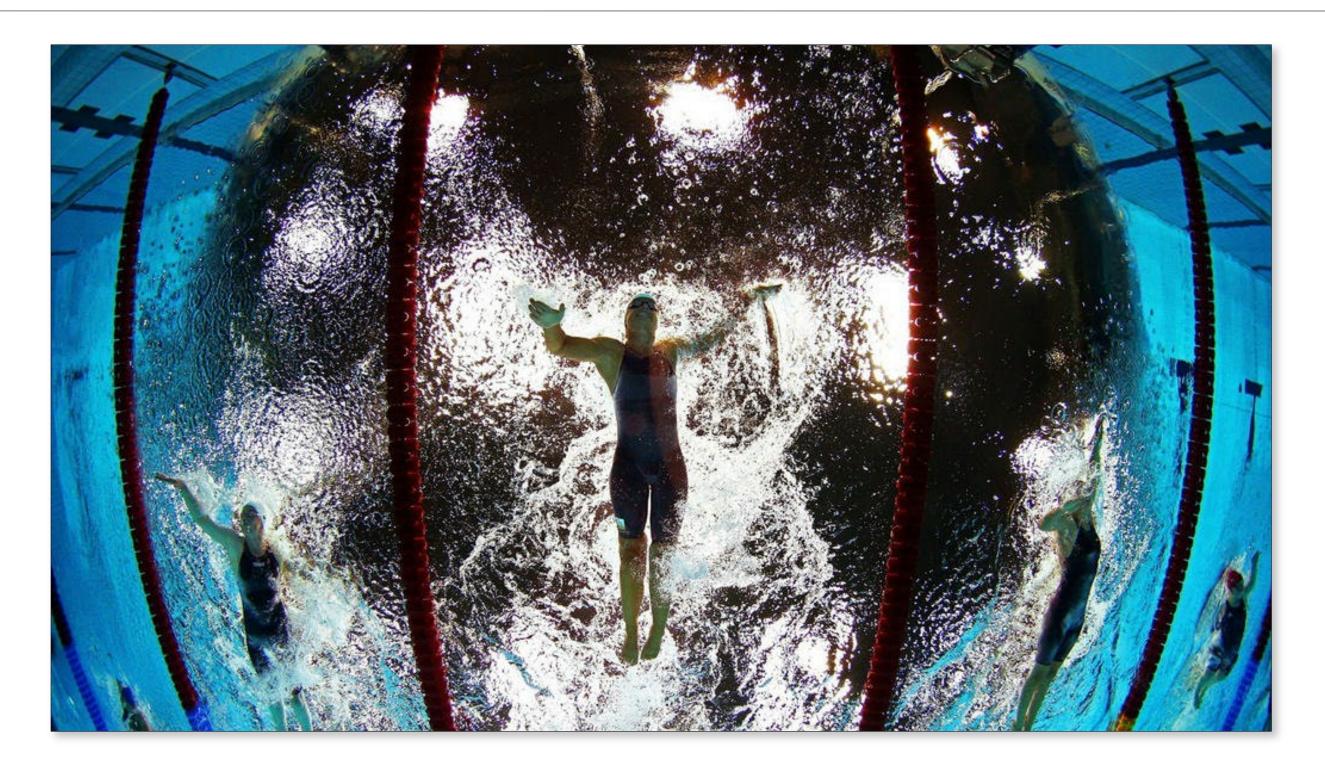


Dispersion





What is this dark circle?

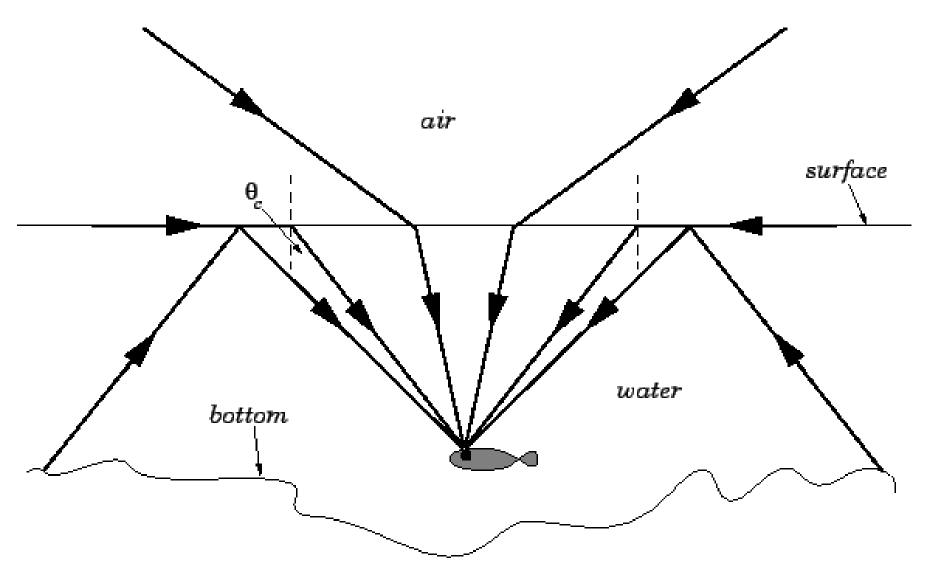


What is this dark circle?

