#### Two-view geometry, stereo, and disparity



15-463, 15-663, 15-862 Computational Photography Fall 2022, Lecture 16

1

#### http://graphics.cs.cmu.edu/courses/15-463

#### Course announcements

- Homework assignment 6 posted, due December 12.
   Start early: Capturing structured light stereo is challenging.
- Grades for homework assignments 3 and 4 posted.
   Photography competition winners still pending.
- Propose topics for this week's reading group.
- Final projects.



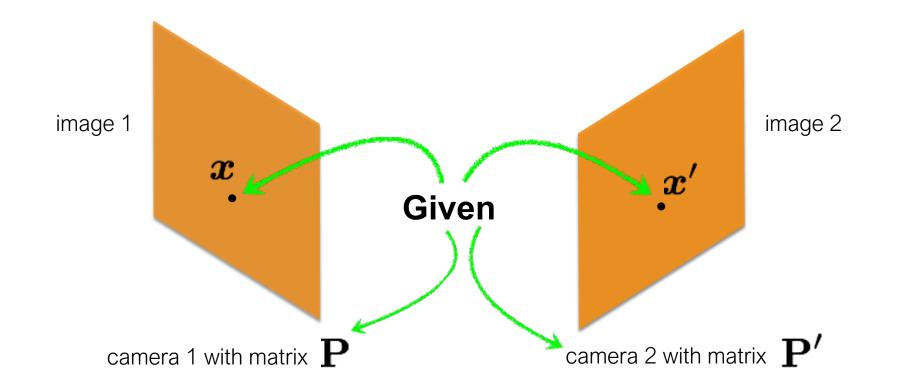
#### Overview of today's lecture

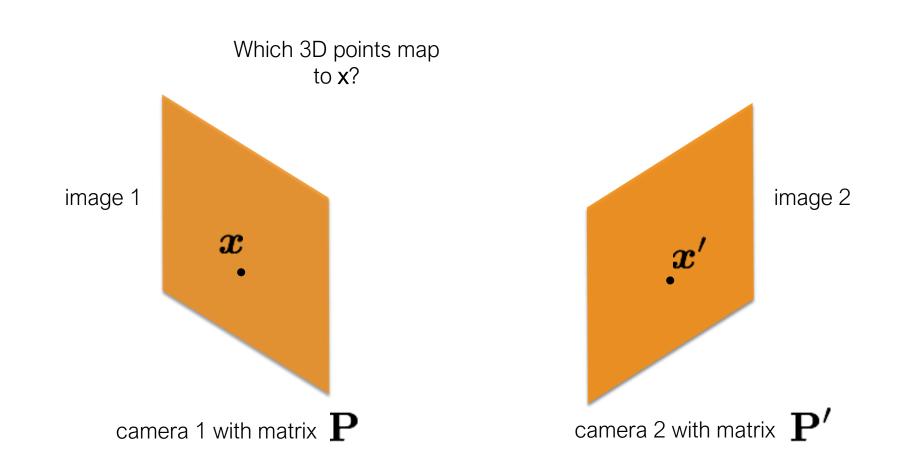
- Triangulation.
- Epipolar geometry.
- Revisiting triangulation.
- Disparity.
- Revisiting lightfields.
- Structured light.
- Some notes on focusing.

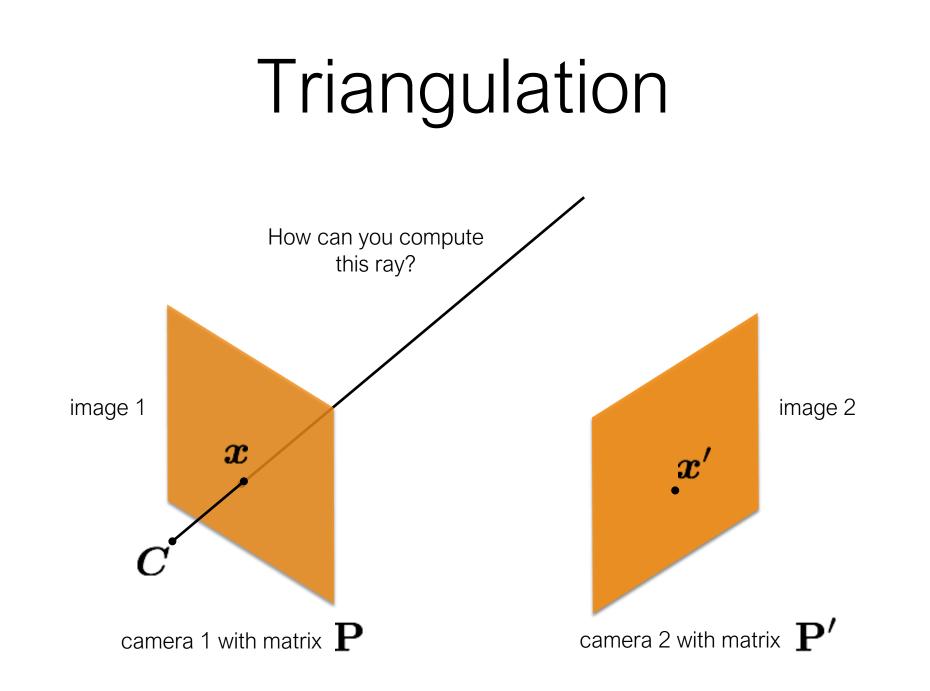
#### Slide credits

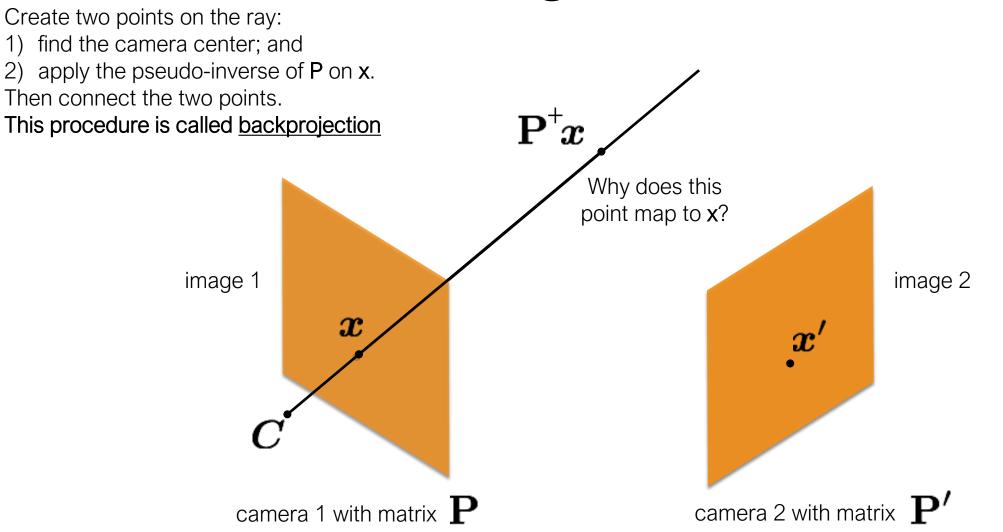
Many of these slides were adapted directly from:

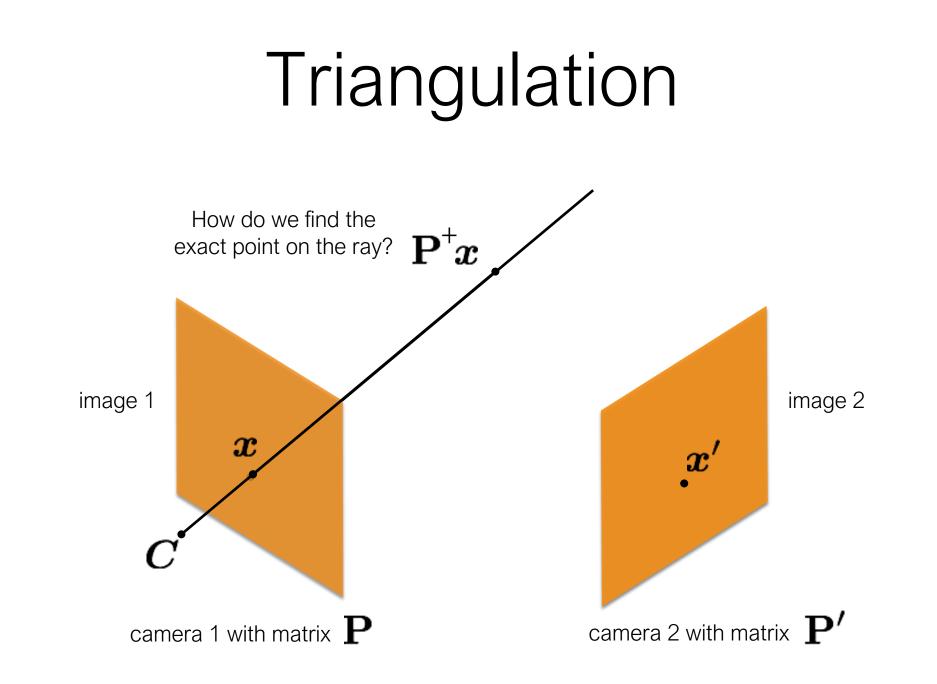
- Kris Kitani (16-385, Spring 2017).
- Srinivasa Narasimhan (16-820, Spring 2017).
- Mohit Gupta (Wisconsin).
- James Tompkin (Brown).

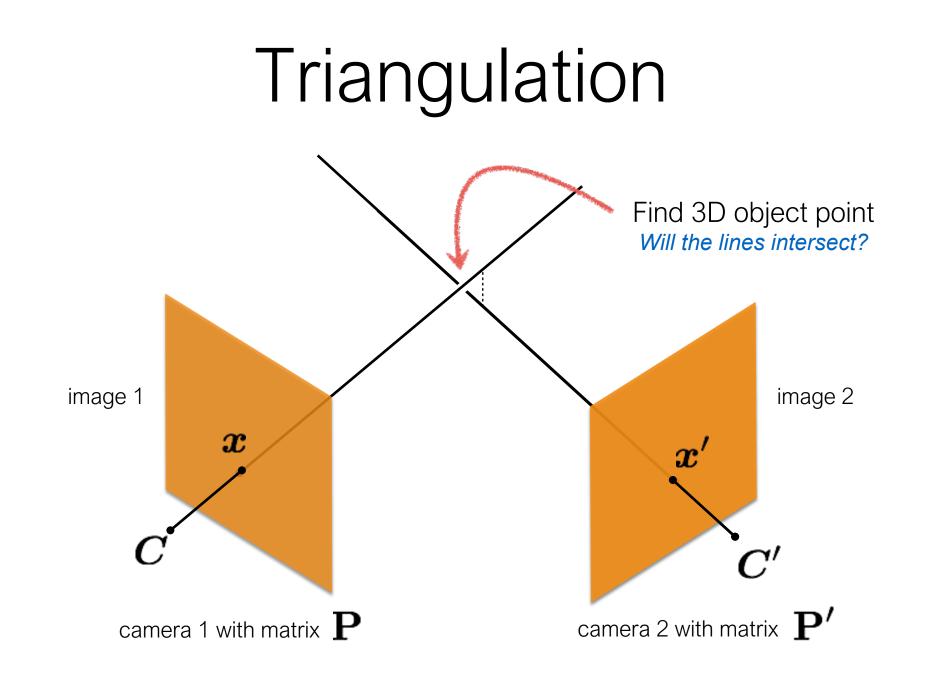


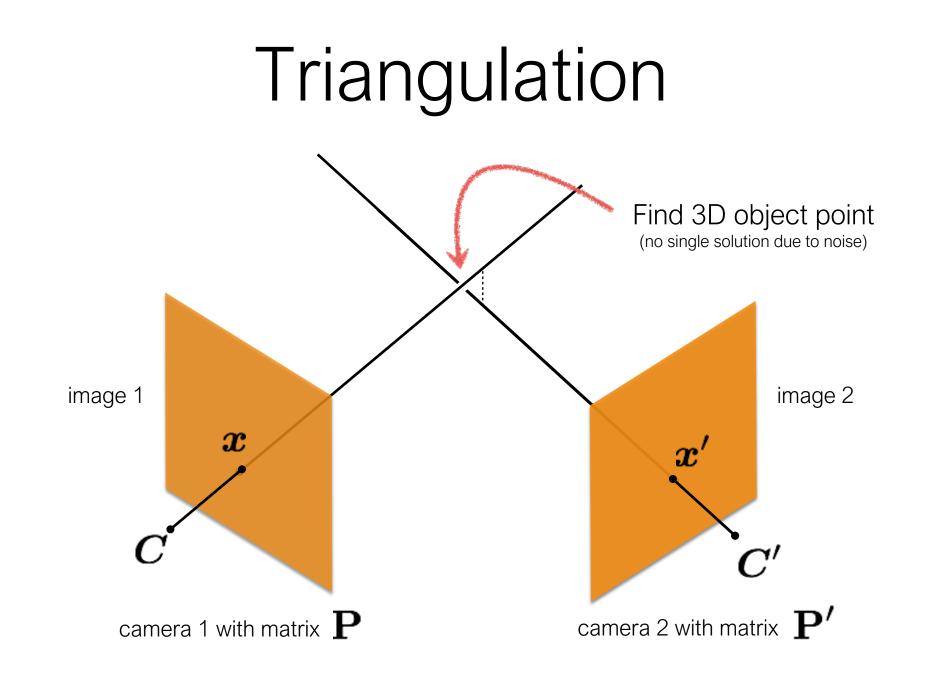










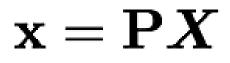


# Given a set of (noisy) matched points $\{m{x}_i,m{x}_i'\}$

and camera matrices  $\mathbf{P},\mathbf{P}'$ 

Estimate the 3D point

#### $\mathbf{X}$

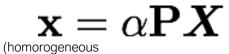


known known

Can we compute **X** from a single correspondence **x**?

 $\mathbf{x} = \mathbf{P} \boldsymbol{X}$ (homogeneous coordinate)

This is a similarity relation because it involves homogeneous coordinates



coordinate)

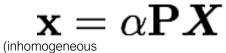
Same ray direction but differs by a scale factor

$$\begin{bmatrix} x \\ y \\ z \end{bmatrix} = \alpha \begin{bmatrix} p_1 & p_2 & p_3 & p_4 \\ p_5 & p_6 & p_7 & p_8 \\ p_9 & p_{10} & p_{11} & p_{12} \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \\ 1 \end{bmatrix}$$

How do we solve for unknowns in a similarity relation?

#### $\mathbf{x} = \mathbf{P} \mathbf{X}$

Also, this is a similarity relation because it involves homogeneous coordinates



coordinate)

Same ray direction but differs by a scale factor

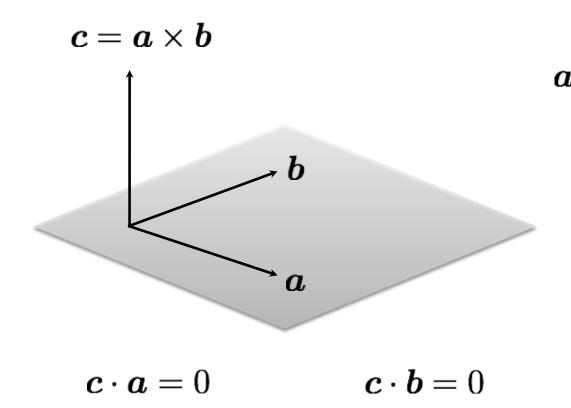
$$\begin{bmatrix} x \\ y \\ z \end{bmatrix} = \alpha \begin{bmatrix} p_1 & p_2 & p_3 & p_4 \\ p_5 & p_6 & p_7 & p_8 \\ p_9 & p_{10} & p_{11} & p_{12} \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \\ 1 \end{bmatrix}$$

How do we solve for unknowns in a similarity relation?

## Linear algebra reminder: cross product

Vector (cross) product

takes two vectors and returns a vector perpendicular to both



$$a imes m{b} = \left[ egin{array}{c} a_2 b_3 - a_3 b_2 \ a_3 b_1 - a_1 b_3 \ a_1 b_2 - a_2 b_1 \end{array} 
ight]$$

cross product of two vectors in the same direction is zero vector

 $\boldsymbol{a} \times \boldsymbol{a} = 0$ 

remember this!!!

