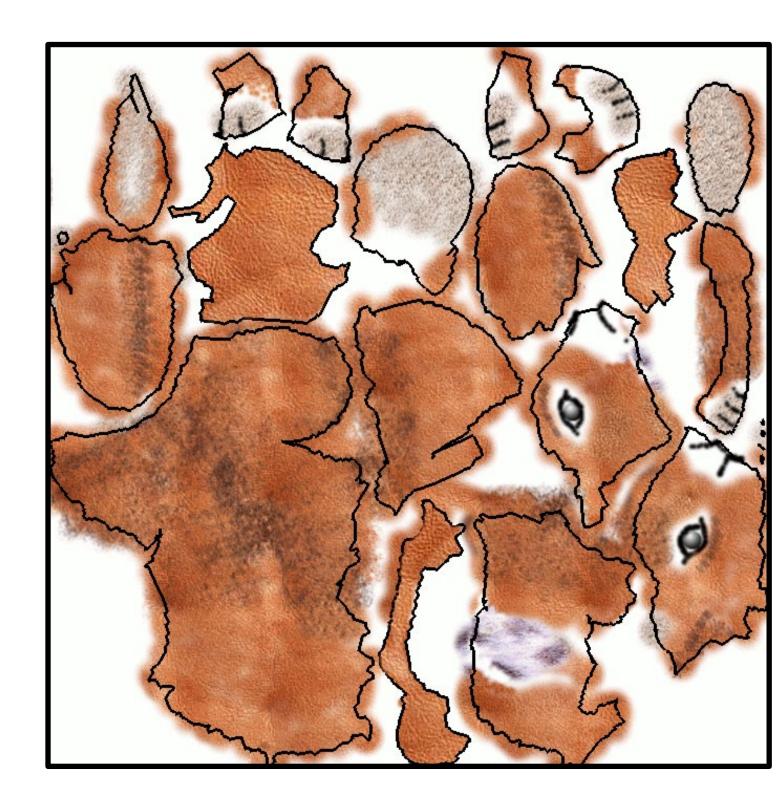
Texture mapping



http://graphics.cs.cmu.edu/courses/15-468



15-468, 15-668, 15-868 Physics-based Rendering Spring 2021, Lecture 4

Course announcements

- Take-home quiz 1 posted, due Wednesday 2/17 at 23:59.
 We will be switching to the Tuesday schedule starting with take-home quiz 2.
 Make sure to re-download if you downloaded before 8 am today.
- Take-home quiz 2 will be posted tonight, due next Tuesday at 23:59.
- Programming assignment 1 posted, due Friday 2/26 at 23:59. - How many of you have looked at/started/finished it? - Any questions?

Overview of today's lecture

- lacksquare
- Texture mapping.

Leftover from previous lecture: Specular reflection, specular refraction, lighting.

Slide credits

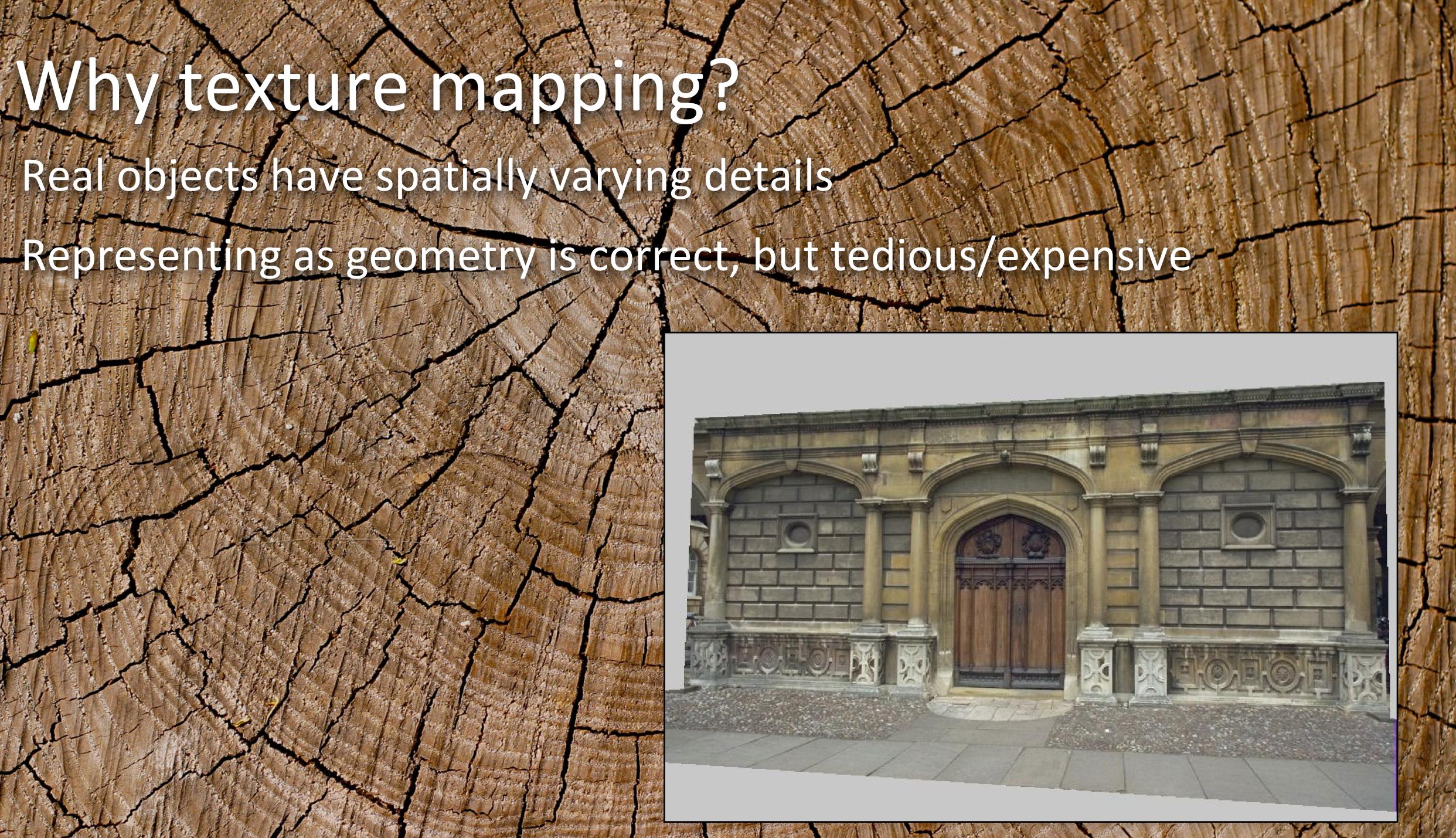
Most of these slides were directly adapted from:

• Wojciech Jarosz (Dartmouth).

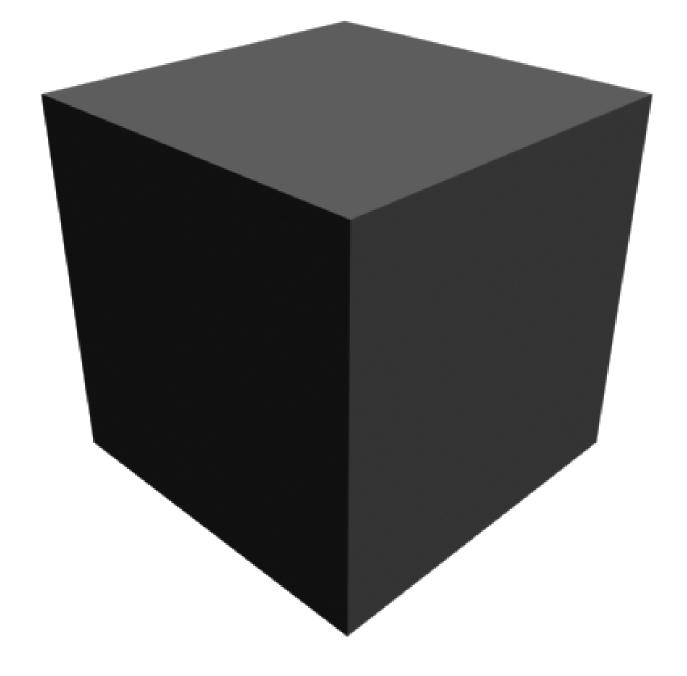


Why fexture mapping?

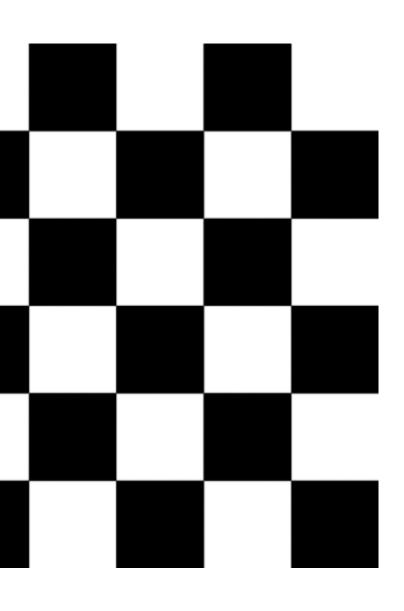
Real objects have spatially varying details

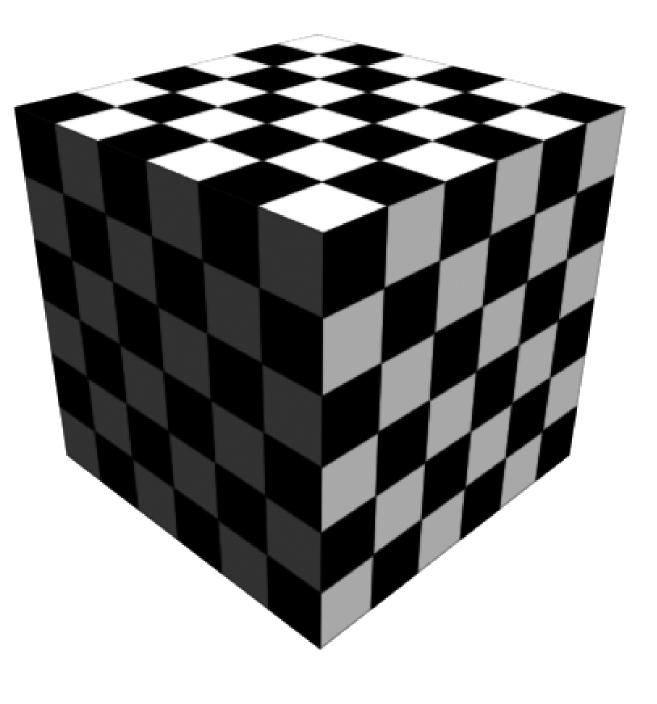


Why texture mapping? Use simple geometry Store varying properties in images Map to objects



Proposed by Ed Catmull in the 70s

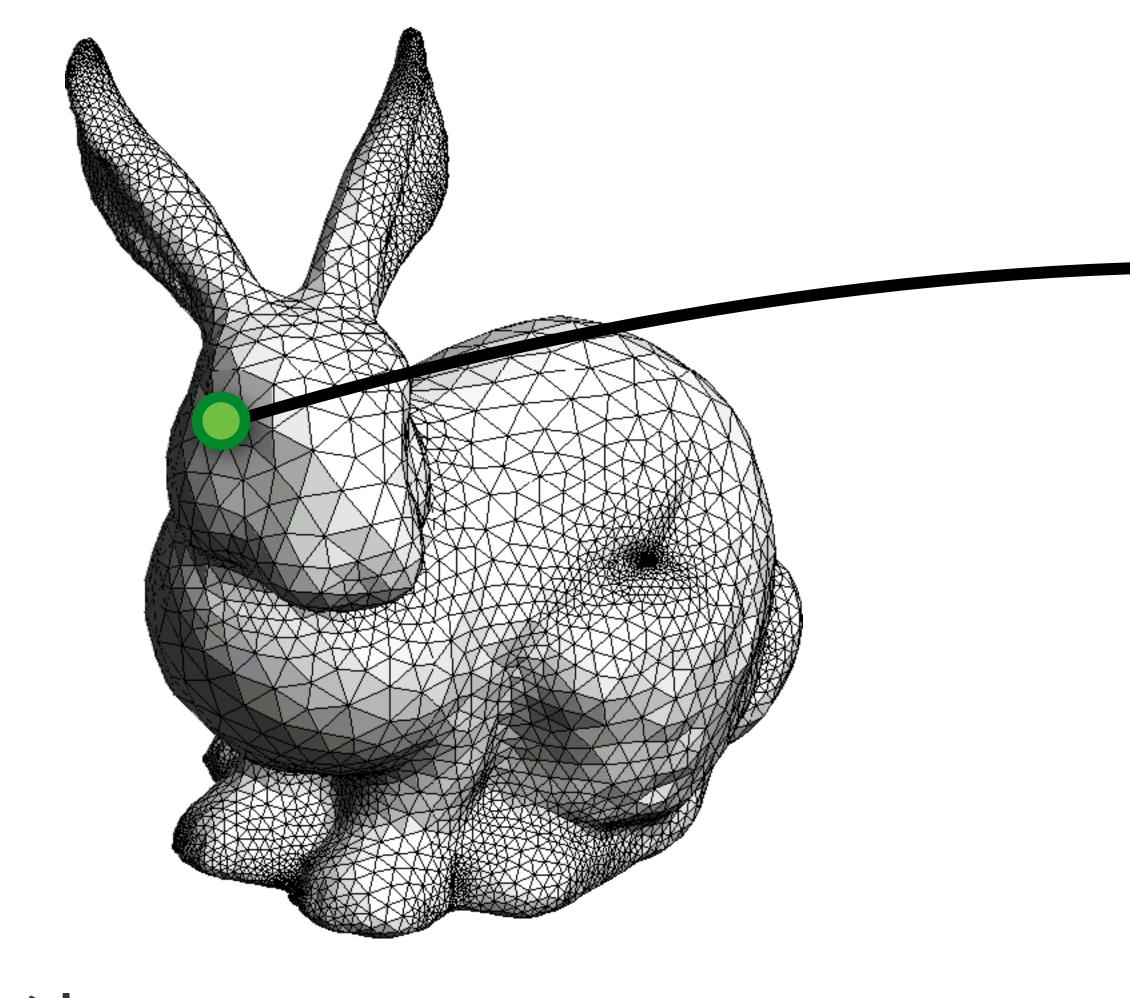




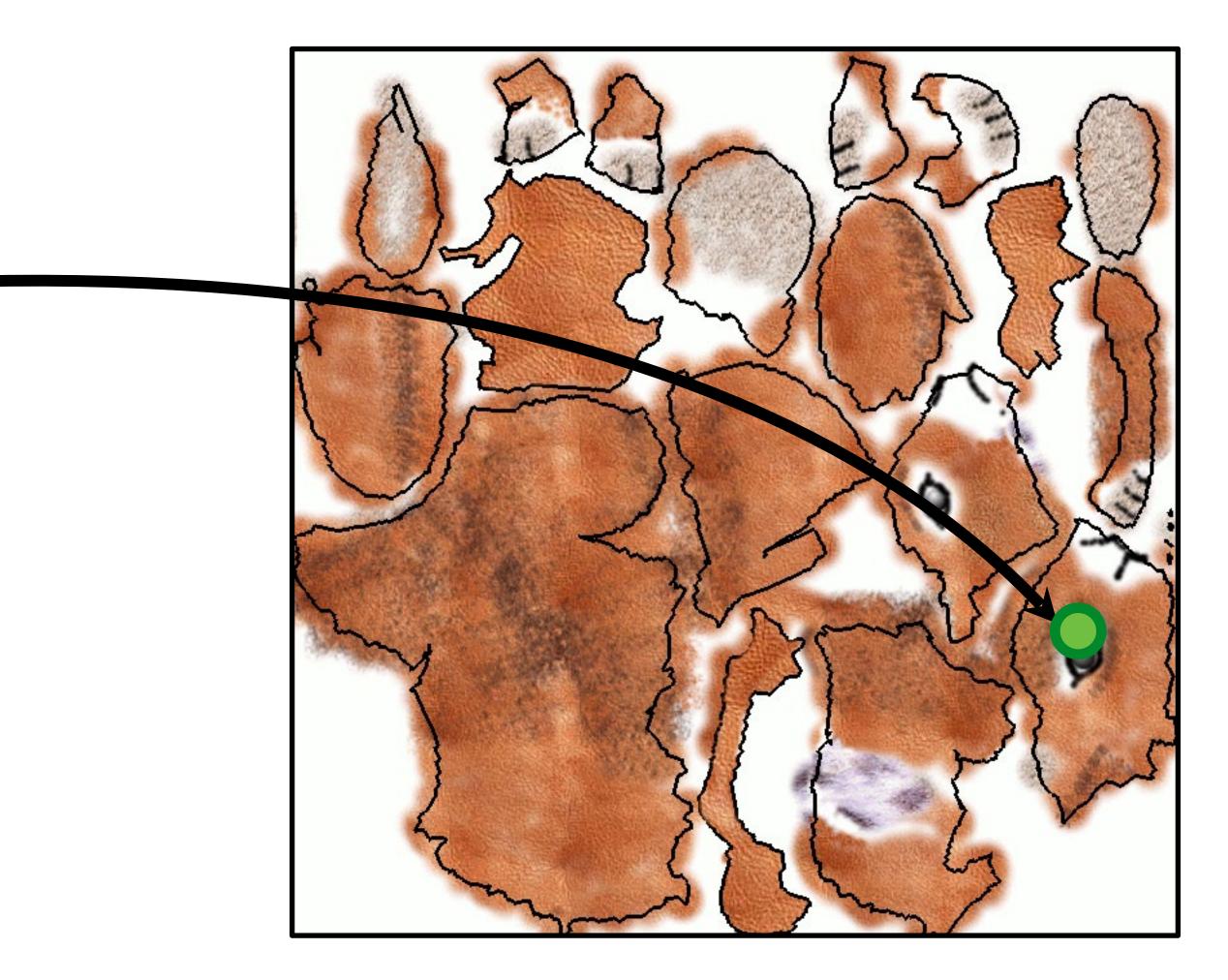




Mapping between the surface and the image



Panozzo Daniele lide by After a s ▼ € !

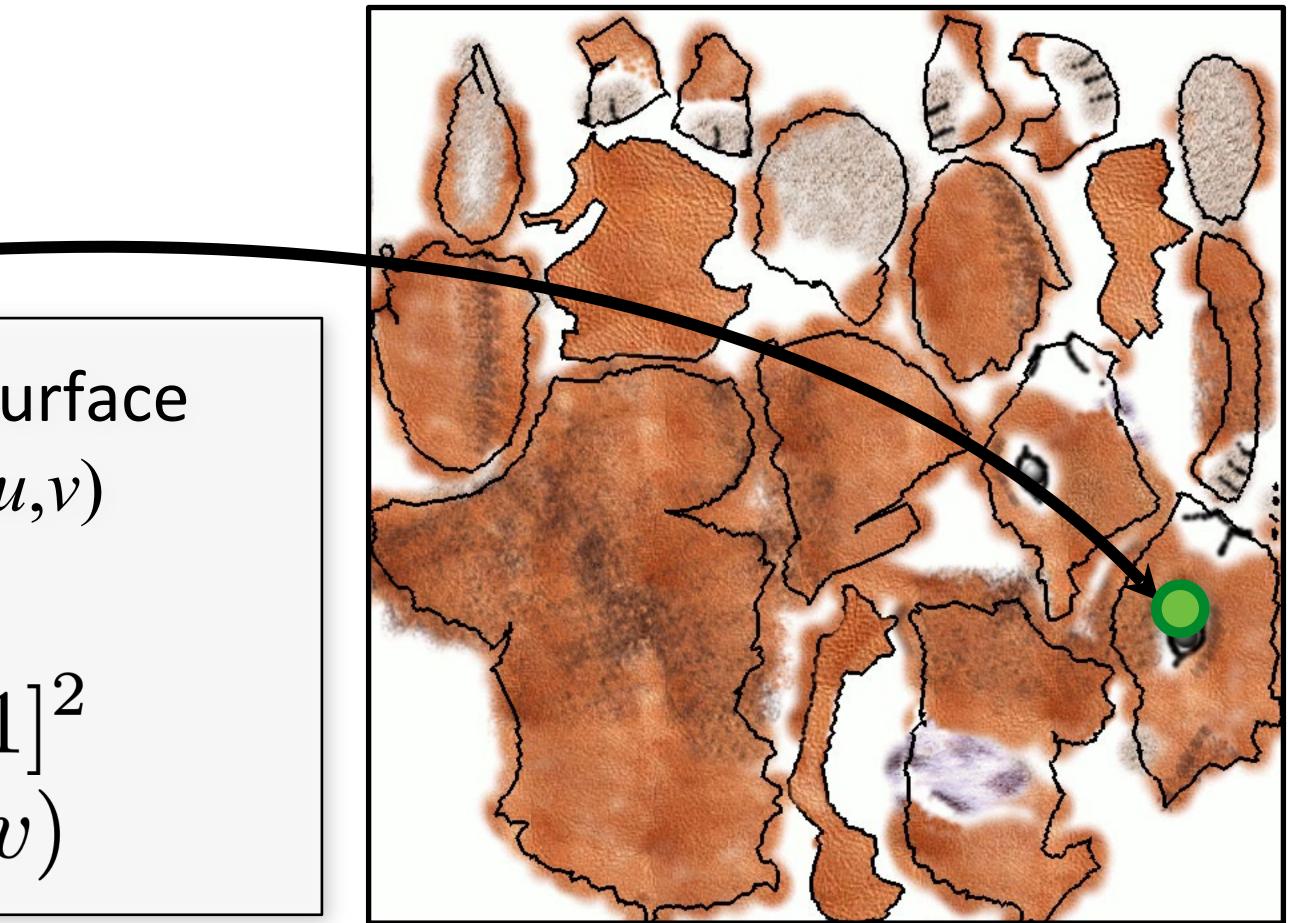




Mapping between the surface and the image

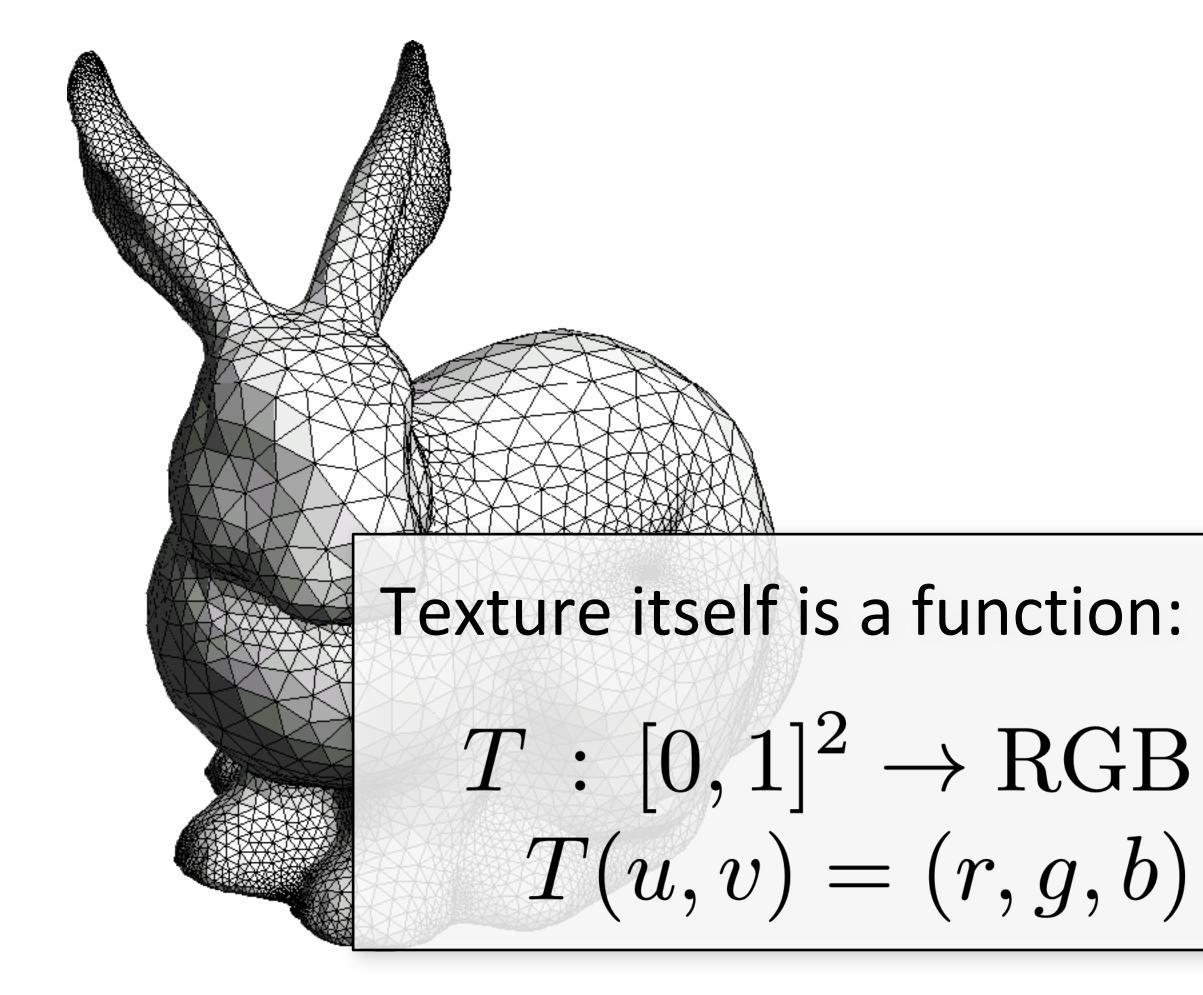
Each point (x,y,z) on the surface has mapped coordinates (u,v)in the texture image:

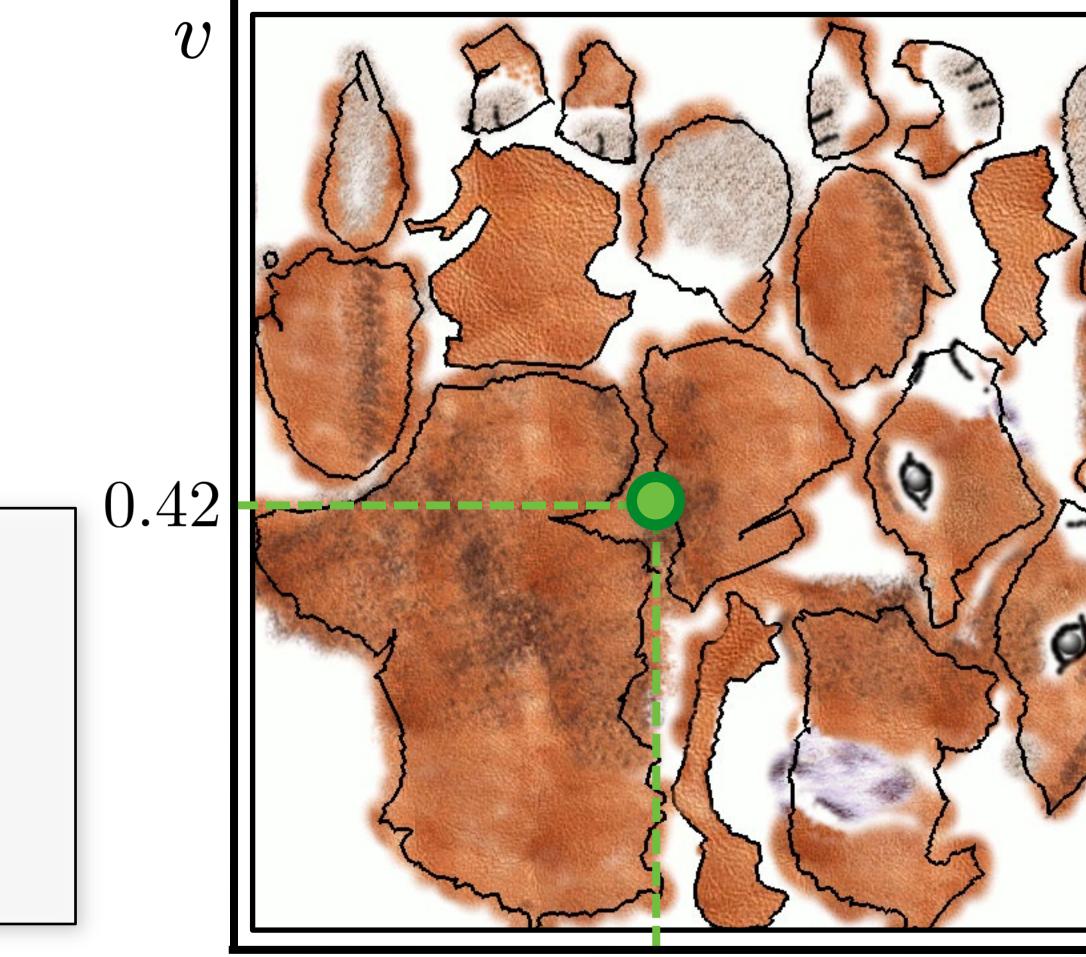
 $f: \mathbb{R}^3 \to [0,1]^2$ f(x, y, z) = (u, v)





Mapping between the surface and the image



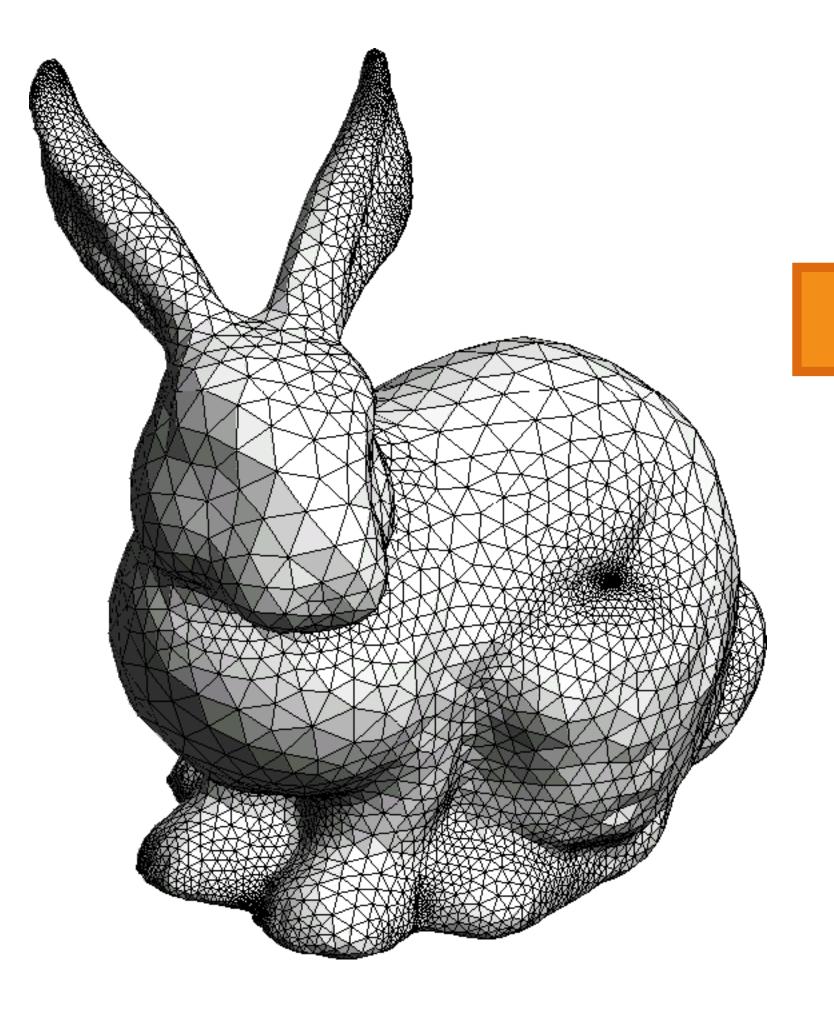


0.4



U

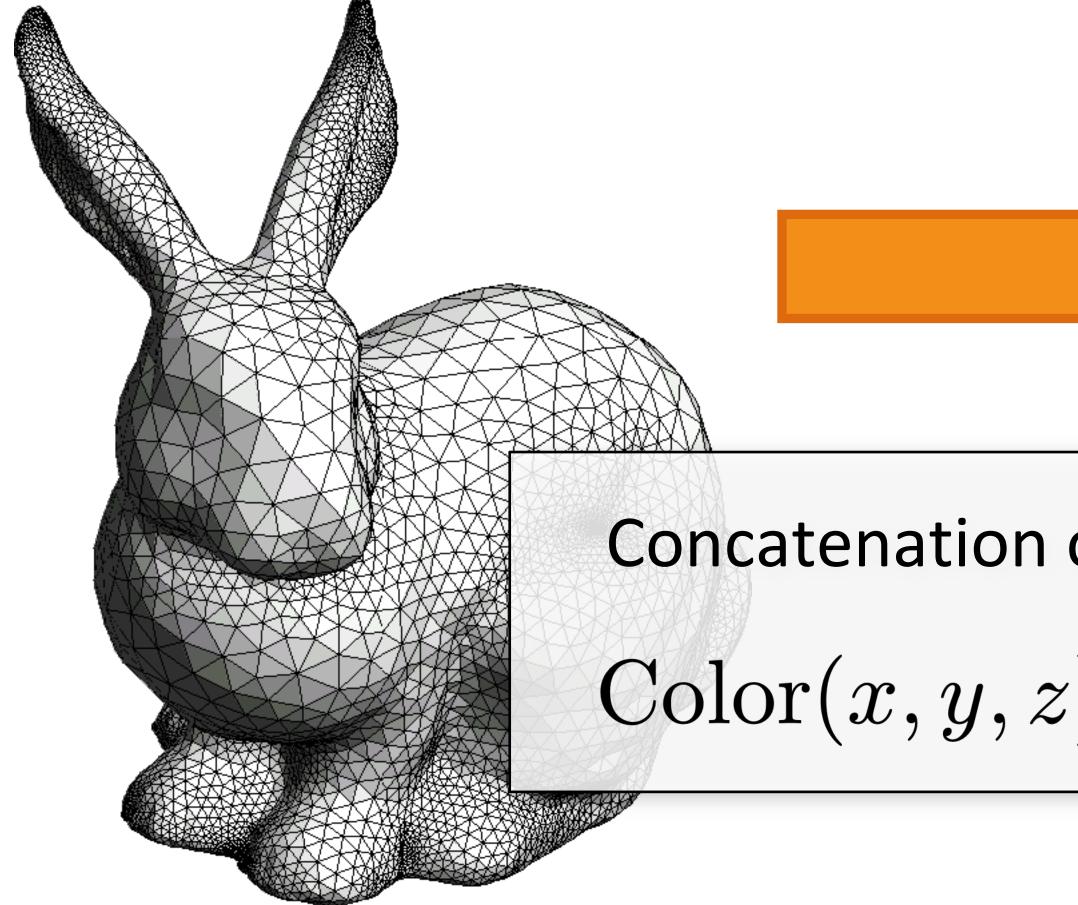
Mapping between the surface and the image







Mapping between the surface and the image



Concatenation of the two functions:

Color(x, y, z) = T(f(x, y, z))

Why texture mapping? Produces compelling results





Agenda

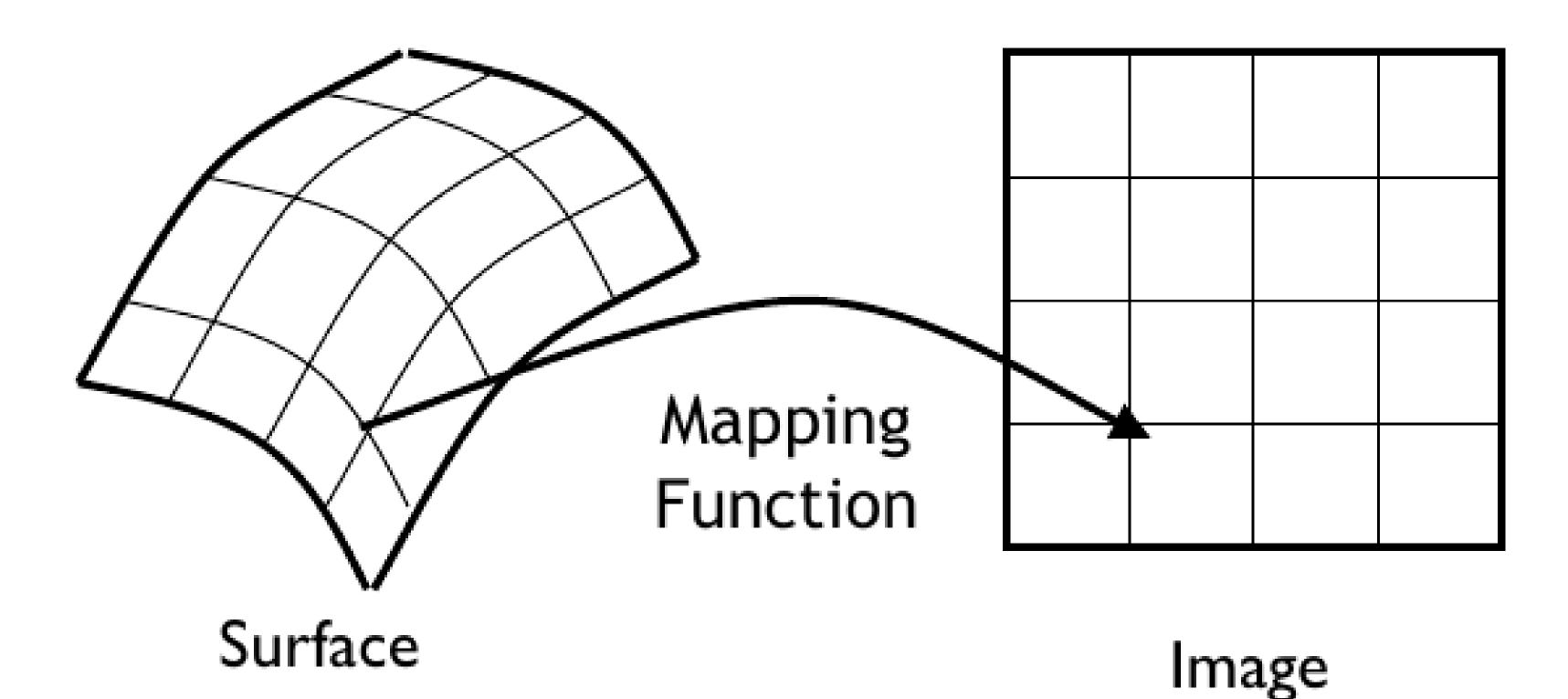
How do we map between surface and texture? What do we map onto the surface?