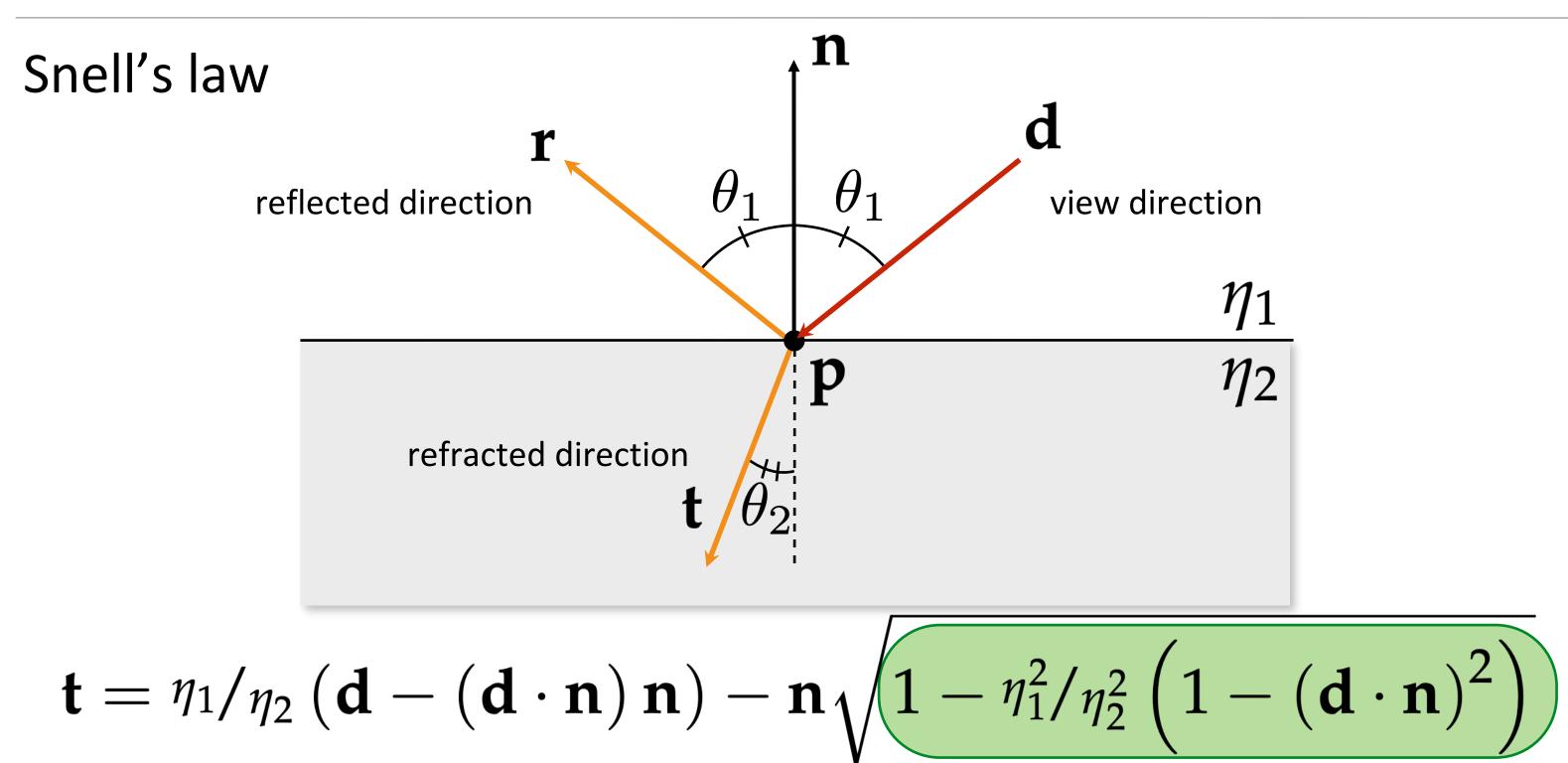


Called "Snell's window"