#### Linear algebra reminder: cross product

Cross product

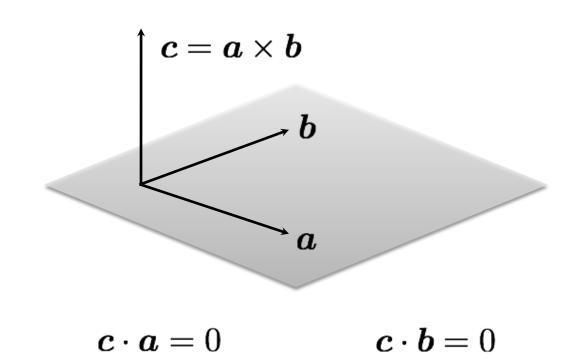
$$m{a} imes m{b} = \left[ egin{array}{c} a_2 b_3 - a_3 b_2 \ a_3 b_1 - a_1 b_3 \ a_1 b_2 - a_2 b_1 \end{array} 
ight]$$

Can also be written as a matrix multiplication

$$m{a} imes m{b} = [m{a}]_{ imes} m{b} = egin{bmatrix} 0 & -a_3 & a_2 \ a_3 & 0 & -a_1 \ -a_2 & a_1 & 0 \end{bmatrix} egin{bmatrix} b_1 \ b_2 \ b_3 \end{bmatrix}$$

**Skew symmetric** 

## Compare with: dot product



dot product of two orthogonal vectors is (scalar) zero

# Back to triangulation

#### $\mathbf{x} = \alpha \mathbf{P} \mathbf{X}$

Same direction but differs by a scale factor

How can we rewrite this using vector products?

#### $\mathbf{x} = \alpha \mathbf{P} \mathbf{X}$

Same direction but differs by a scale factor

#### $\mathbf{x} \times \mathbf{P} \boldsymbol{X} = \mathbf{0}$

Cross product of two vectors of same direction is zero (this equality removes the scale factor)

$$\begin{bmatrix} x \\ y \\ z \end{bmatrix} = \alpha \begin{bmatrix} p_1 & p_2 & p_3 & p_4 \\ p_5 & p_6 & p_7 & p_8 \\ p_9 & p_{10} & p_{11} & p_{12} \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \\ 1 \end{bmatrix}$$
for first e camera points
$$\begin{bmatrix} x \\ y \\ z \end{bmatrix} = \alpha \begin{bmatrix} - p_1^\top - p_2^\top \\ - p_2^\top \\ - p_3^\top \\ X \end{bmatrix} \begin{bmatrix} X \\ Y \\ z \end{bmatrix}$$

$$\begin{bmatrix} x \\ y \\ z \end{bmatrix} = \alpha \begin{bmatrix} p_1^\top X \\ p_2^\top X \\ p_3^\top X \end{bmatrix}$$

$$\begin{bmatrix} x \\ y \\ z \end{bmatrix} = \alpha \begin{bmatrix} p_1^\top X \\ p_2^\top X \\ p_3^\top X \end{bmatrix}$$

Do the same after first expanding out the camera matrix and points Using the fact that the cross product should be zero

# $\mathbf{x} \times \mathbf{P} \mathbf{X} = \mathbf{0}$ $\begin{bmatrix} y \mathbf{p}_3^\top \mathbf{X} - \mathbf{p}_2^\top \mathbf{X} \\ \mathbf{p}_1^\top \mathbf{X} - x \mathbf{p}_3^\top \mathbf{X} \\ x \mathbf{p}_2^\top \mathbf{X} - y \mathbf{p}_1^\top \mathbf{X} \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}$

Third line is a linear combination of the first and second lines. (x times the first line plus y times the second line) Using the fact that the cross product should be zero

$$\mathbf{x} \times \mathbf{P} \mathbf{X} = \mathbf{0}$$
$$\begin{bmatrix} y \mathbf{p}_3^\top \mathbf{X} - \mathbf{p}_2^\top \mathbf{X} \\ \mathbf{p}_1^\top \mathbf{X} - x \mathbf{p}_3^\top \mathbf{X} \\ x \mathbf{p}_2^\top \mathbf{X} - y \mathbf{p}_1^\top \mathbf{X} \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}$$

Third line is a linear combination of the first and second lines. (x times the first line plus y times the second line)

One 2D to 3D point correspondence give you 2 equations

$$\left[\begin{array}{c} y \boldsymbol{p}_3^\top \boldsymbol{X} - \boldsymbol{p}_2^\top \boldsymbol{X} \\ \boldsymbol{p}_1^\top \boldsymbol{X} - x \boldsymbol{p}_3^\top \boldsymbol{X} \end{array}\right] = \left[\begin{array}{c} 0 \\ 0 \end{array}\right]$$

Remove third row, and rearrange as system on unknowns

$$egin{array}{c} y oldsymbol{p}_3^{ op} - oldsymbol{p}_2^{ op} \ oldsymbol{p}_1^{ op} - x oldsymbol{p}_3^{ op} \end{array} iggree egin{array}{c} oldsymbol{X} = \left[ egin{array}{c} 0 \ 0 \end{array} 
ight] oldsymbol{X} = \left[ egin{array}{c} 0 \ 0 \end{array} 
ight]$$

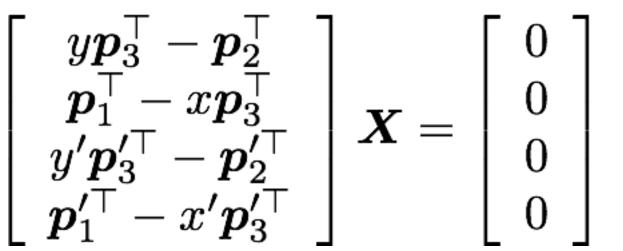
 $\mathbf{A}_i \boldsymbol{X} = \boldsymbol{0}$ 

Now we can make a system of linear equations (two lines for each 2D point correspondence)

Concatenate the 2D points from both images

Two rows from camera one

Two rows from camera two



sanity check! dimensions?

 $\mathbf{A}X = \mathbf{0}$ 

How do we solve homogeneous linear system?

Concatenate the 2D points from both images

$$\begin{bmatrix} y \boldsymbol{p}_3^\top - \boldsymbol{p}_2^\top \\ \boldsymbol{p}_1^\top - x \boldsymbol{p}_3^\top \\ y' \boldsymbol{p}_3'^\top - \boldsymbol{p}_2'^\top \\ \boldsymbol{p}_1'^\top - x' \boldsymbol{p}_3'^\top \end{bmatrix} \boldsymbol{X} = \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}$$

#### $\mathbf{A}X = \mathbf{0}$

How do we solve homogeneous linear system?

SVD!

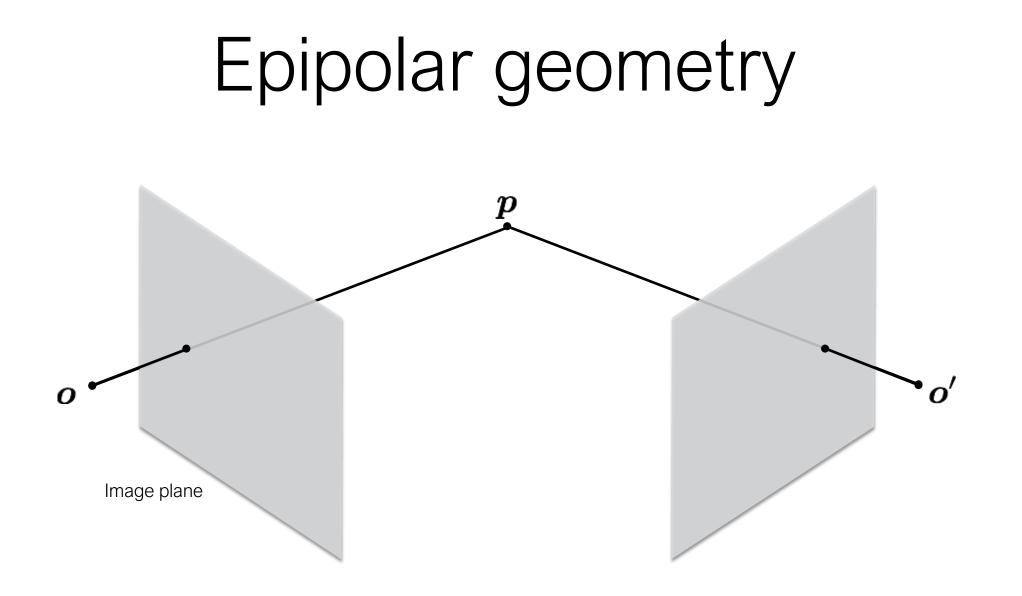
#### How would you reconstruct 3D points?