Surface parameterization

A surface in 3D is a two-dimensional thing

- How do we map a surface point to a point in a texture?
- Defining 2D coordinates is parameterizing the surface



Surface parameterization

A surface in 3D is a two-dimensional thing

How do we map a surface point to a point in a texture?

- Defining 2D coordinates is parameterizing the surface Examples:
- cartesian coordinates on a rectangle (or other planar shape) - cylindrical coordinates (θ, y) on a cylinder
- latitude and longitude on the Earth's surface
- spherical coordinates (θ , ϕ) on a sphere



Arectangle

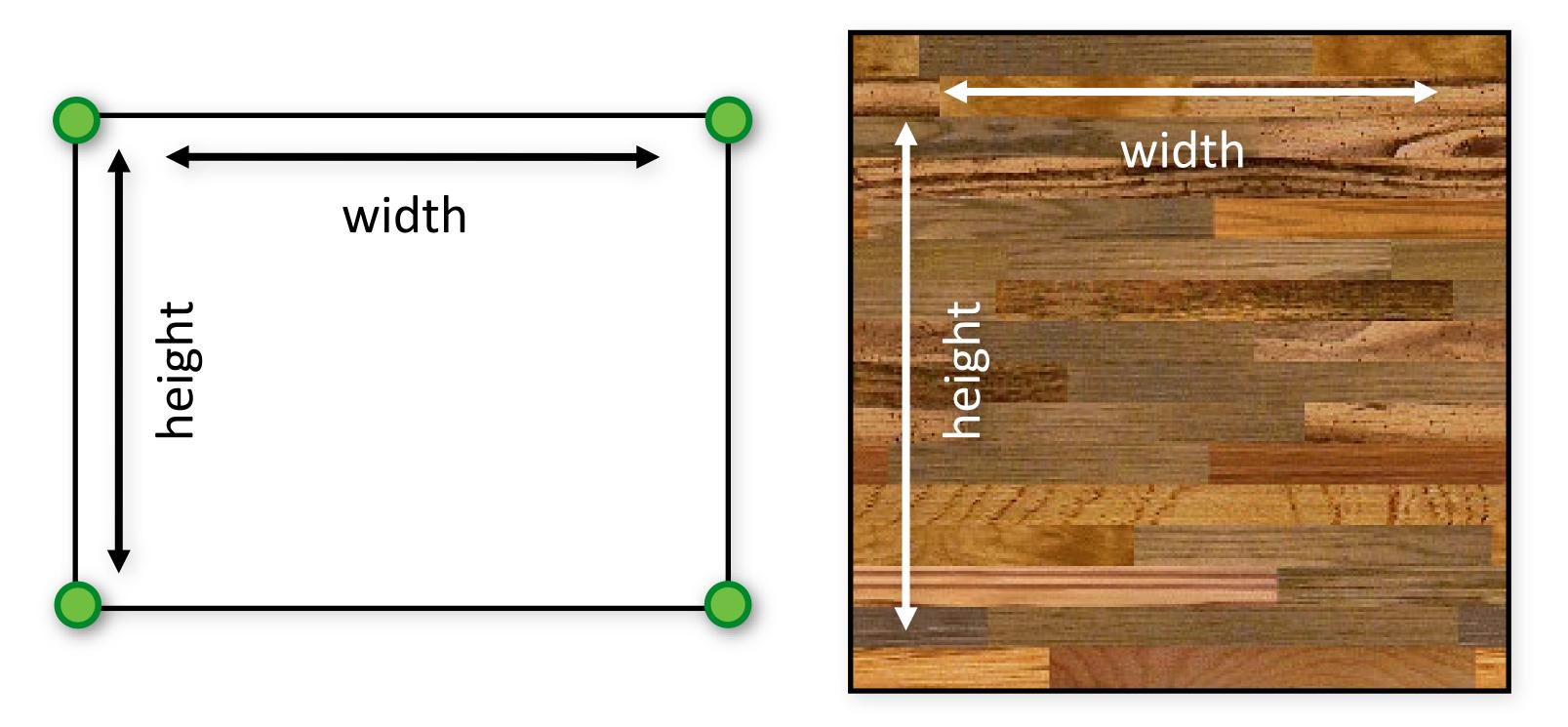
Image can be mapped directly, unchanged





Texturing a rectangle

Image can be mapped directly, unchanged



Object Space



Texture Space

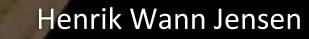
Object Space



A textured rectangle

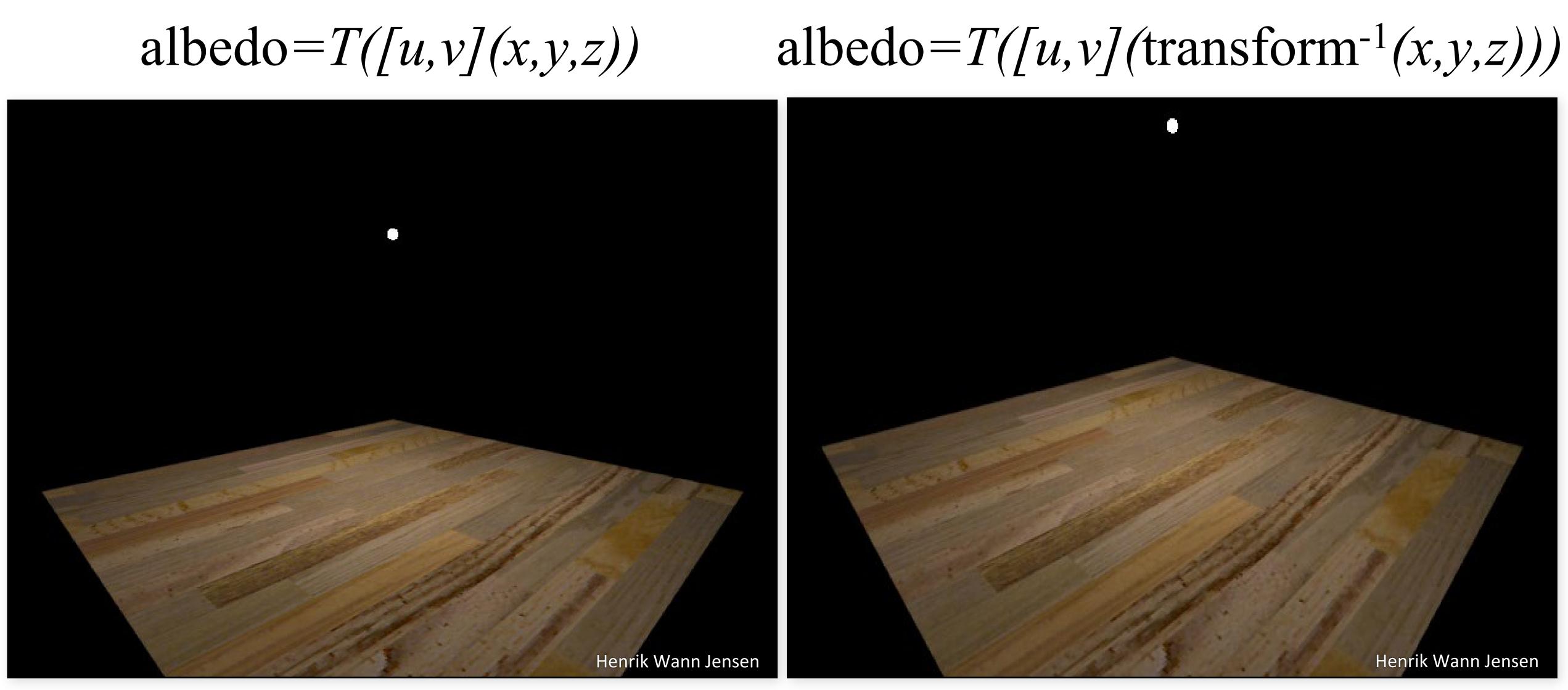
albedo = T(u,v)





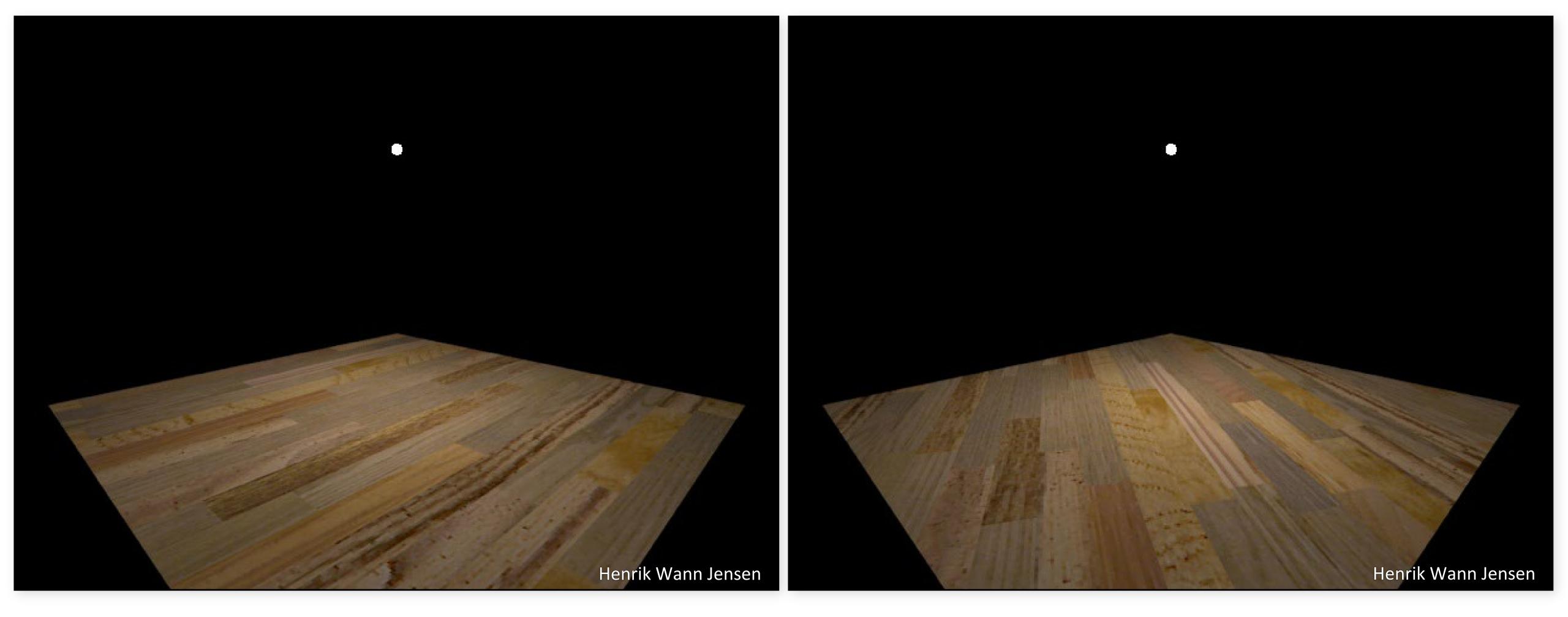


Transformation of shape



Transformation of texture

albedo=T([u,v](x,y,z))



albedo=T(transform[u,v](x,y,z))





What if the object is not rectangular?

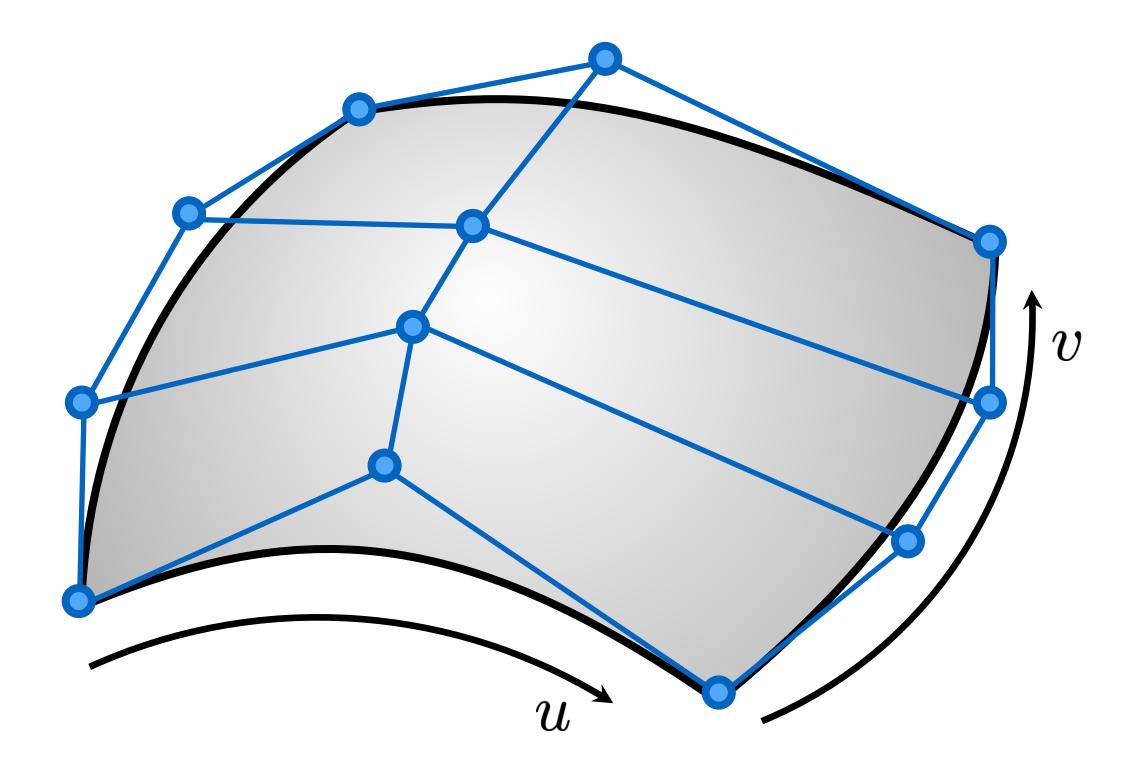
Need to determine mapping from 3D coordinates to 2D texture coordinates

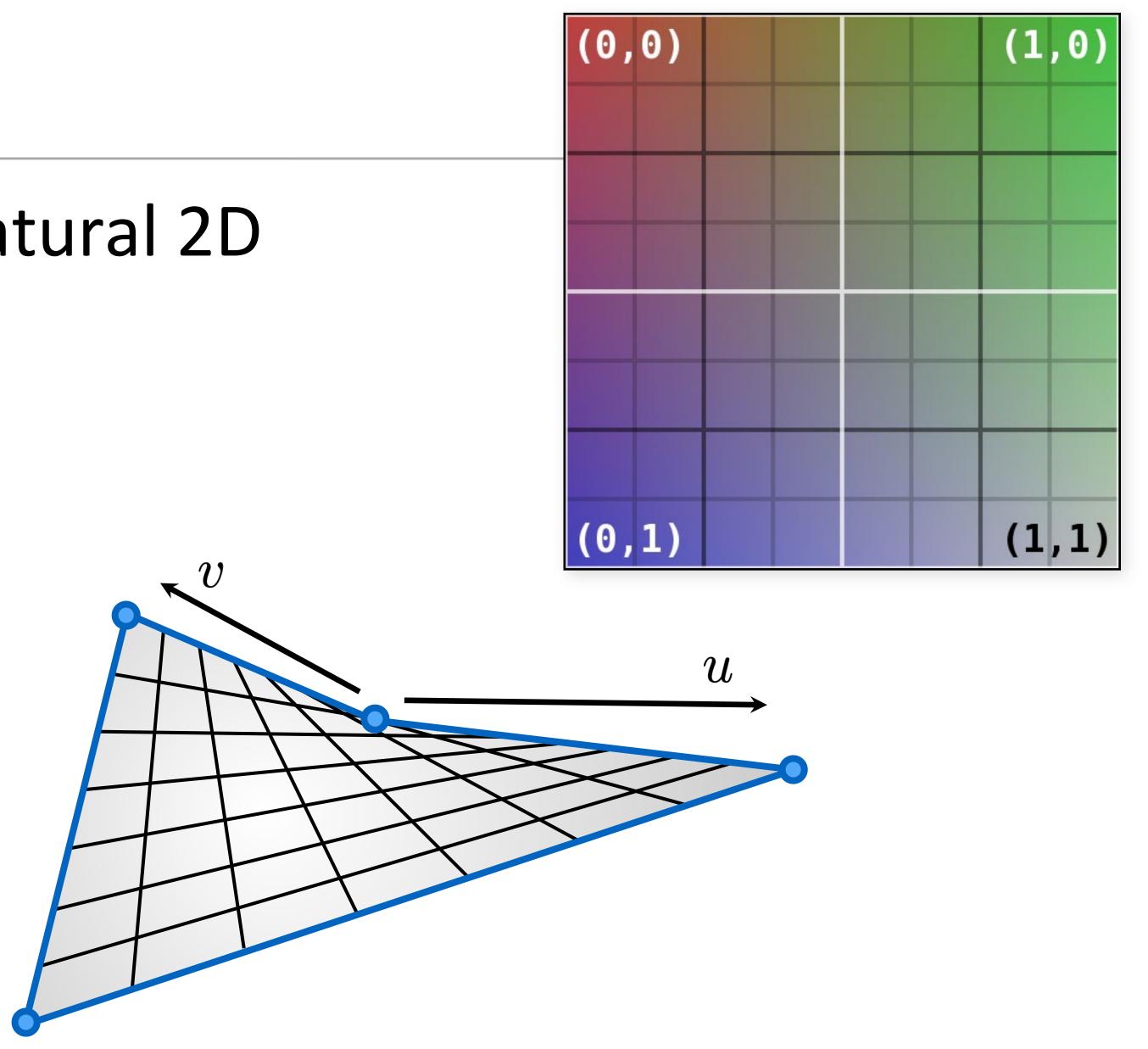
- Parametric surfaces
- Projection mapping
- UV mapping



Parametric surfaces

Parametric surfaces have a natural 2D coordinate system.



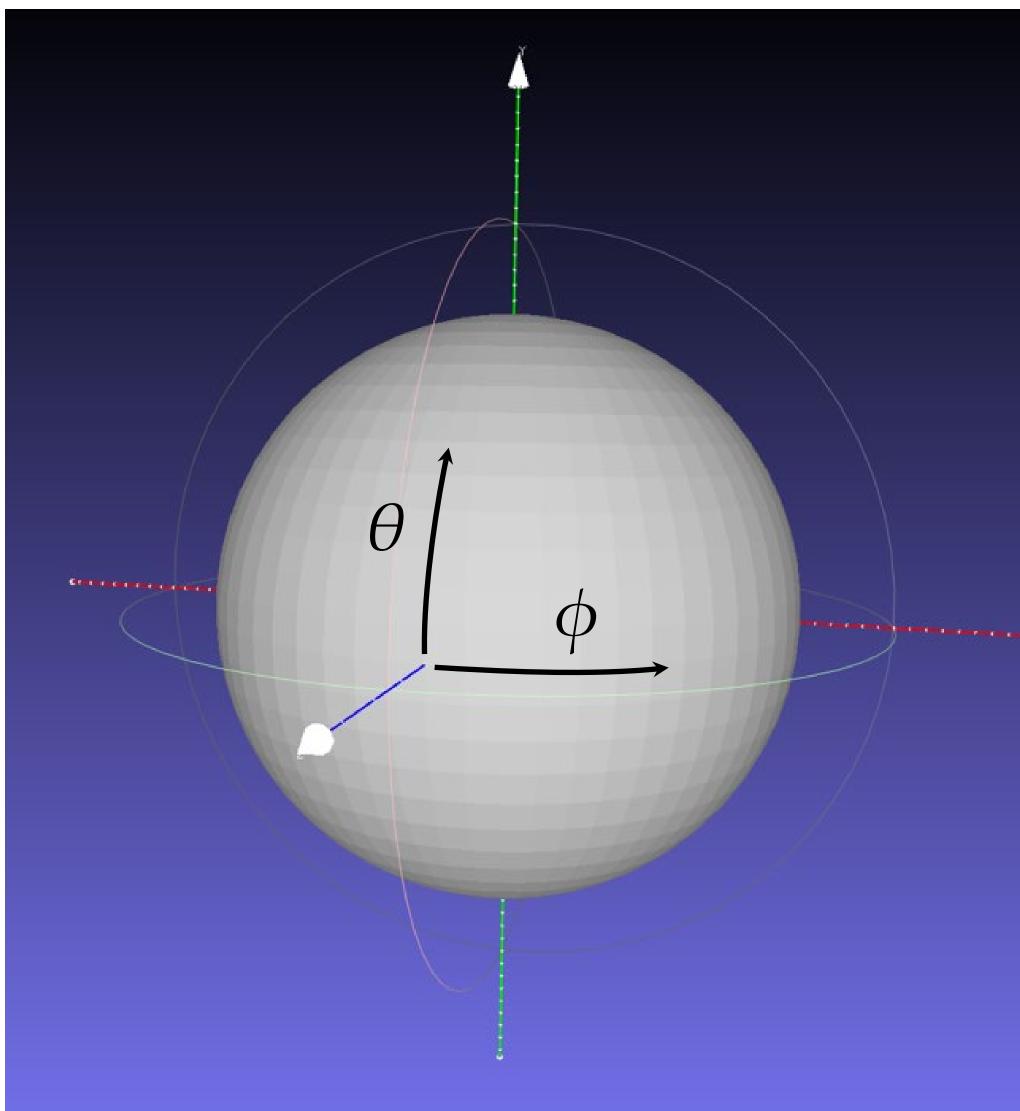




Can also define a sphere parametrically

Position:

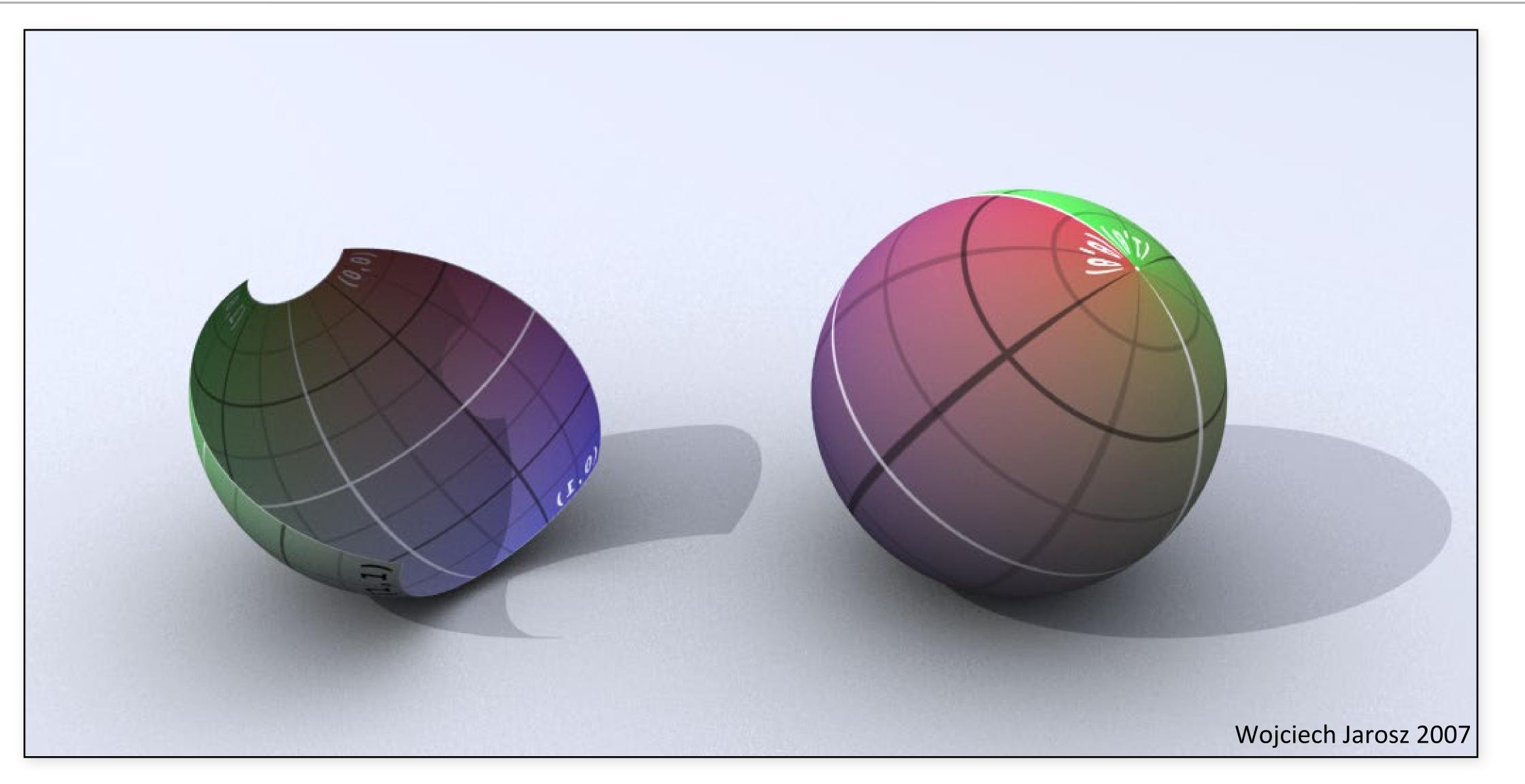
 $x = \cos \theta \sin \phi$ $y = \sin \theta$ $z = \cos \theta \cos \phi$