Caused by total internal reflection

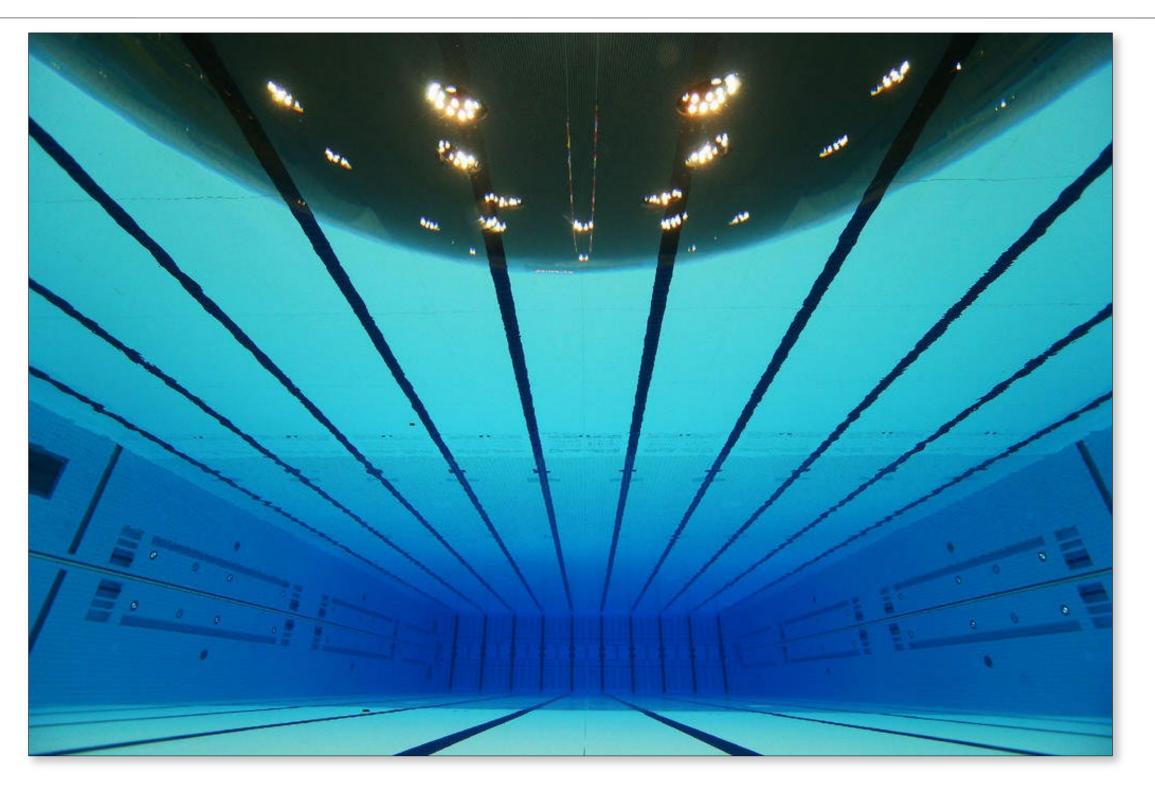


Recall...



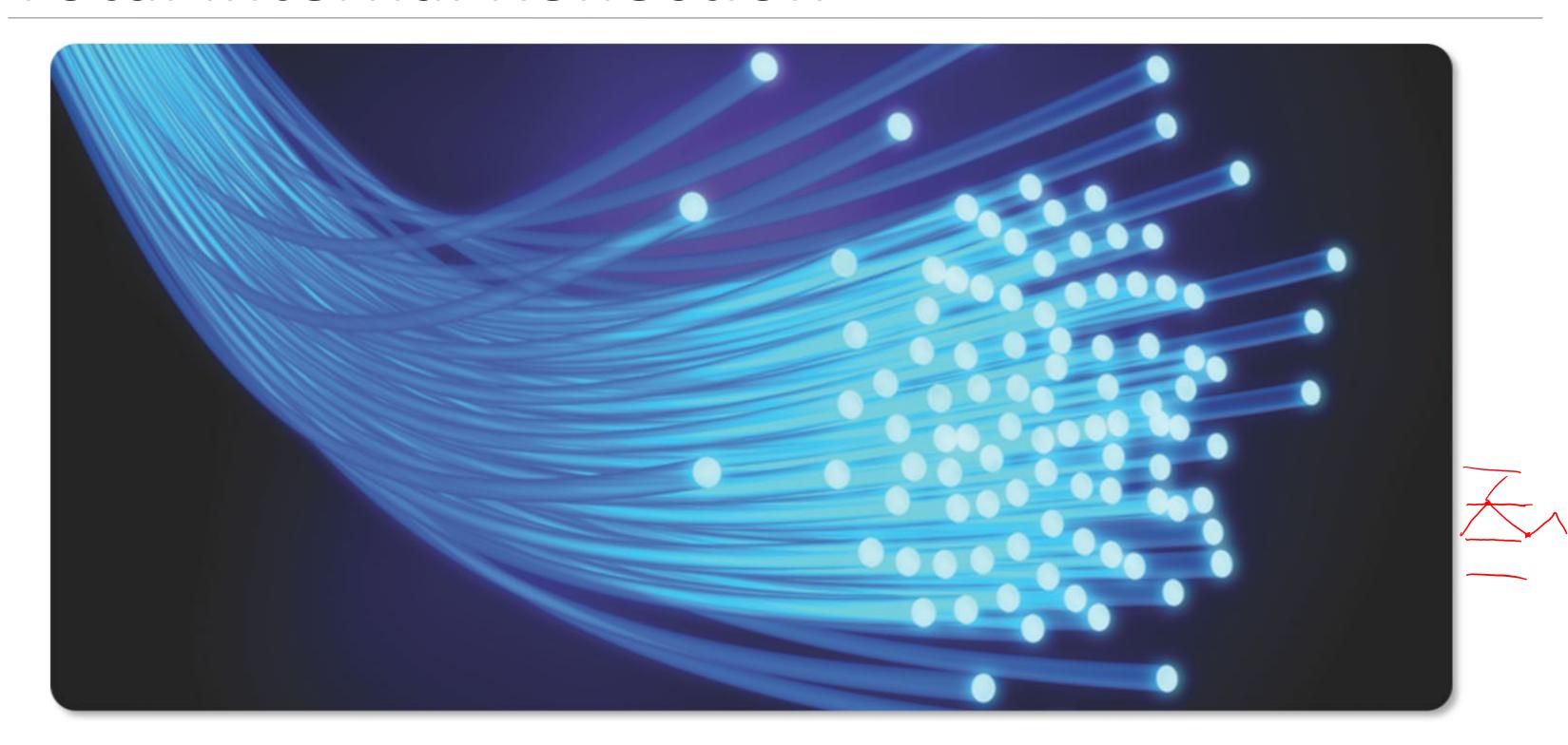
When can total internal reflection happen?