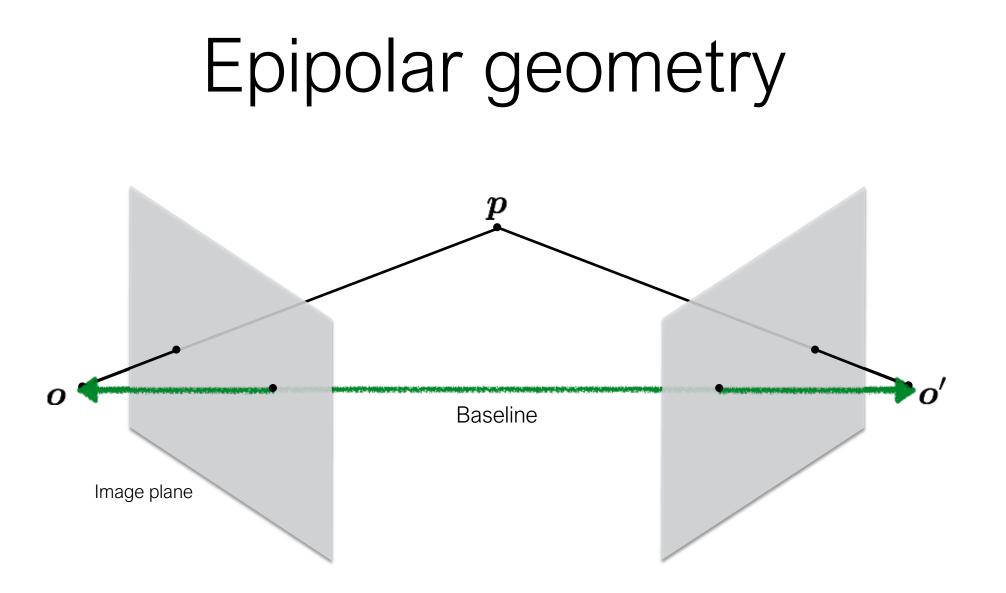


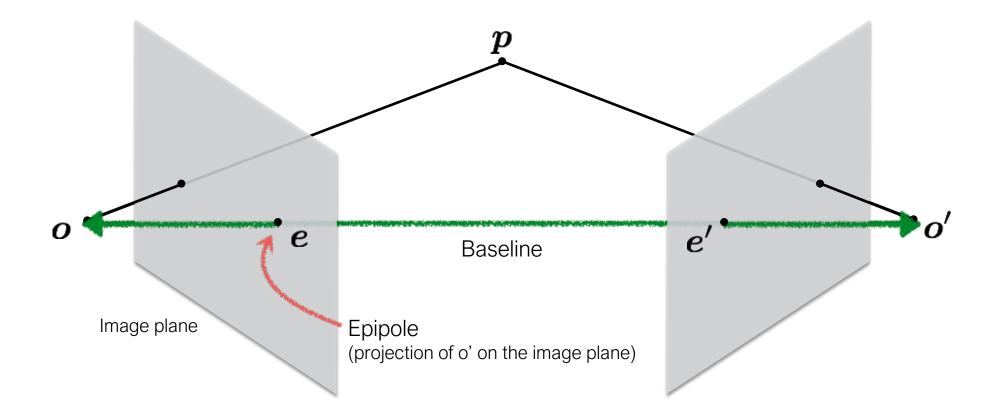
Left image

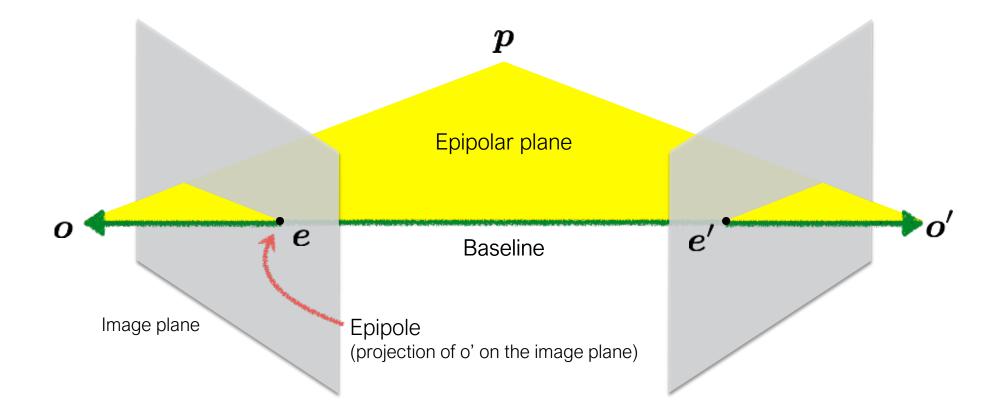


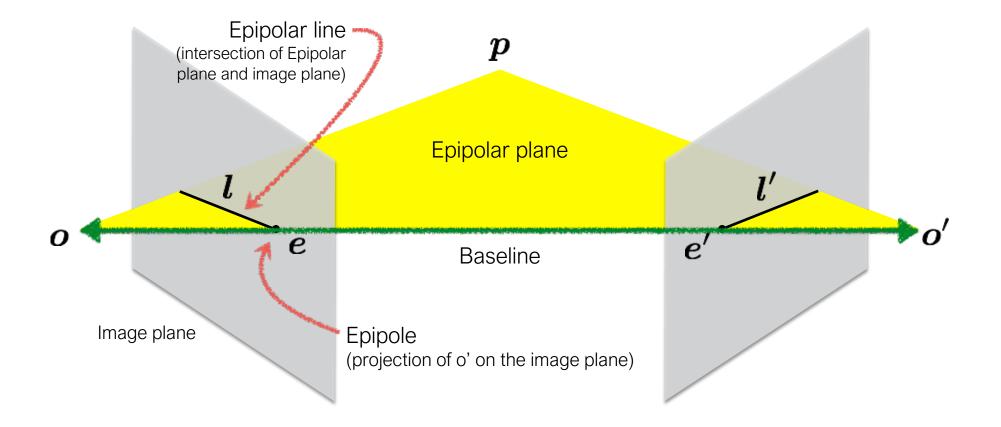
Right image

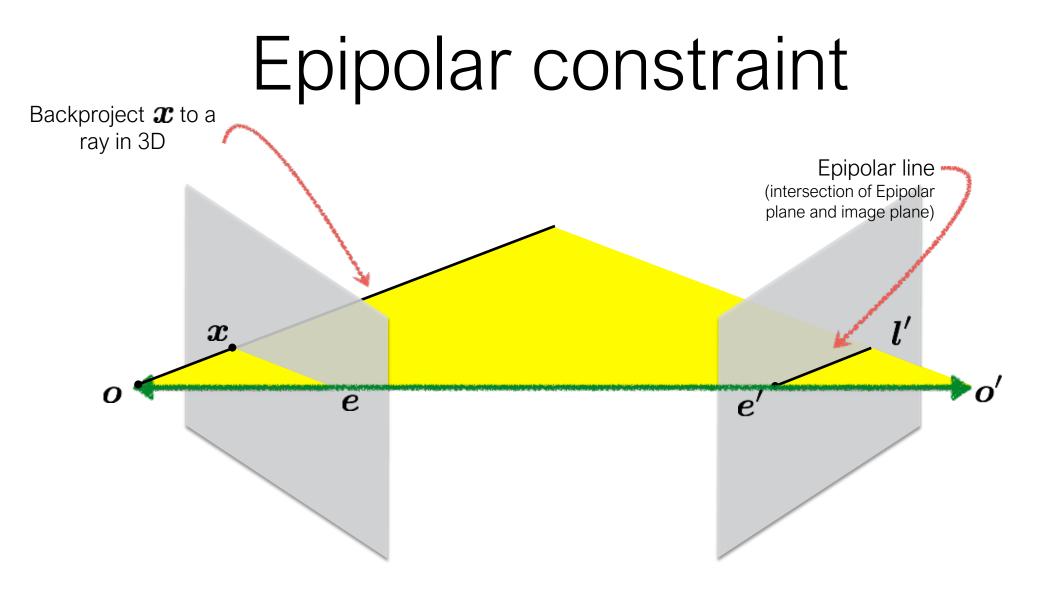






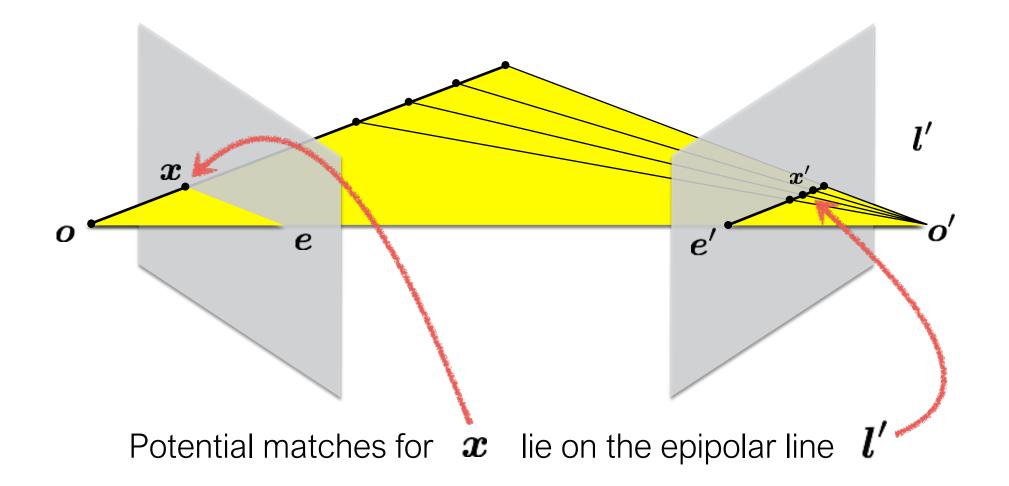




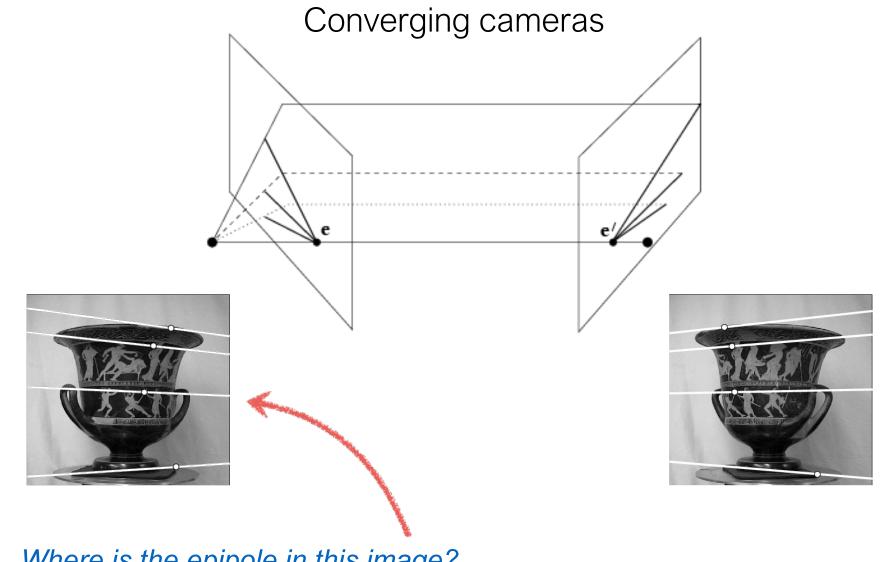


Another way to construct the epipolar plane, this time given  $oldsymbol{x}$ 

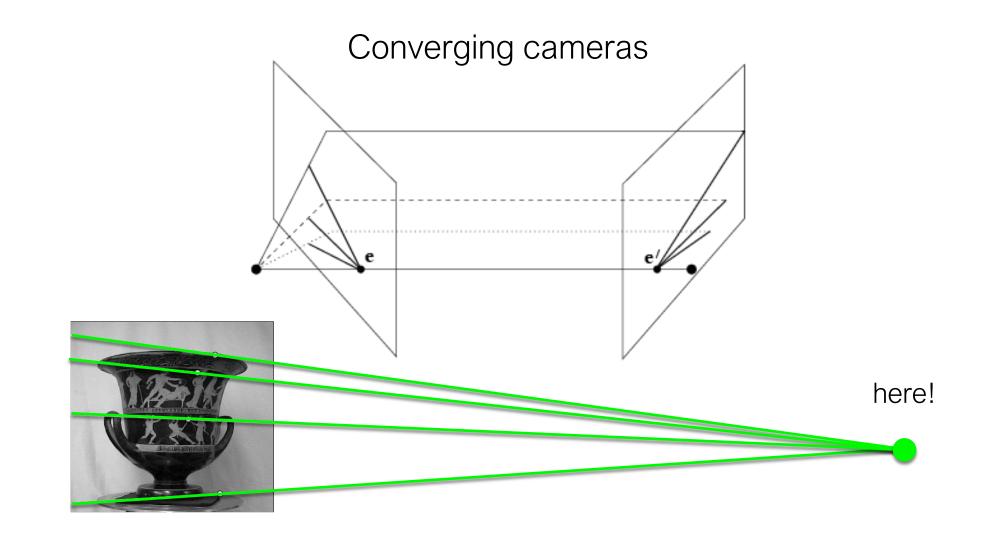




o e	e'o'
The point <b>x</b> (left image) maps to a	in the right image
The baseline connects the	and
An epipolar line (left image) maps to a _	in the right image
An epipole <b>e</b> is a projection of the	
All epipolar lines in an image interse	ct at the



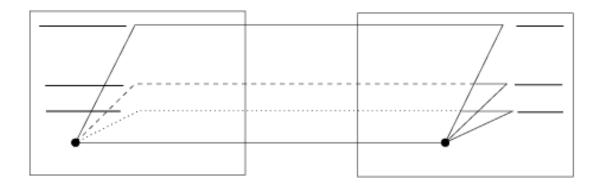
Where is the epipole in this image?

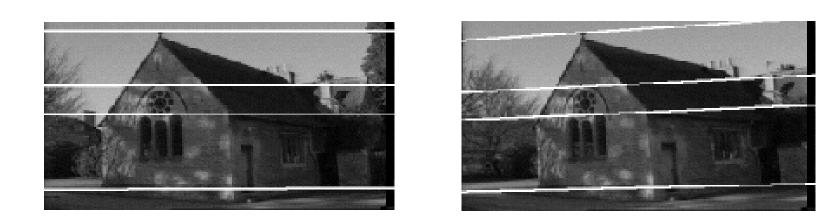


Where is the epipole in this image?

It's not always in the image

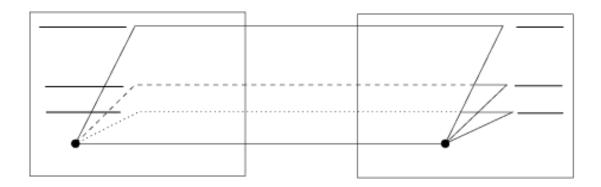
#### Parallel cameras

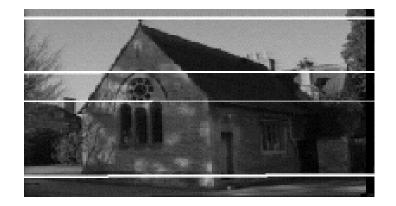


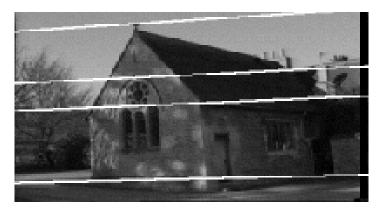


Where is the epipole?

## Parallel cameras







epipole at infinity

The epipolar constraint is an important concept for stereo vision

#### Task: Match point in left image to point in right image

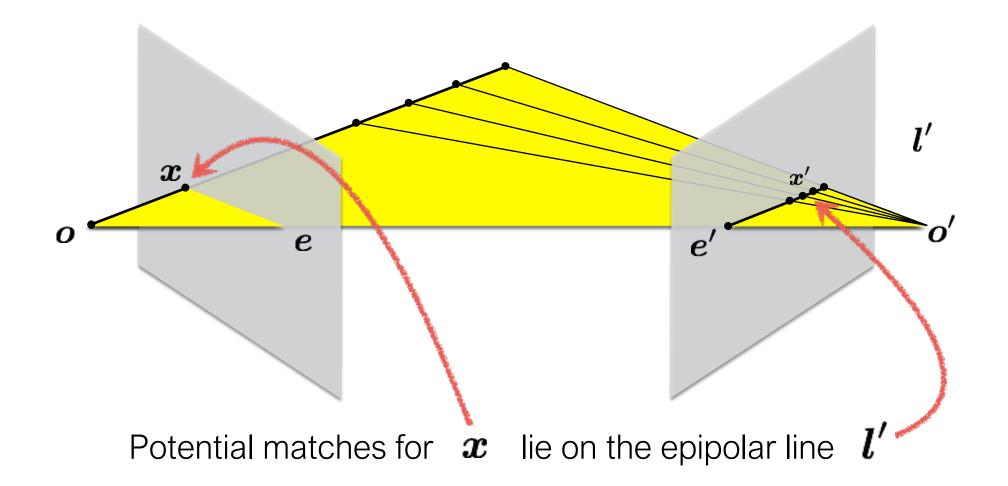


Left image

Right image

#### How would you do it?





The epipolar constraint is an important concept for stereo vision

#### Task: Match point in left image to point in right image



Left image

Right image

Want to avoid search over entire image

Epipolar constraint reduces search to a single line



Left image





Left image

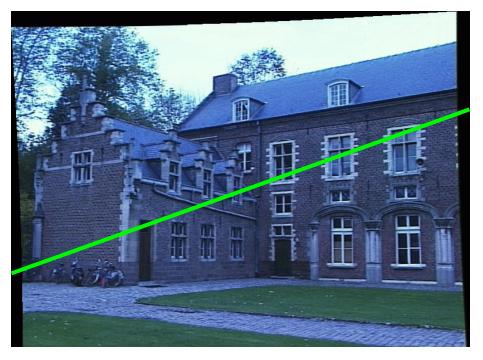


Right image

1. Select point in one image



Left image



- 1. Select point in one image
- 2. Form epipolar line for that point in second image (how?)



Left image



- 1. Select point in one image
- 2. Form epipolar line for that point in second image (how?)
- 3. Find matching point along line (how?)



Left image

- 1. Select point in one image
- 2. Form epipolar line for that point in second image (how?)
- 3. Find matching point along line (how?)
- 4. Perform triangulation (how?)

## Stereo rectification



## What's different between these two images?







## Objects that are close move more or less?

The amount of horizontal movement is inversely proportional to ...





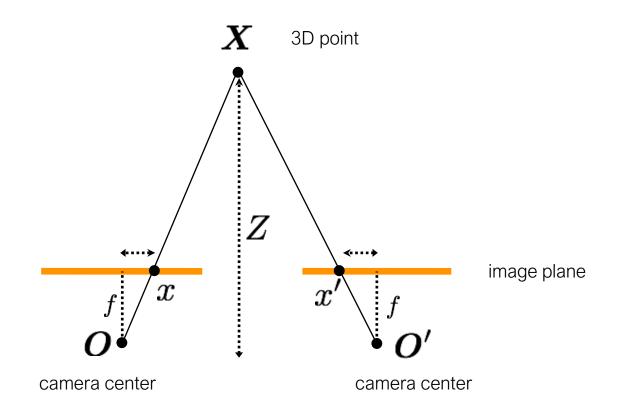


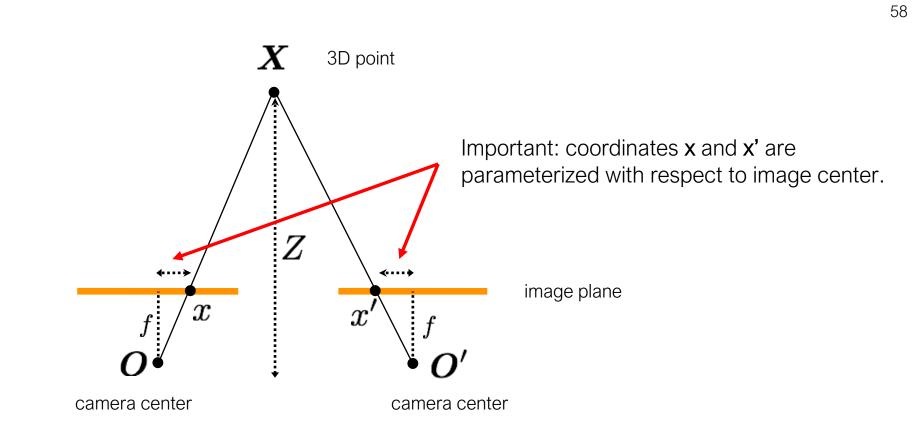
The amount of horizontal movement is inversely proportional to ...

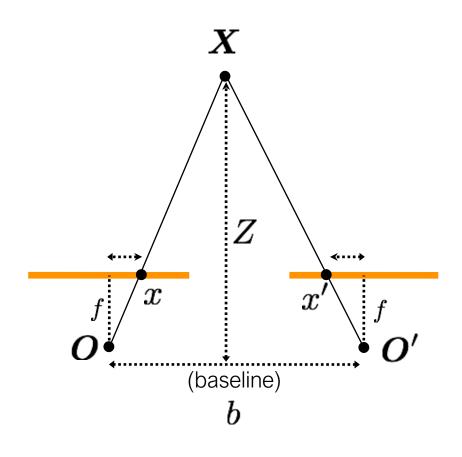


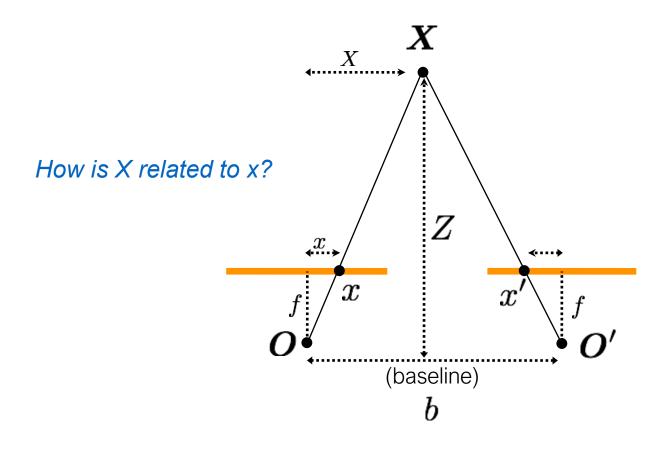
... the distance from the camera.

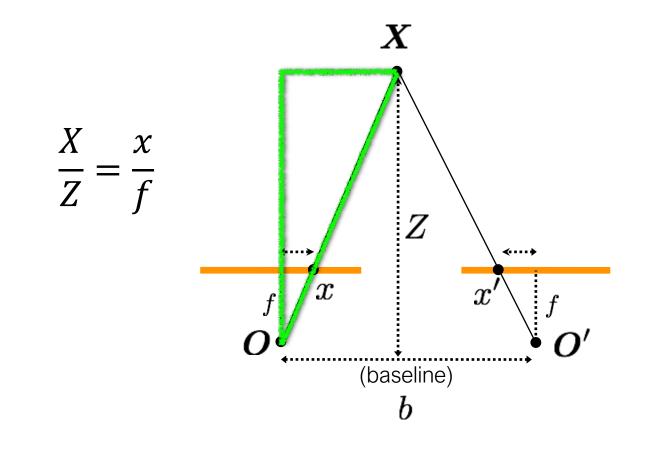
More formally...