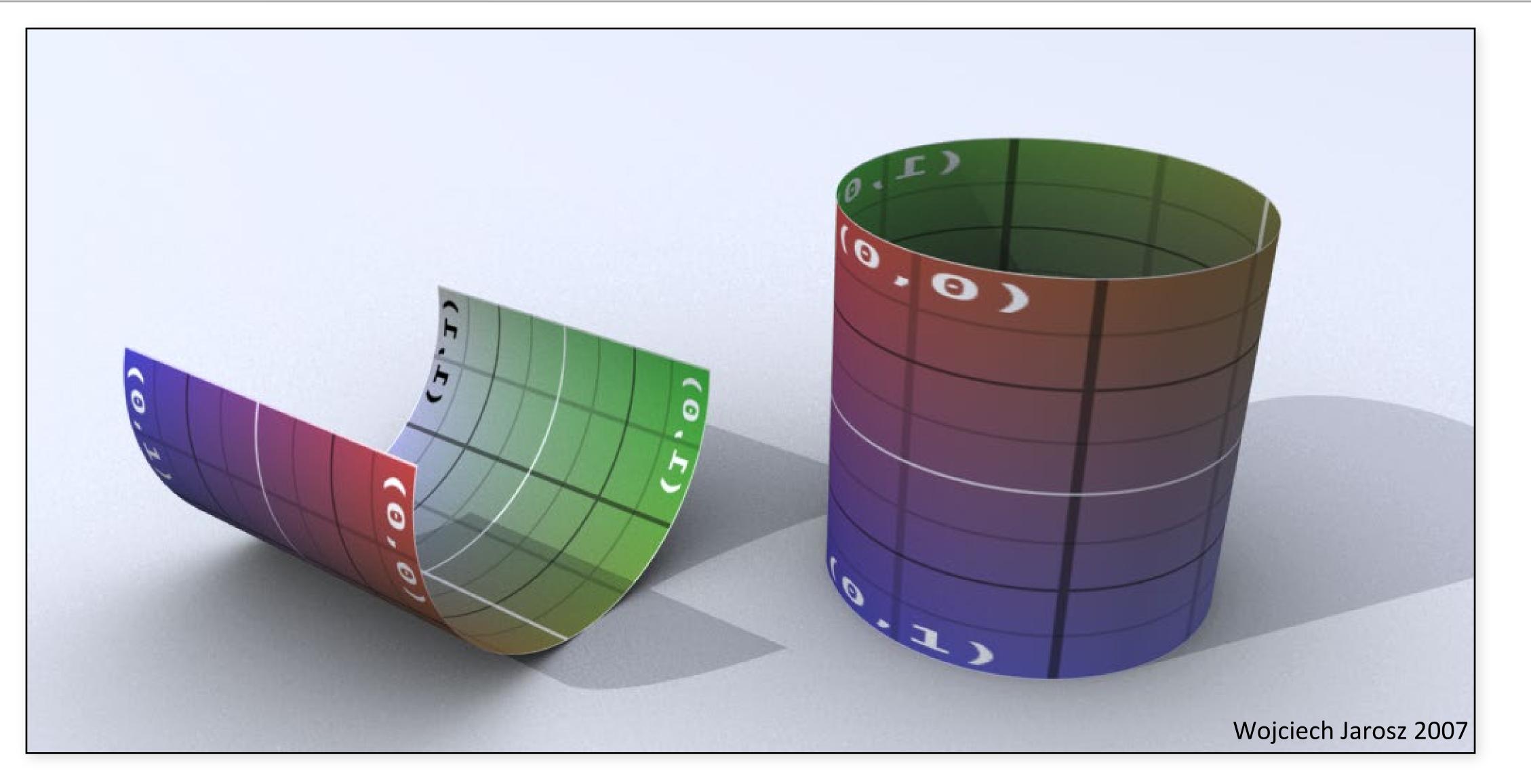


Parametric spheres



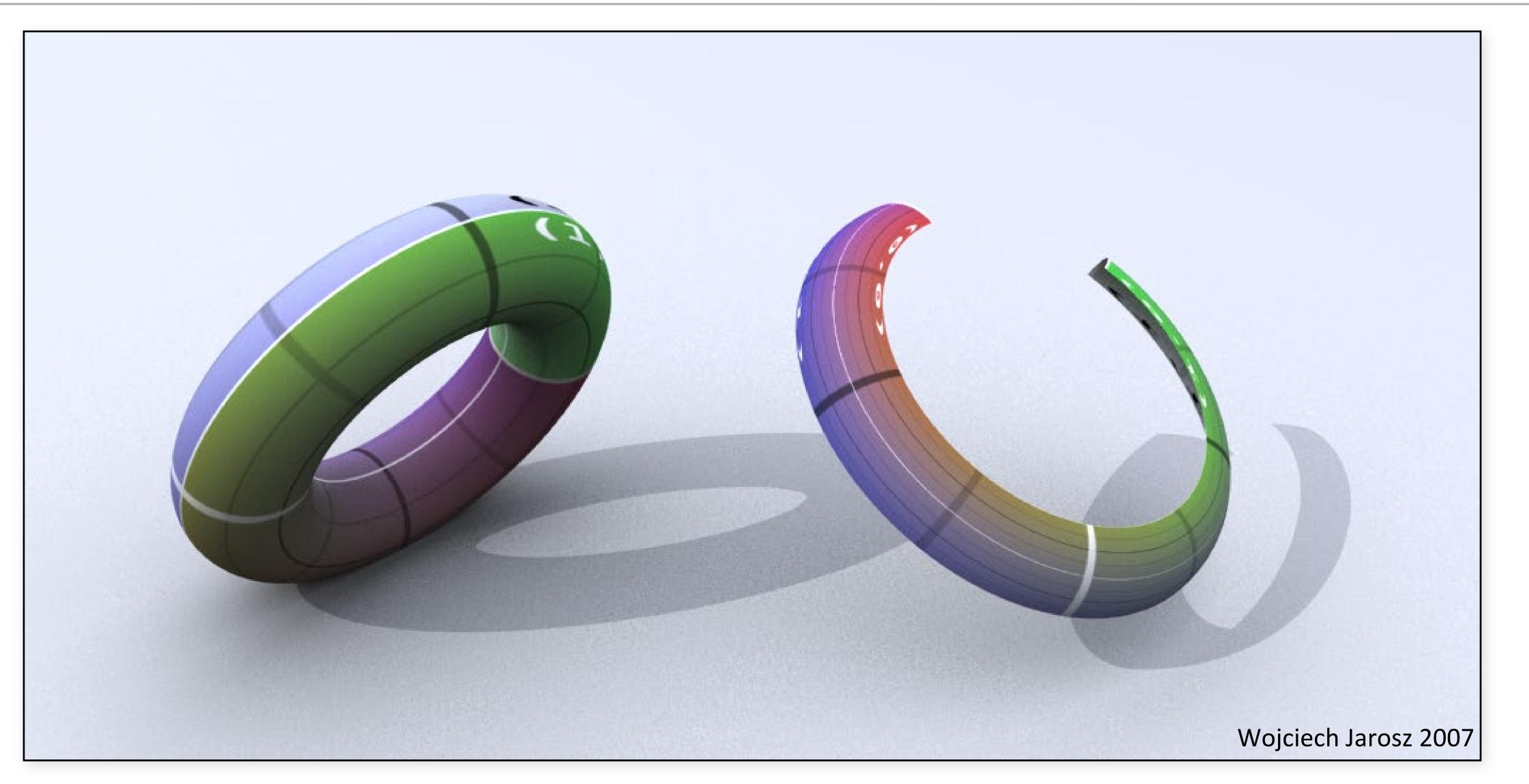


Parametric cylinders



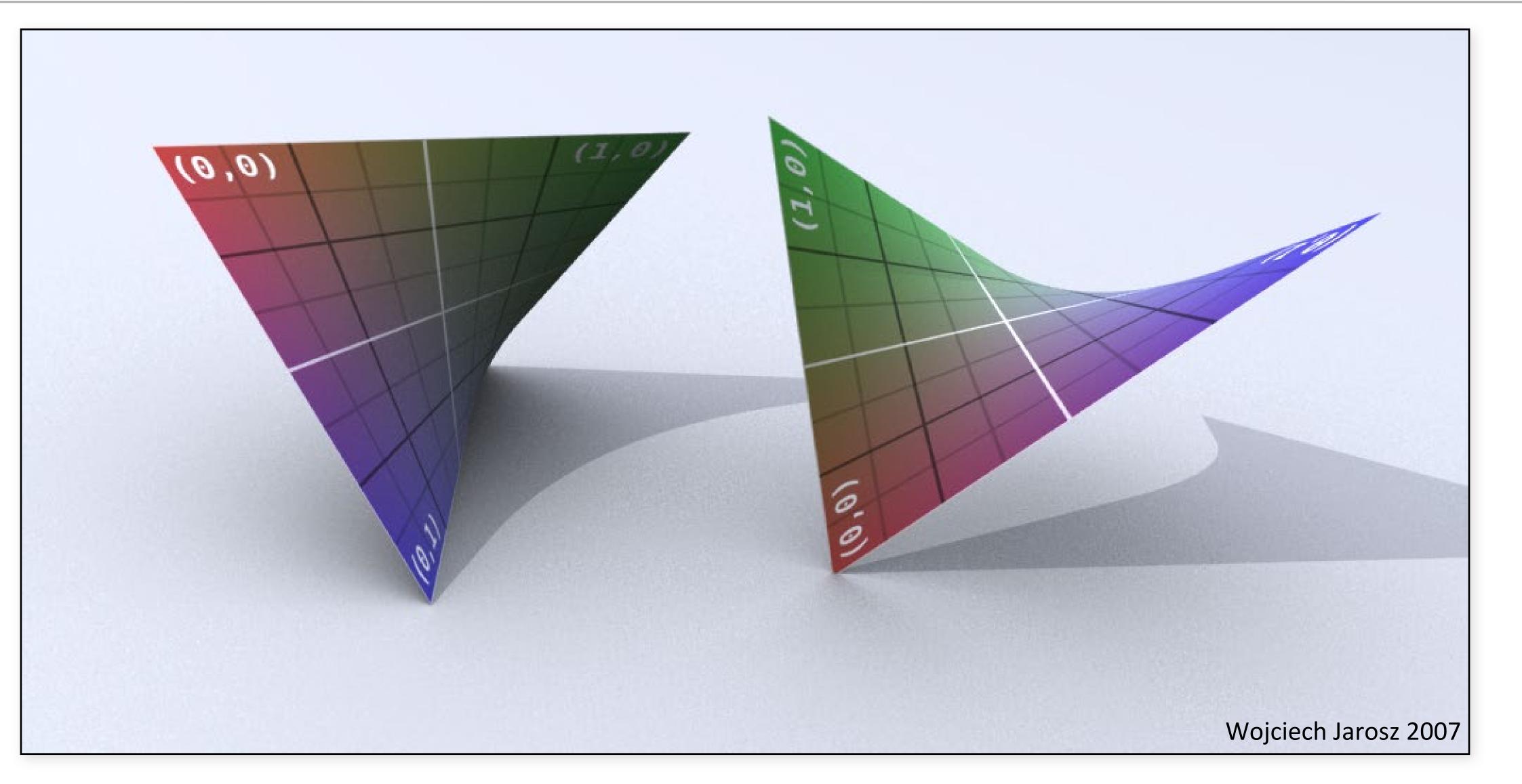


Parametric toruses



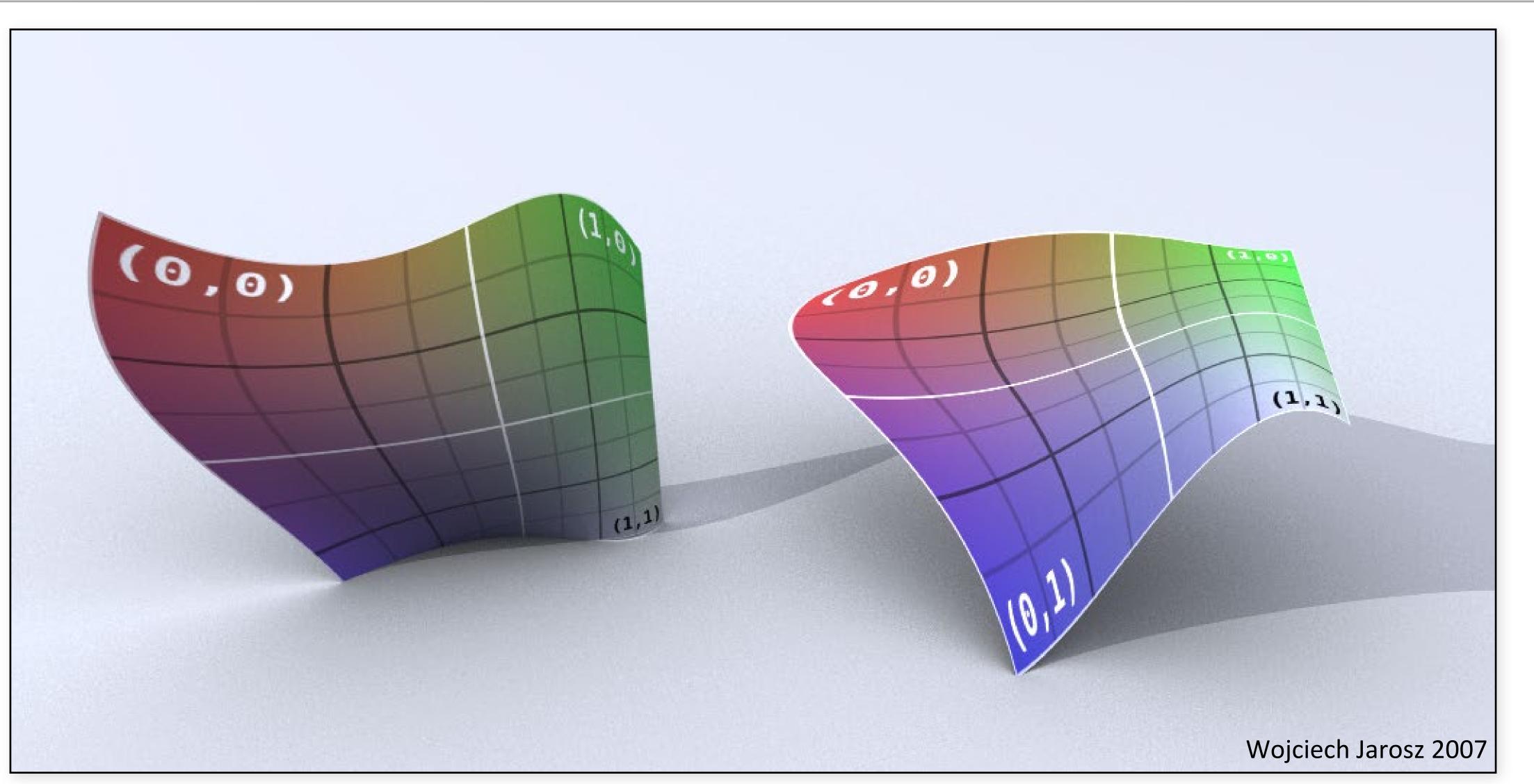


Bilinear patches





Bicubic patches





Creating parameterizations

For non-parametric surfaces it is trickier

Need to create a parametrization!

- Projection mapping
- UV mapping

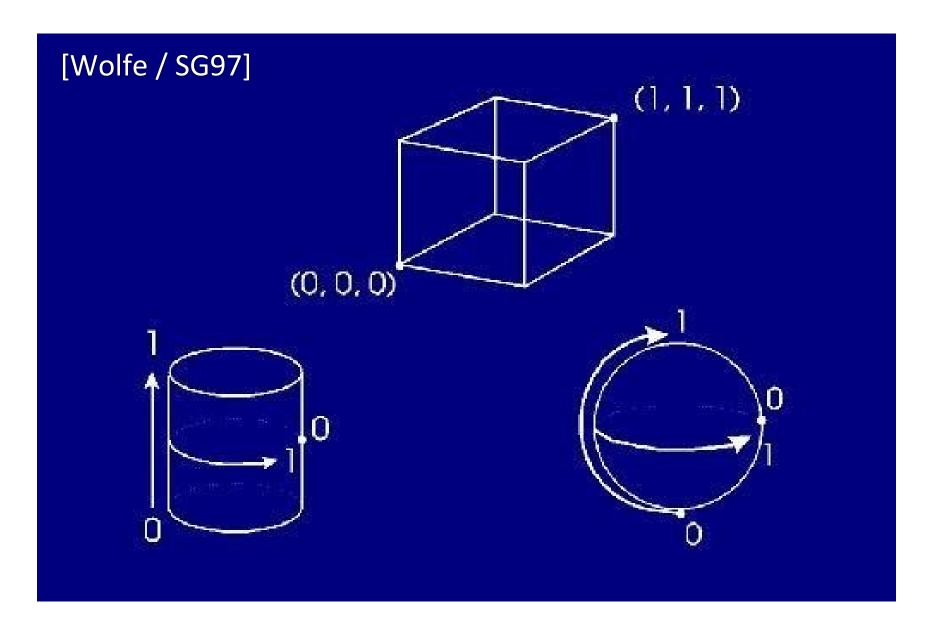
[Wolfe / SG97]



Projection mapping Maps 3D surface points to 2D image coordinates $f: \mathbb{R}^3 \to [0,1]^2$

Different types of projections

- often corresponding to simple shapes
- useful for simple objects

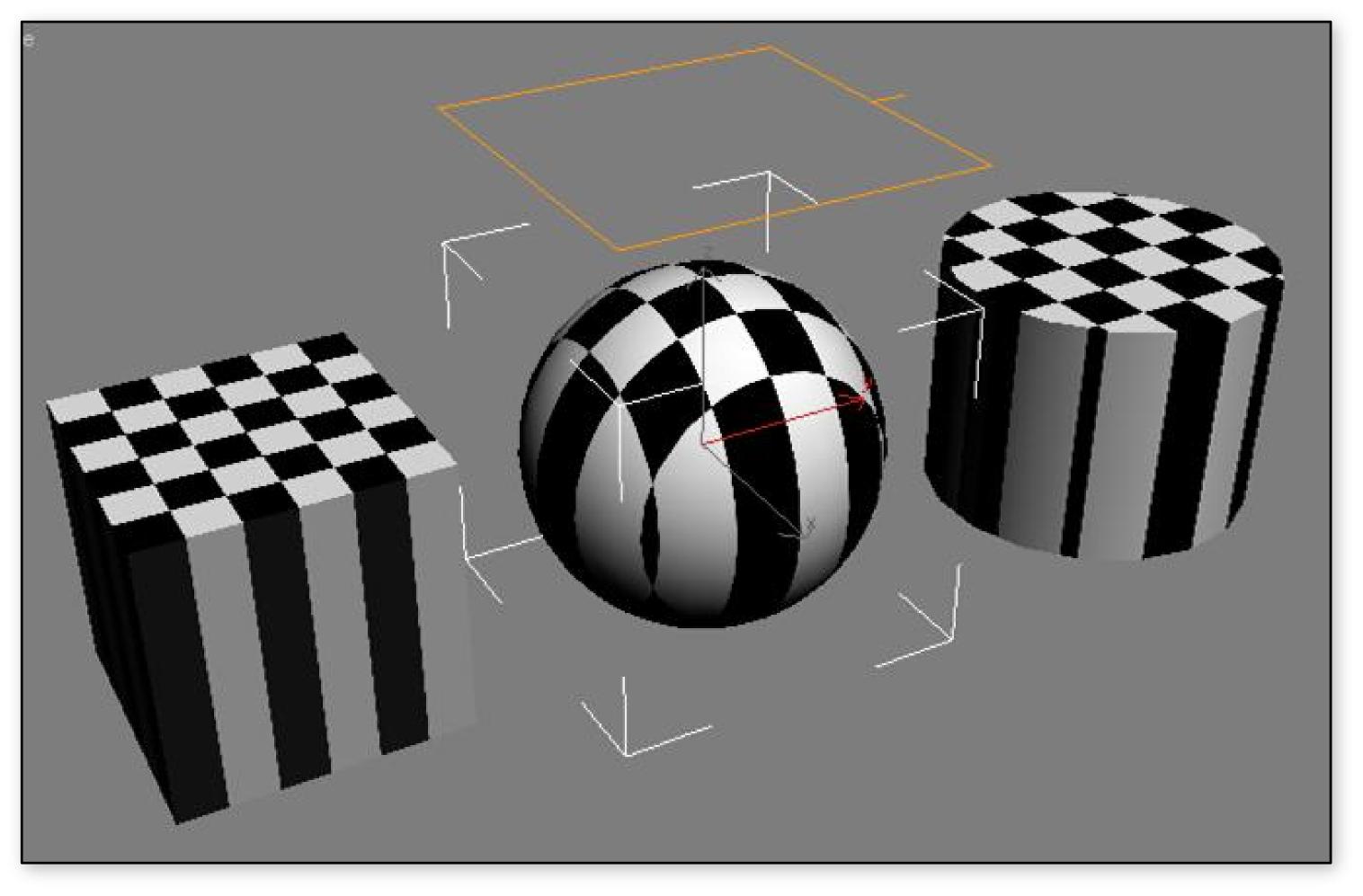




Projections — planar

Planar projection along xy plane of size (w, h)

$$f(\mathbf{p}) = \begin{vmatrix} \frac{p_x}{w} \\ \frac{p_y}{h} \end{vmatrix}$$

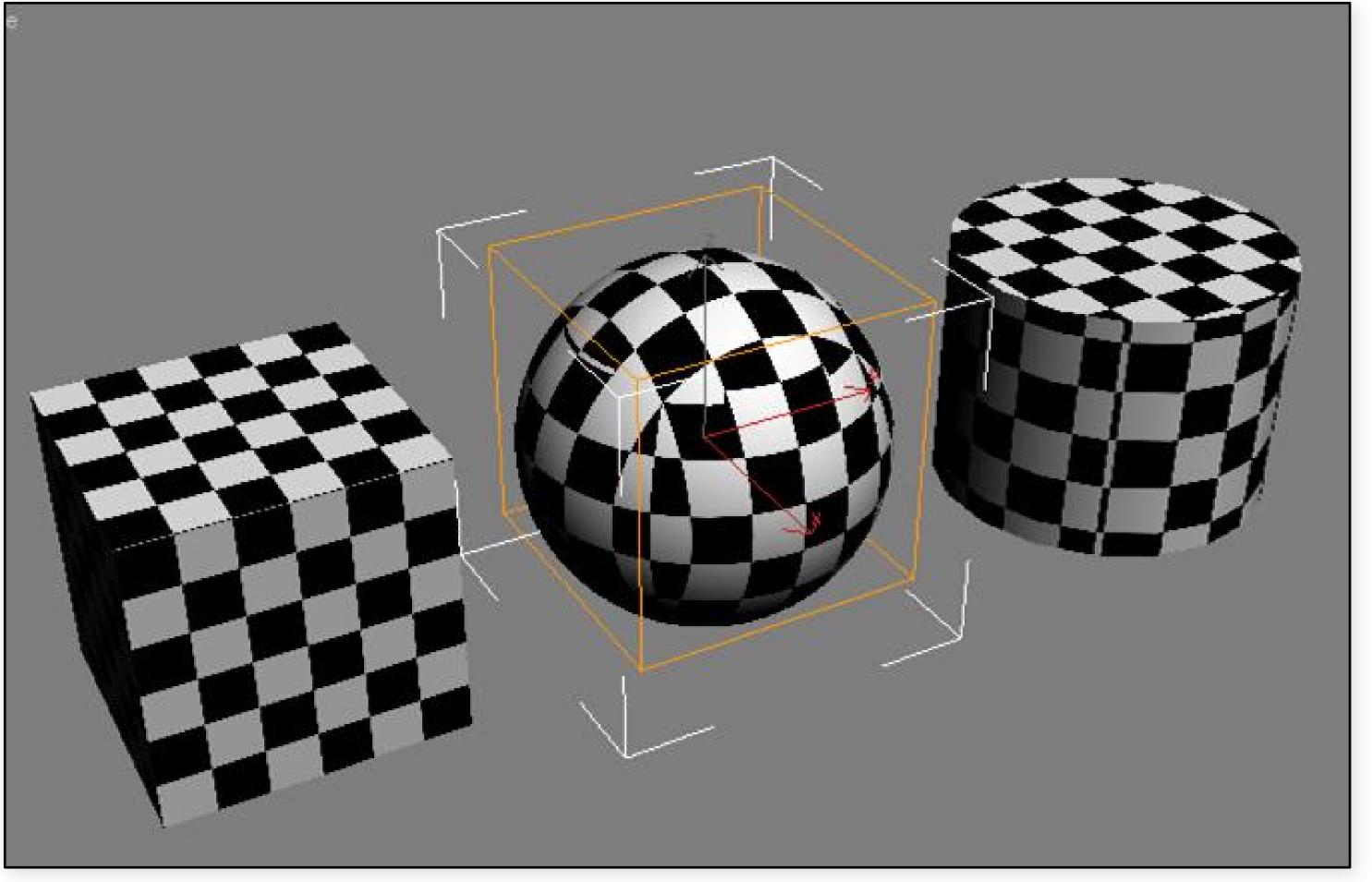






Projections — cubical

Planar projection onto one of 6 faces of a cube based on surface normal

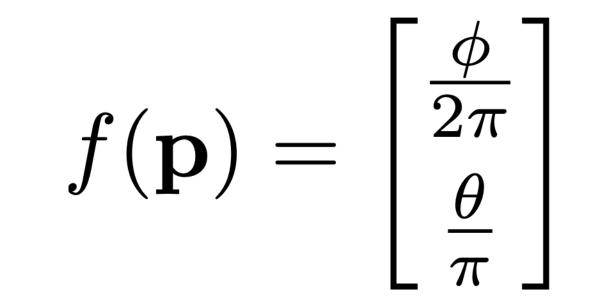


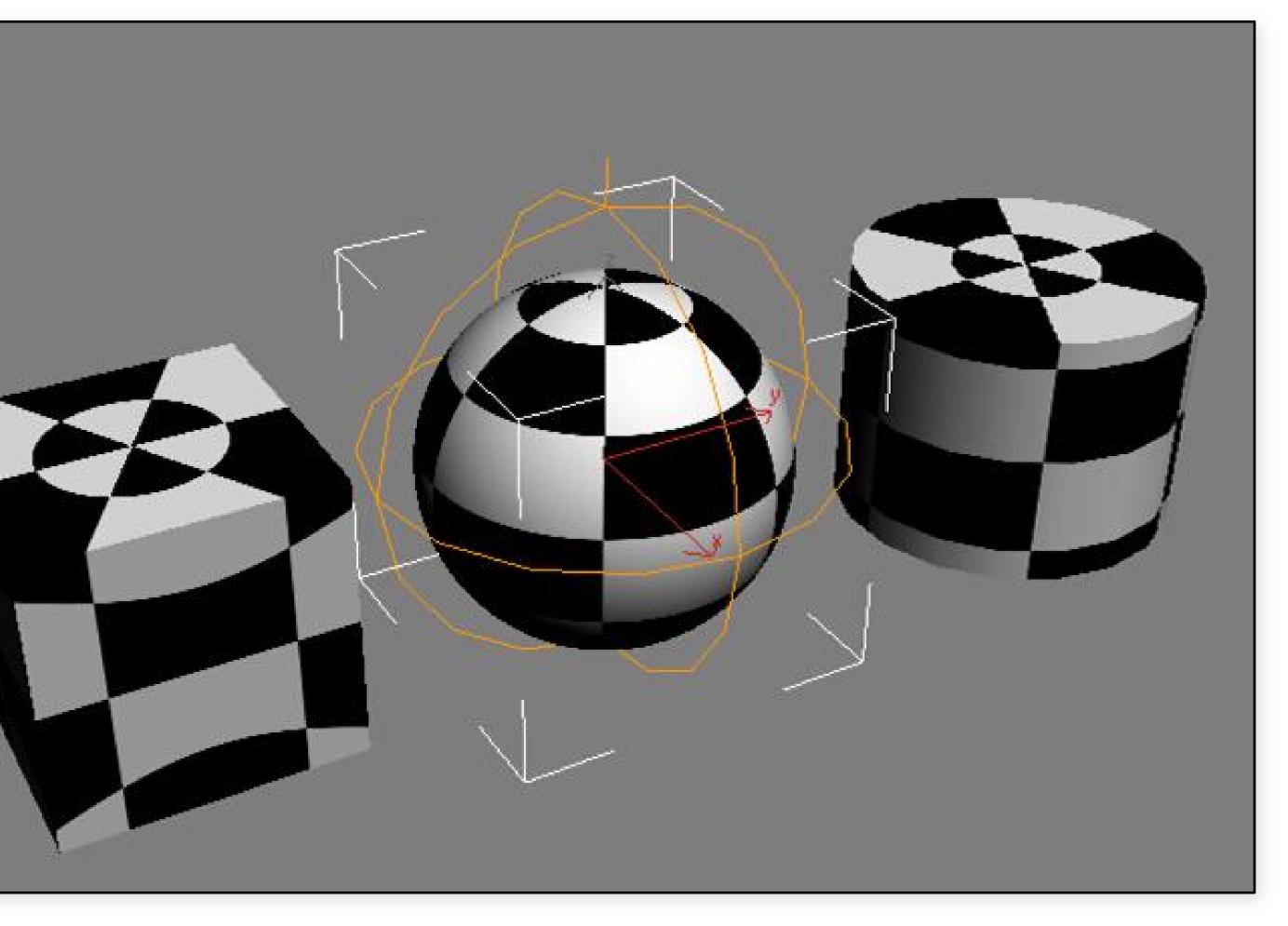


Projections — spherical

Project point onto unit sphere

- compute spherical coordinates



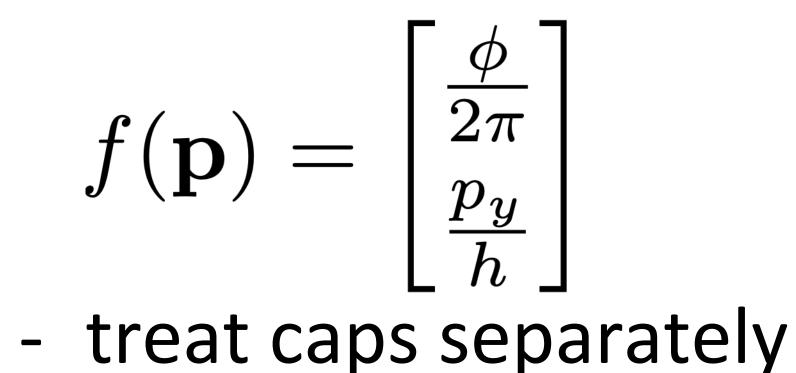




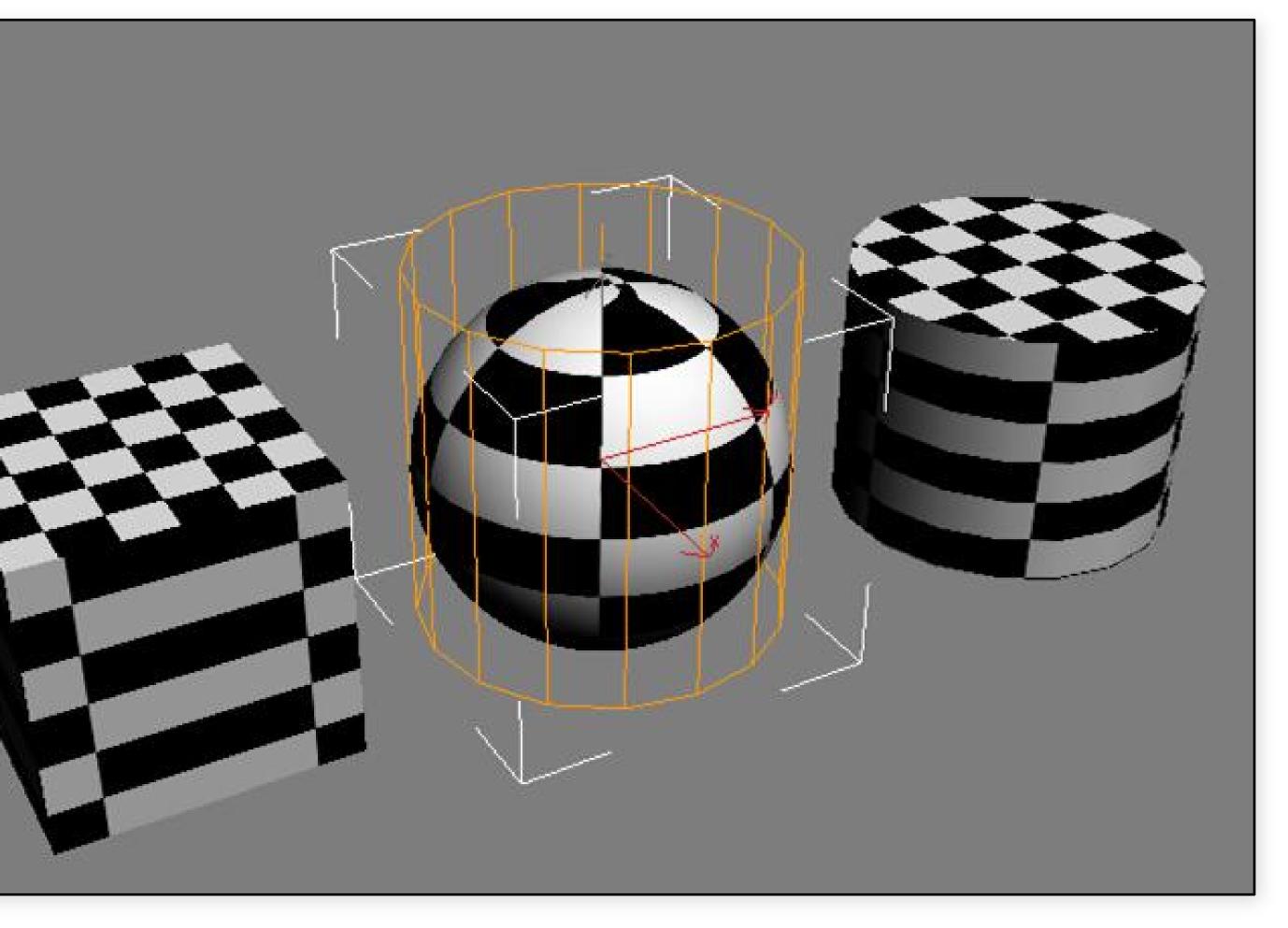
Projections — cylindrical

Project point onto cylinder of height h

- compute cylindrical coordinates



Fabio Pellacini lide by S After a

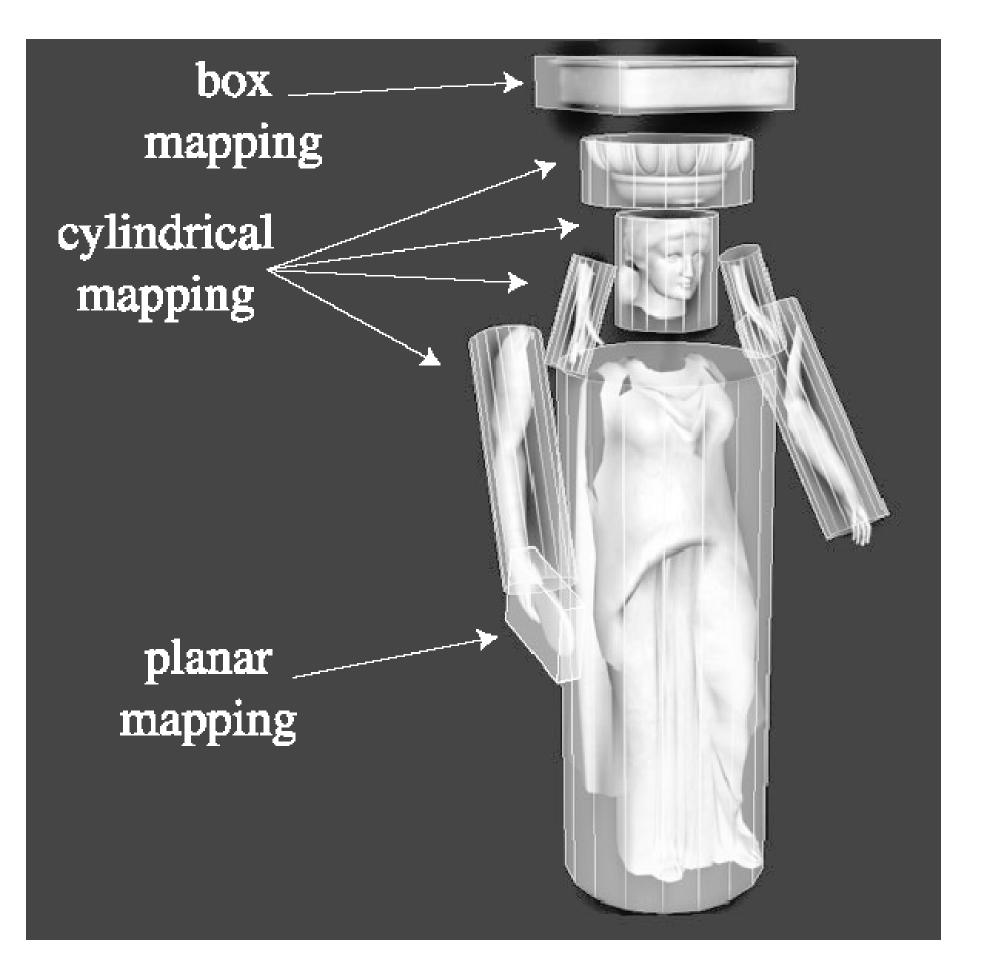




Combining projections

Non-parametric surfaces: project pieces to parametric surface





[Moller & Haines 2002]

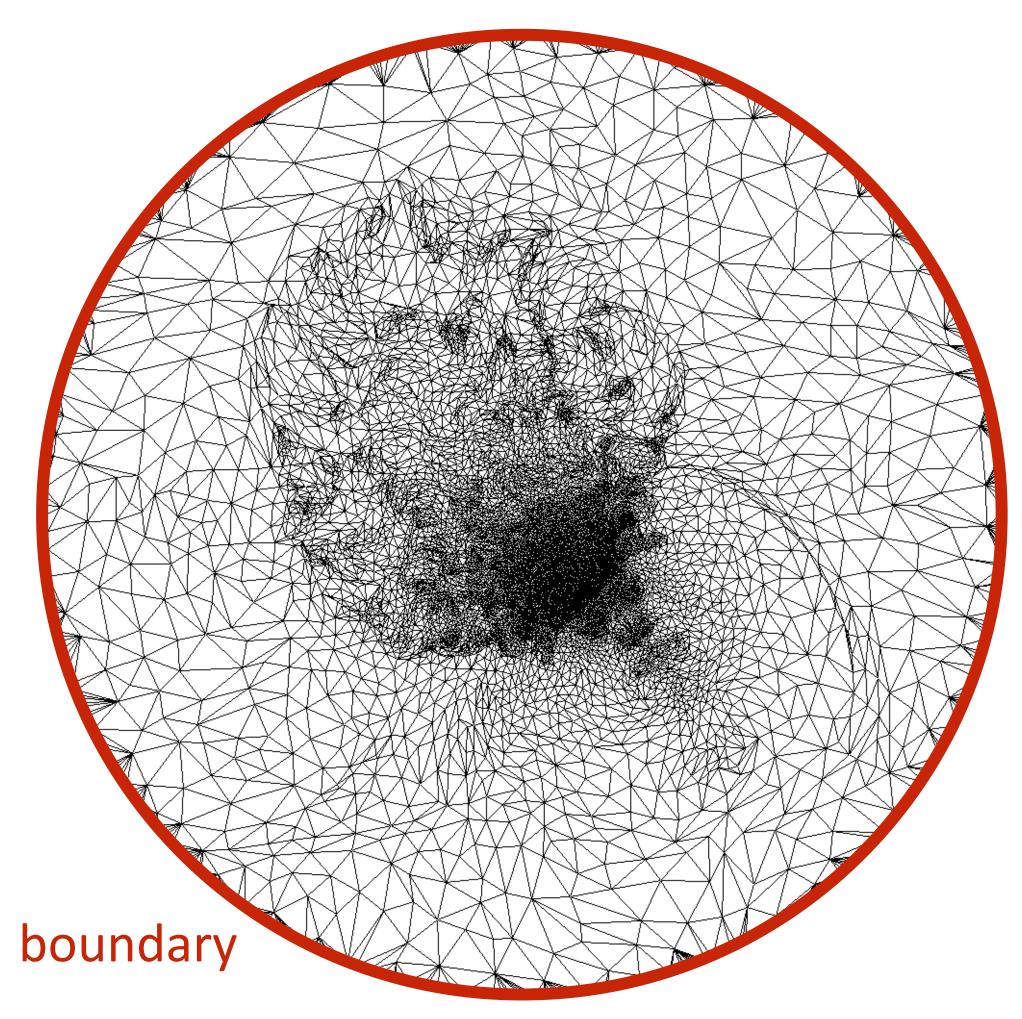


Creating UV parameterizations

3D space (x,y,z)

boundary

2D parameter domain (u,v)