Can only happen when the ray starts in the higher index medium







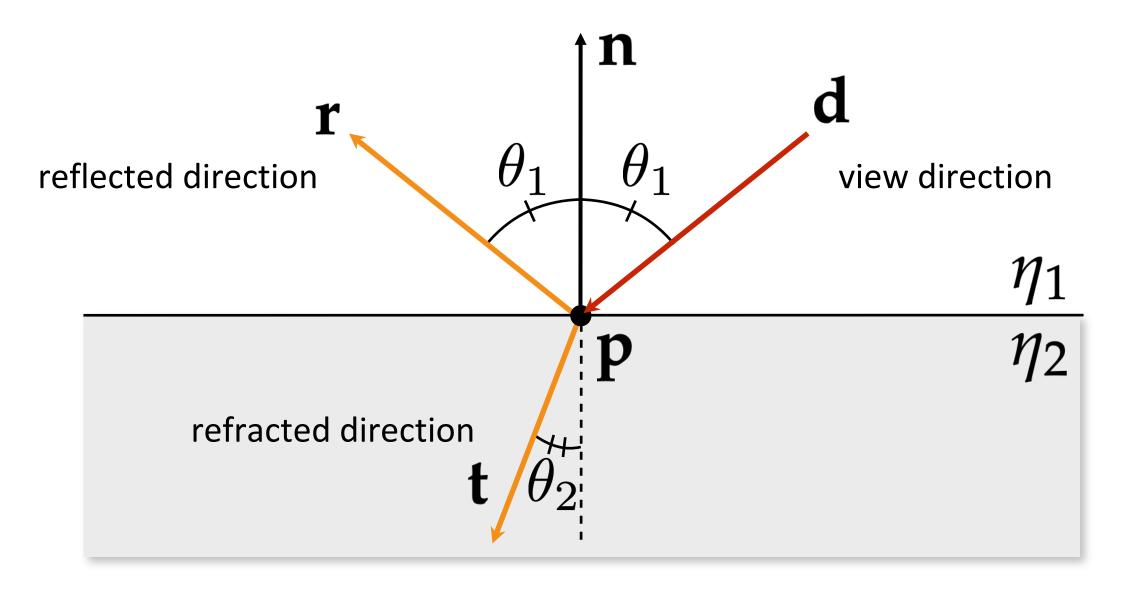




Reflection vs. Refraction

How much light is reflected vs. refracted?

- in reality determined by "Fresnel equations"



Fresnel Equations

Reflection and refraction from smooth dielectric (e.g. glass) surfaces

Reflection from conducting (e.g. metal) surfaces

Derived from Maxwell equations

Involves polarization of the wave

Fresnel Equations for Dielectrics

Reflection of light polarized parallel and perpendicular to the plane of refraction

$$\begin{split} \rho_{||} &= \frac{\eta_2 \cos \theta_1 - \eta_1 \cos \theta_2}{\eta_2 \cos \theta_1 + \eta_1 \cos \theta_2} \qquad \text{reflected:} \quad F_r = \frac{1}{2} \left(\rho_{||}^2 + \rho_{\perp}^2 \right) \\ \rho_{\perp} &= \frac{\eta_1 \cos \theta_1 - \eta_2 \cos \theta_2}{\eta_1 \cos \theta_1 + \eta_2 \cos \theta_2} \qquad \text{refracted:} \quad F_t = 1 - F_r \end{split}$$

What's happening in this photo?