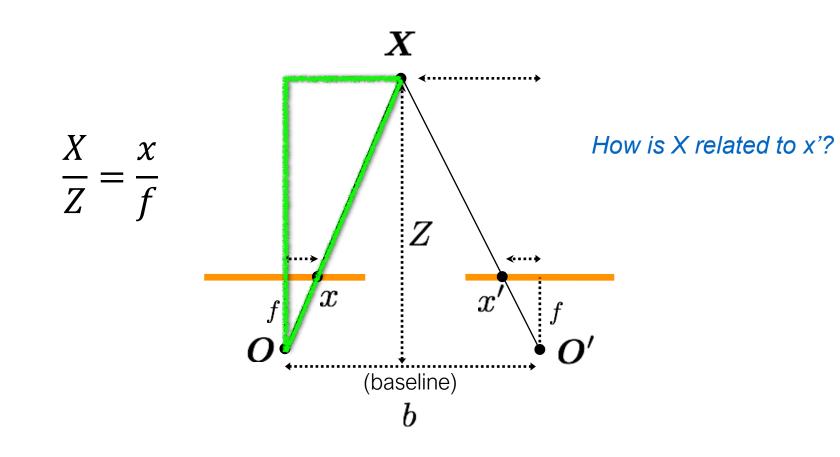




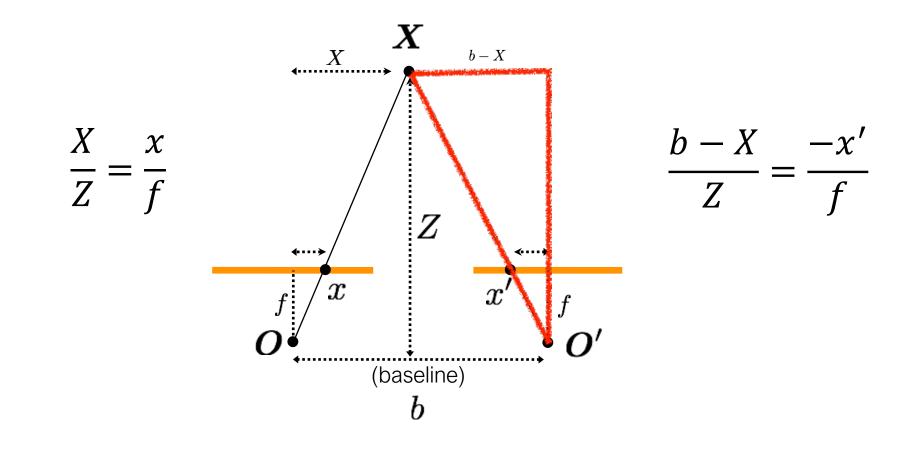


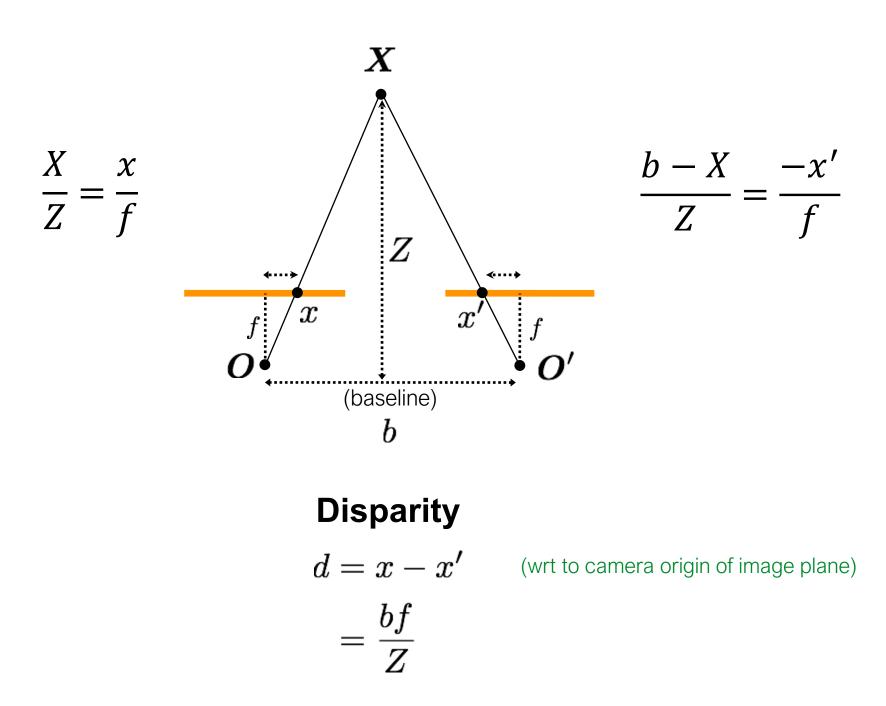


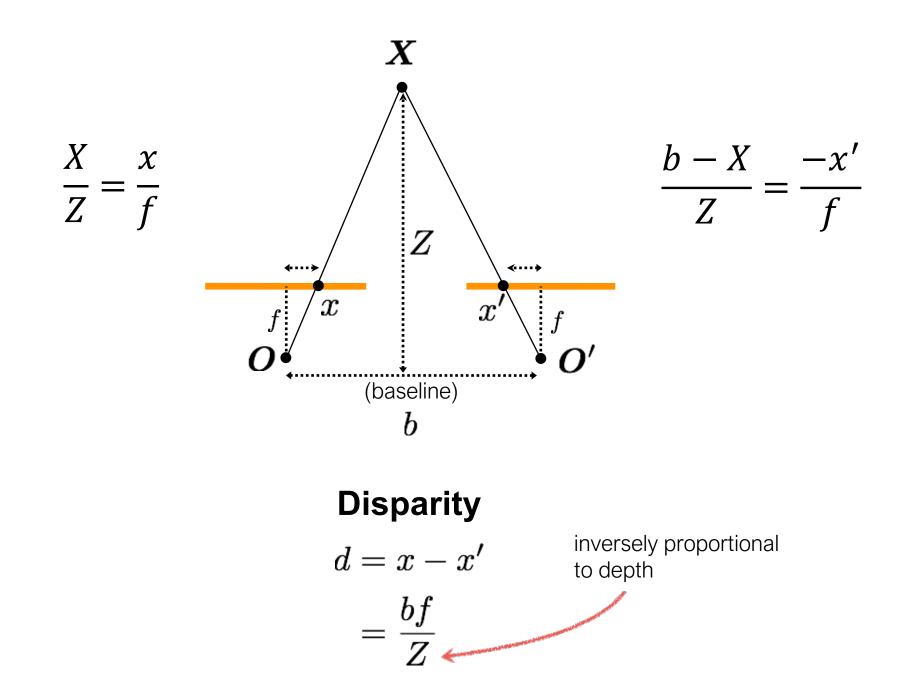












#### Real-time stereo sensing



#### Nomad robot searches for meteorites in Antartica http://www.frc.ri.cmu.edu/projects/meteorobot/index.html



## Subaru Eyesight system

## Pre-collision braking

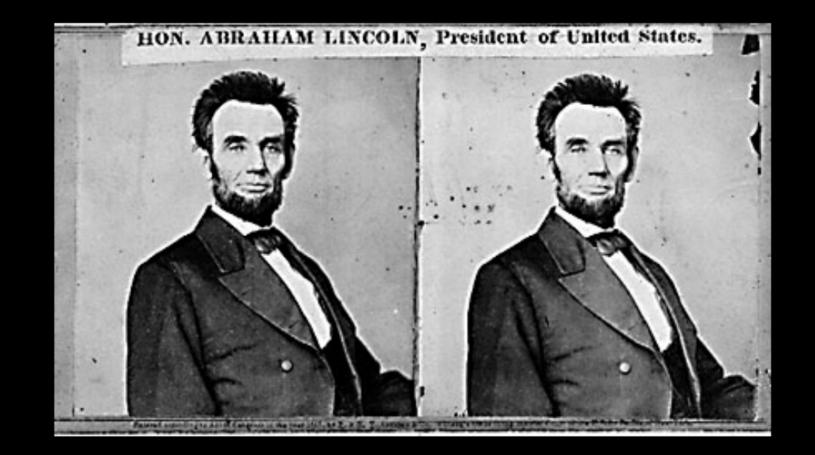


# What other vision system uses disparity for depth sensing?

## Stereoscopes: A 19<sup>th</sup> Century Pastime









Public Library, Stereoscopic Looking Room, Chicago, by Phillips, 1923





Teesta suspension bridge-Darjeeling, India

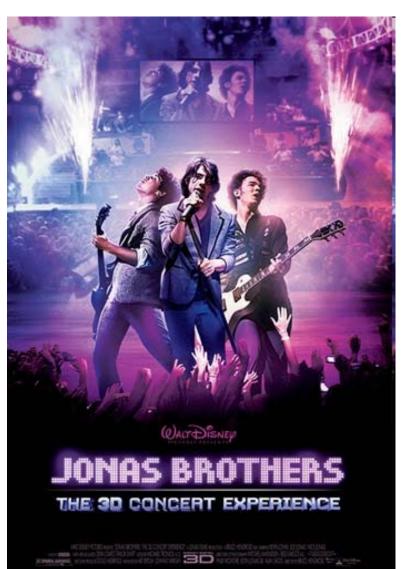


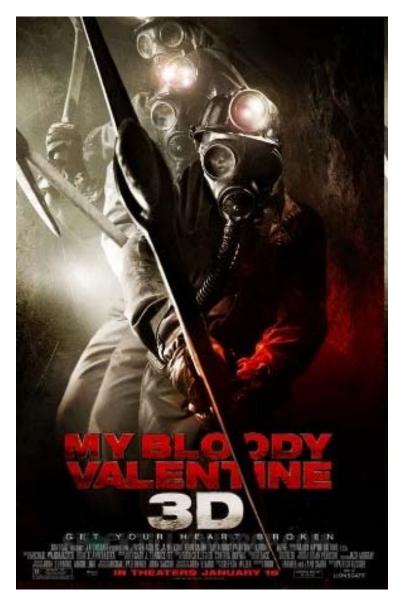


Mark Twain at Pool Table", no date, UCR Museum of Photography

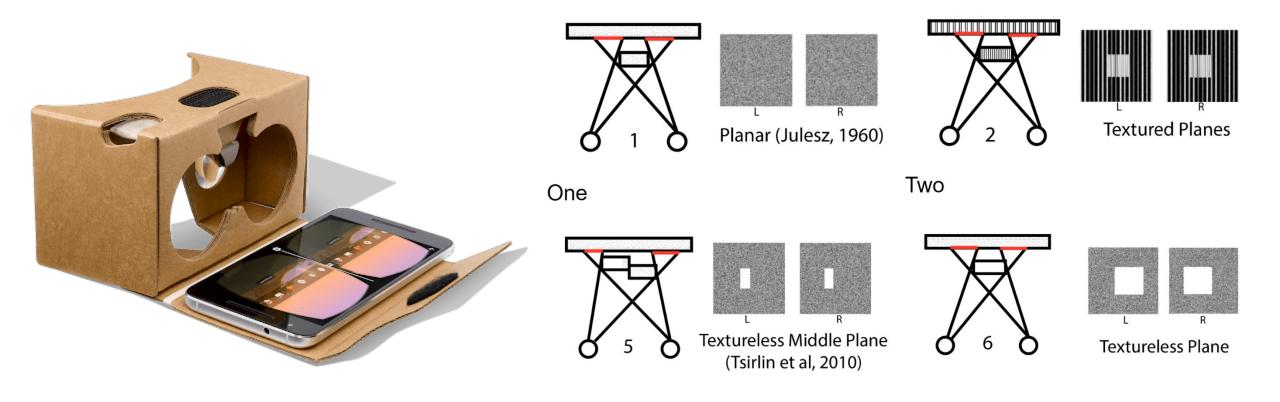


#### This is how 3D movies work





### Simple stereoscope

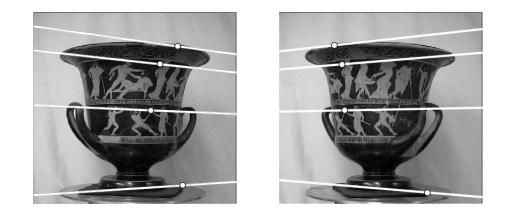


Google cardboard

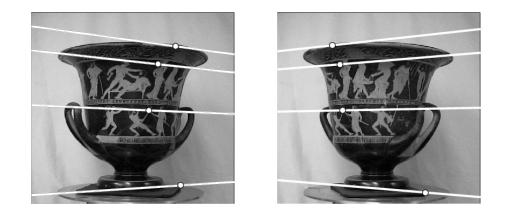
Fun patterns: random dot stereograms

http://vision.seas.harvard.edu/stereo/

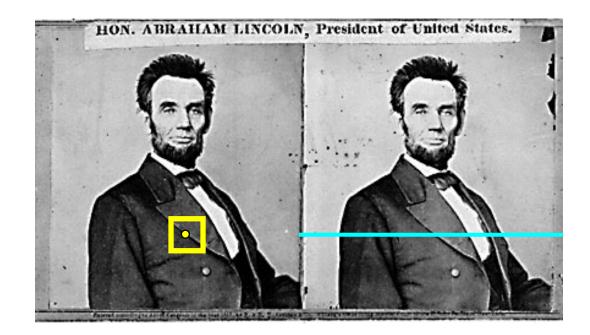
So can I compute depth using disparity from any two images of the same object?



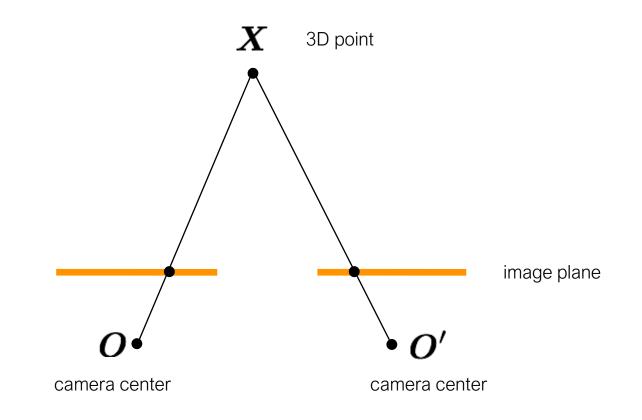
So can I compute depth using disparity from any two images of the same object?



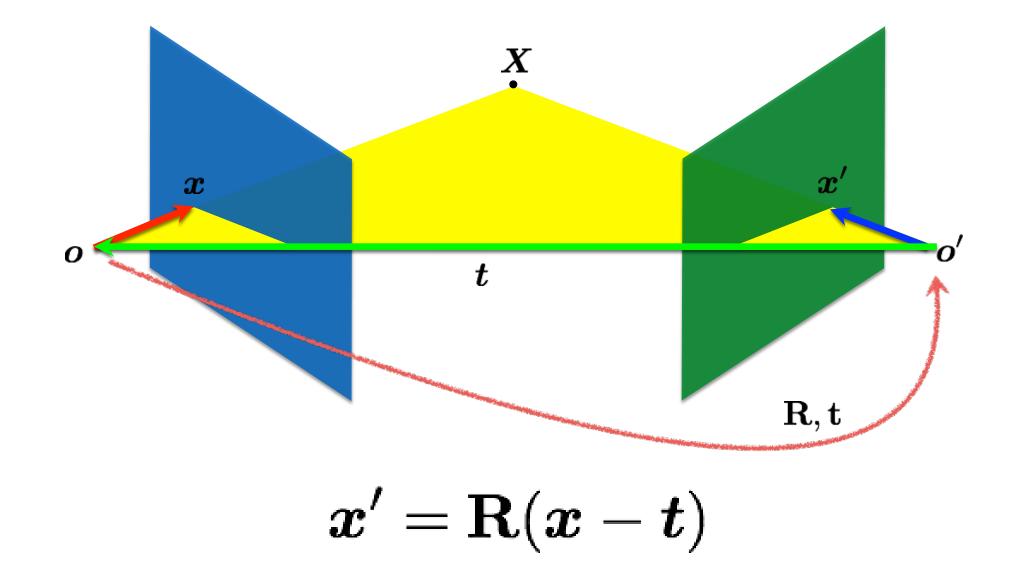
- 1. Need sufficient baseline
- 2. Images need to be 'rectified' first (make epipolar lines horizontal)



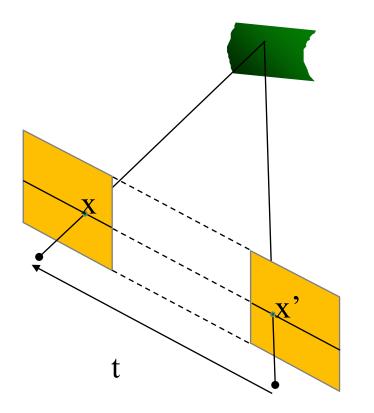
#### How can you make the epipolar lines horizontal?