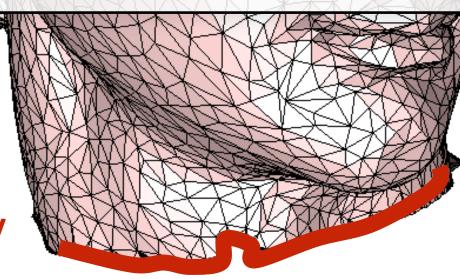




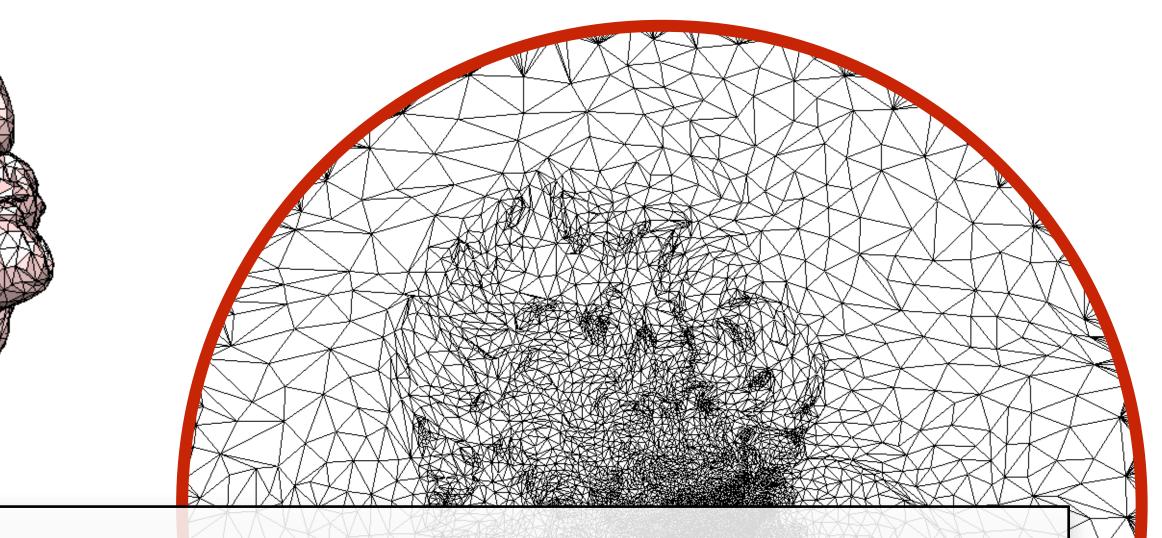
Creating UV parameterizations

3D space (x,y,z)

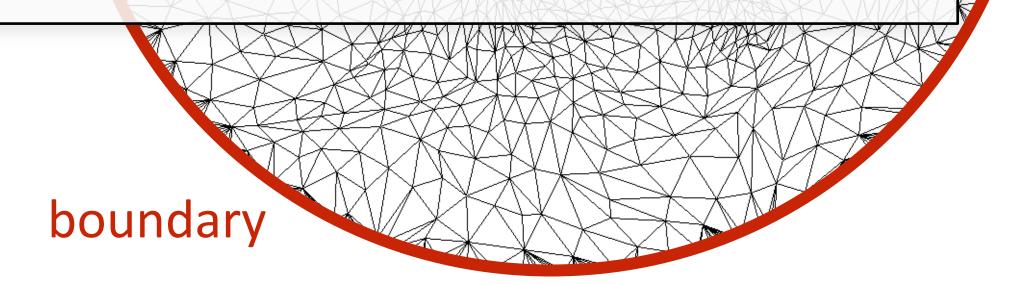
boundary



2D parameter domain (u,v)

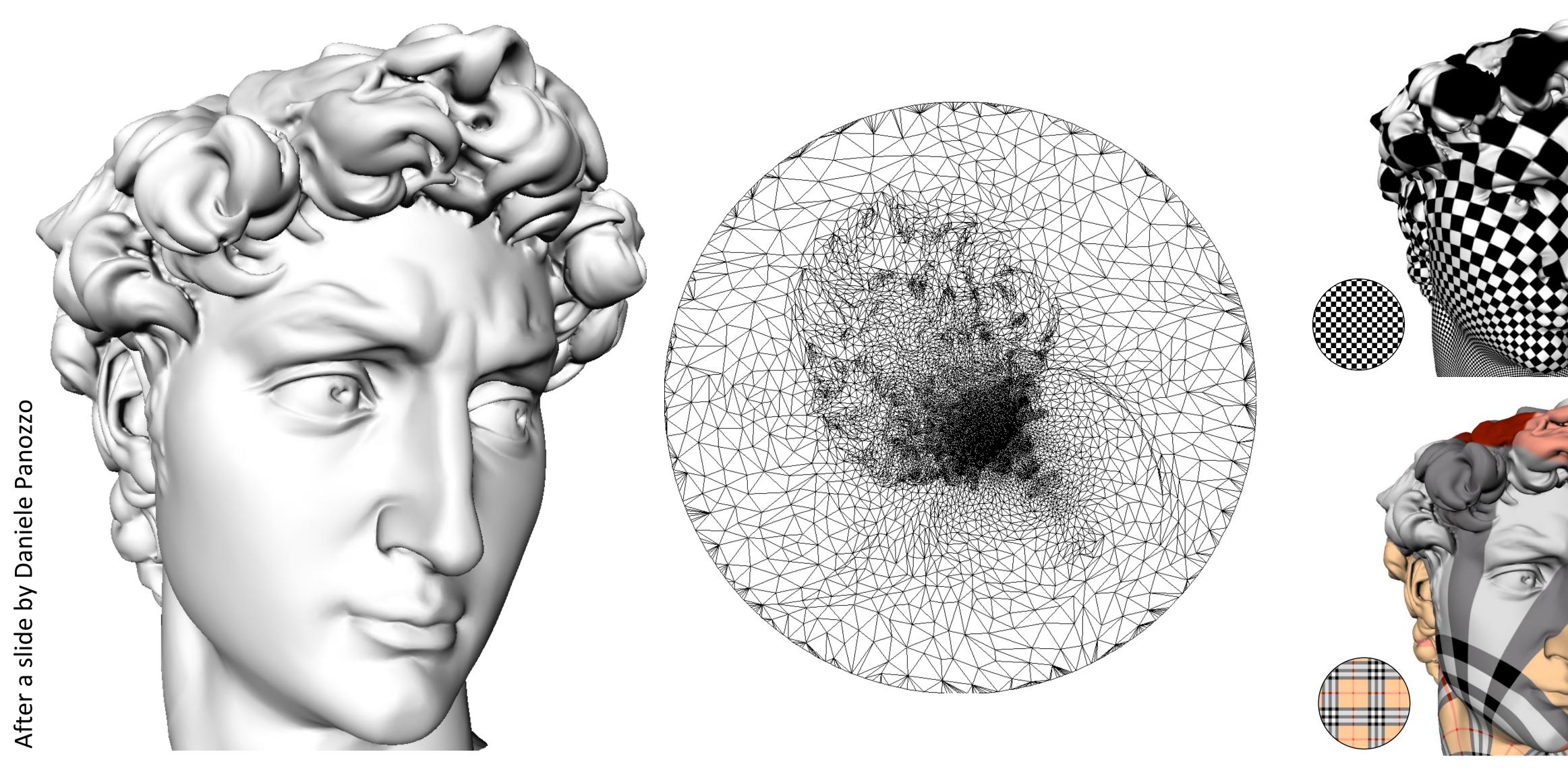


Assign (u,v) coordinates for each mesh vertex. Inside each triangle interpolate using barycentric coordinates.





Creating UV parameterizations

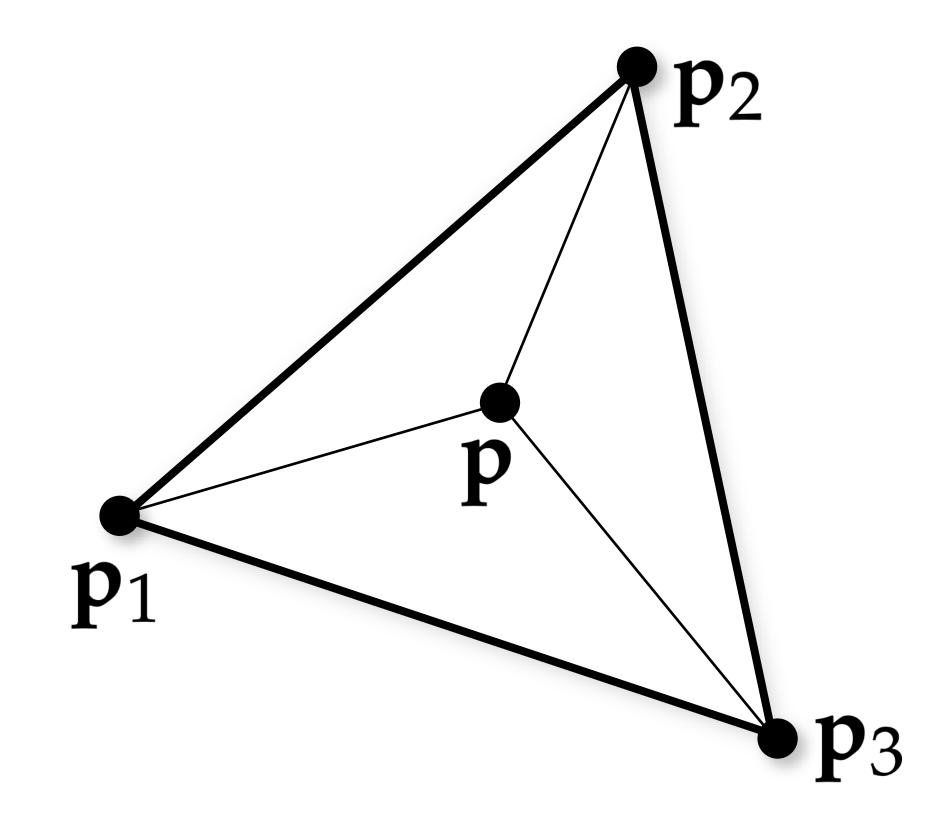






Barycentric coordinates

Barycentric interpolation:



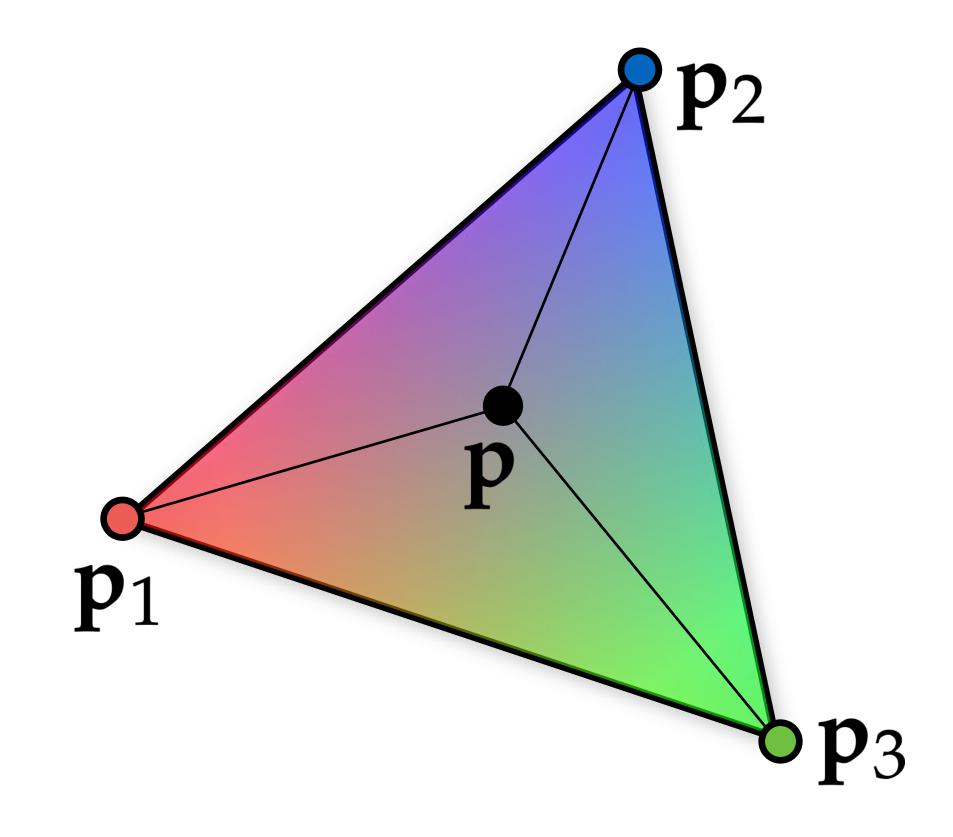
 $\mathbf{p}(\alpha,\beta,\gamma) = \alpha \mathbf{p}_1 + \beta \mathbf{p}_2 + \gamma \mathbf{p}_3$

Can use this eqn. to interpolate any vertex quantity across triangle!



Barycentric coordinates

Barycentric interpolation:

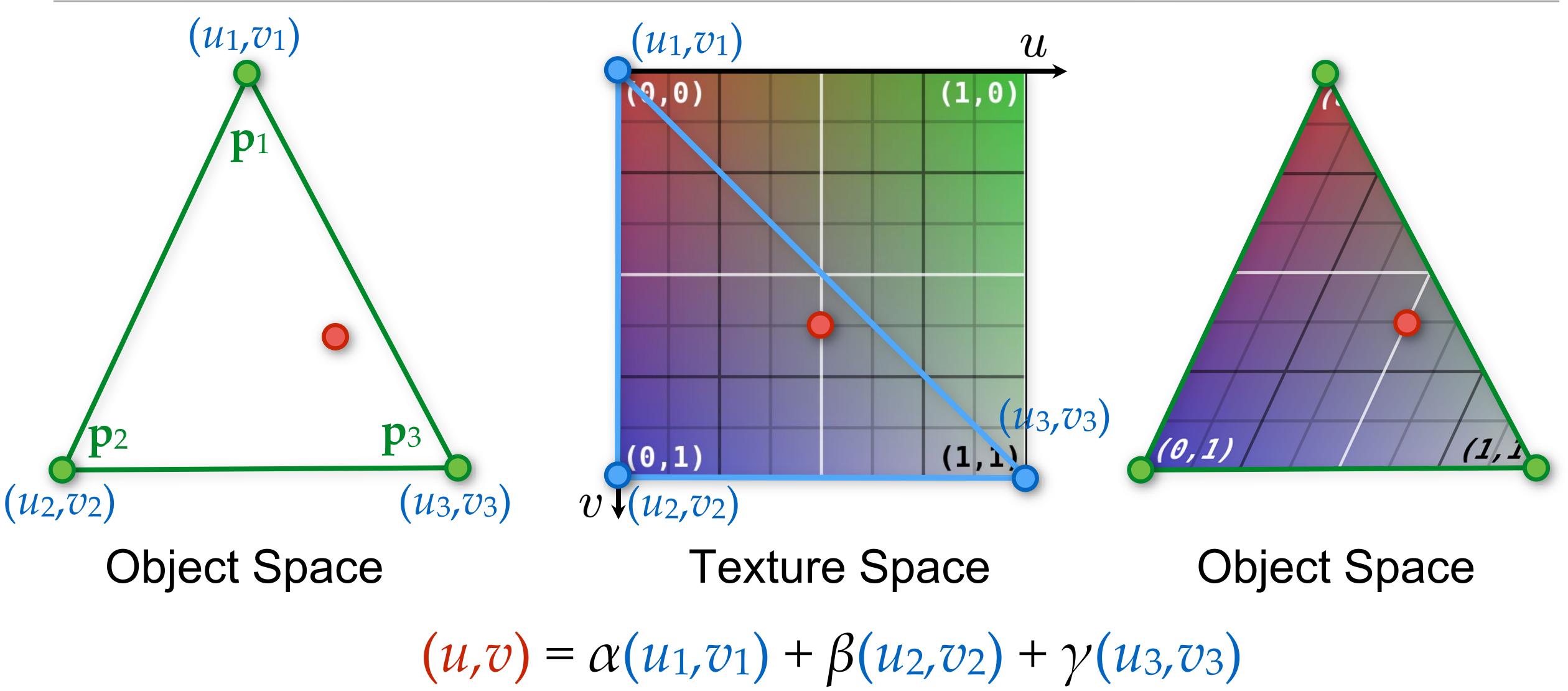


$\mathbf{p}(\alpha, \beta, \gamma) = \alpha \mathbf{p}_1 + \beta \mathbf{p}_2 + \gamma \mathbf{p}_3$ $\mathbf{c}(\alpha, \beta, \gamma) = \alpha \mathbf{c}_1 + \beta \mathbf{c}_2 + \gamma \mathbf{c}_3$

Can use this eqn. to interpolate any vertex quantity across triangle!

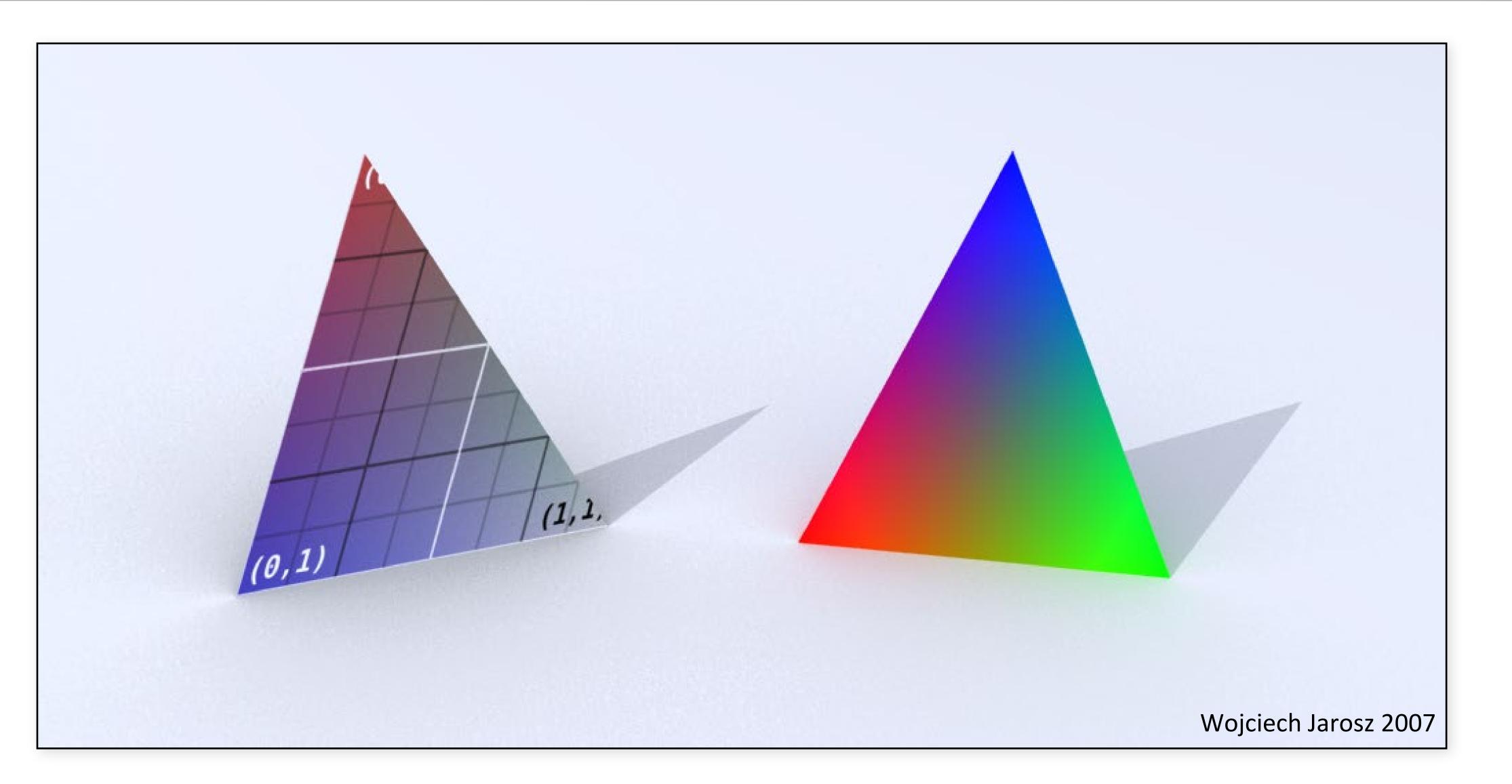


UV texturing



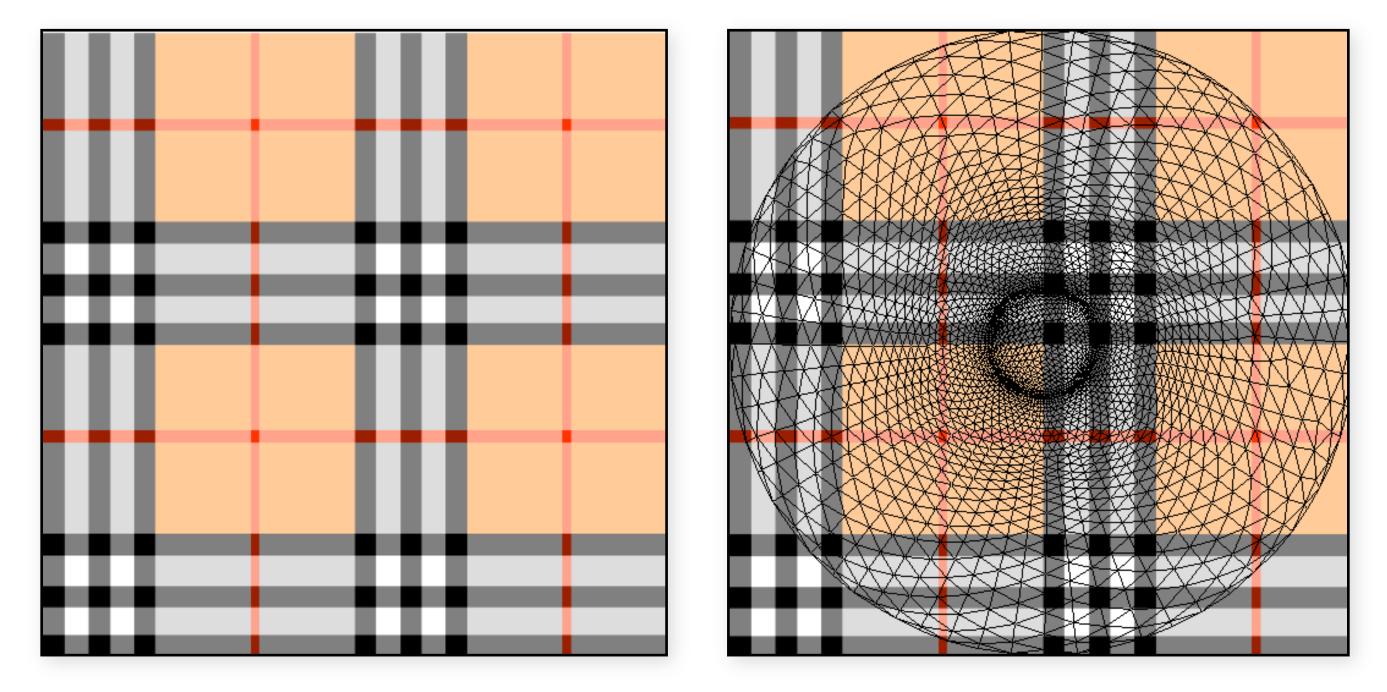


UV texturing

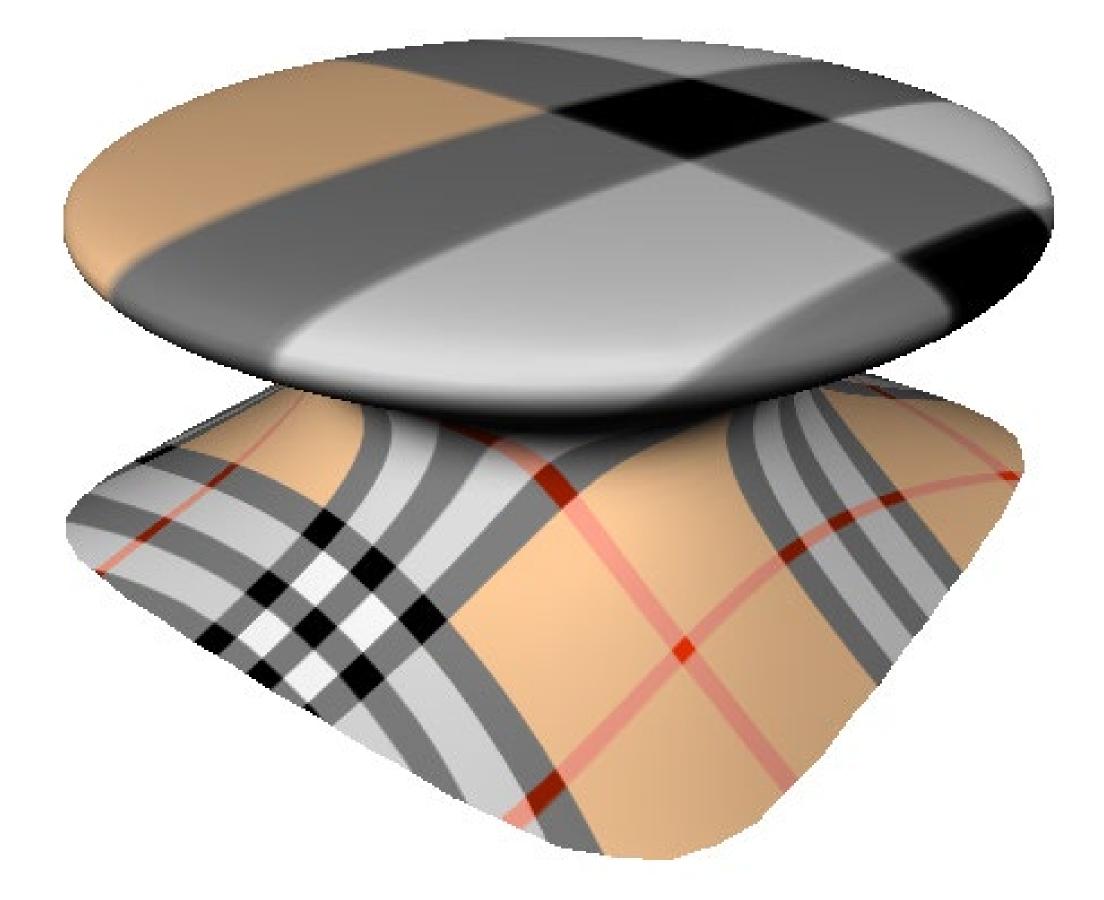




Area distortion vs. angle distortion



After a slide by Daniele Panozzo

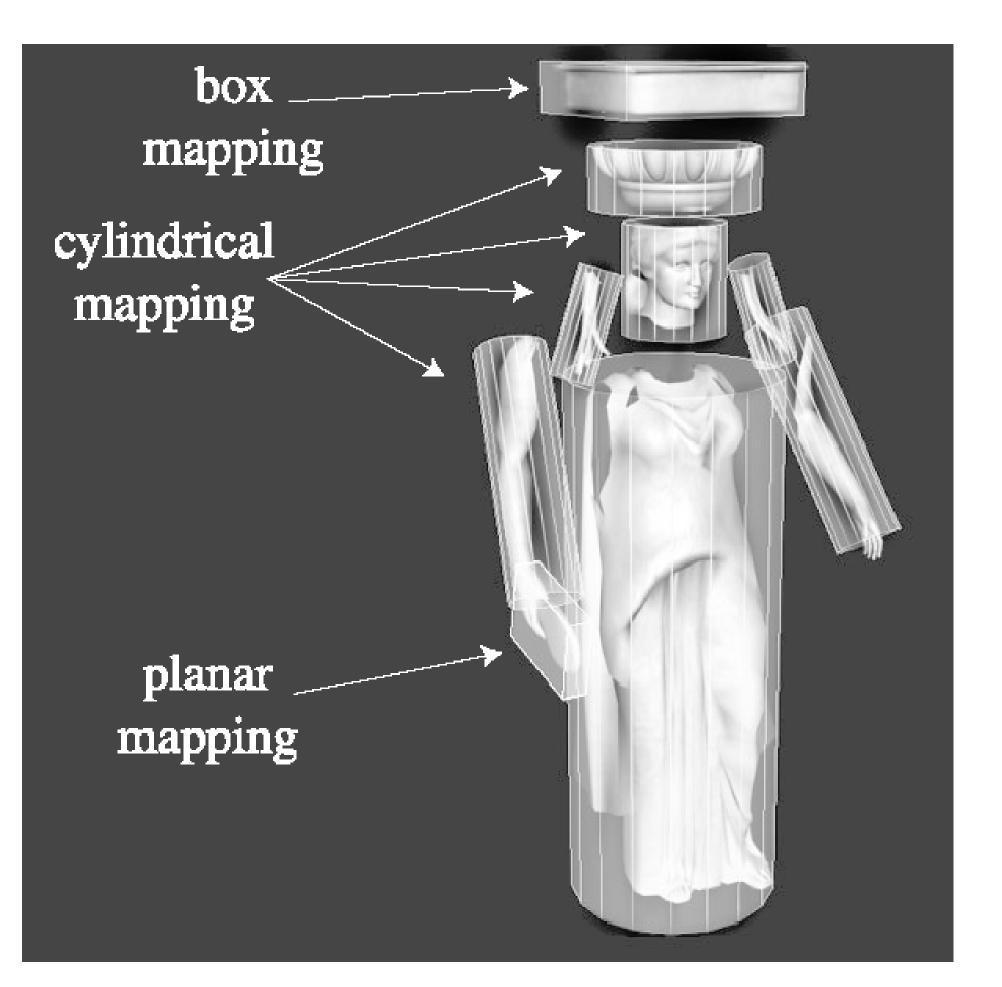




Creating UV parameterizations

Can compute vertex UVs using projections





[Moller & Haines 2002]



Creating UV parameterizations

"Atlas" - break up model into single texture

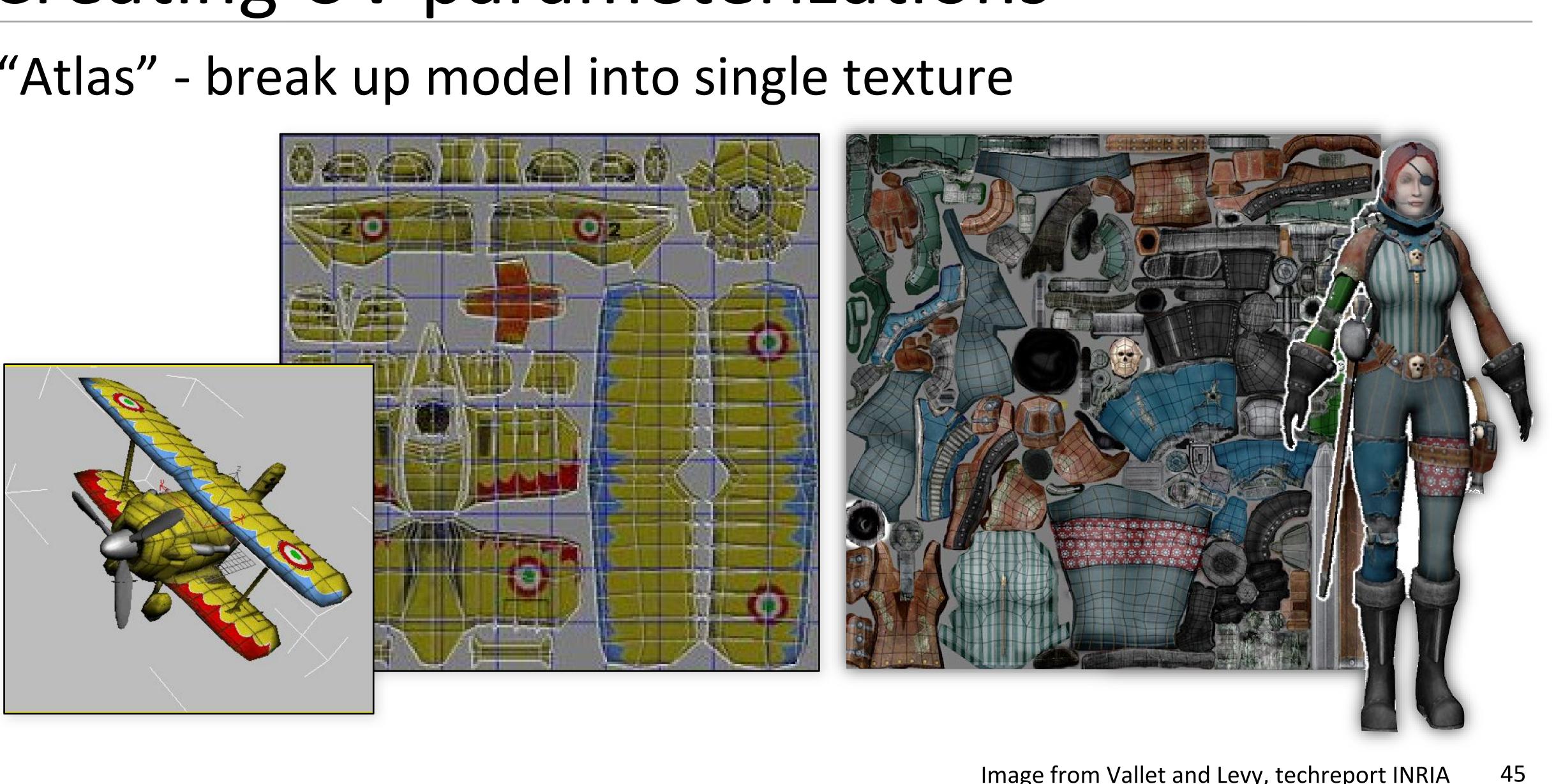


Image from Vallet and Levy, techreport INRIA

Texture lookup

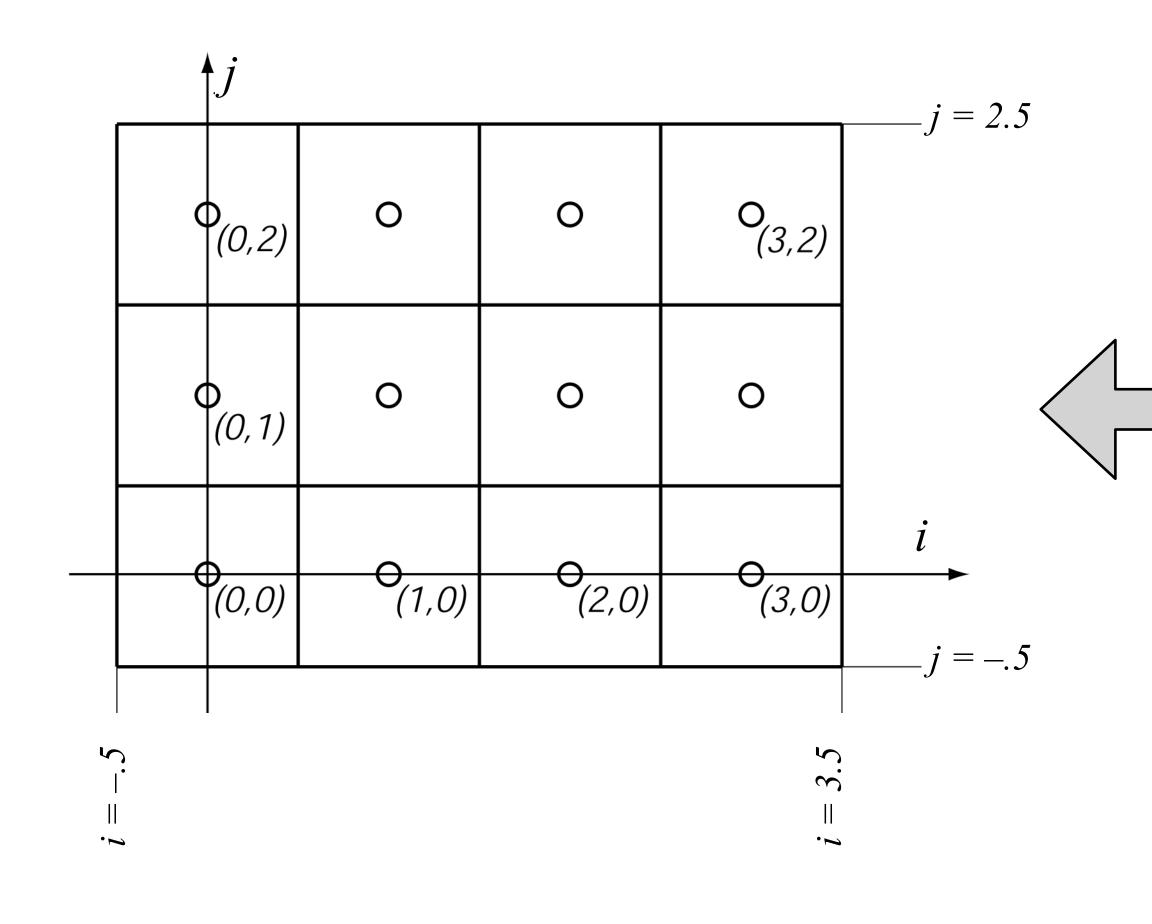
Texture lookups and wrapping

In shading calculation, when you need a texture value you perform a *texture lookup*