Polarizing Filter



Polarization



Without Polarizer



With Polarizing Filter

Polarization



Without Polarizer

With Polarizing Filter

Effect of Polarization



Effect of Polarization



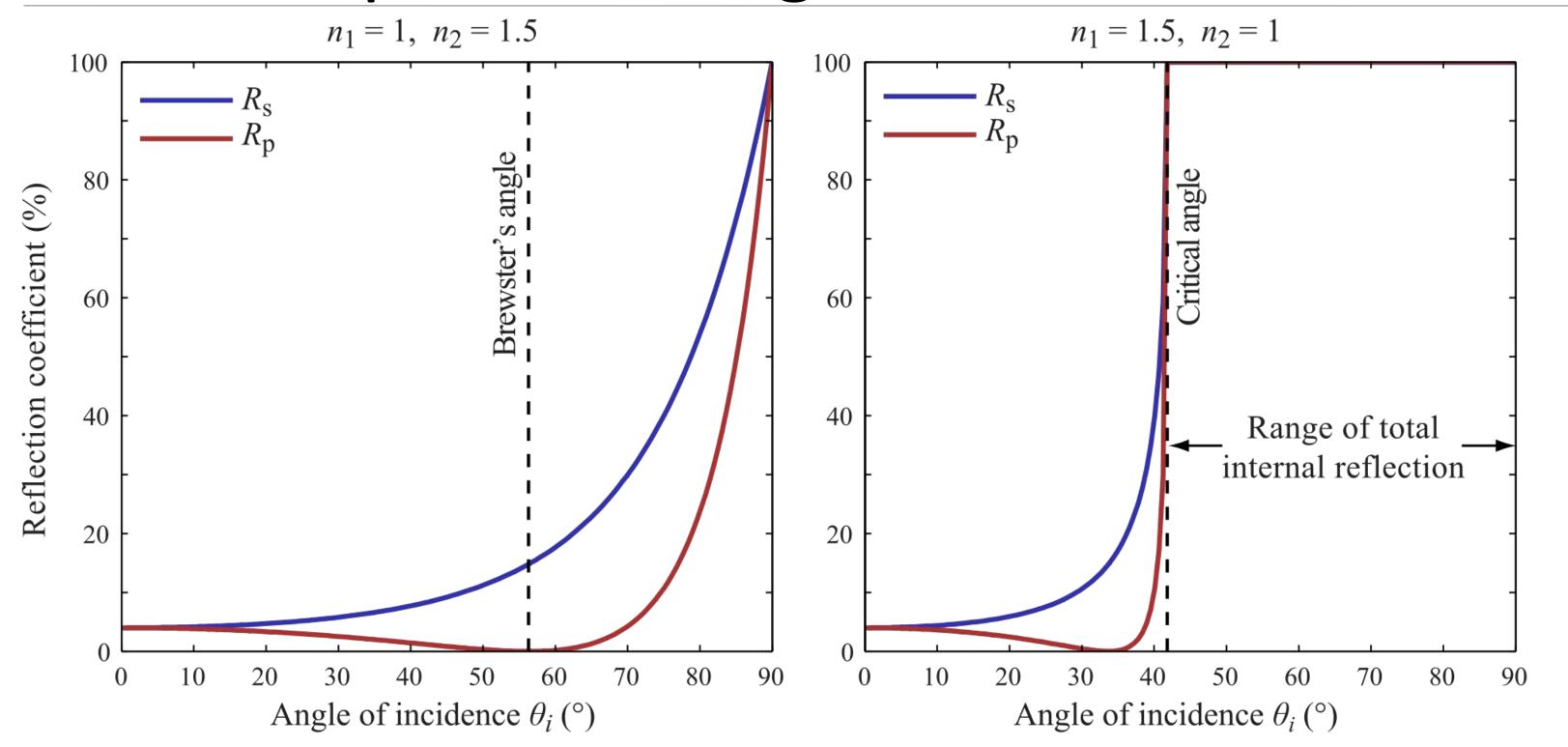
Fresnel Equations for Dielectrics

Reflection of light polarized parallel and perpendicular to the plane of refraction

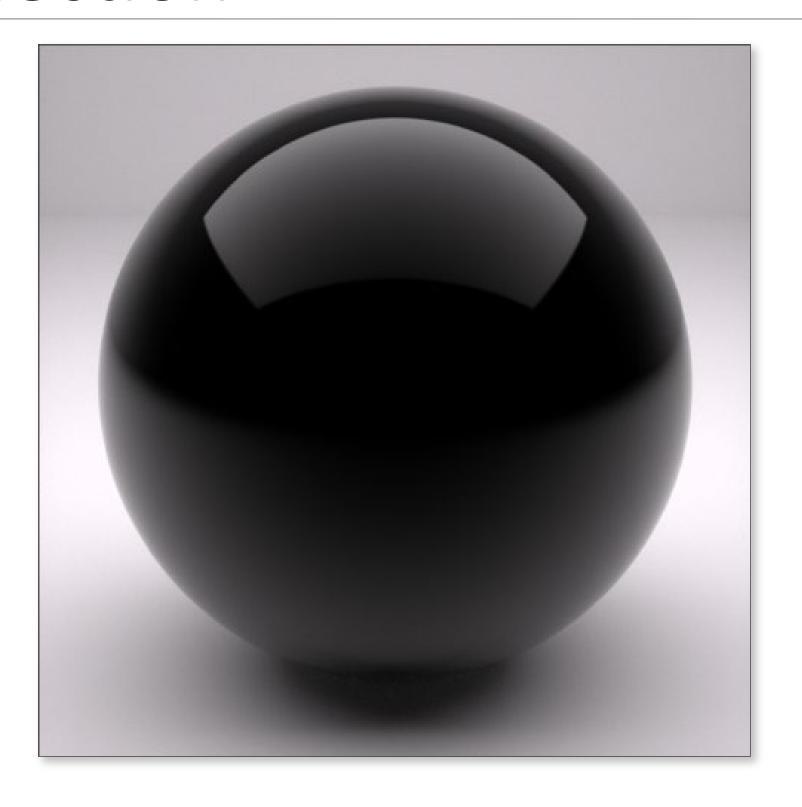
$$\begin{split} \rho_{||} &= \frac{\eta_2 \cos \theta_1 - \eta_1 \cos \theta_2}{\eta_2 \cos \theta_1 + \eta_1 \cos \theta_2} \qquad \text{reflected:} \quad F_r = \frac{1}{2} \left(\rho_{||}^2 + \rho_{\perp}^2 \right) \\ \rho_{\perp} &= \frac{\eta_1 \cos \theta_1 - \eta_2 \cos \theta_2}{\eta_1 \cos \theta_1 + \eta_2 \cos \theta_2} \qquad \text{refracted:} \quad F_t = 1 - F_r \end{split}$$

- The Shirley book uses a faster approximation (Schlick), but to get full accuracy you'd need to use these equations