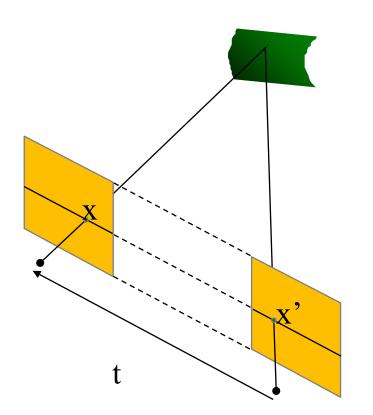
#### What's special about these two cameras?



When are epipolar lines horizontal?

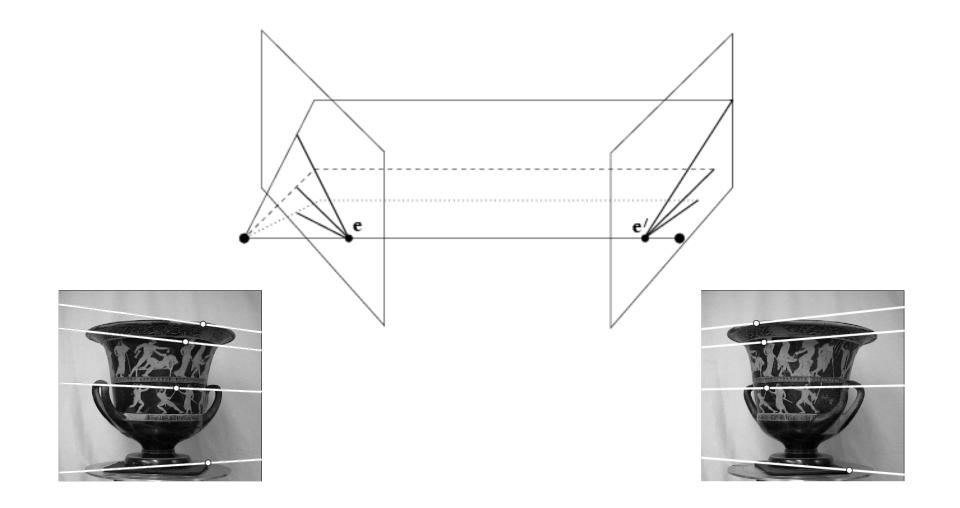


#### When are epipolar lines horizontal?



When this relationship holds:

$$R = I \qquad t = (T, 0, 0)$$



#### It's hard to make the image planes exactly parallel

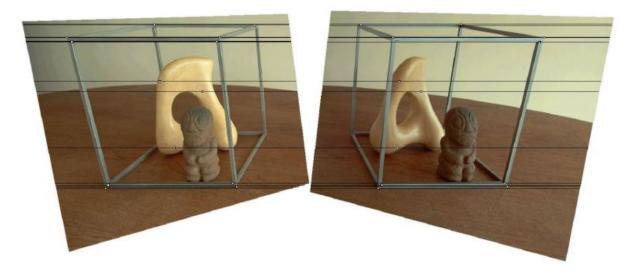


#### How can you make the epipolar lines horizontal?





#### Use stereo rectification

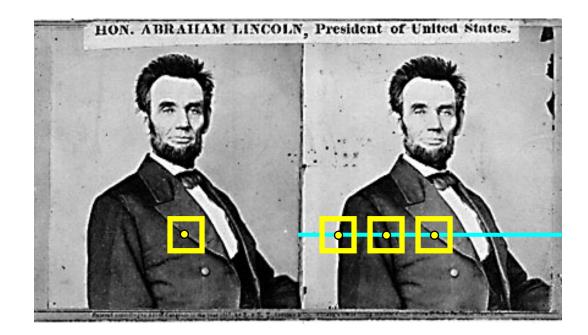


## Stereo matching



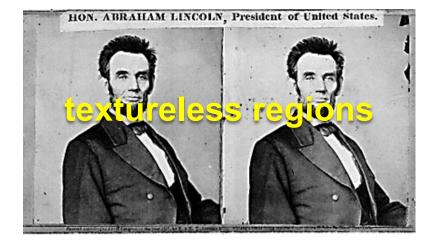
#### Depth Estimation via Stereo Matching

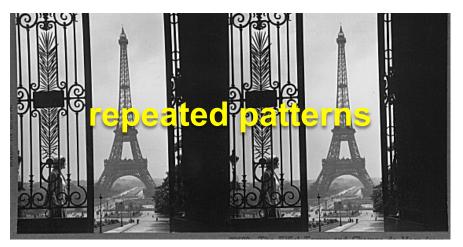




1. Rectify images (make epipolar lines horizontal) 2. For each pixel a. Find epipolar line b. Scan line for best match  $\longleftarrow$  How would c. Compute depth from disparity  $Z = \frac{bf}{d}$  When are correspondences difficult?

#### When are correspondences difficult?



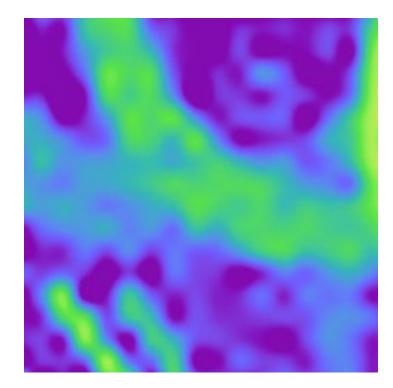




### Depth discontinuities

What is the problem here?







One of two input images

Depth from disparity

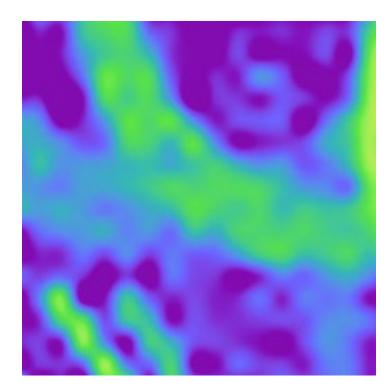
Groundtruth depth

## Depth discontinuities

What is the problem here?

• (Patch-wise) stereo matching blurs along the edges. How can we fix this?







One of two input images

Depth from disparity

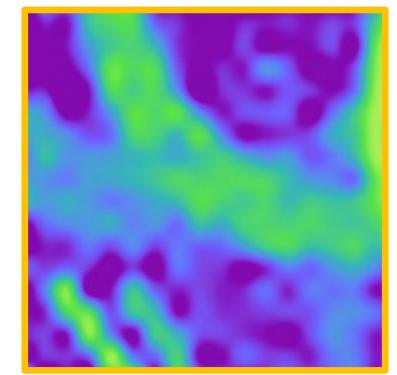
Groundtruth depth

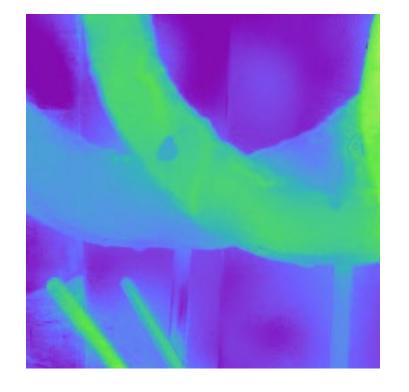
### Edge-aware depth denoising

$$A_{p(col)} = \frac{1}{k(p(col))} \sum_{p' \in \Omega} \frac{g_d(|p - p'|)}{g_r(F_{p(col)} - F_{p'(col)})} A_{p'(col)}$$

Use joint bilateral filtering, with the input image as guide.







One of two input images

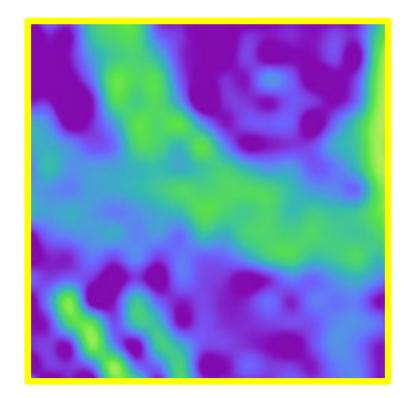
Depth from disparity

Guided filtering

### Fast bilateral solver

Possible to *combine* edge-enforcement and matching in a single optimization problem, instead of just filtering in post-processing.







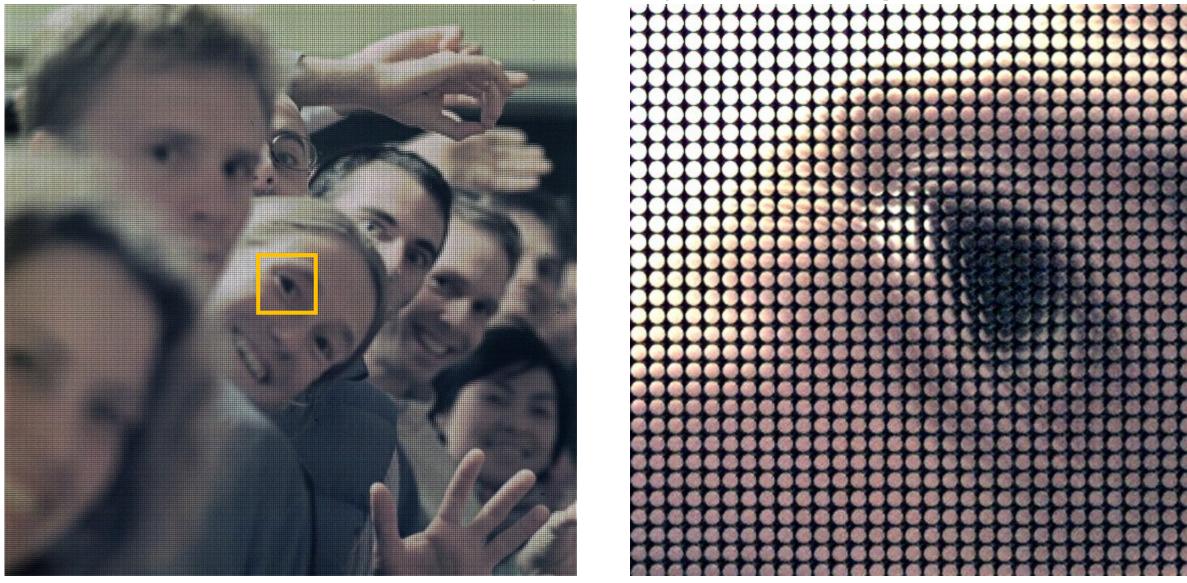
One of two input images

Depth from disparity

Bilateral stereo matching

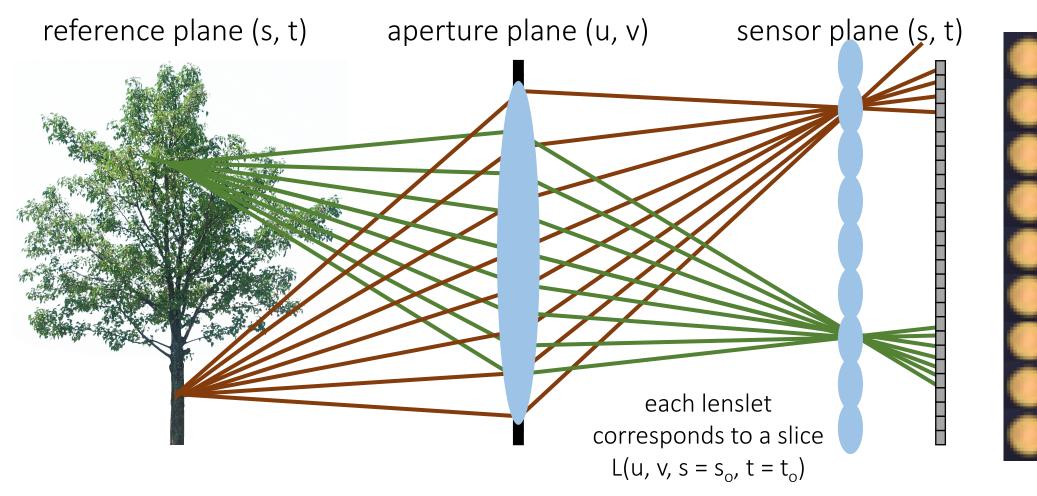
### Disparity and lightfields

### Reminder: a plenoptic "image"



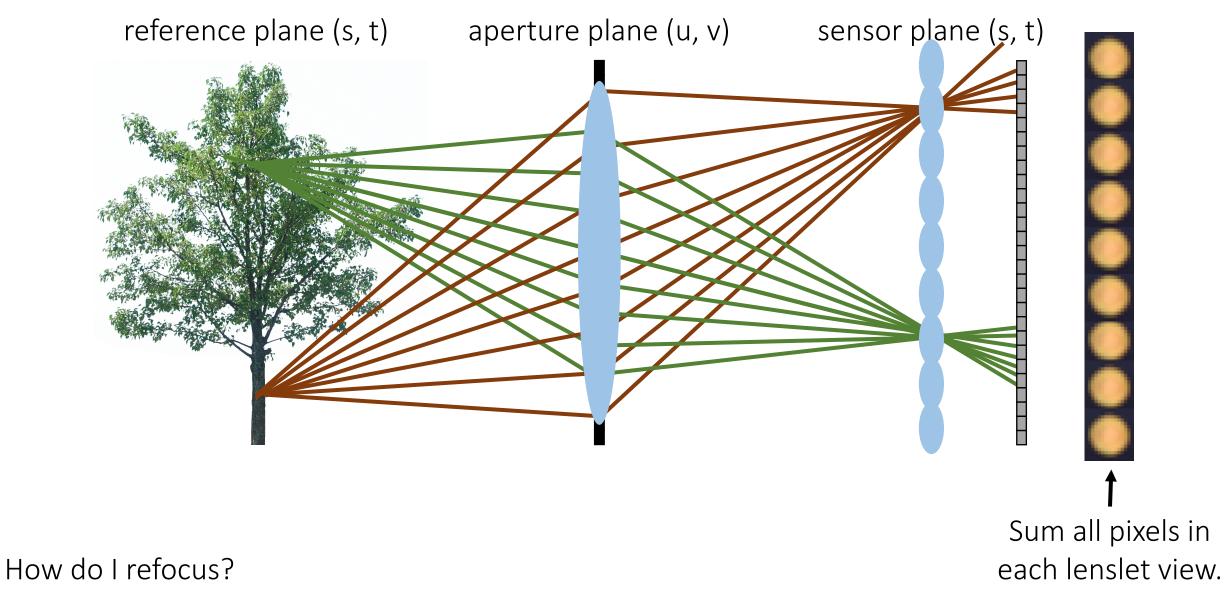
What are these circles?