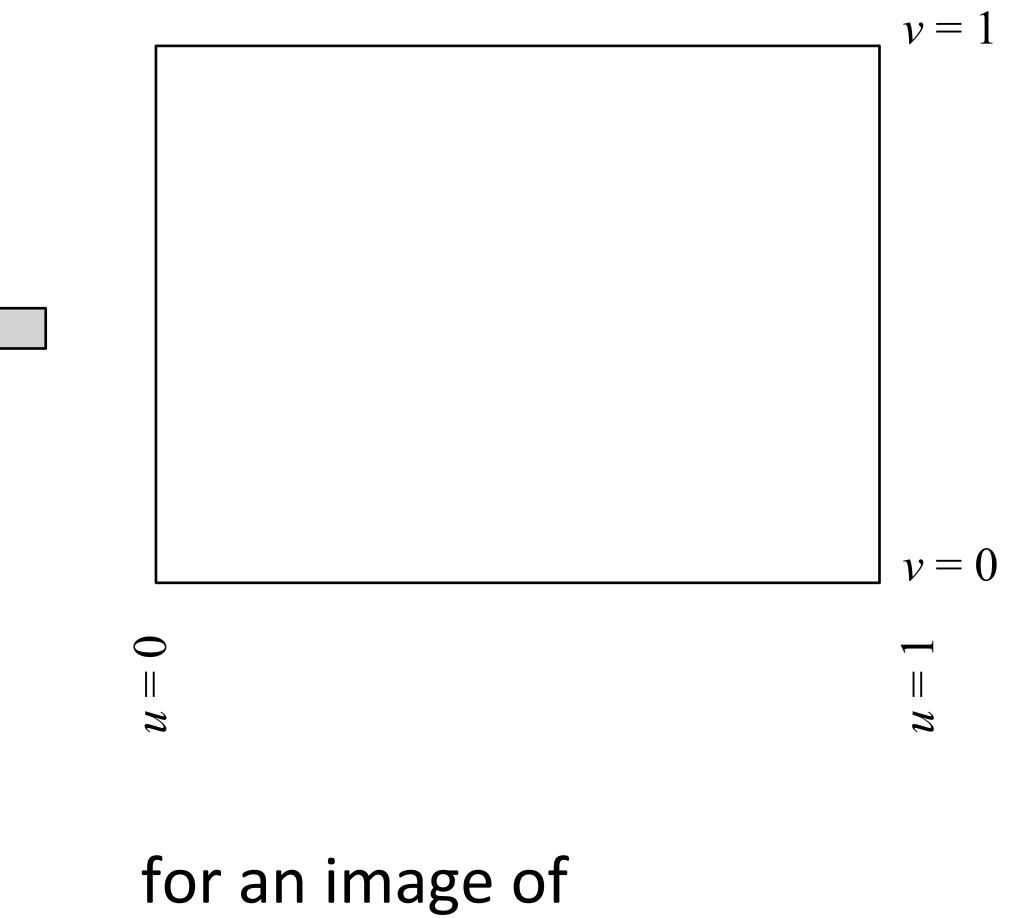
Convert (u, v) texture coordinates to (i, j) texel coordinates, and read a value from the image



Obtaining (i,j) from (u,v)



 $i = u n_x - 0.5$ $j = v n_y - 0.5$



 n_x by n_y pixels

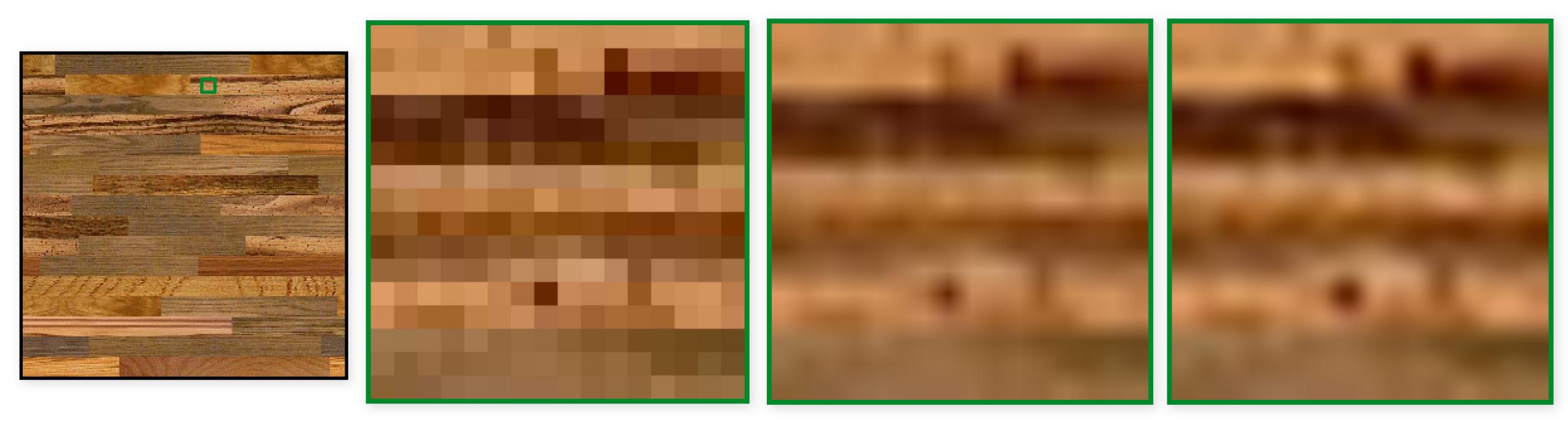


Looking up texture values

- In general, we will not have a 1-to-1 mapping between image pixels and texture pixels, or "texels"
- Lookup locations will fall at fractional texel coordinates
- simplest: round to nearest (nearest neighbor lookup)
- various ways to be smarter and get smoother results
- Two issues arise:
- Magnification: Texel size larger than pixel size
- Minification: Texel size smaller than pixel size (potential aliasing)



Texture Filtering - Magnification



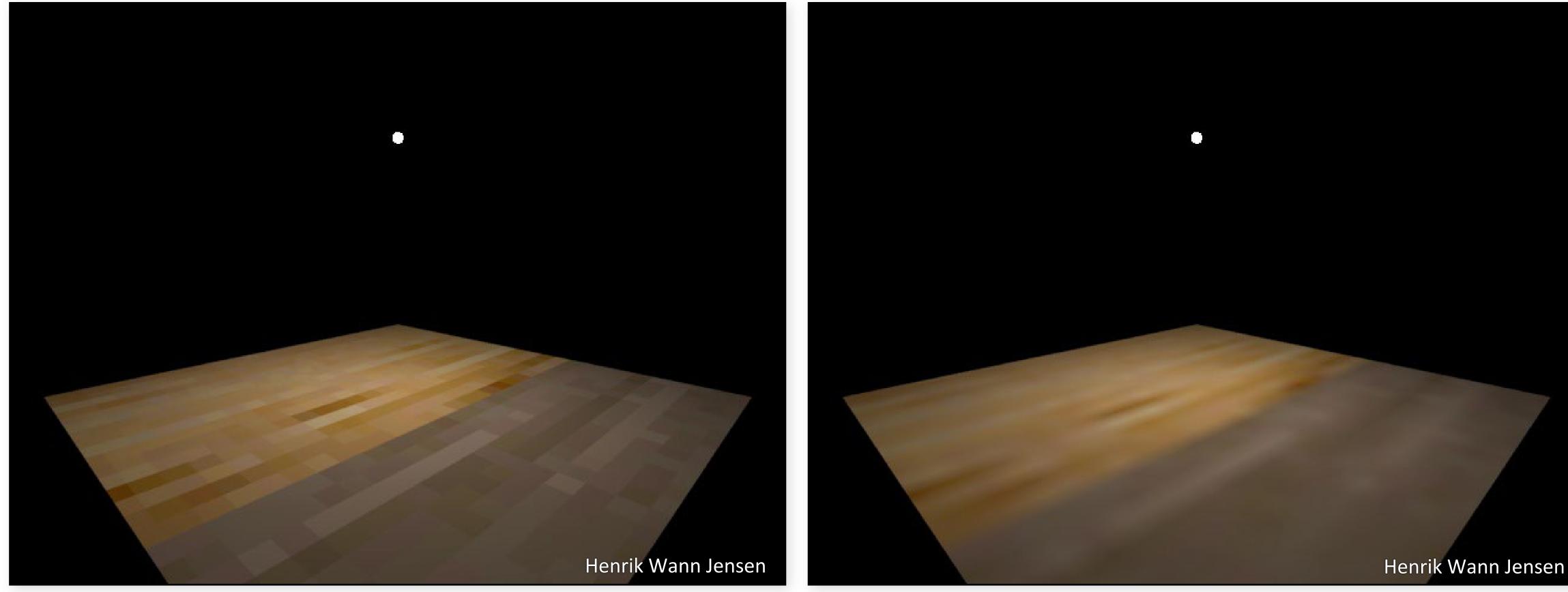
Nearest Neighbor

Bilinear

Bicubic



Texture Filtering - Magnification



Nearest Neighbor

Bilinear





Texture lookups and wrapping What if i and j are out of range? Option 1, clamp: take the nearest pixel that is in the image

 $i_{\text{pixel}} = \max(0, \min(n_x - n_x))$ Option 2, wrap: treat the textu that falling off the right side ca to come in the left

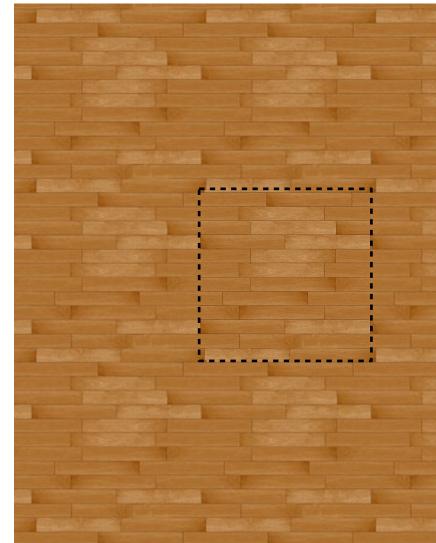
 $i_{\text{pixel}} = \text{remainder}(i_{\text{lookup}})$

$$1, i_{lookup}))$$

ure as periodic, so
auses the look up

$$, n_x)$$



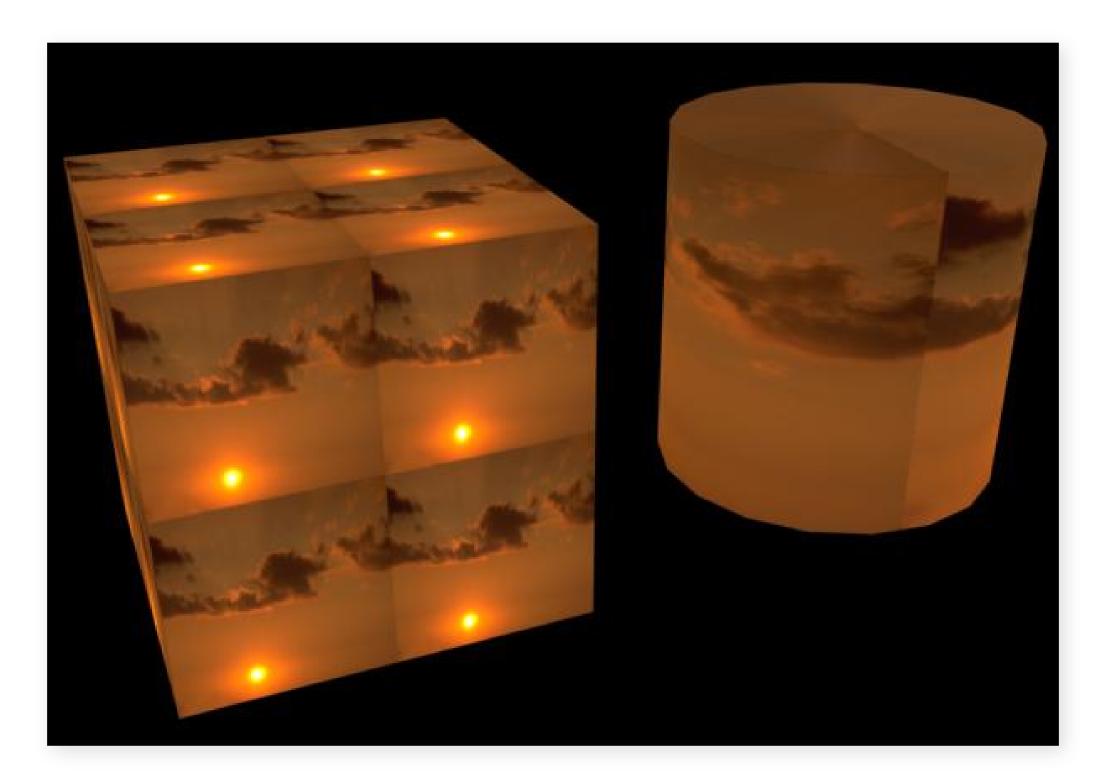






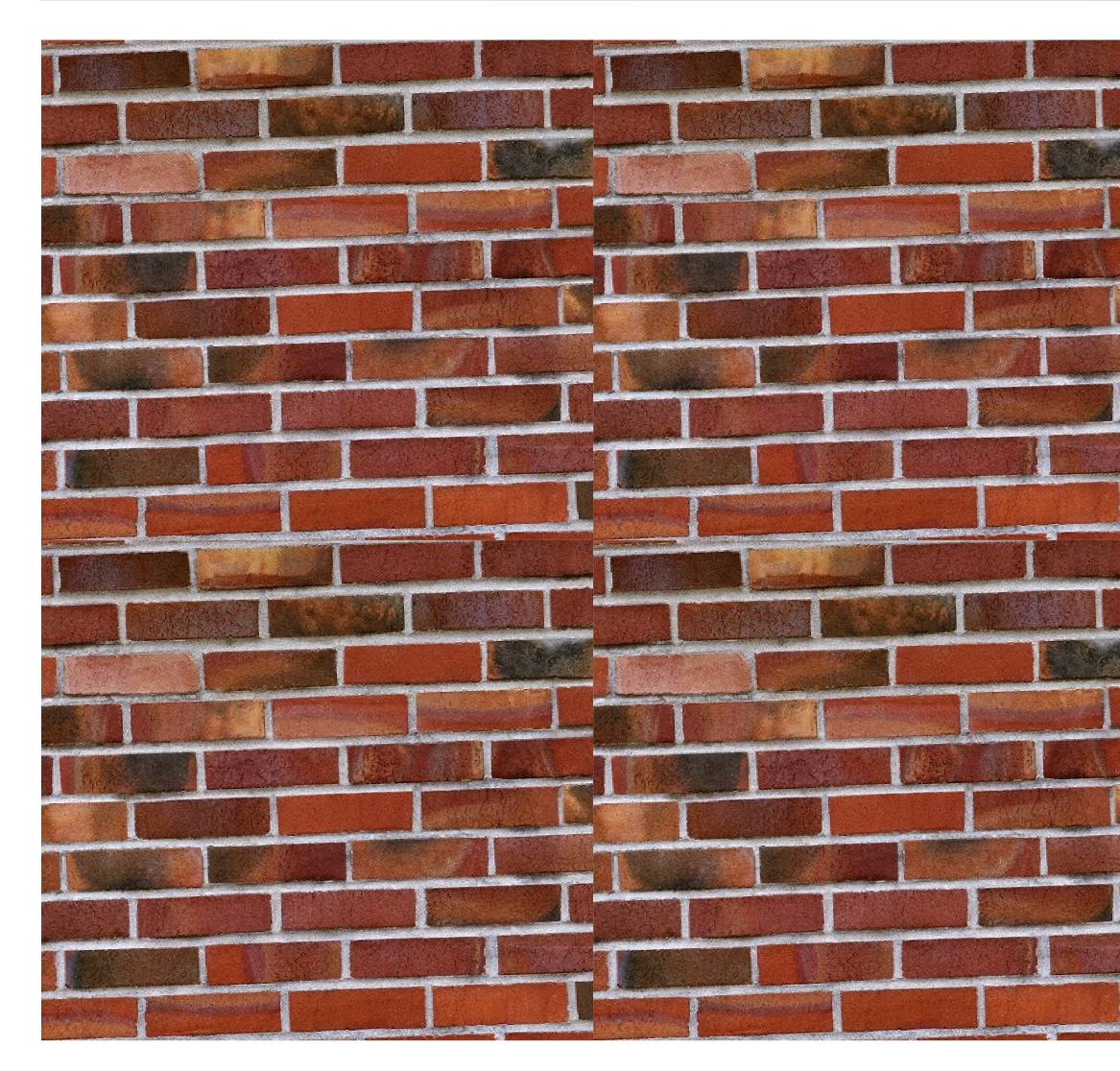
Texture mapping artifacts

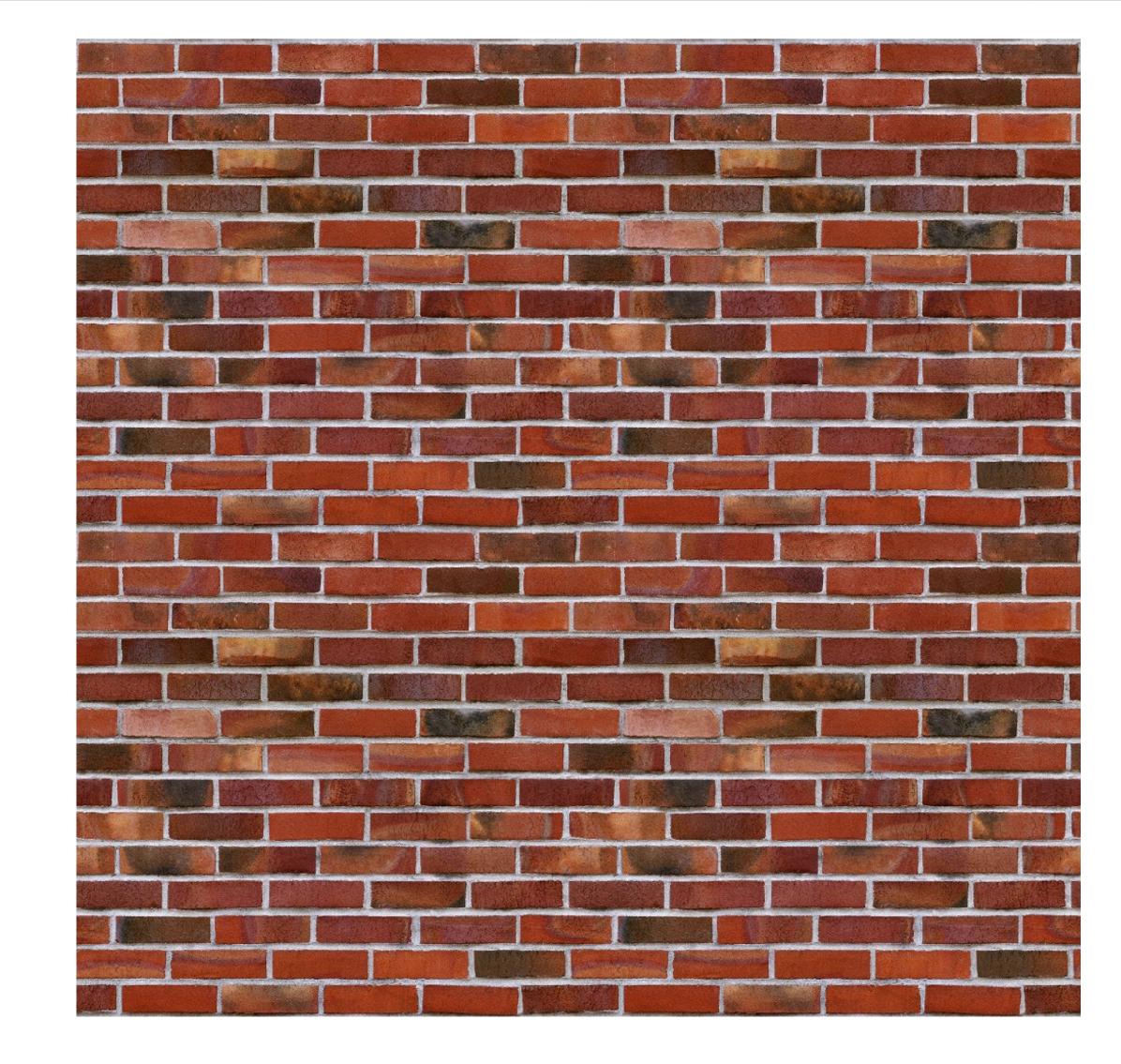
- Tiling textures might introduce seams - discontinuities in the mapping function - change textures to be "tileable" when possible





Seamlessly "tileable" textures

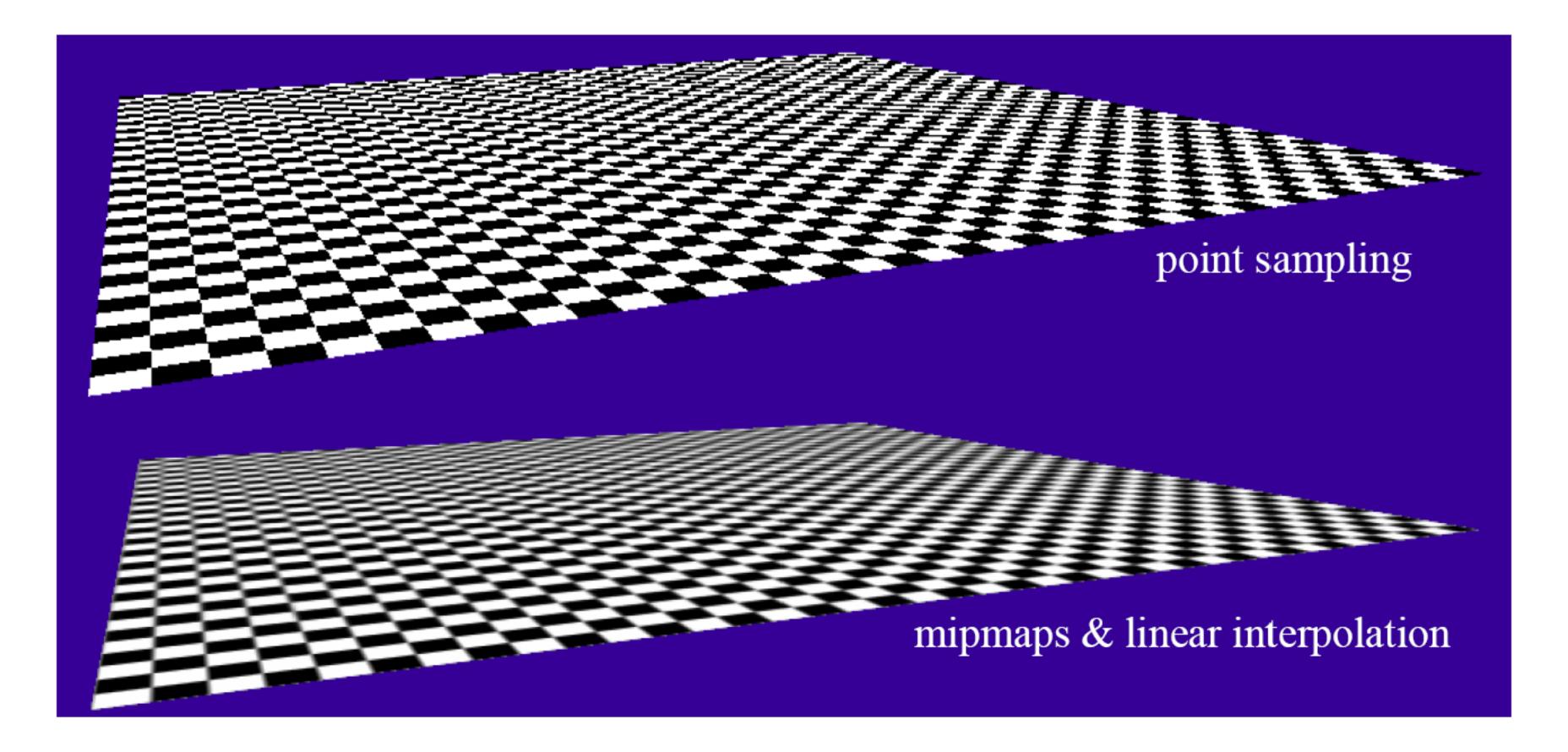






Texture minification (aliasing)

Point-sampling introduces artifacts (aliasing) - need average of texture within area of a pixel



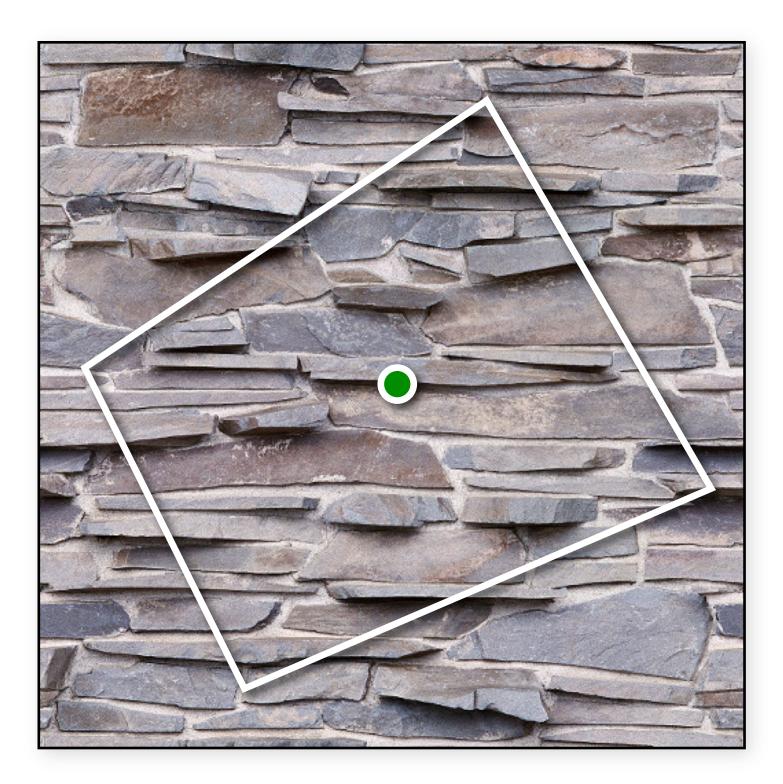


Texture minification

- In ray tracing, in theory, you're already sending many rays randomly through area of pixel
- Minification artifacts will go away, eventually
- In production, texture filtering techniques still useful for improved speed/quality
- mipmapping
- ripmapping
- summed area tables



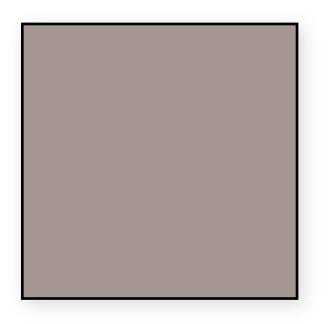
Texture filtering - minification





point sample

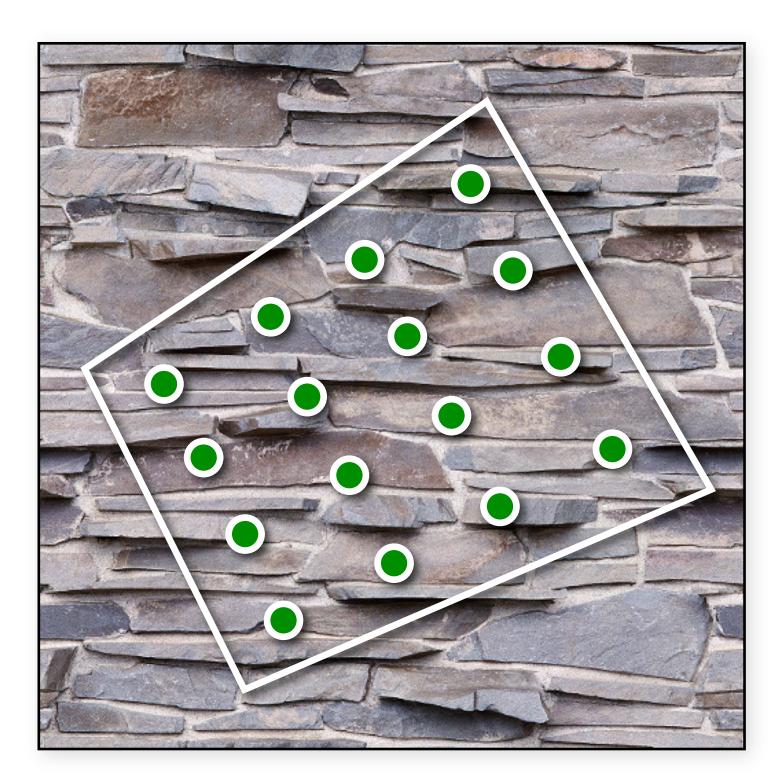


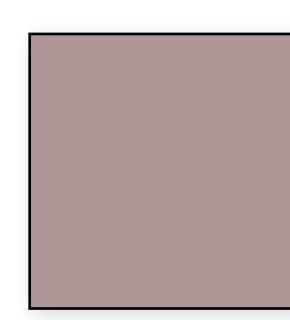


area average



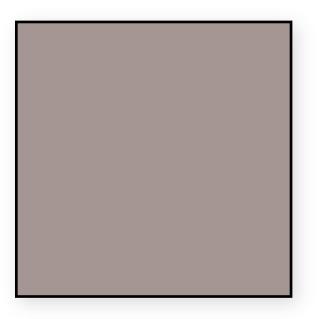
Texture filtering - minification





4×4 supersampling expensive!





area average



Mipmapping

Store textures at different resolutions

Look up in appropriate image based on projected pixel size

olutions based on











Mipmapping

Bilinear: Look up in closest resolution and bilinearly interpolate

- transition artifacts

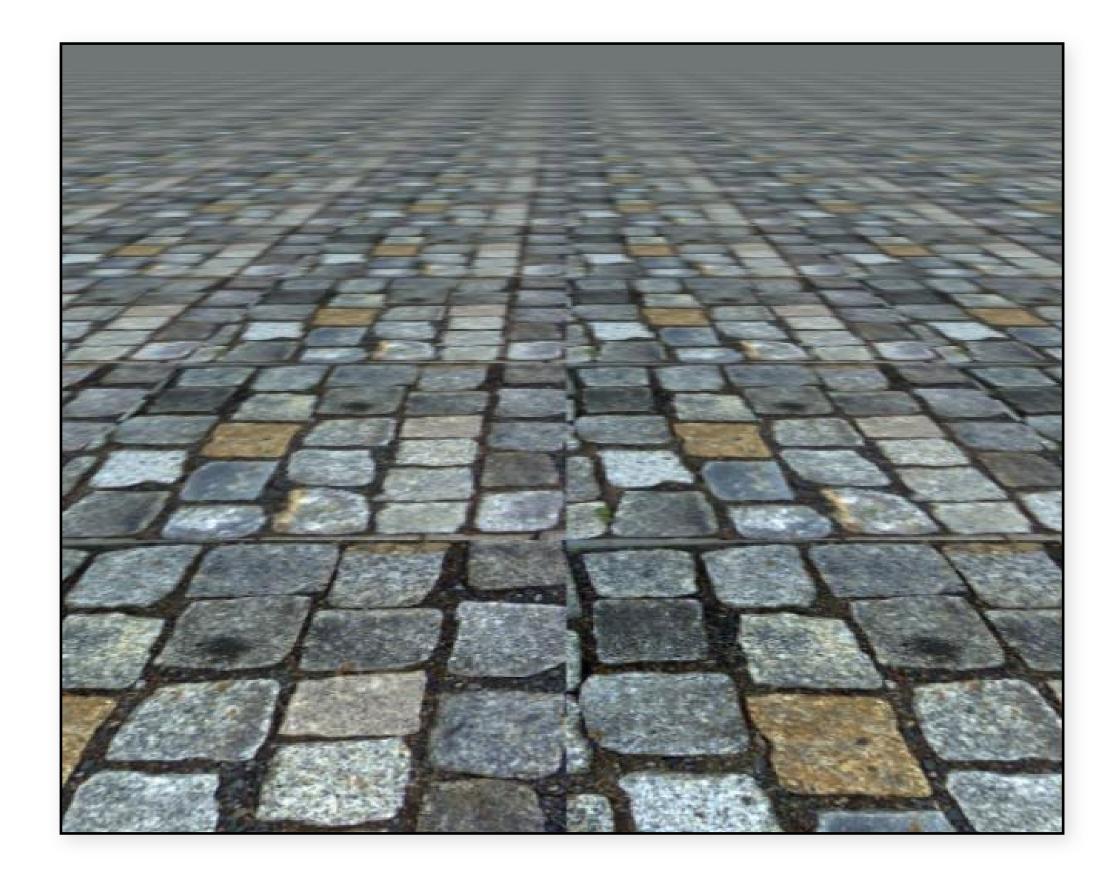
Trilinear: linearly interpolate between two closest levels





Mipmapping

Mipmaps average in squares, but pixel footprints are not square! → overblurring





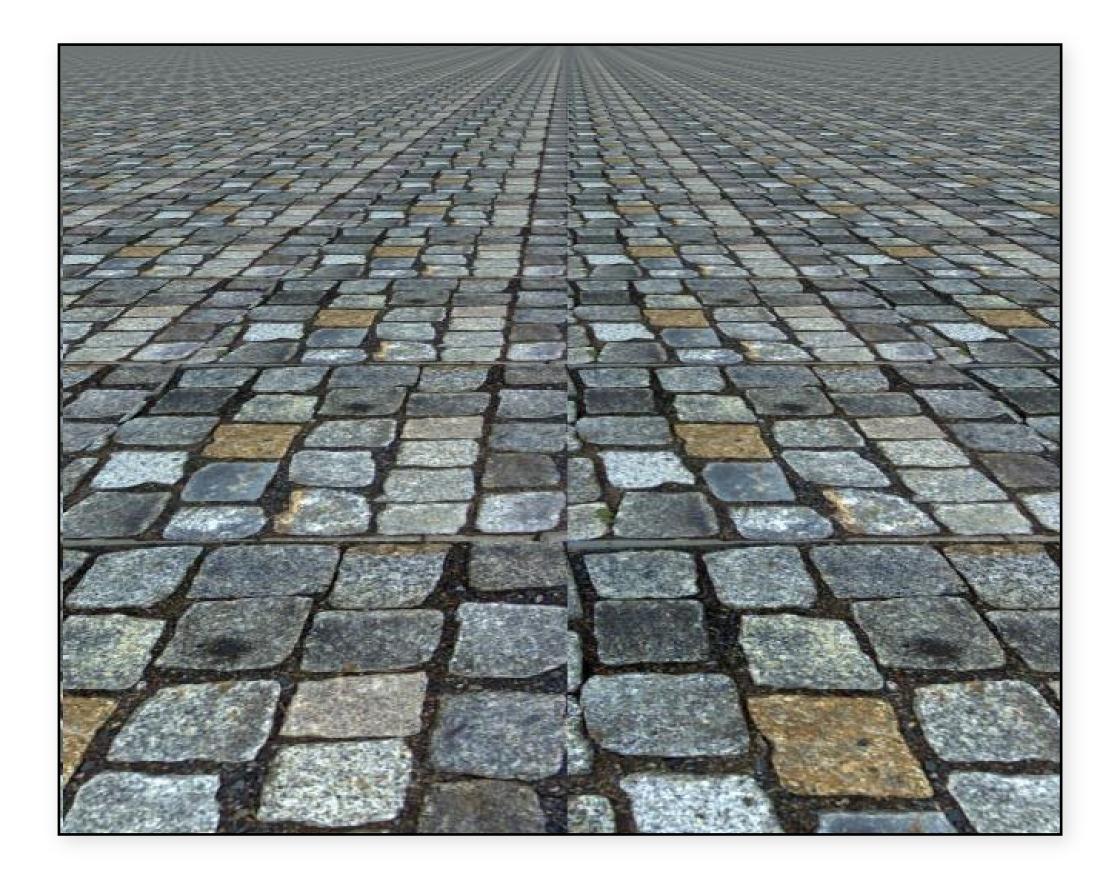






Ripmap

One possible improvement: - downscale independently in x, y







So far

How do we map between surface and texture?