Fresnel equations for glass

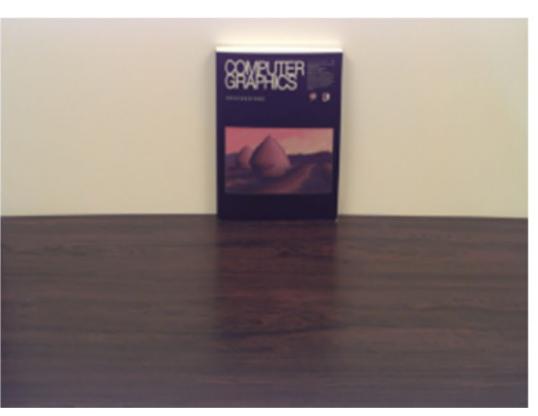


Fresnel reflection



Fresnel reflection/refraction

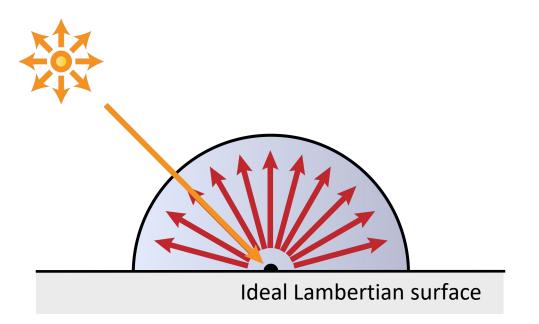




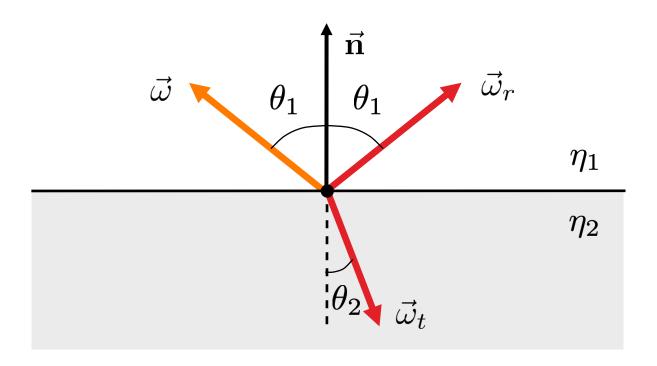


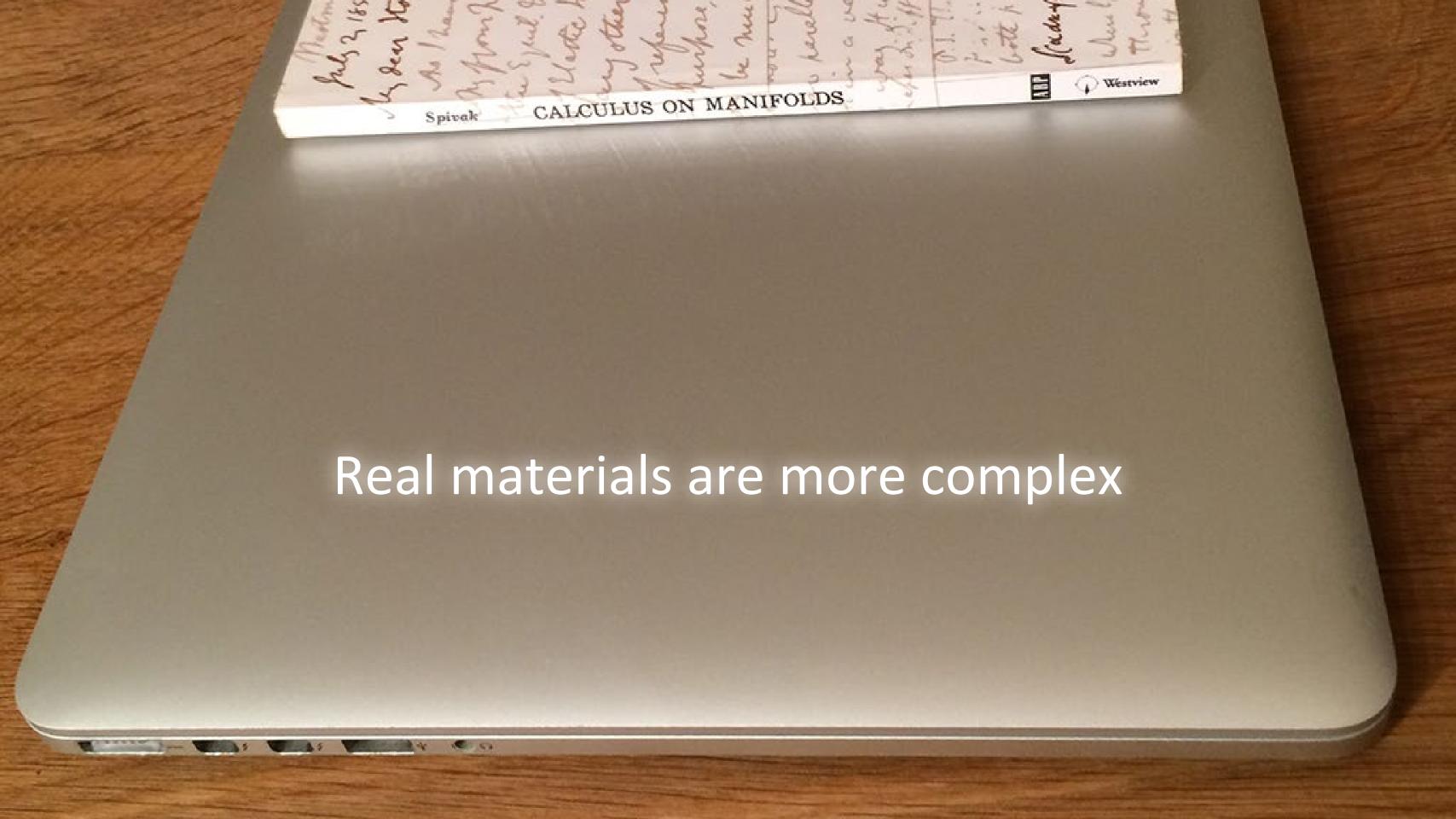
So Far: Idealized BRDF Models

Diffuse



Specular Reflection and Refraction





Rough materials

In reality, most materials are neither perfectly diffuse nor specular, but somewhere in between