## Reminder: a plenoptic camera

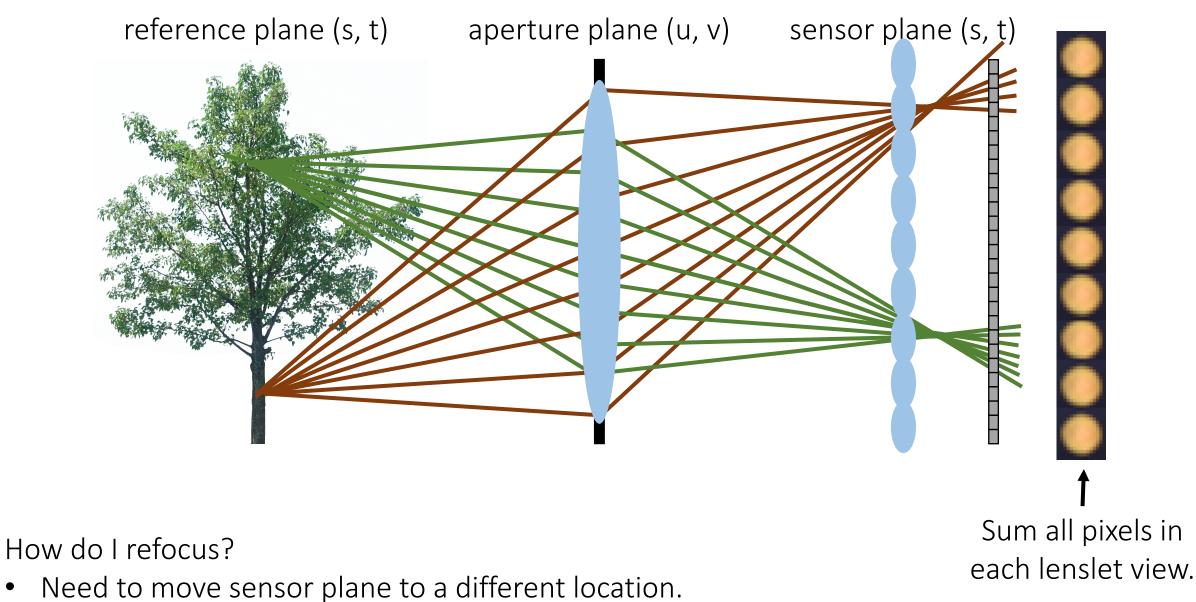


Lightfield L(u, v, s, t)

## Reminder: form lens image



## Reminder: form lens image

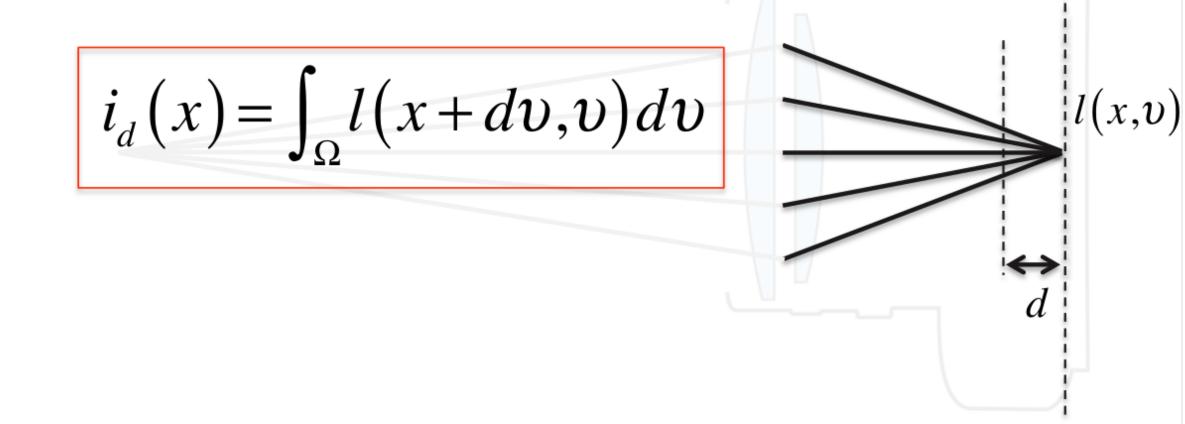


# Understanding Refocus

100

х

- consider light field inside camera
- synthesize image on sensor  $i_{d=0}(x) = \int_{\Omega} l(x,v) dv$

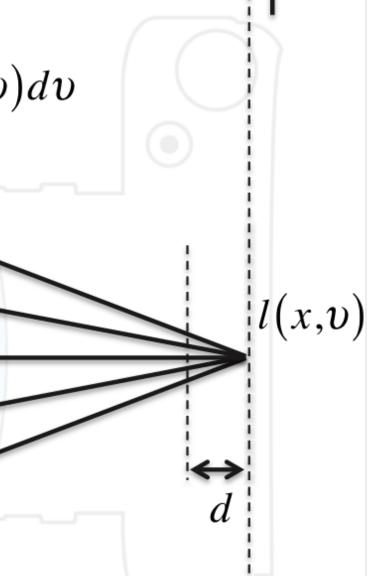


# Understanding Refocus

- consider light field inside camera
- synthesize image on sensor  $i_{d=0}(x) = \int_{\Omega} l(x,v) dv$

 $i_d(x) = \int_{\Omega} l(x + dv, v) dv$ 

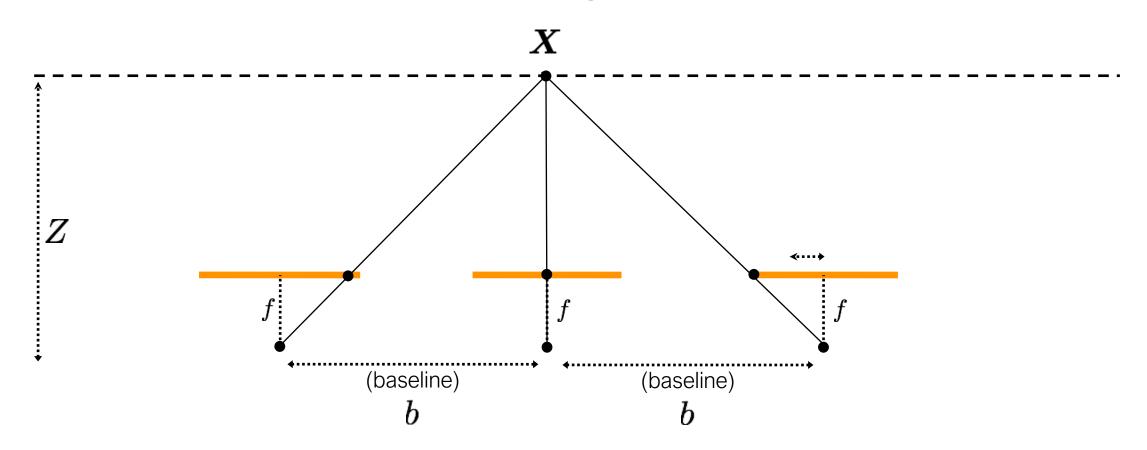
Where did this equation come from?



101

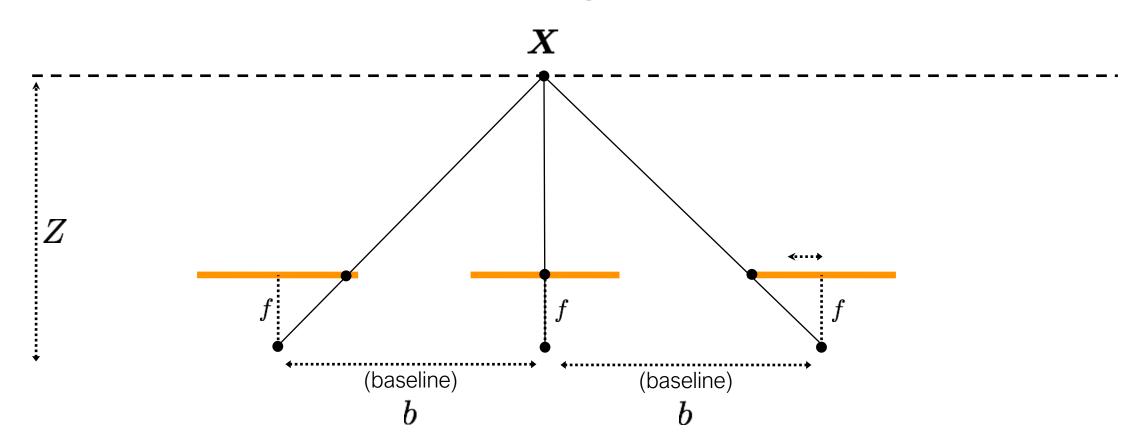
х

#### Stereo view of a lightfield camera



What are the different "cameras" in the lightfield case?

#### Stereo view of a lightfield camera

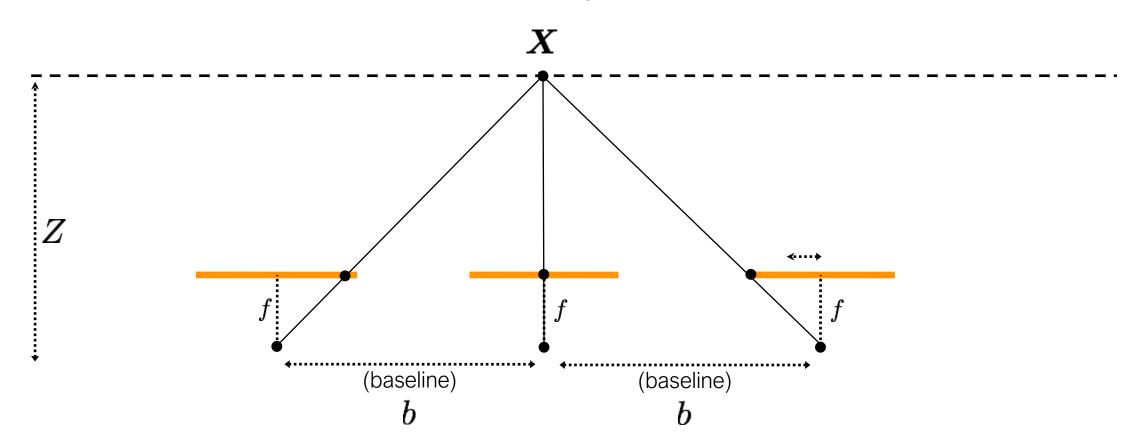


What are the different "cameras" in the lightfield case?

• Different aperture views  $L(u = u_o, v = v_o, s, t)$ .

By how much do I need to shift each aperture to focus (i.e., align) at depth Z?

#### Stereo view of a lightfield camera



What are the different "cameras" in the lightfield case?

• Different aperture views  $L(u = u_o, v = v_o, s, t)$ .

By how much do I need to shift each aperture to focus (i.e., align) at depth Z?

• By an amount equal to the disparity relative to the center view for depth Z.

## Refocusing example



## Refocusing example



## Refocusing example

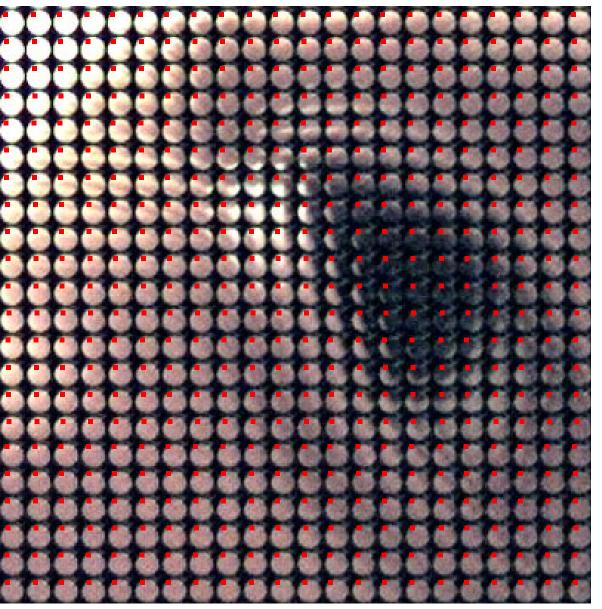


## 3D from lightfield

Simulate different viewpoints?

• Pick same pixel within each aperture view

Can we use different viewpoints for stereo?



# 3D from lightfield

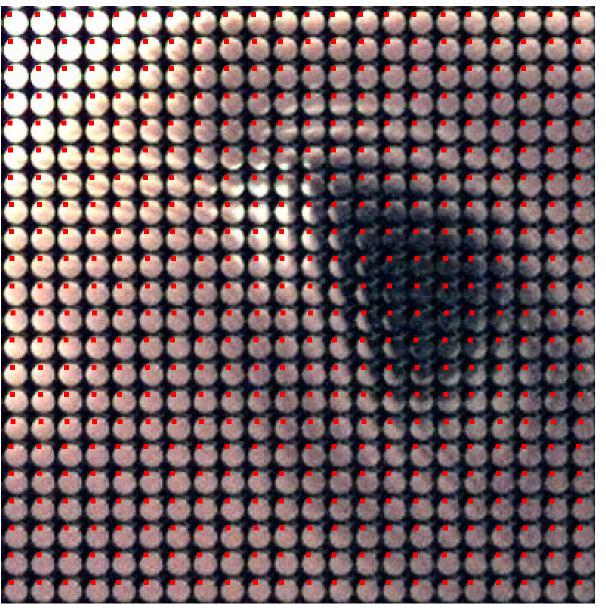
Simulate different viewpoints?

• Pick same pixel within each aperture view

Can we use different viewpoints for stereo?

- Very small baseline to use disparity algorithm.
- Standard algorithm only works with two views.

Can we do something better?



# 3D from lightfield

Simulate different viewpoints?

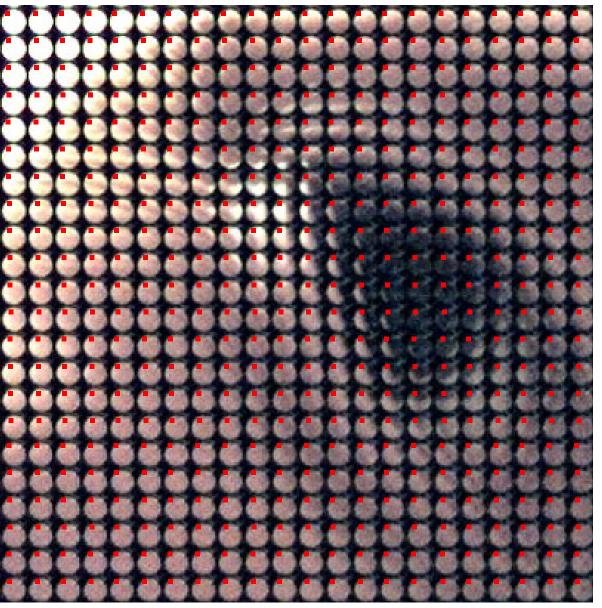
• Pick same pixel within each aperture view

Can we use different viewpoints for stereo?

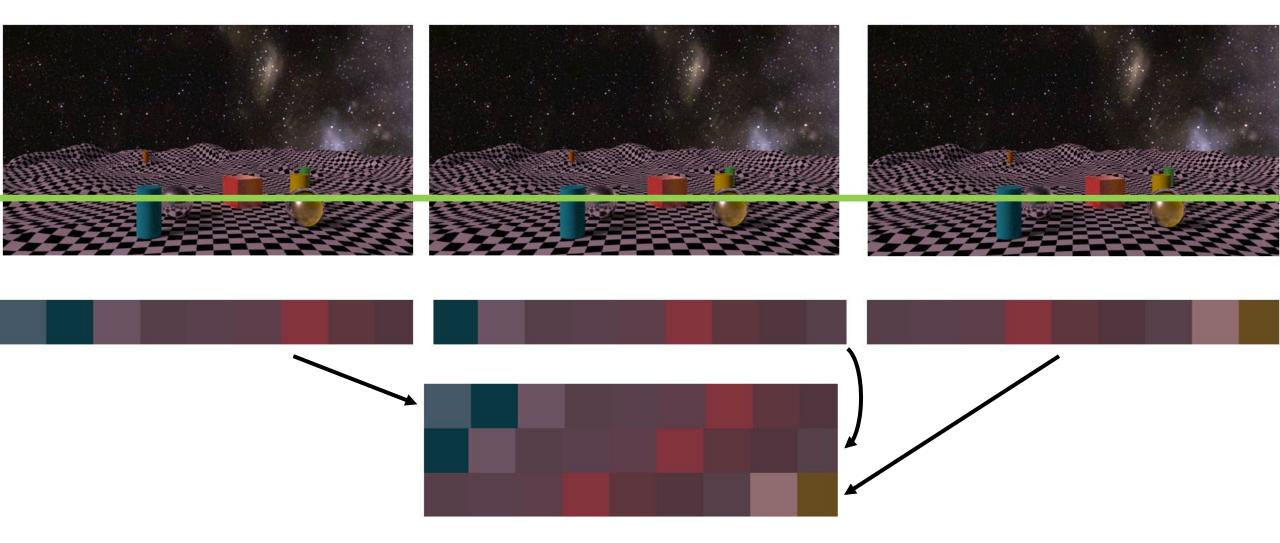
- Very small baseline to use disparity algorithm.
- Standard algorithm only works with two views.