- parametric surfaces
- projection mapping
- uv texturing
- texture lookup



Agenda

- What do we map onto the surface? - reflectance (color, diffuse + specular coeffs., etc) - surface normal (bump mapping)
- geometry (displacement mapping)
- illumination (environment, reflection, shadows)



Texturing reflectance properties

Texture mapping

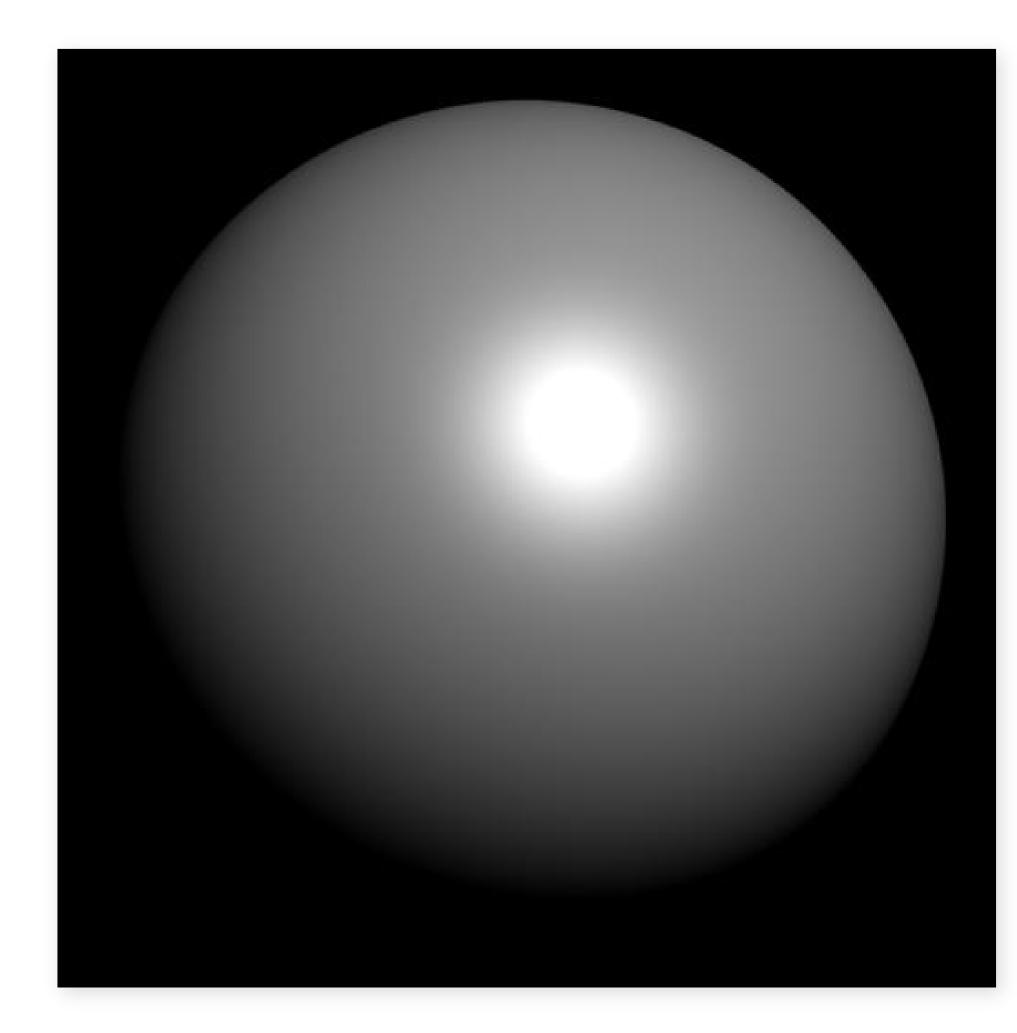
Surface properties are not the same everywhere

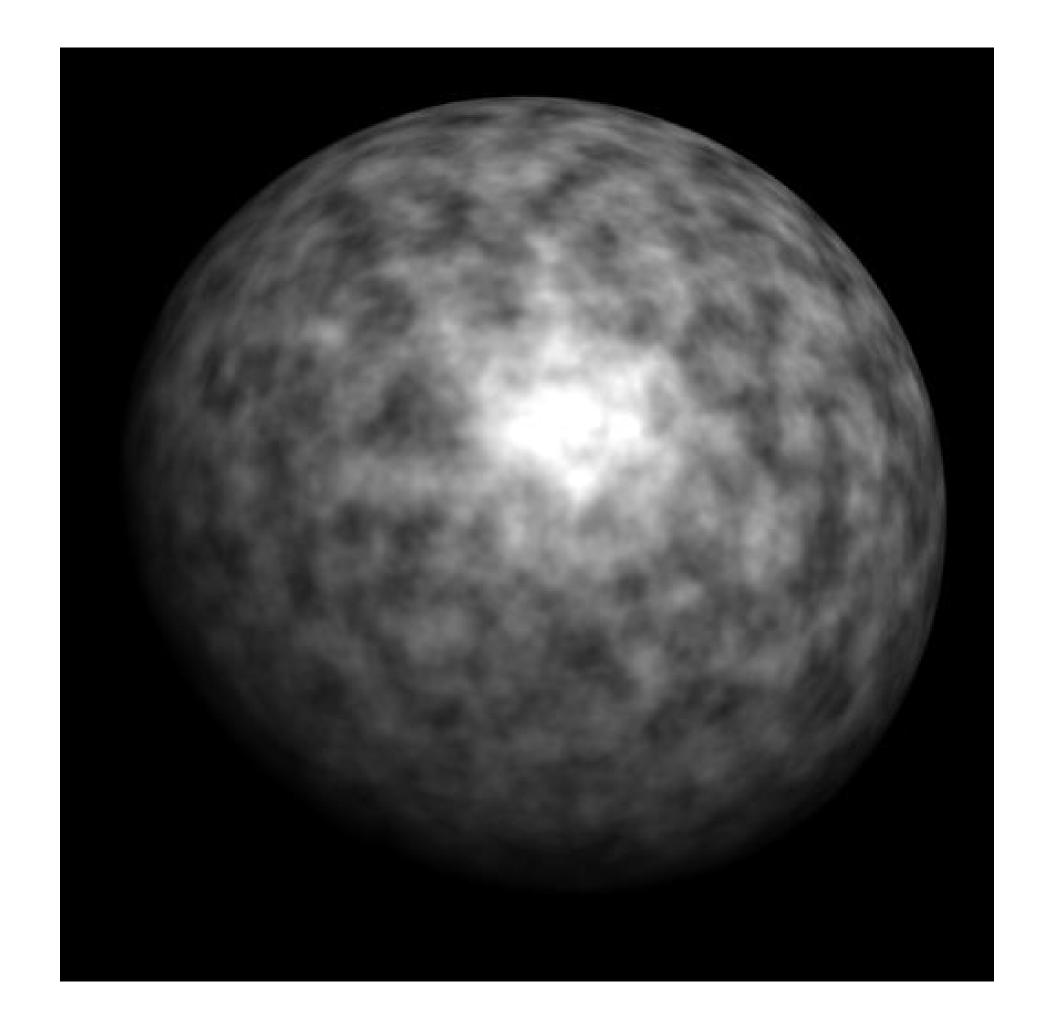
- diffuse color varies due to changing pigmentation
- roughness varies due to changing roughness and surface contamination

e same everywhere nging pigmentation ging roughness and surface



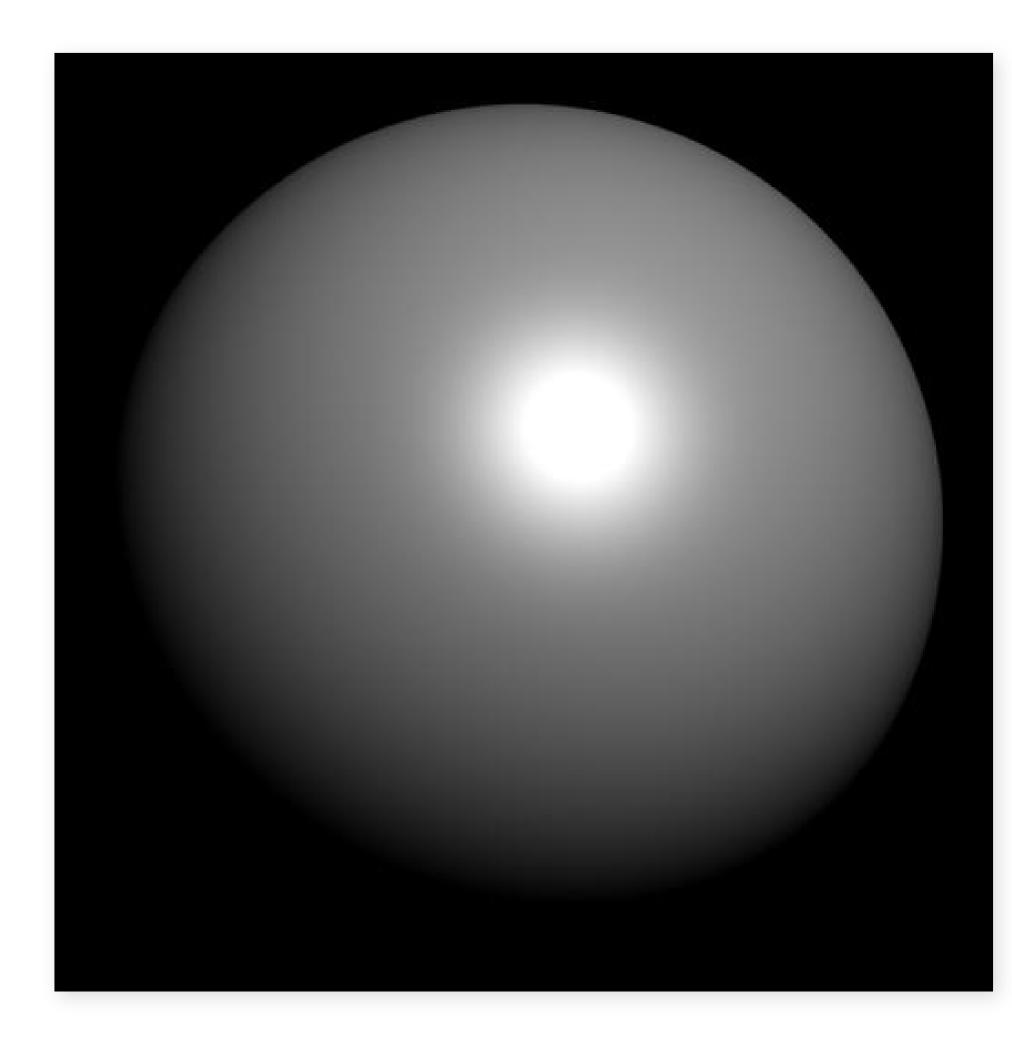
Diffuse coefficient



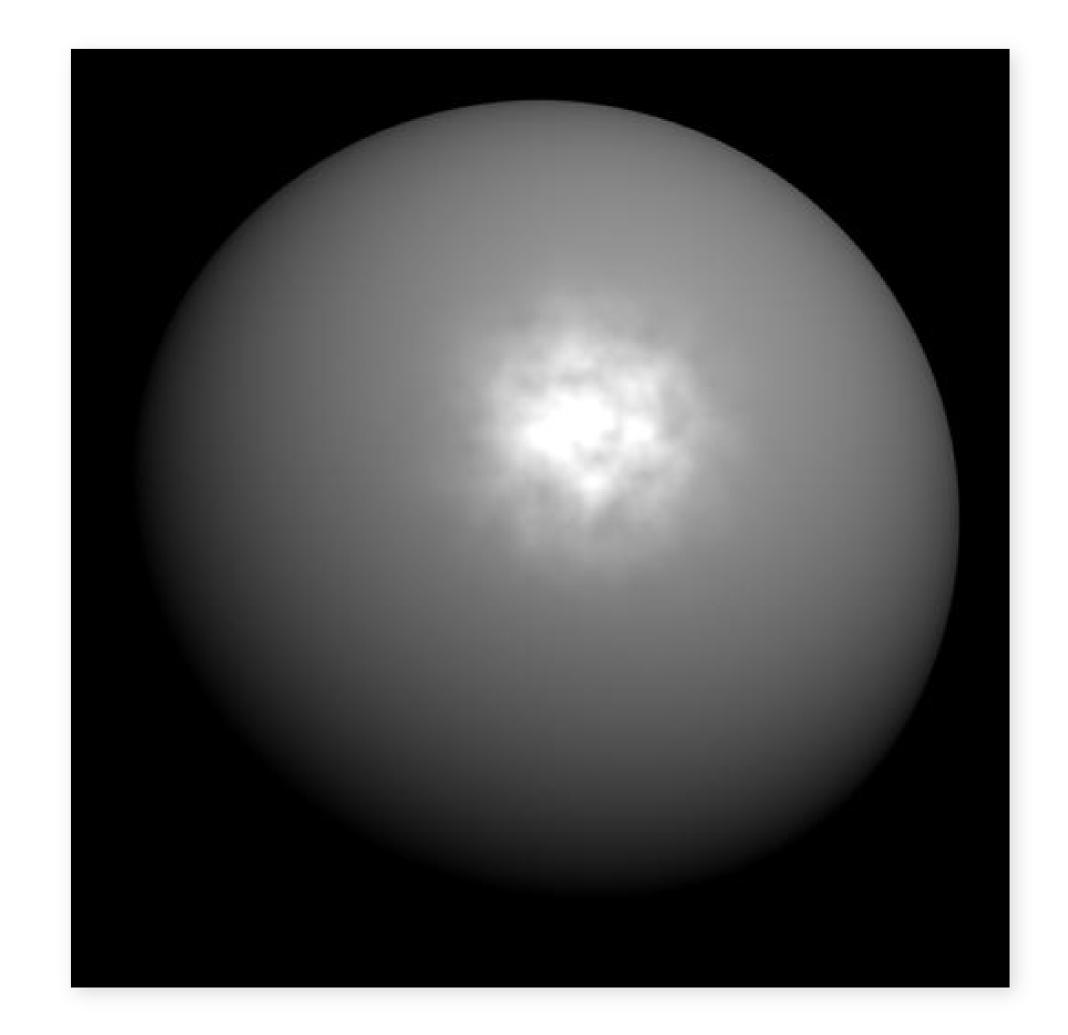




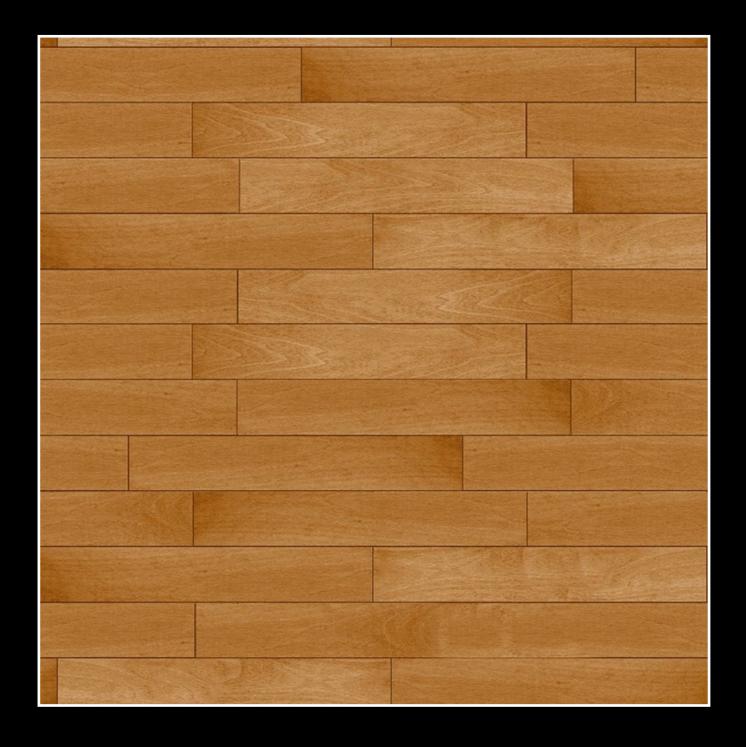
Specular "shininess" coefficient



After a slide by Fabio Pellacini

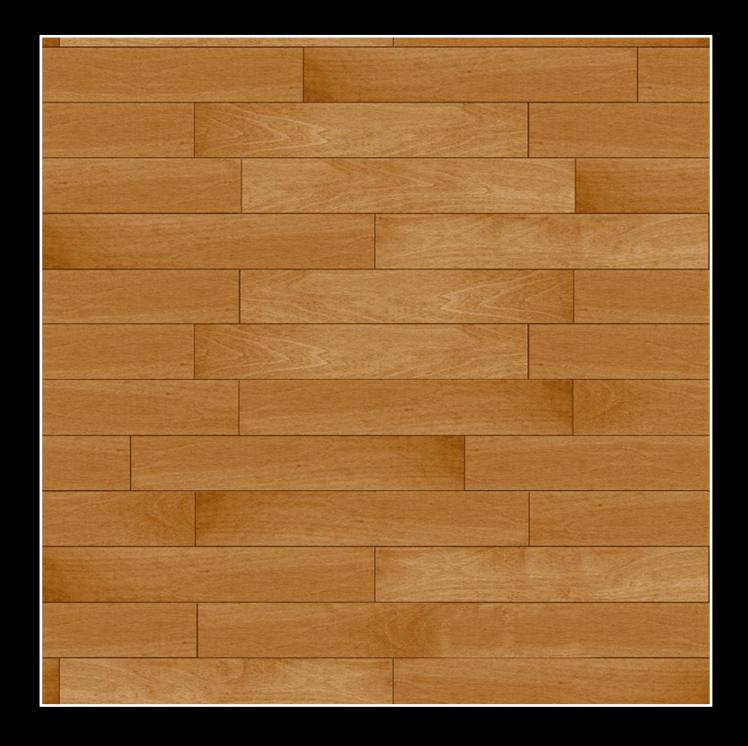






After a slide by Steve Marschner



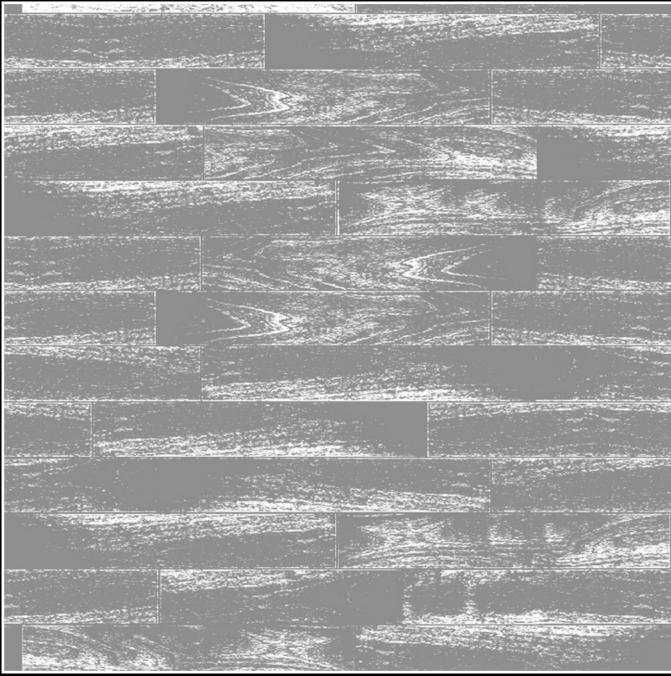


After a slide by Steve Marschner











detail

Texturing geometric

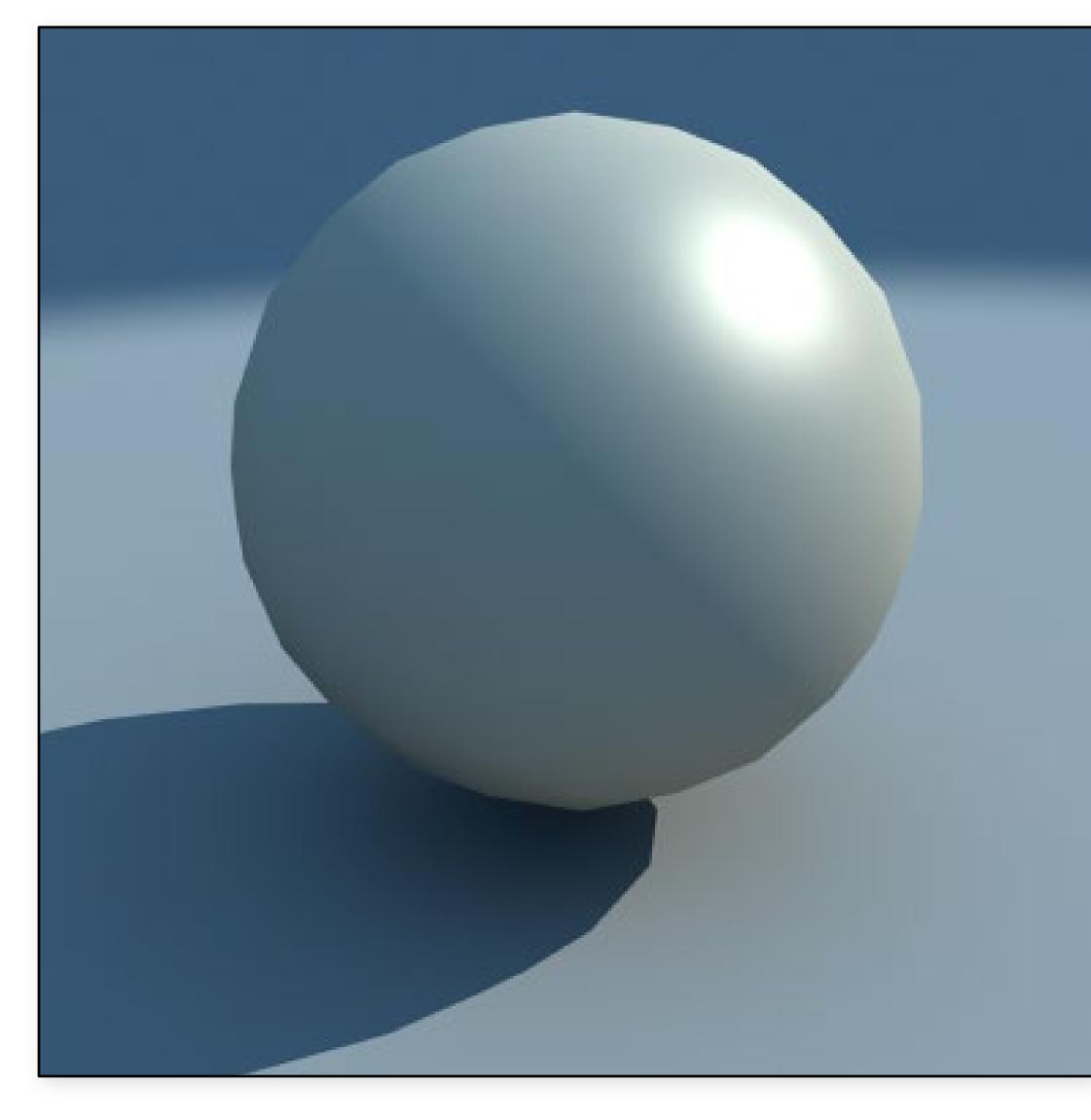
Texturing geometric detail

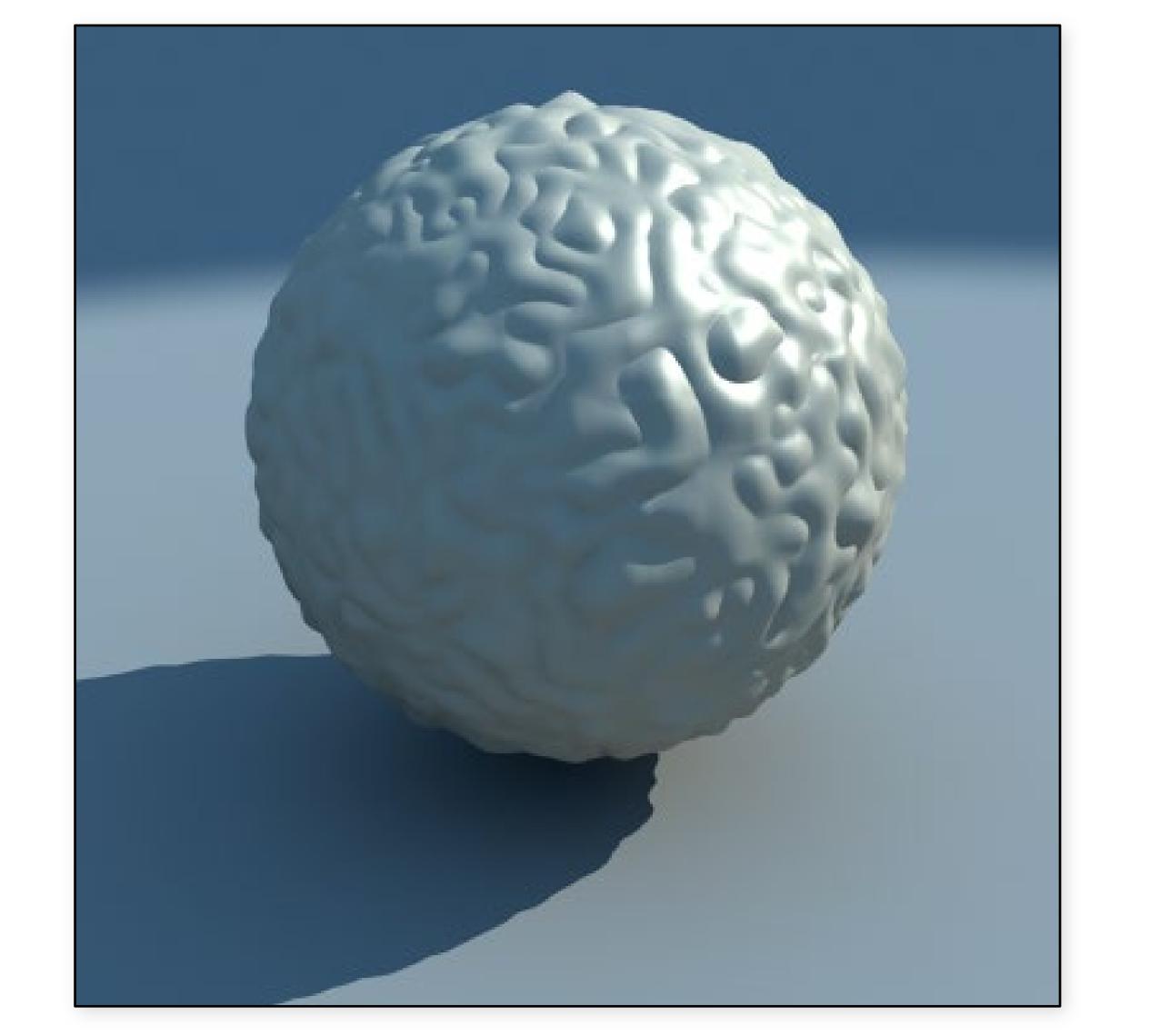
Modify geometric properties based on a texture

- normals
- surface positions



Displacement mapping





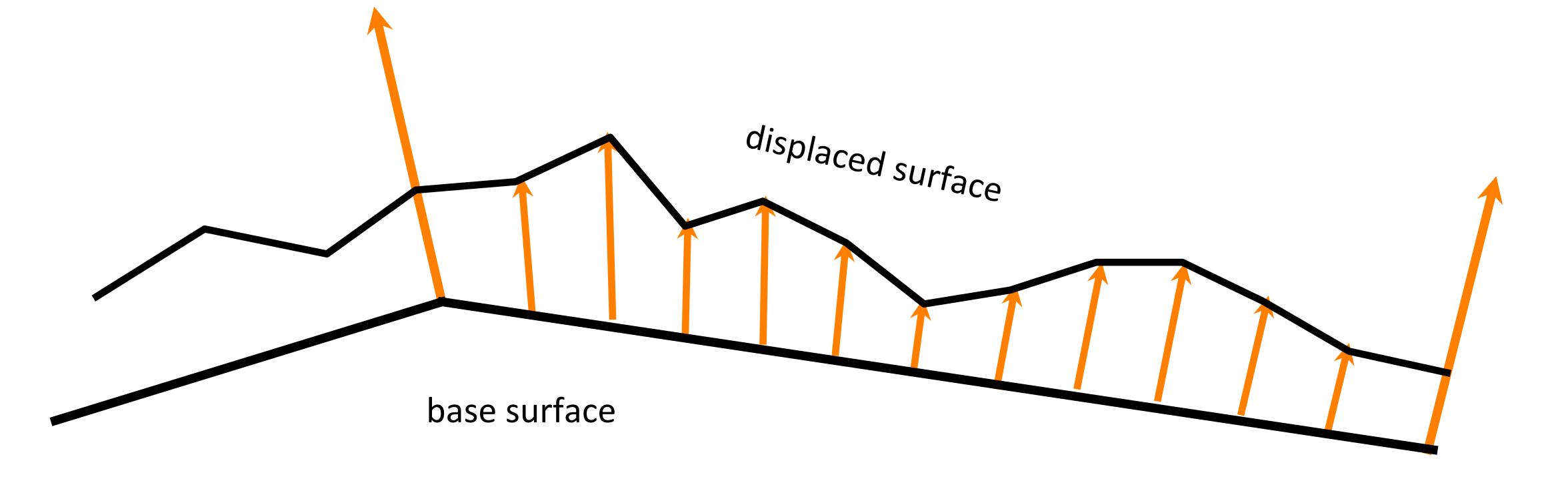
from: www.spot3d.com

74

Displacement mapping

Encode a displacement distance in the texture map

- Measured e.g. along interpolated normal

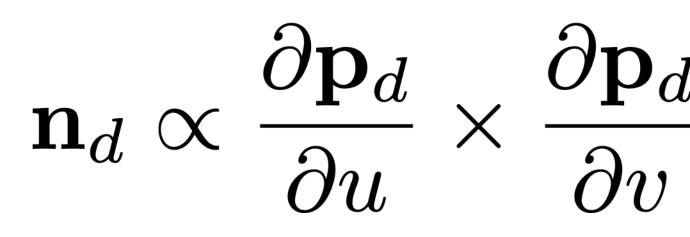


ce in the texture map ted normal



Displacement mapping Update position by displacing points along normal $\mathbf{p}_d = \mathbf{p} + h\mathbf{n}$

Recompute normals by evaluating derivatives - often no closed form solution, so use finite differences