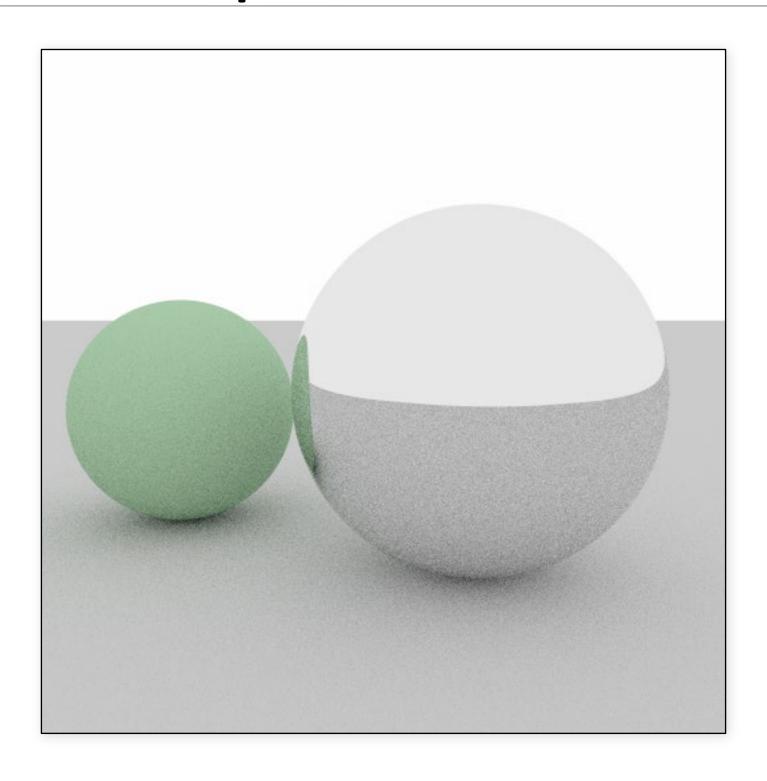
- Imagine a shiny surface scratched up at a microscopic level

We will look at a more principled way to handle this later.

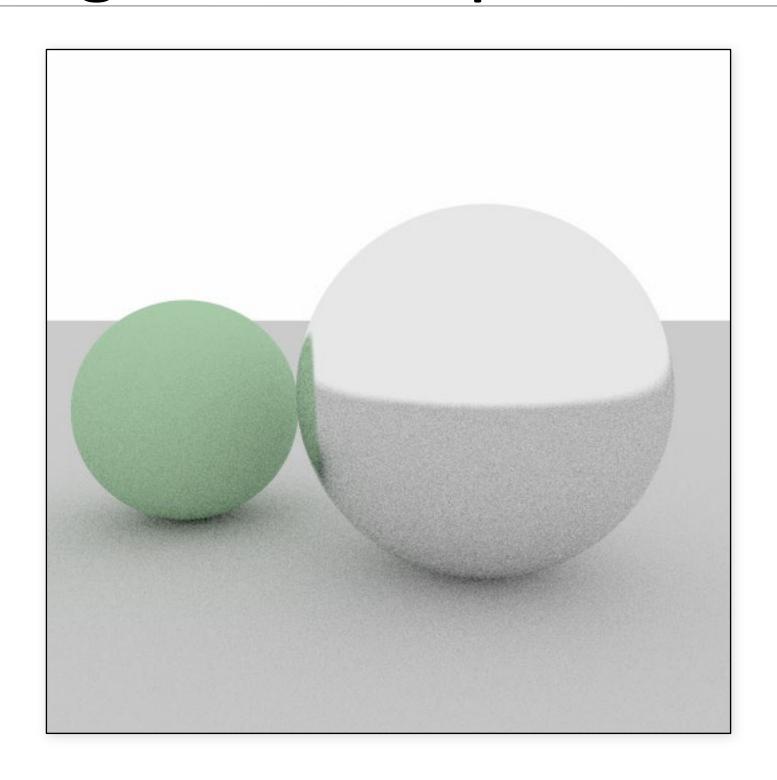
For now, we can easily approximate one important characteristic: blurred reflections

- Compute reflection direction, then add a random offset to it
- Sample random offset from sphere. Scale it to increase/decrease fuzziness