Can we do something better?

- Take advantage of *dense* set of views.
- Use disparity to explain changes in views.

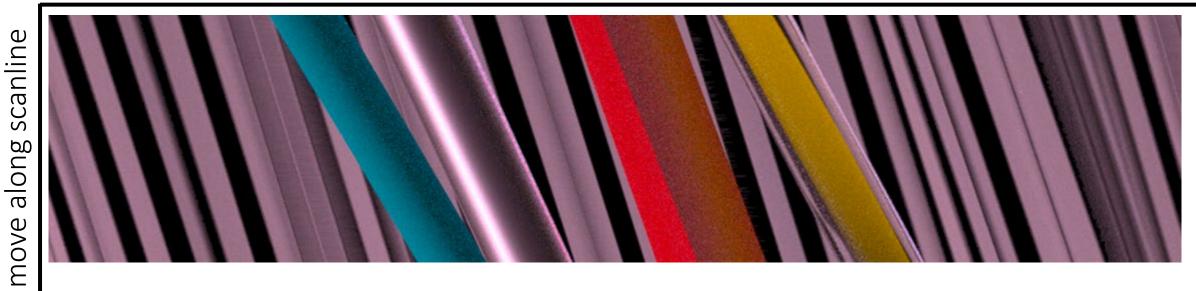


Use lightfield to synthesize images for all aperture views on a horizontal line (*scanline*).



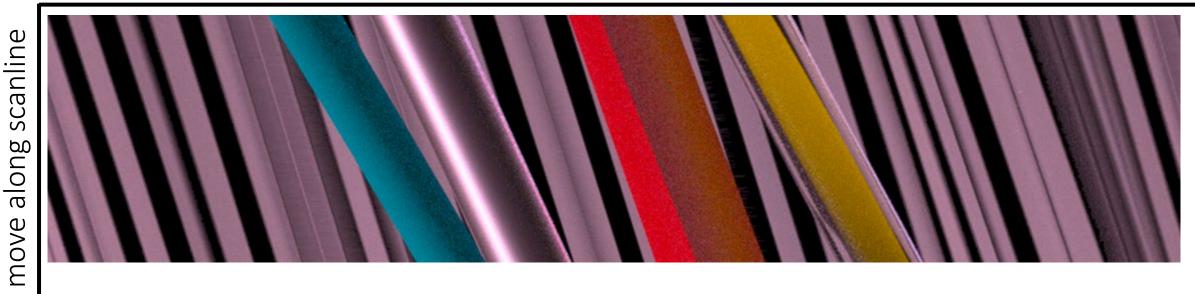
Why do we see straight lines?

#### move along image columns



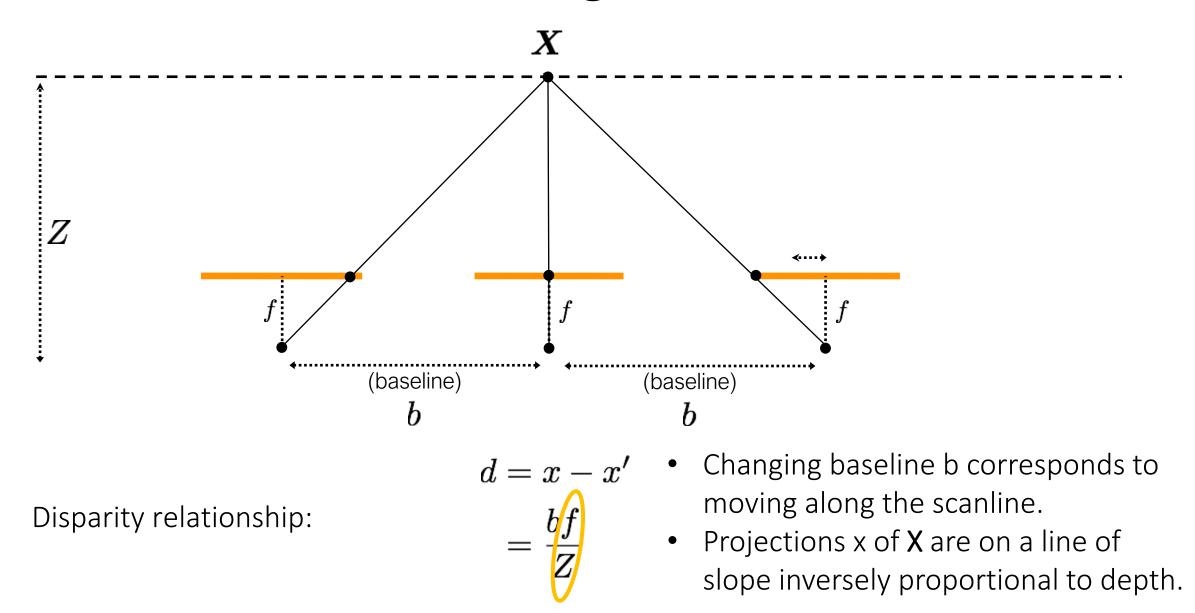
Why do we see straight lines?

• Same 3D point changes location as viewpoint changes (i.e., *disparity*). What does the slope of each line correspond to?

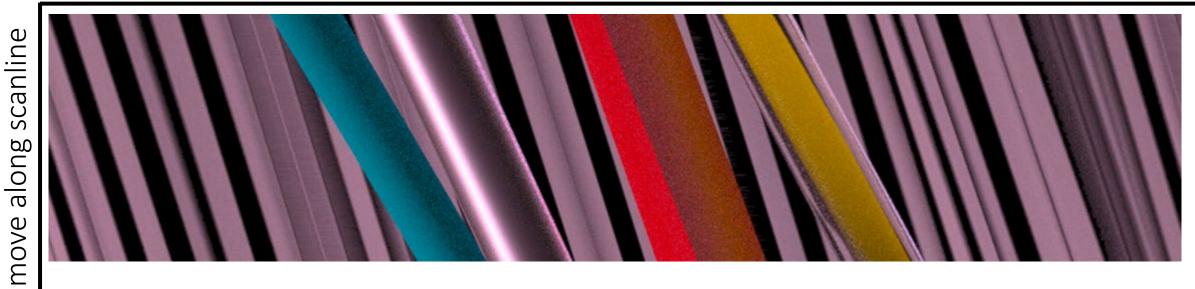


move along image columns

### Stereo view of a lightfield camera

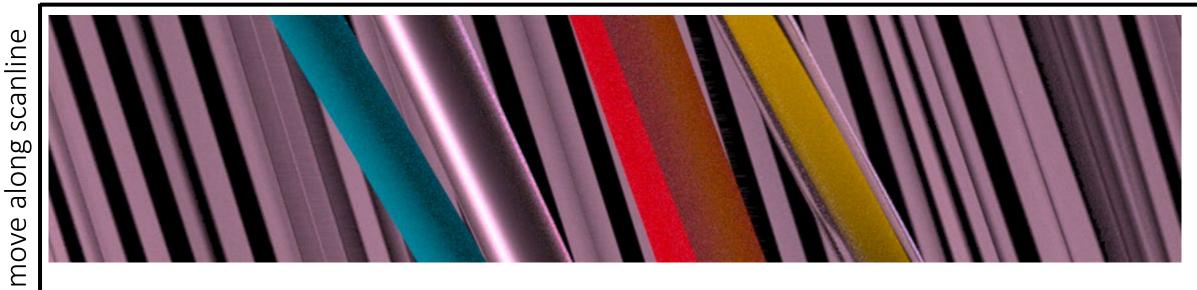


Per-pixel depth detection through line fitting and slope estimation.



move along image columns

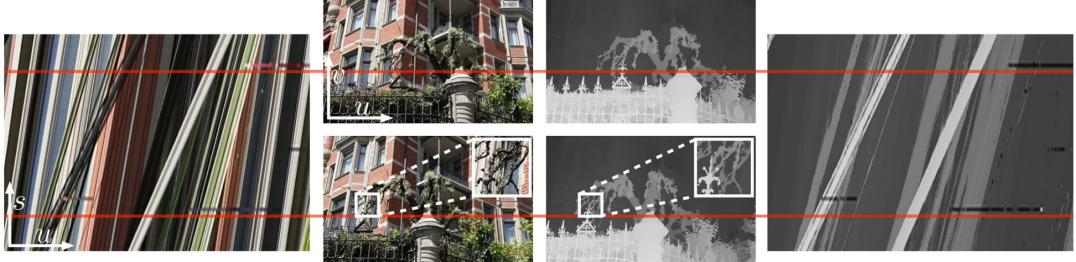
Per-pixel depth detection through line fitting and slope estimation.



move along image columns

#### Scene Reconstruction from High Spatio-Angular Resolution Light Fields

Changil Kim<sup>1,2</sup> Henning Zimmer<sup>1,2</sup> Yael Pritch<sup>1</sup> Alexander Sorkine-Hornung<sup>1</sup> Markus Gross<sup>1,2</sup> <sup>1</sup>Disney Research Zurich <sup>2</sup>ETH Zurich

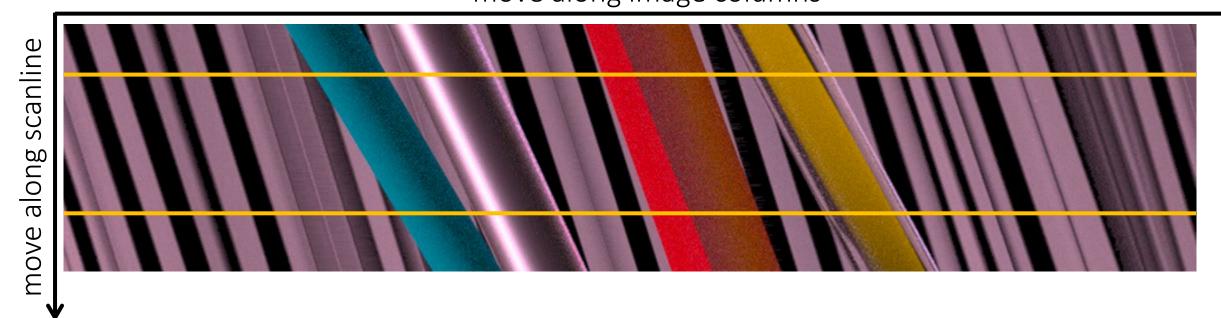


**Figure 1:** Our method reconstructs accurate depth from light fields of complex scenes. The images on the left show a 2D slice of a 3D input light field, a so called epipolar-plane image (EPI), and two out of one hundred 21 megapixel images that were used to construct the light field. Our method computes 3D depth information for all visible scene points, illustrated by the depth EPI on the right. From this representation, individual depth maps or segmentation masks for any of the input views can be extracted as well as other representations like 3D point clouds. The horizontal red lines connect corresponding scanlines in the images with their respective position in the EPI.

What part of the EPI is captured when we use a stereo pair of cameras?



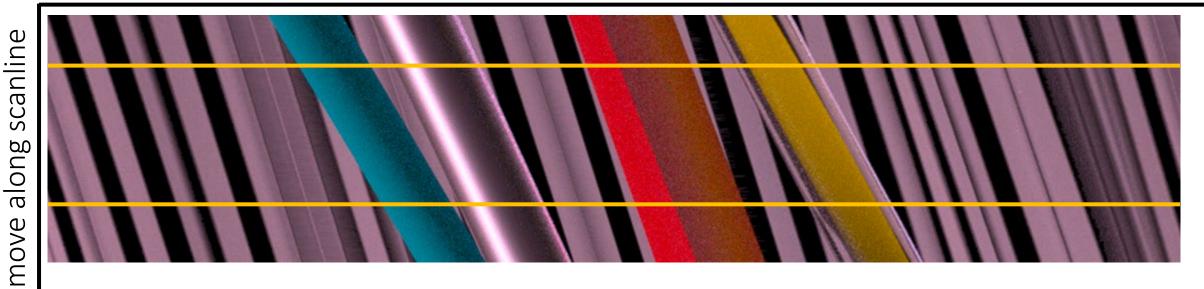
What part of the EPI is captured when we use a stereo pair of cameras?



What part of the EPI is captured when we use a stereo pair of cameras?

• Two horizontal lines.

When are these two views sufficient to infer depth?

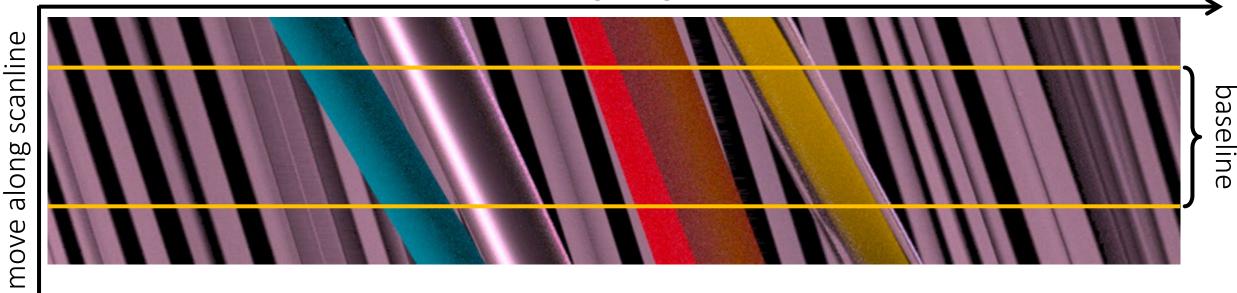


What part of the EPI is captured when we use a stereo pair of cameras?

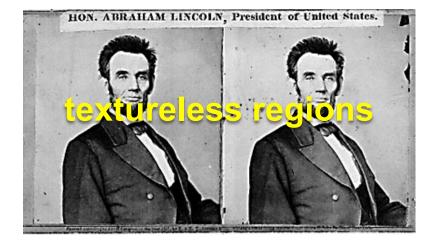
• Two horizontal lines.

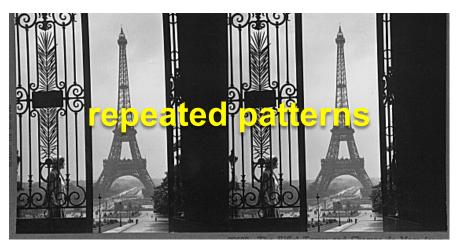
When are these two views sufficient to infer depth?

• When their *baseline* is large enough to infer the slope of the lines in EPIs.