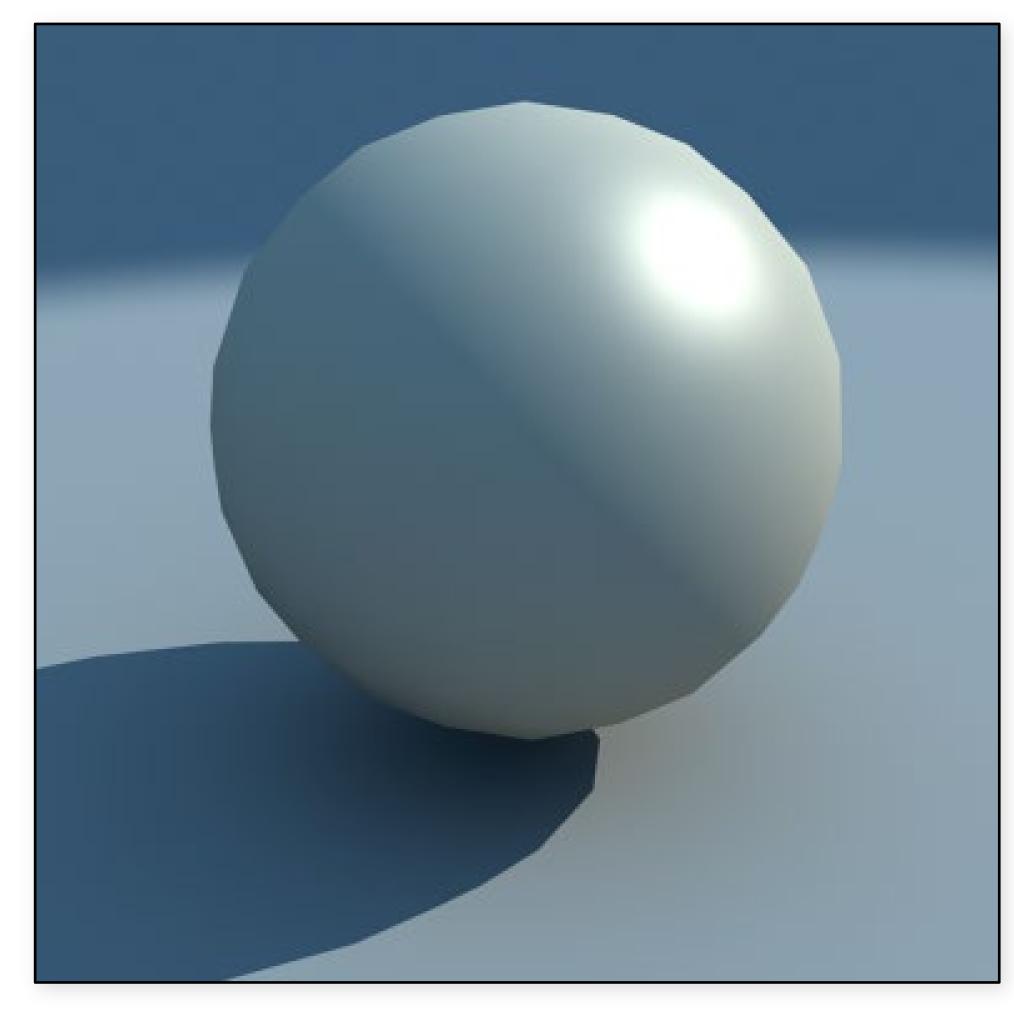


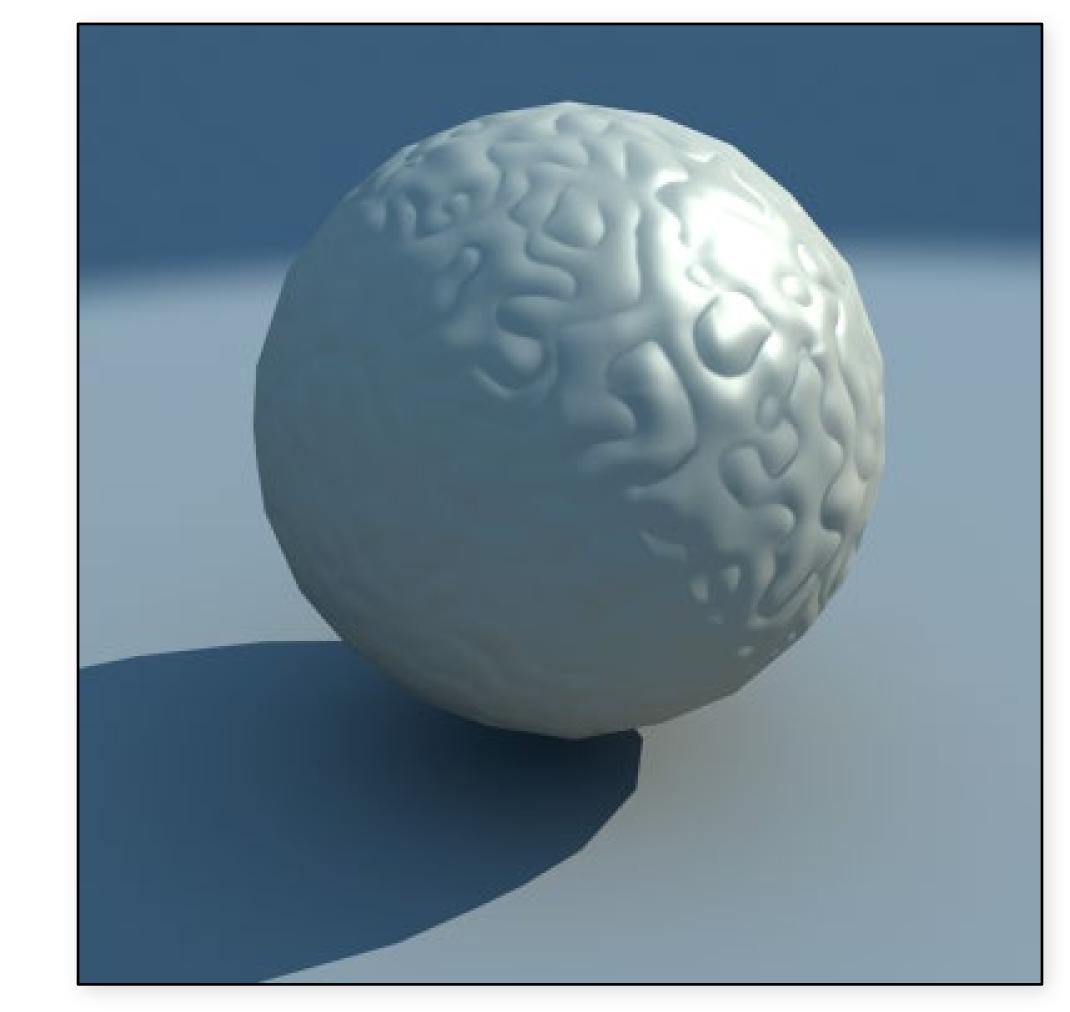
$$\frac{d}{v} \approx \frac{\Delta \mathbf{p}_d}{\Delta u} \times \frac{\Delta \mathbf{p}_d}{\Delta v}$$



Bump mapping

Apply normal perturbation without updating positions



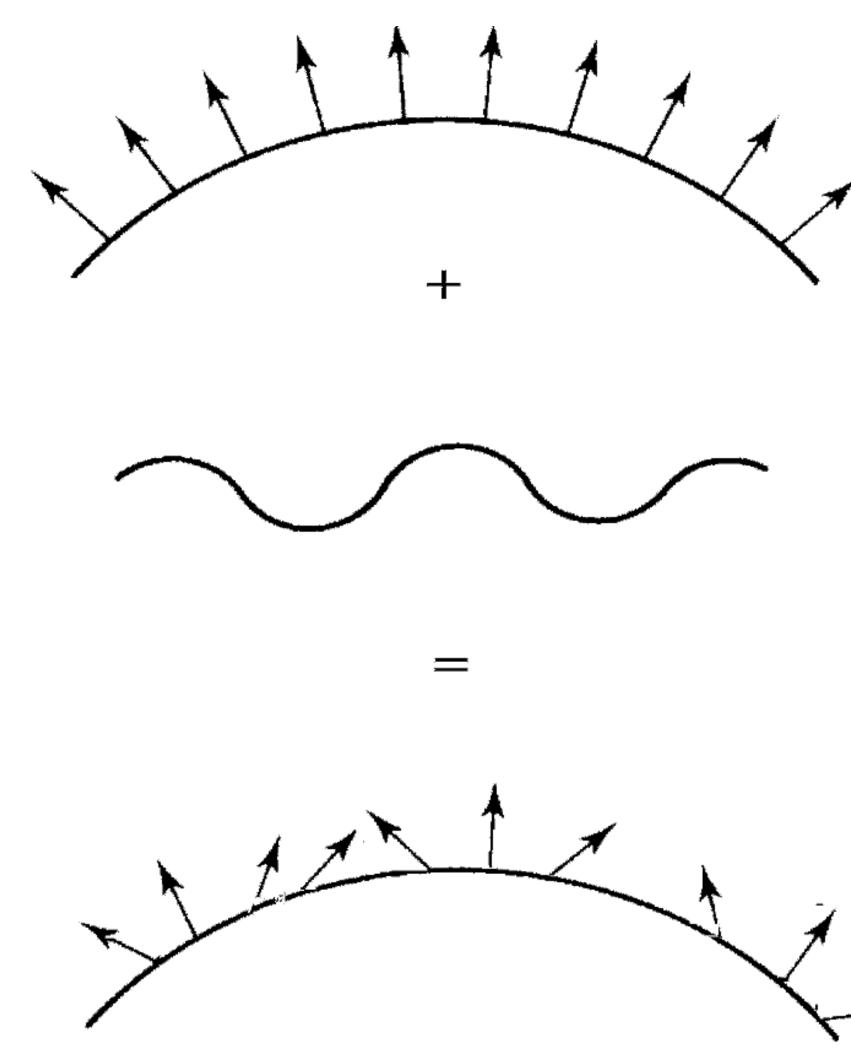


from: www.spot3d.com



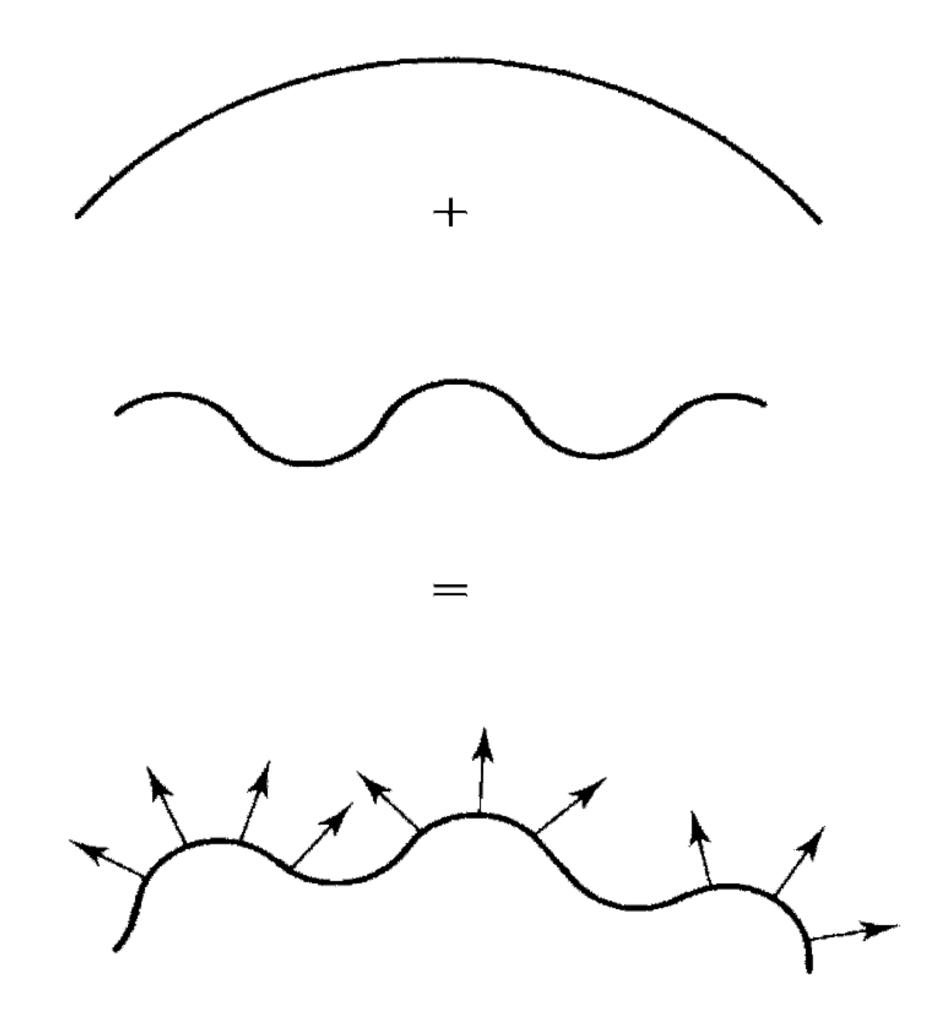
Bump vs. displacement mapping

bump map



After a slide by Fabio Pellacini

displacement map

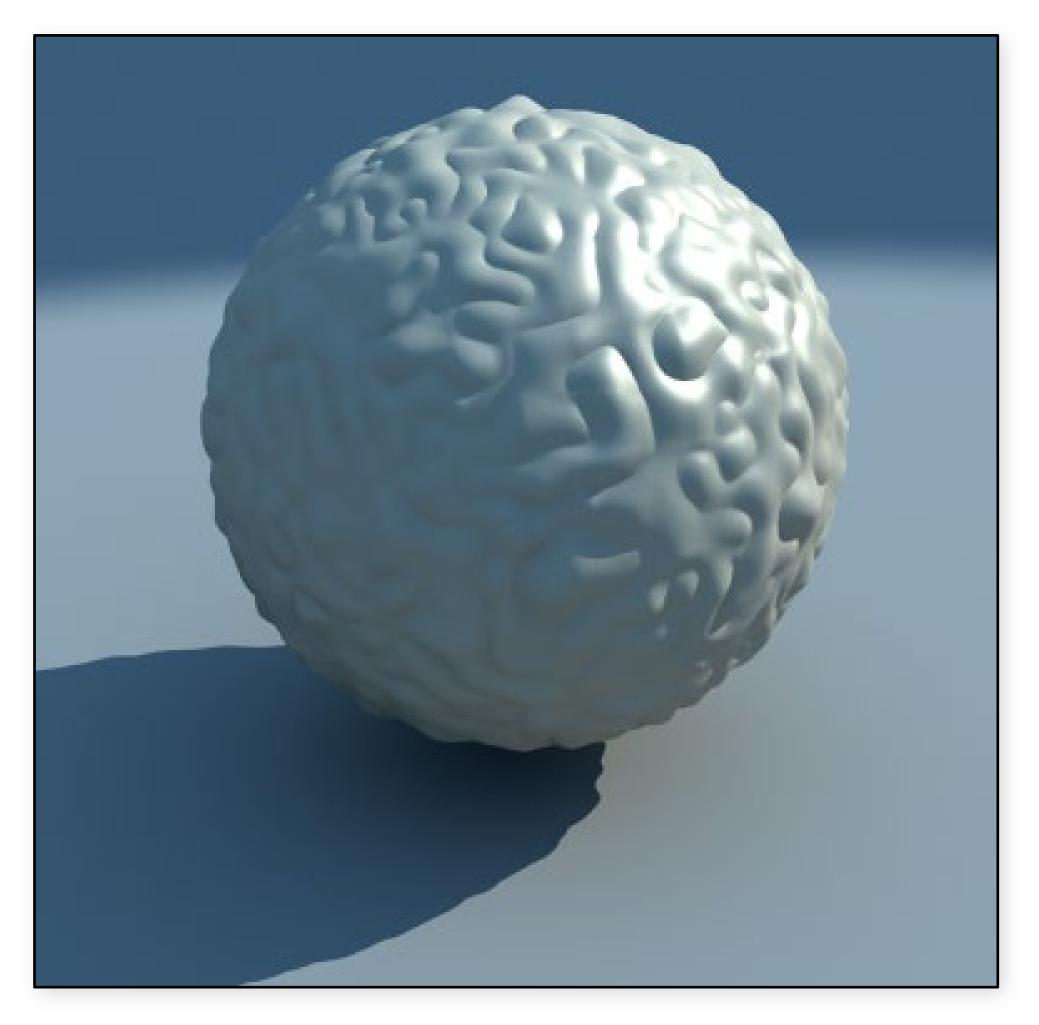


Bump vs. displacement mapping

bump map



displacement map



from: www.spot3d.com



Bump mapping example Bump mapping xy plane $\mathbf{p}_d(u, v) = \mathbf{p}(u, v) + h(u, v)\mathbf{n}$ **Recompute normals** $\mathbf{n}_d \propto \frac{\partial \mathbf{p}_d}{\partial u} \times \frac{\partial \mathbf{p}_d}{\partial v} = \left(\mathbf{x} + \frac{\partial h}{\partial u}\mathbf{z}\right) \times \left(\mathbf{y} + \frac{\partial h}{\partial v}\mathbf{z}\right)$ $= \mathbf{z} - \frac{\partial h}{\partial u} \mathbf{x} - \frac{\partial u}{\partial v} \mathbf{y}$

After a slide by Fabio Pellacini

 $= u\mathbf{x} + v\mathbf{y} + h(u, v)\mathbf{z}$



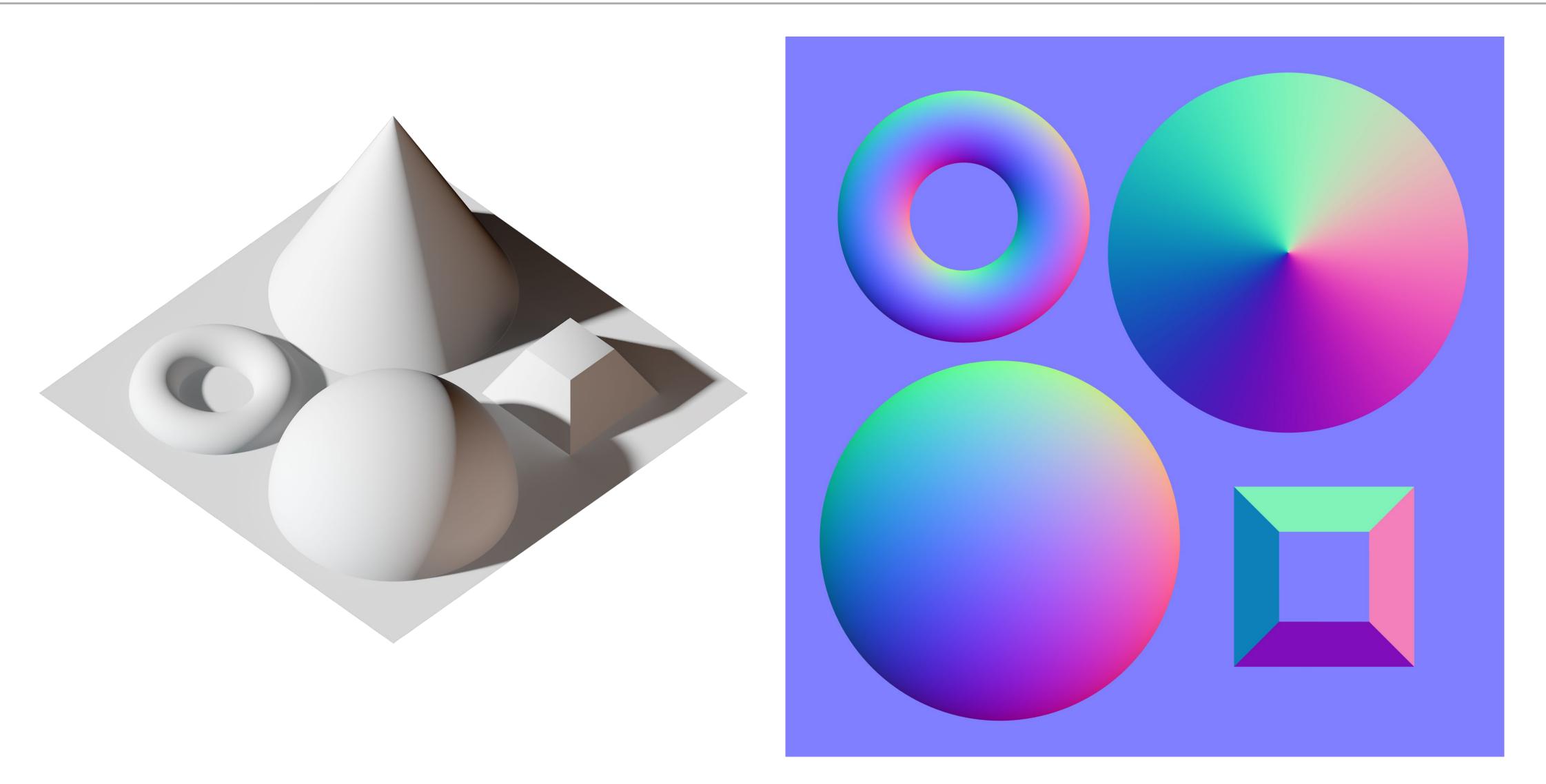
Displacement vs. bump mapping

Max Displace 1.5Mil

Normal Map 2900Tris

Wire

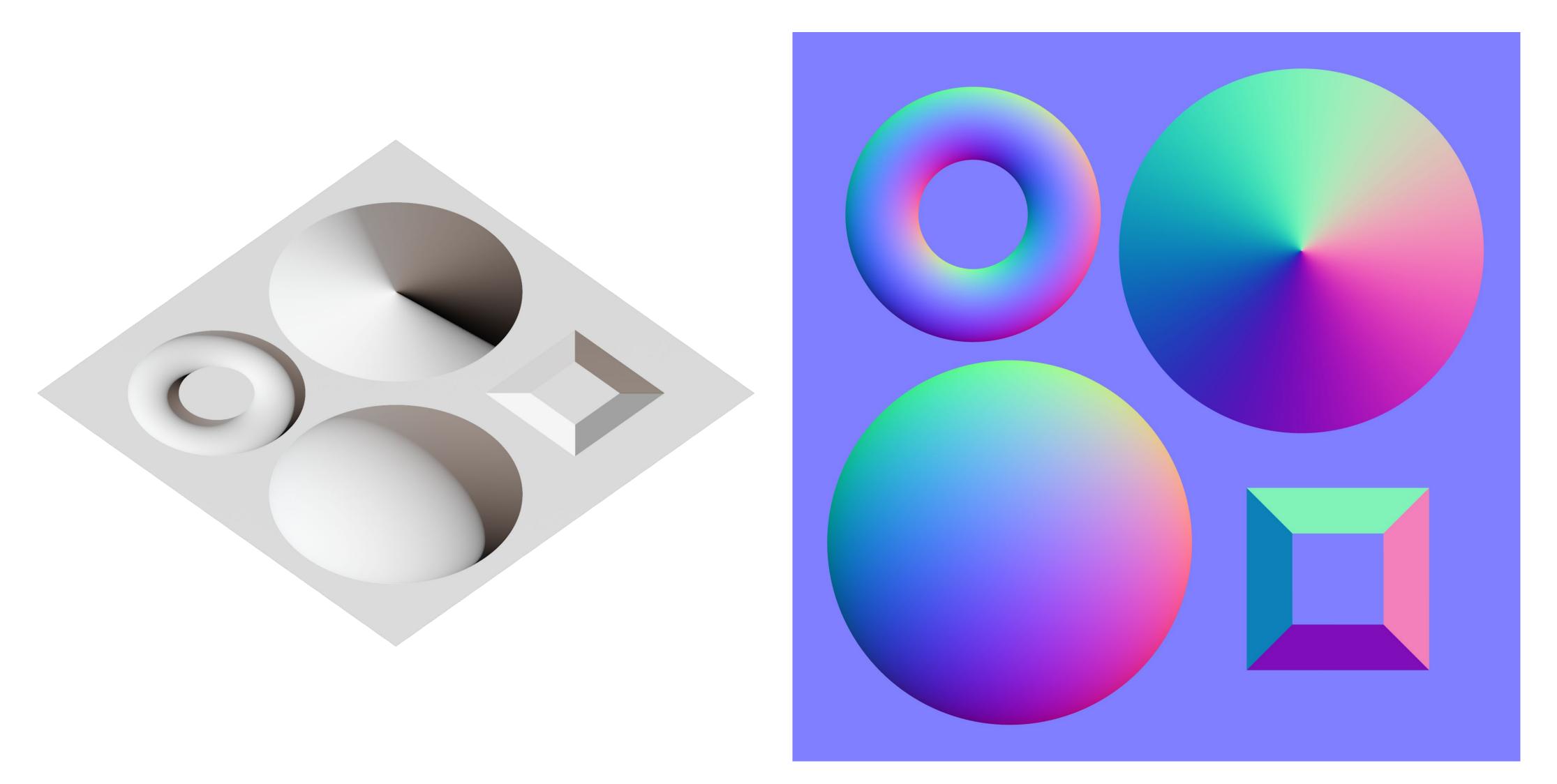
Surface normals



[Wikipedia]



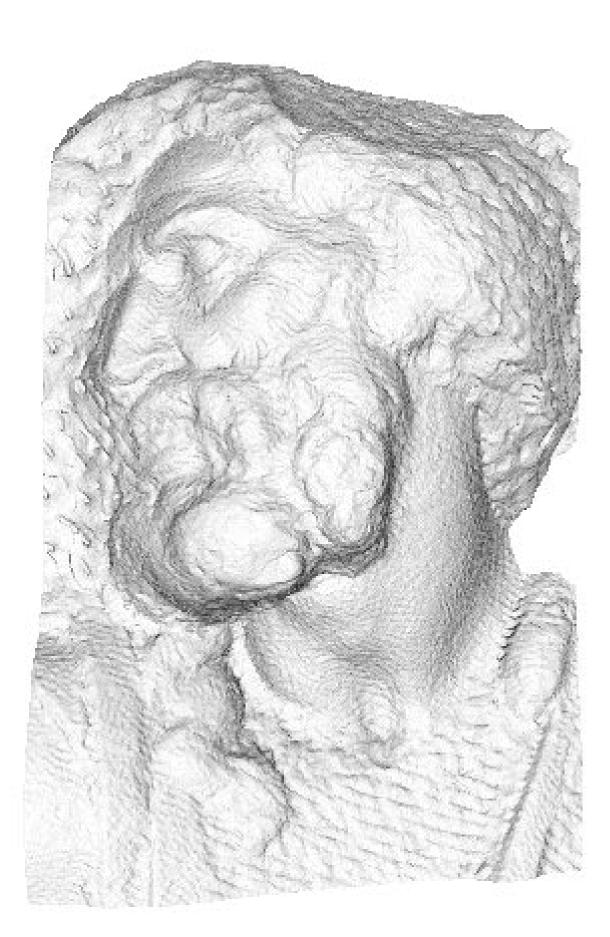
Normal mapping

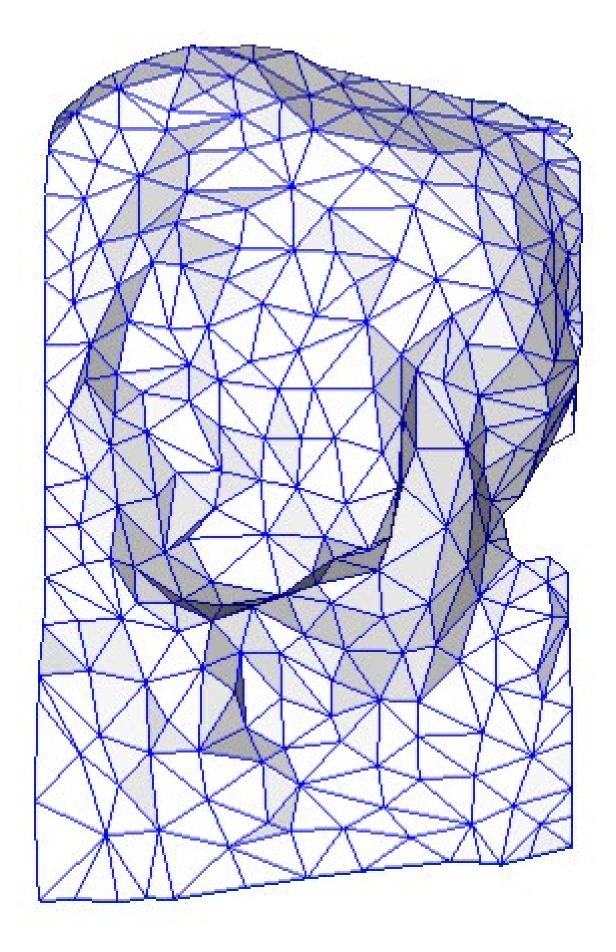


[Wikipedia]



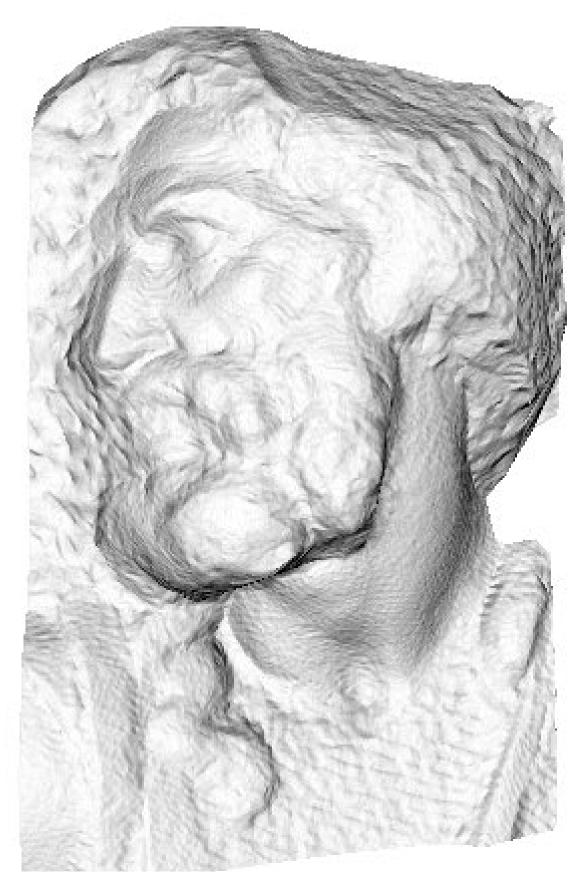
Normal mapping





original mesh 4M triangles

simplified mesh 500 triangles



simplified mesh and normal mapping 500 triangles



Environment & Reflection mapping

Shiny objects

The key to creating a realistic shiny-looking material is providing something for it to reflect.





Environment/reflection mapping

Sidesteps tedious modeling of the environment by representing it using one or more images

The image "wraps" around the virtual scene, serving as a source for reflections





Environment map

A function from the sphere to colors, stored as a texture.



After a slide by Steve Marschner



[Blinn & Newell 1976]



Reflection mapping (1982)



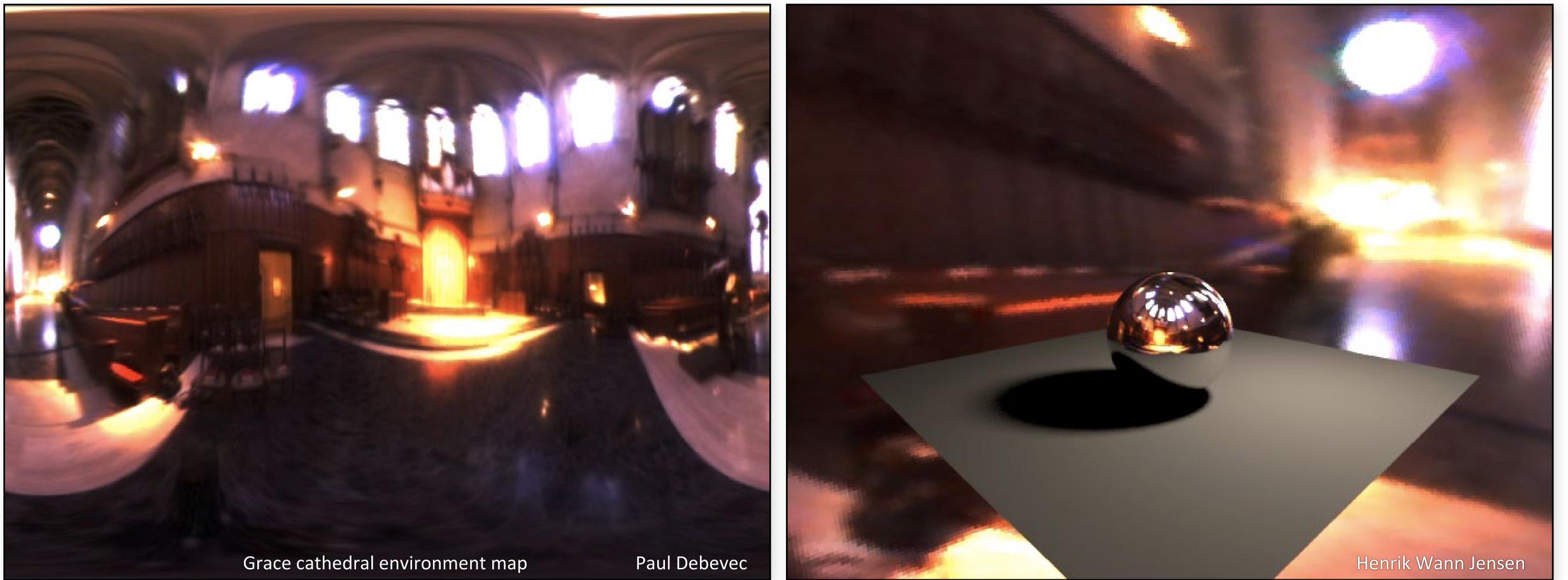


Terminator 2 (1991)





Environment mapping Ray tracing easy: rays that hit nothing look up in envmap





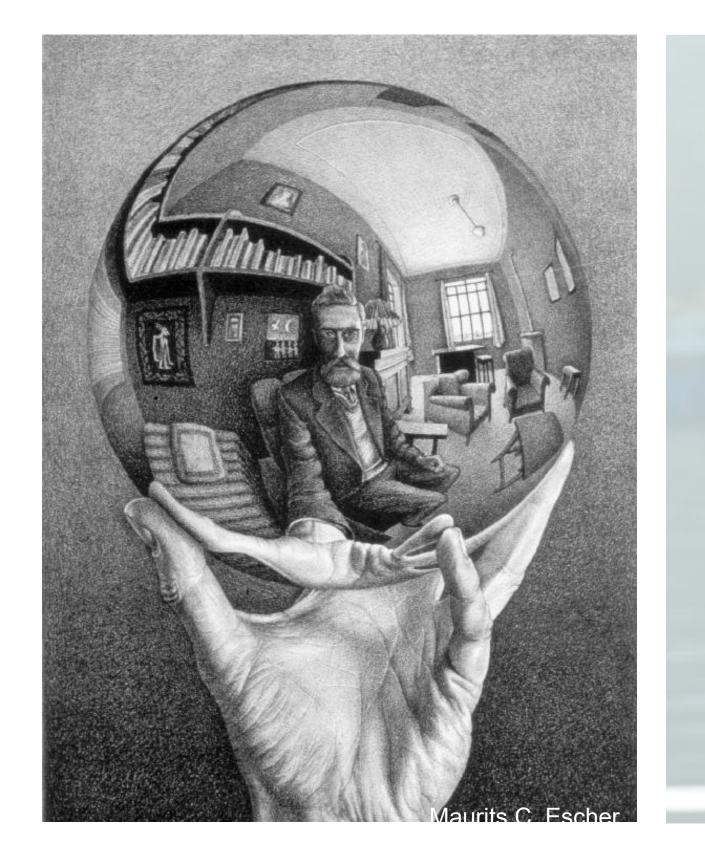
Acquiring environment maps

Mirrored ball + camera

- Fisheye lens images
- Stitching images together
- Panoramic camera



Acquisition - Low Tech.