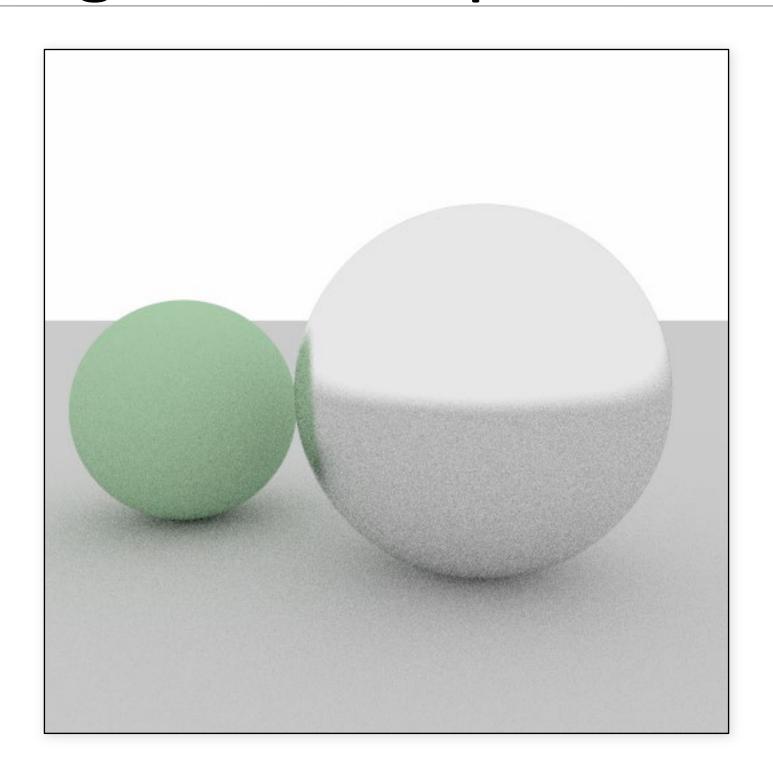
Diffuse & mirror spheres



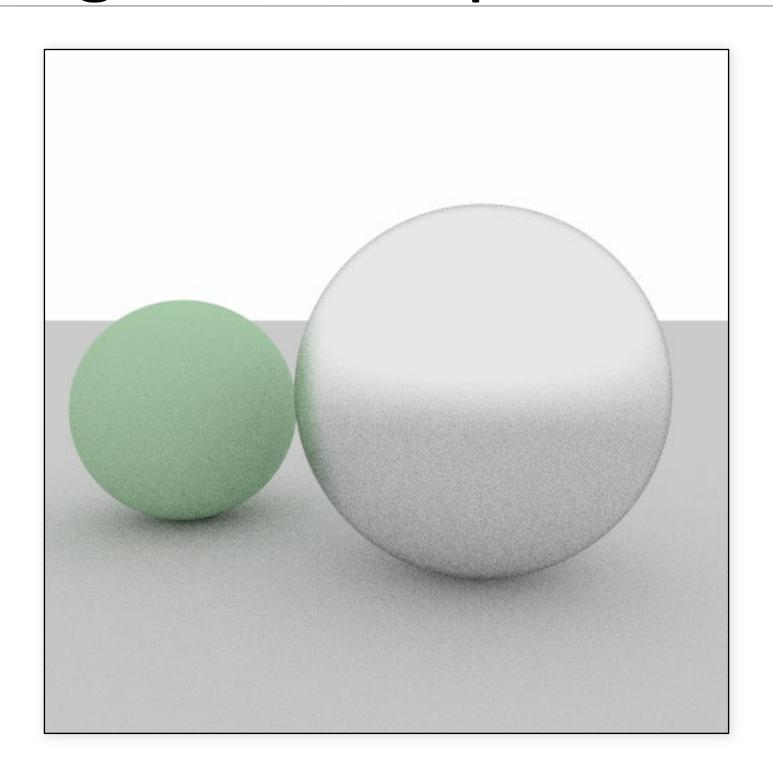
Diffuse & rough mirror spheres



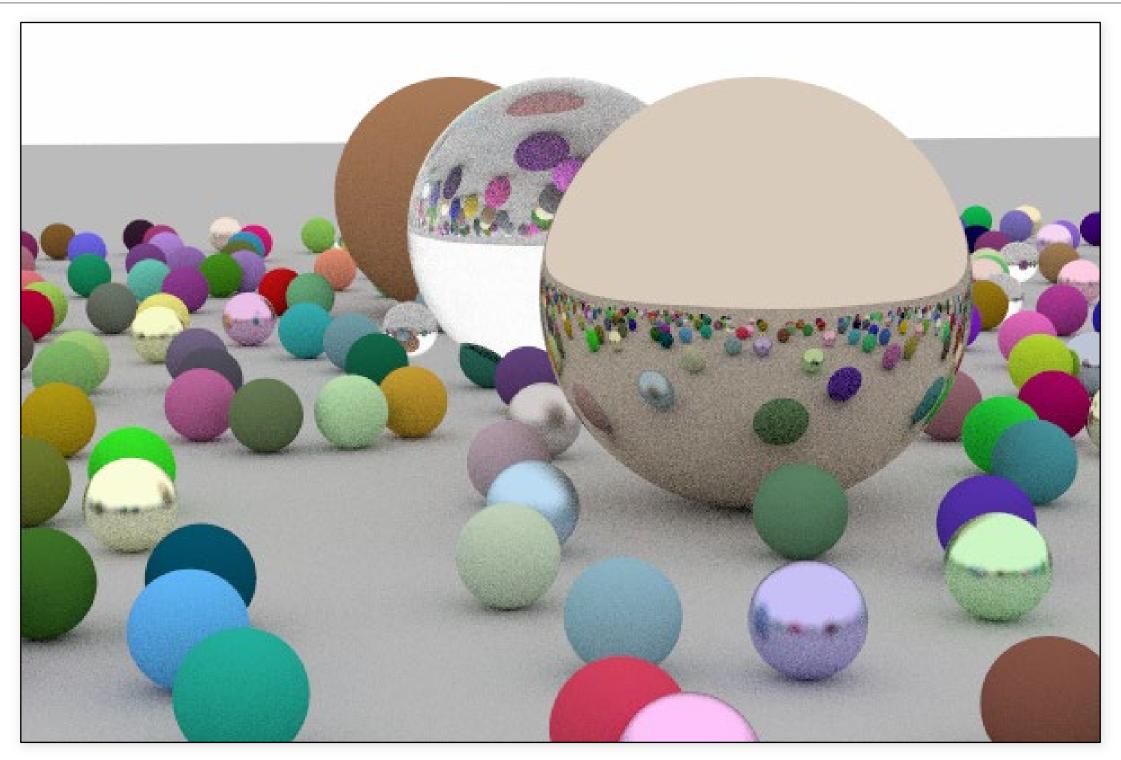
Diffuse & rough mirror spheres



Diffuse & rough mirror spheres



Putting it together



Lighting

Lighting

So far, the sky or background has been the only source of emitted light

But we can easily make any surface a light source!

- Just return an emitted color when a ray hits that surface
- Add a function to material that returns emitted color
 - Returns black (all zeros) for regular (non-emissive) surfaces
 - Color will often be greater than (1,1,1)
- Also possible for surfaces to emit & scatter (but not common)

Pseudo-code

```
Scene::trace(Ray ray)
   hit = surfaces.intersect(ray);
   if hit
      [col, sRay] = hit->mat->scatter(ray)
      return col * trace(sRay);
   else
      return backgroundColor;
```

Pseudo-code

```
Scene::trace(Ray ray)
   hit = surfaces.intersect(ray);
   if hit
      emit = hit->mat->emit(ray)
      [col, sRay] = hit->mat->scatter(ray)
      return emit + col * trace(sRay);
   else
      return backgroundColor;
```