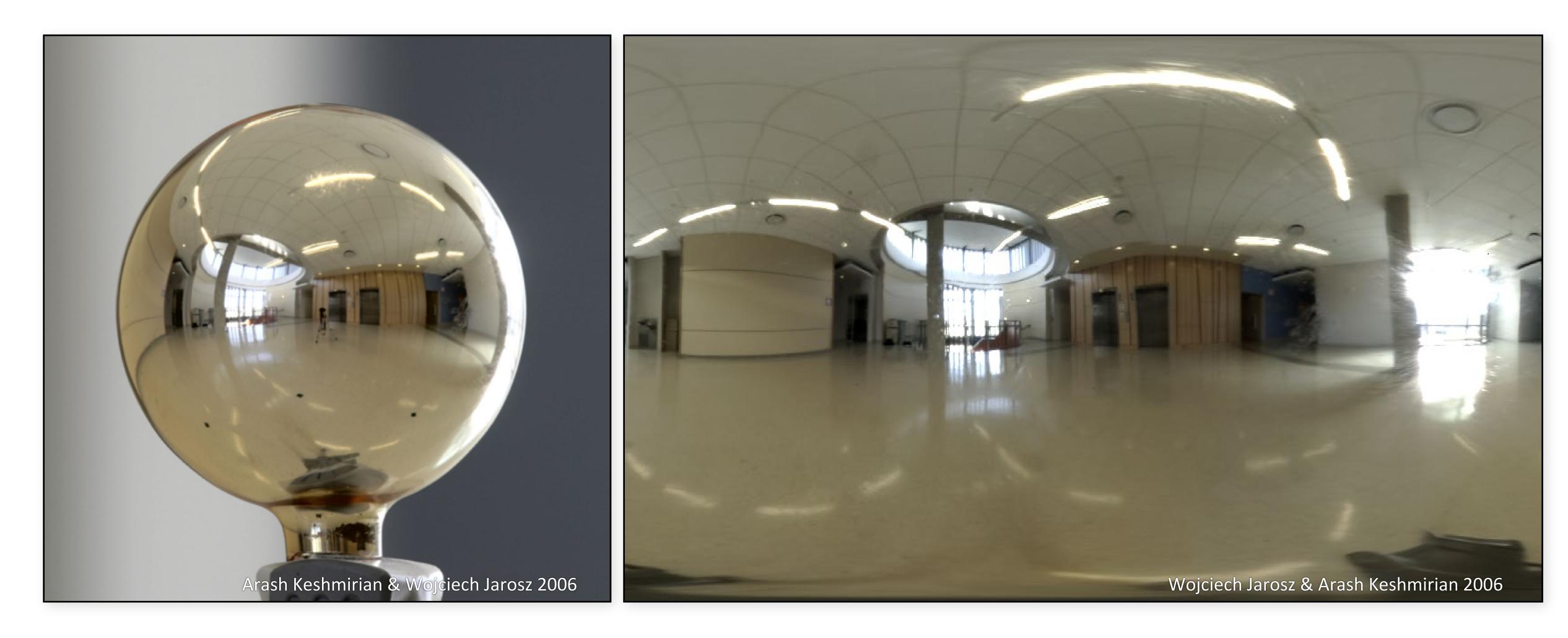
Lightprobe



omnidirectional, 360° panoramic, HDR image



Acquisition - Even Lower Tech.





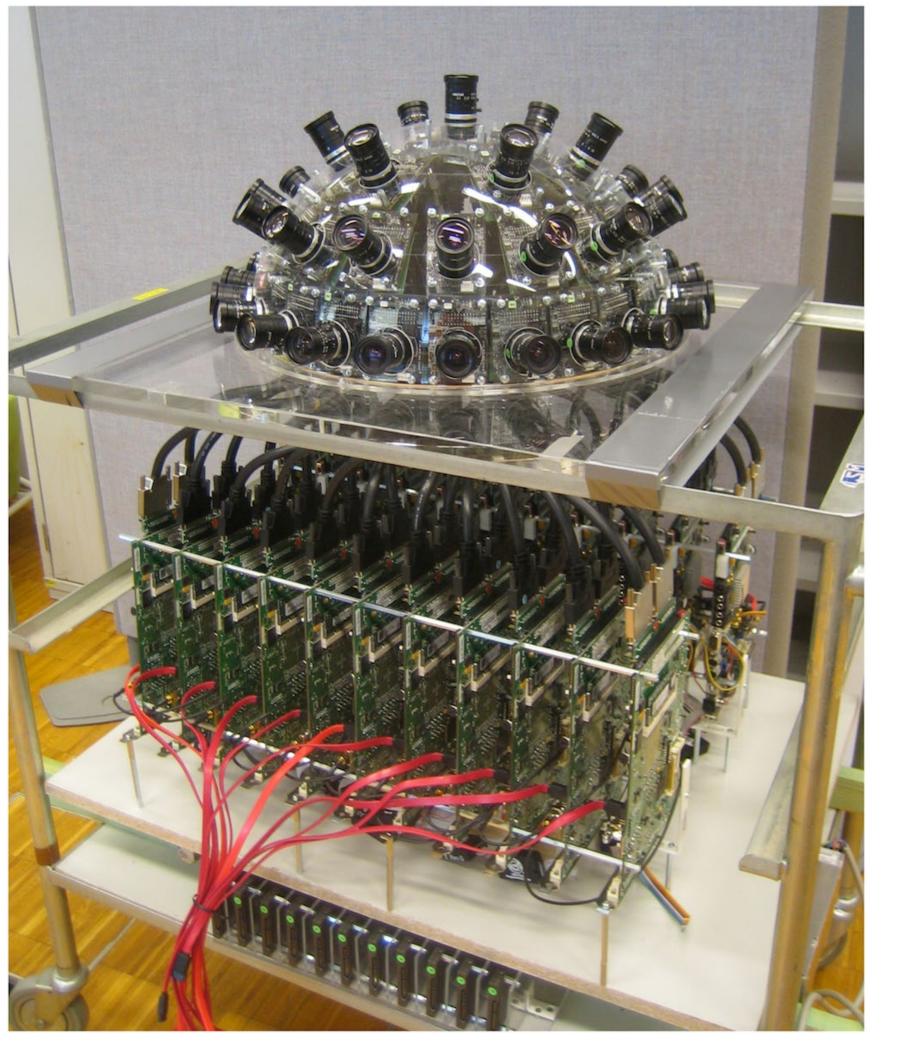
Acquisition - Stitched Panorama



source: photoanswers.co.uk



Acquisition - High Tech.



lsm.epfl.ch





immersivemedia.com



Acquisition









Storing environment maps

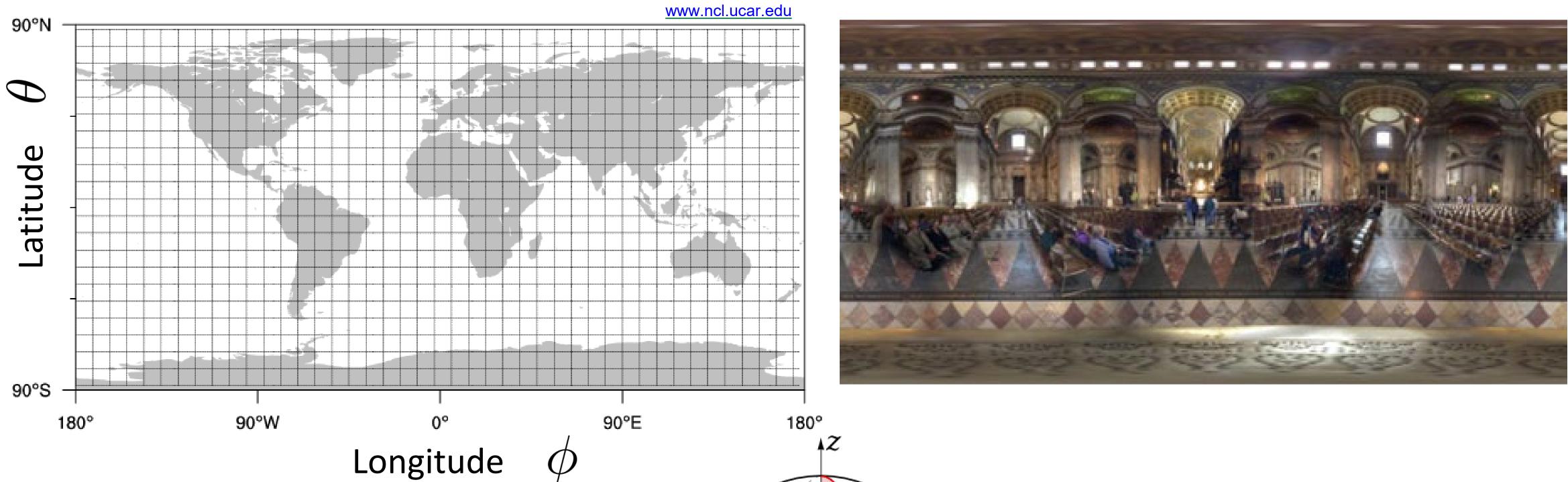
Various ways to parametrize environment maps

Related to cartography

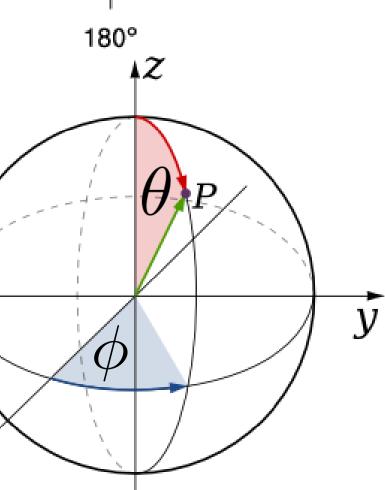
- Projecting the earth (sphere) onto a plane



Latitude/Longitude Map



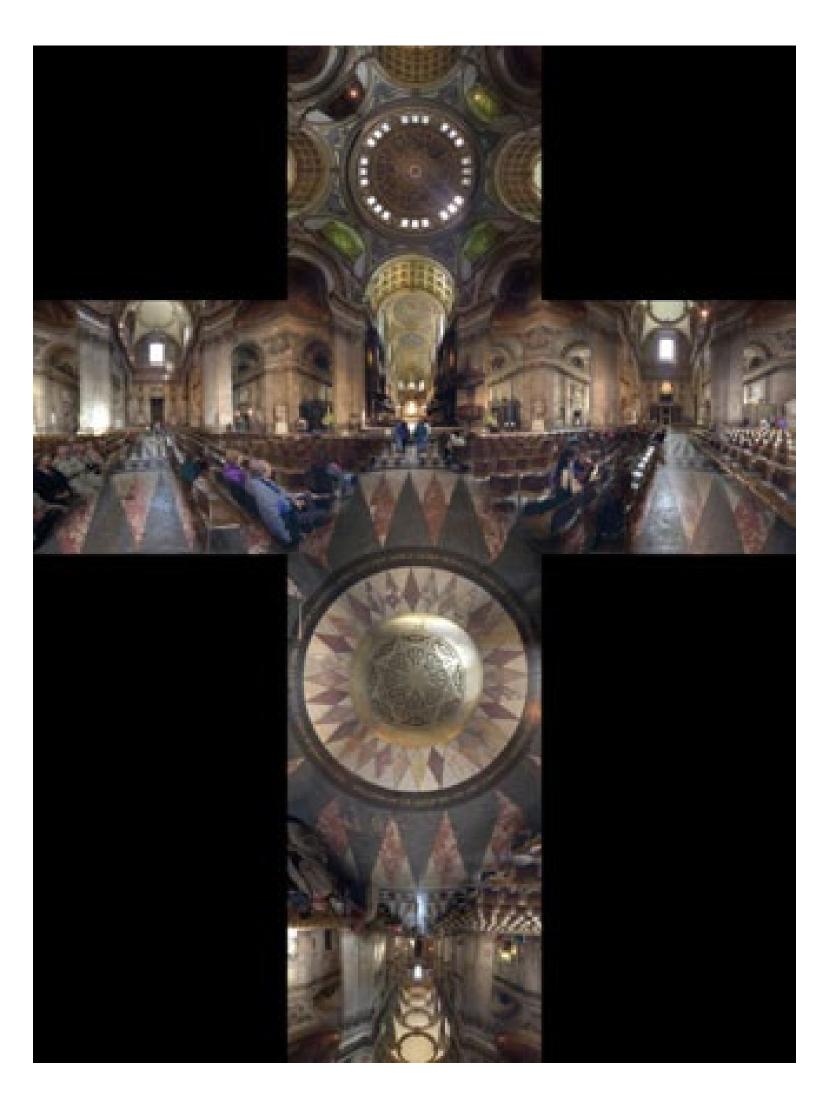
 $\boldsymbol{\chi}$





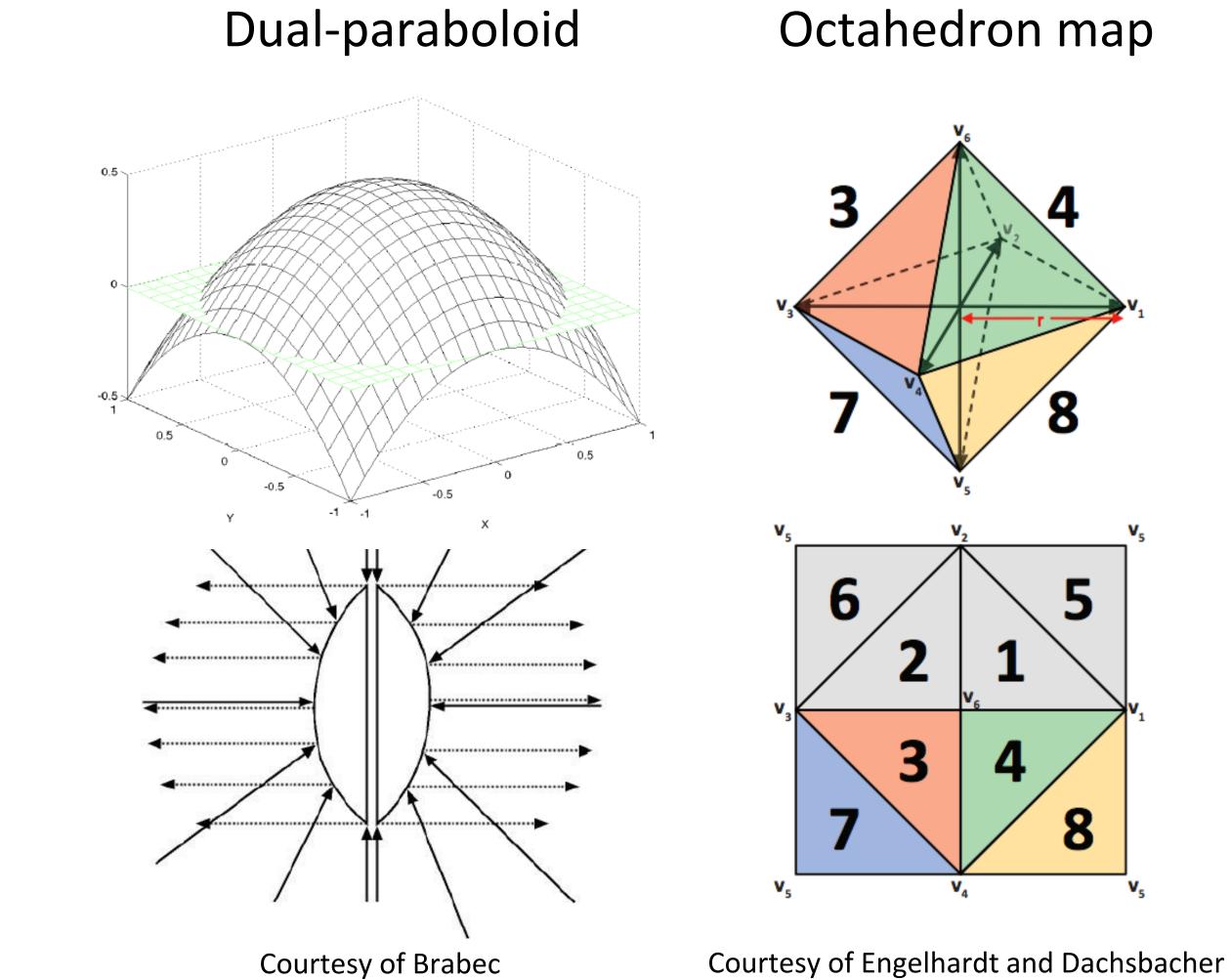
Cube Map (Skybox)

| | top | | |
|------|--------|-------|--|
| left | front | right | |
| | bottom | | |
| | back | | |

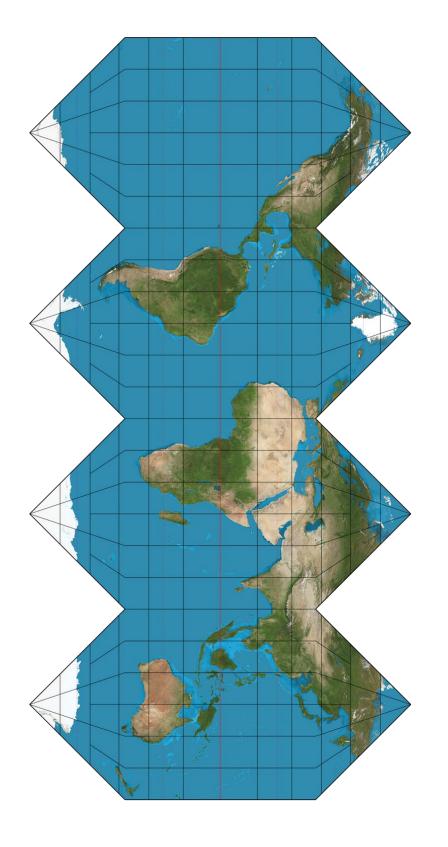




Other Parameterizations







Courtesy of Ryazanov

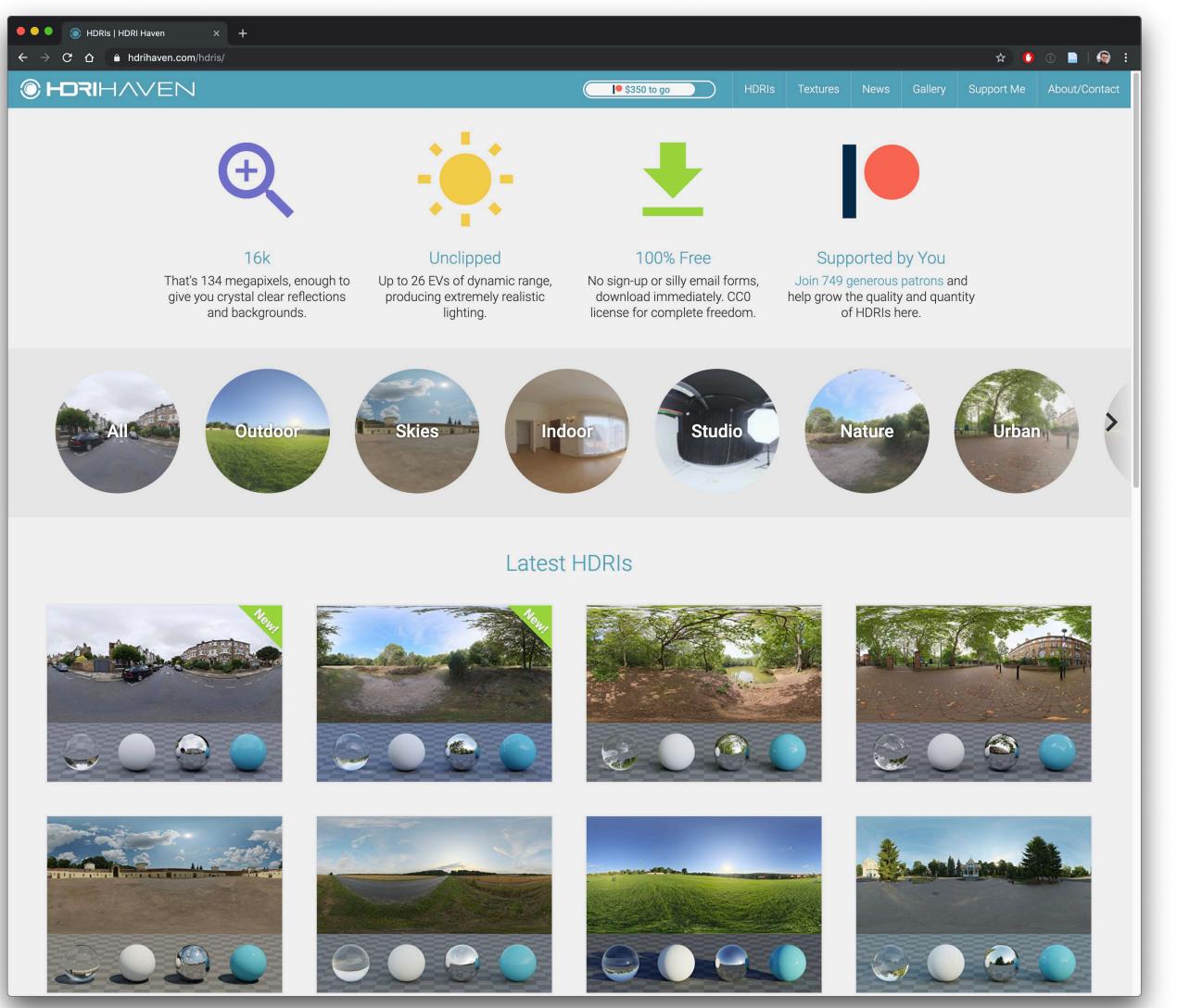


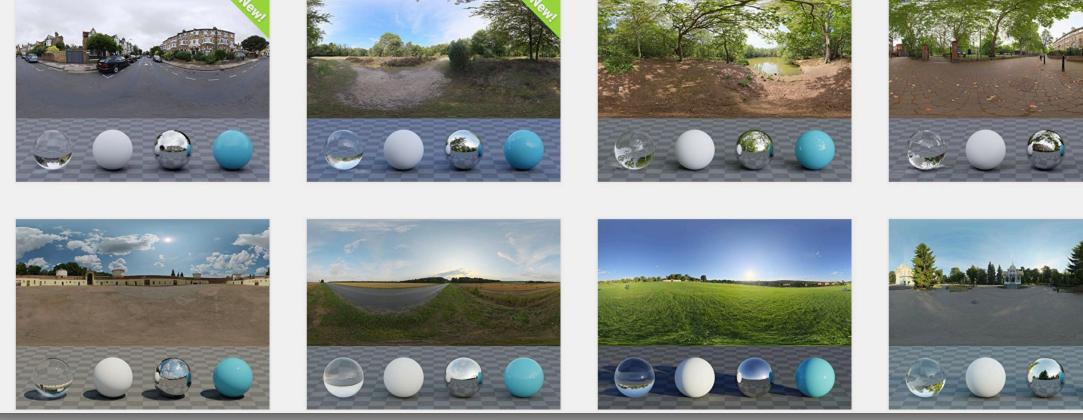
Get them online

hdrihaven.com

The original:

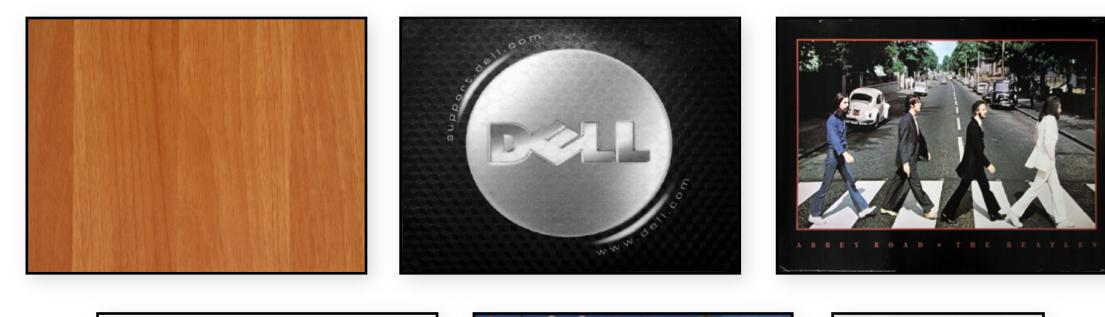
- www.pauldebevec.com/Probes
- gl.ict.usc.edu/Data/HighResProbes -

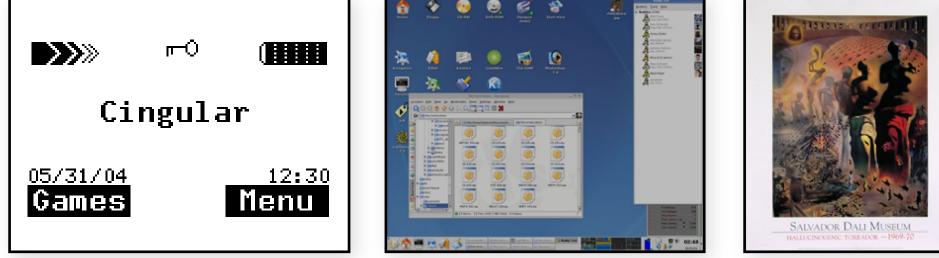


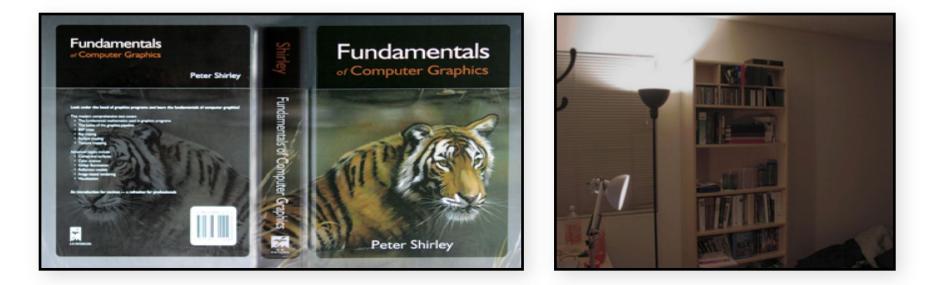




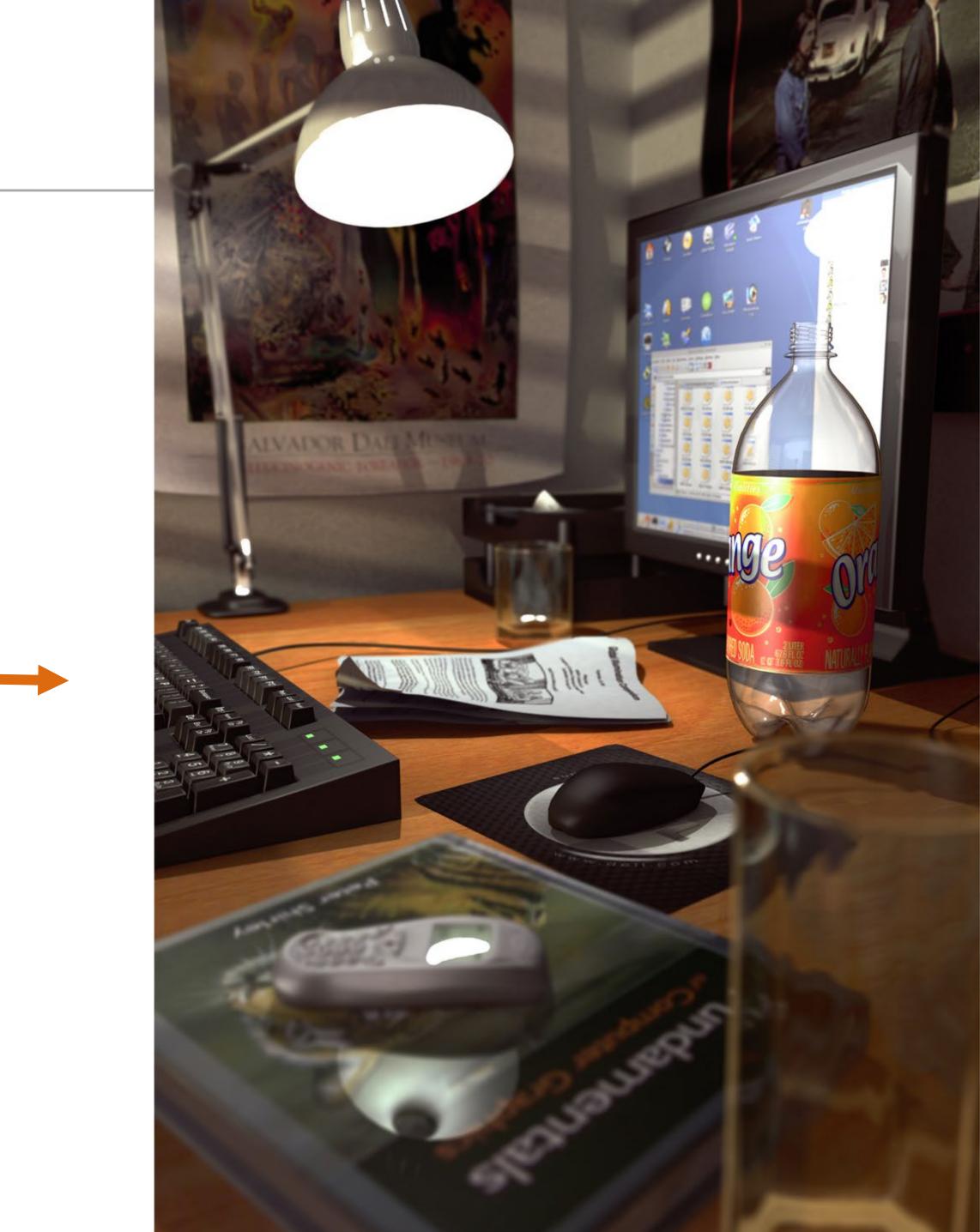
Exploit texturing!





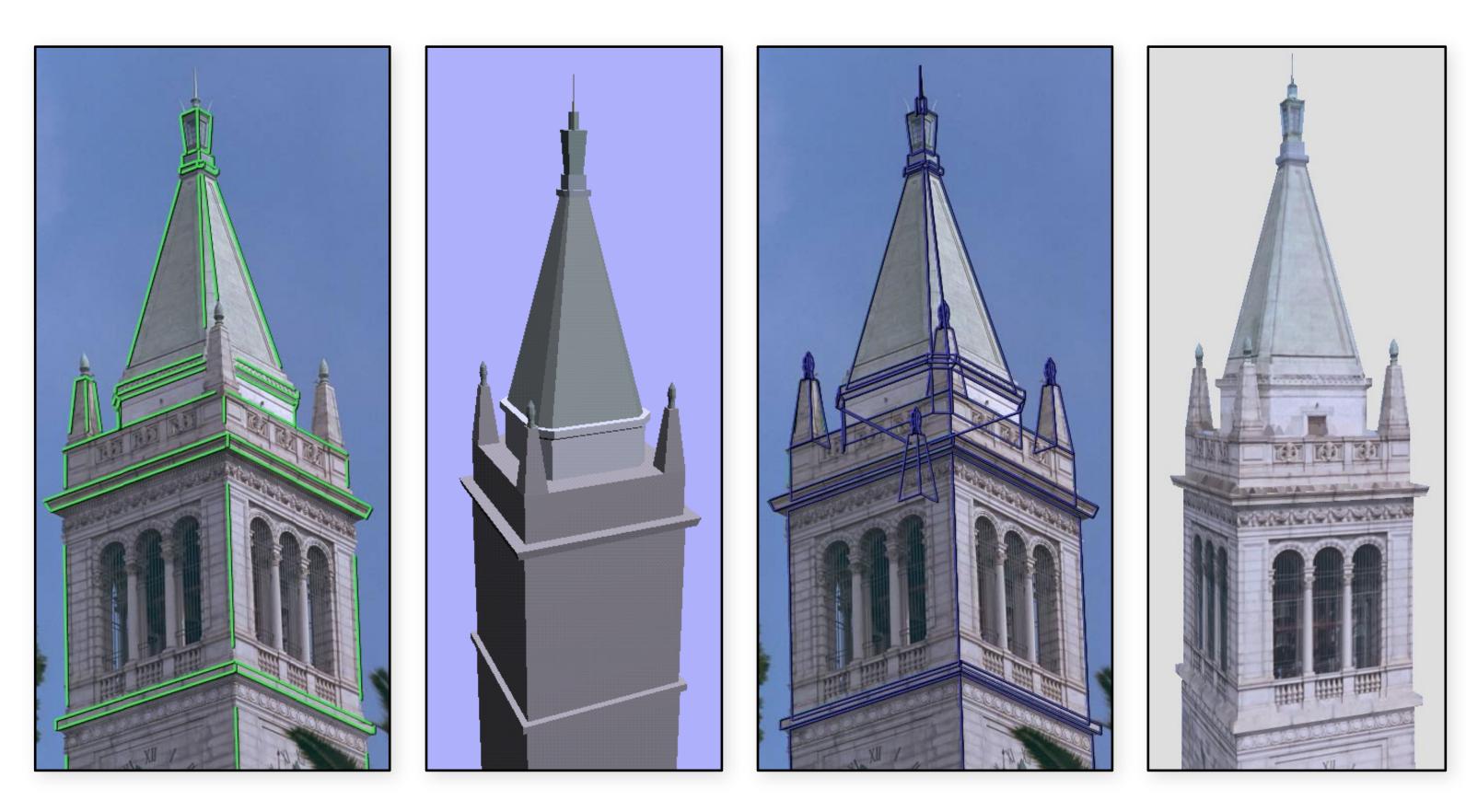








Projective texture example Modeling from photographs Using input photos as textures



[Debevec et al. 1996]



Fiat LUX

SIGGRAPH 99 Electronic Theater

More details

- "Rendering with Natural Light"
- http://www.pauldebevec.com/RNL/
- "Fiat Lux"
- http://www.pauldebevec.com/FiatLux/
- History of reflection mapping
- http://www.pauldebevec.com/ReflectionMapping/

111