#### When are correspondences difficult?



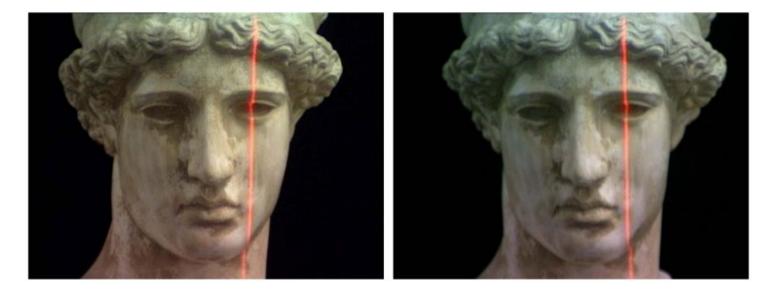


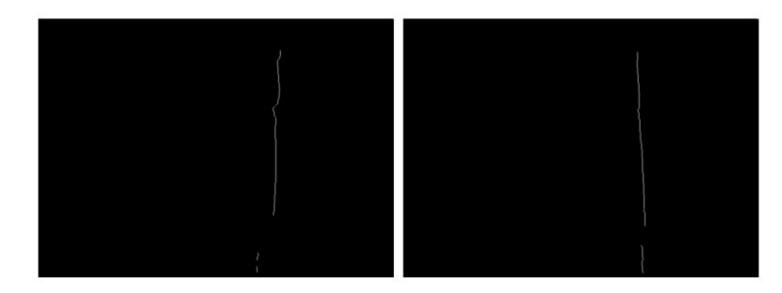


### Structured light

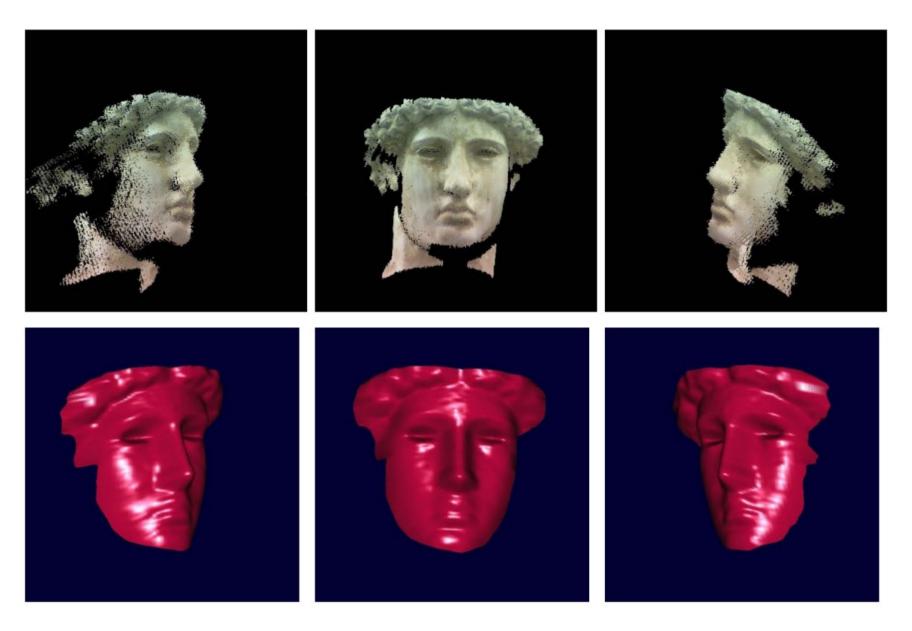
#### Use controlled ("structured") light to make correspondences easier

Disparity between laser points on the same scanline in the images determines the 3-D coordinates of the laser point on object

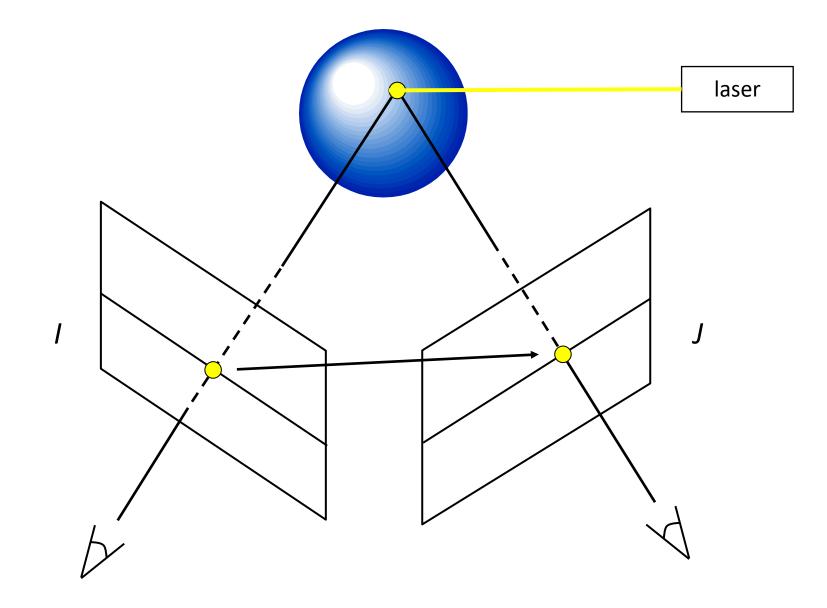




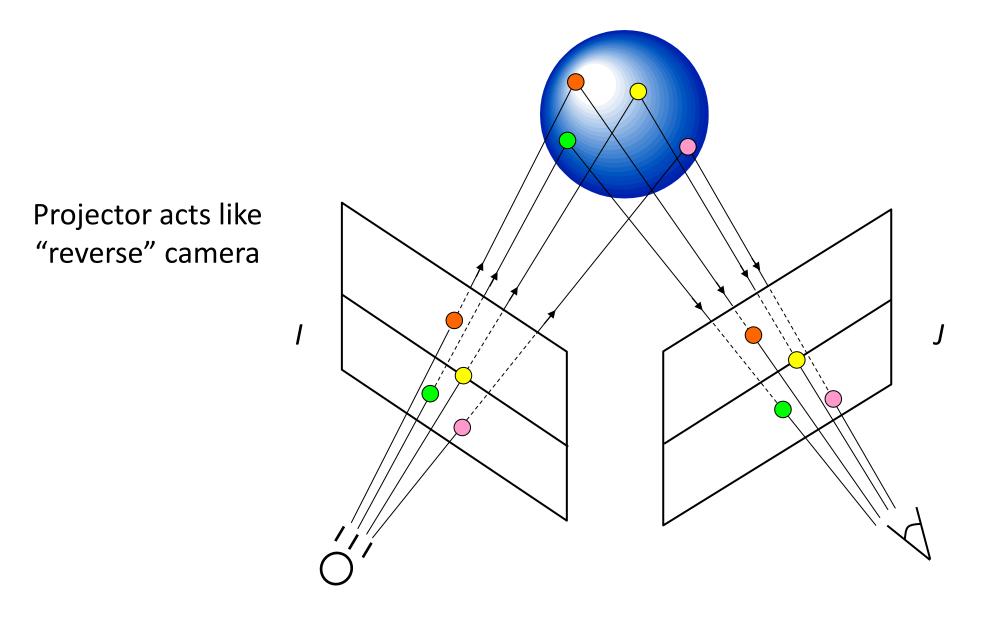
#### Use controlled ("structured") light to make correspondences easier



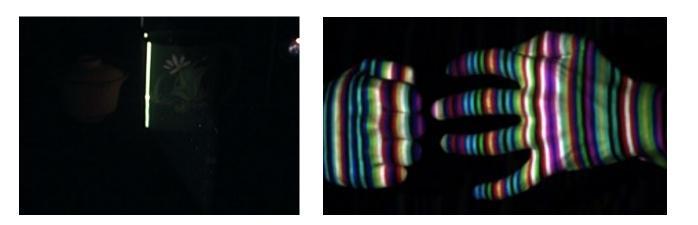
### Structured light and two cameras

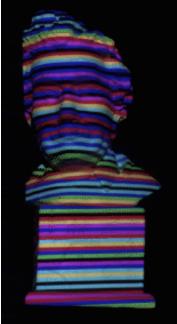


### Structured light and one camera



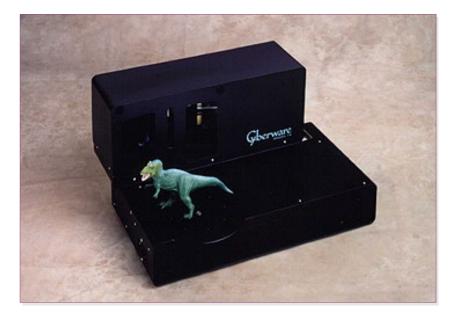
### Structured Light

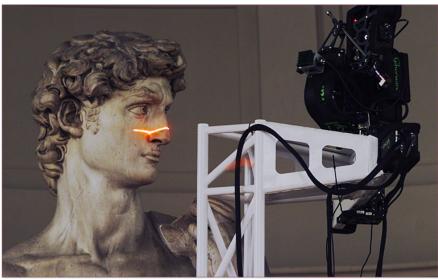




- Any spatio-temporal pattern of light projected on a surface (or volume).
- Cleverly illuminate the scene to extract scene properties (eg., 3D).
- Avoids problems of 3D estimation in scenes with complex texture/BRDFs.
- Very popular in vision and successful in industrial applications (parts assembly, inspection, etc).

### 3D Scanning using structured light



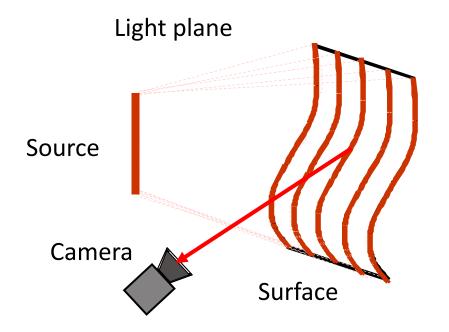


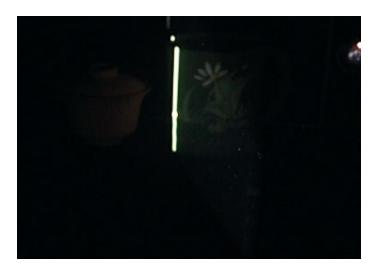




#### Do we need to illuminate the scene point by point?

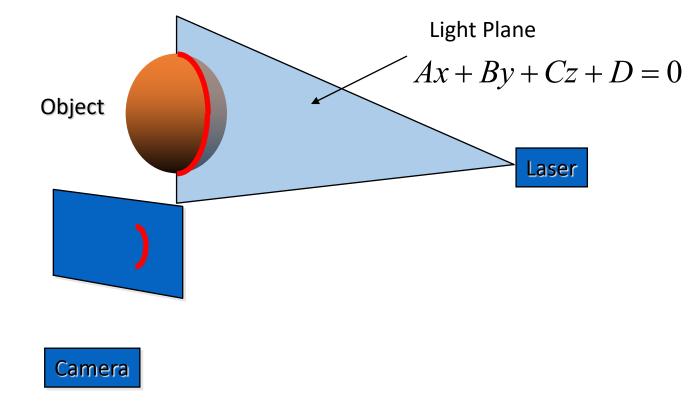
### Light Stripe Scanning – Single Stripe





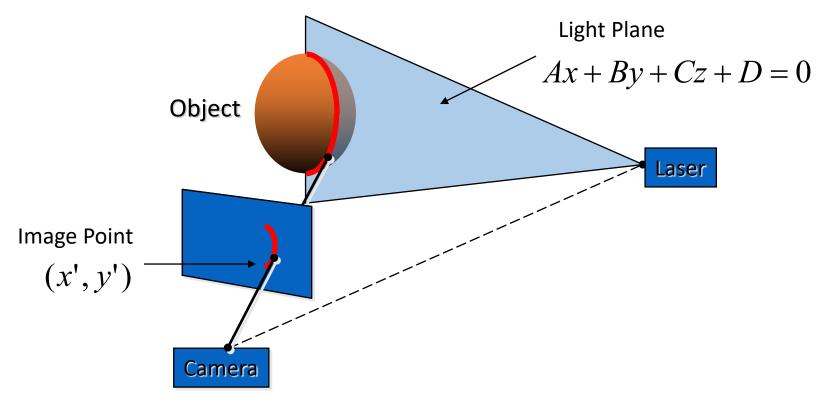
- Faster optical triangulation:
  - Project a single stripe of laser light
  - Scan it across the surface of the object
  - This is a very precise version of structured light scanning
  - Good for high resolution 3D, but still needs many images and takes time

### Triangulation



• Project laser stripe onto object

### Triangulation



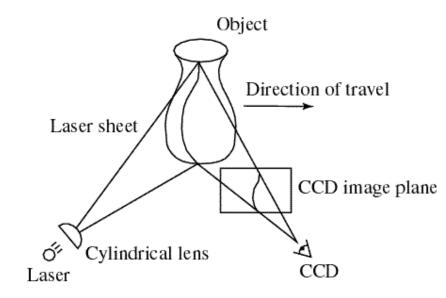
- Depth from ray-plane triangulation:
  - Intersect camera ray with light plane

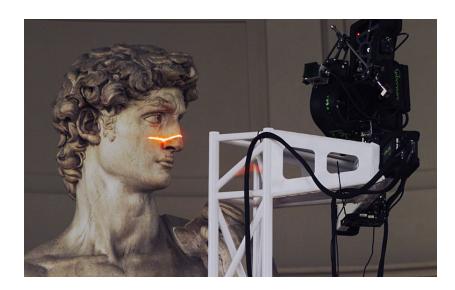
$$x = x'z / f$$
  

$$y = y'z / f$$
  

$$z = \frac{-Df}{Ax'+By'+Cf}$$

### Example: Laser scanner





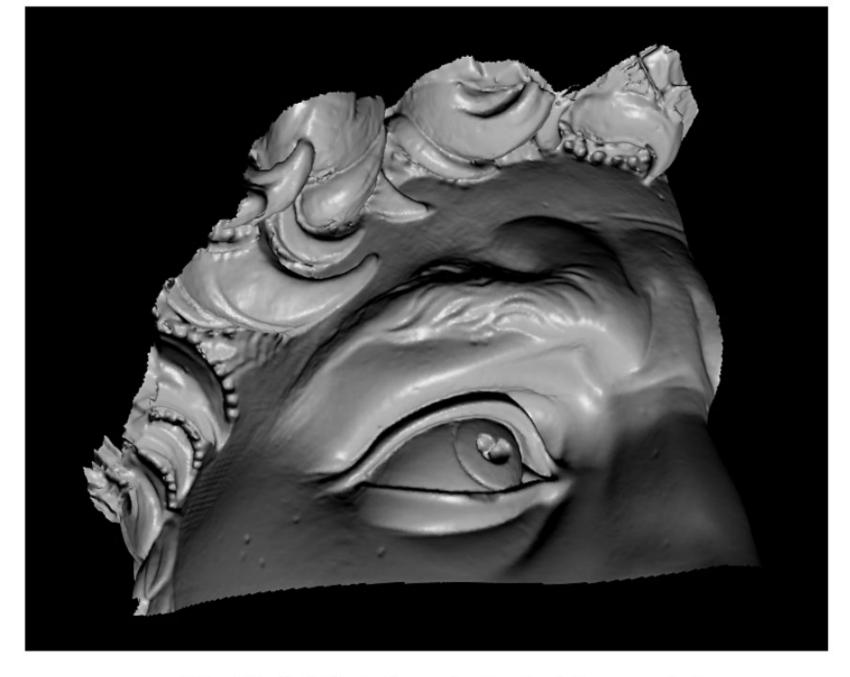
Digital Michelangelo Project http://graphics.stanford.edu/projects/mich/



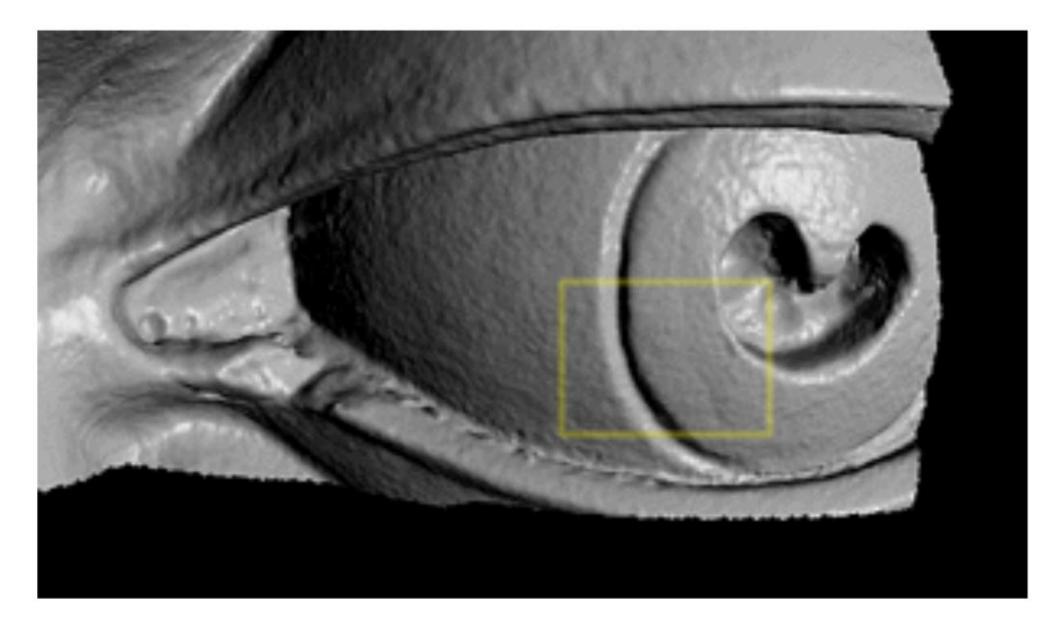
The Digital Michelangelo Project, Levoy et al.



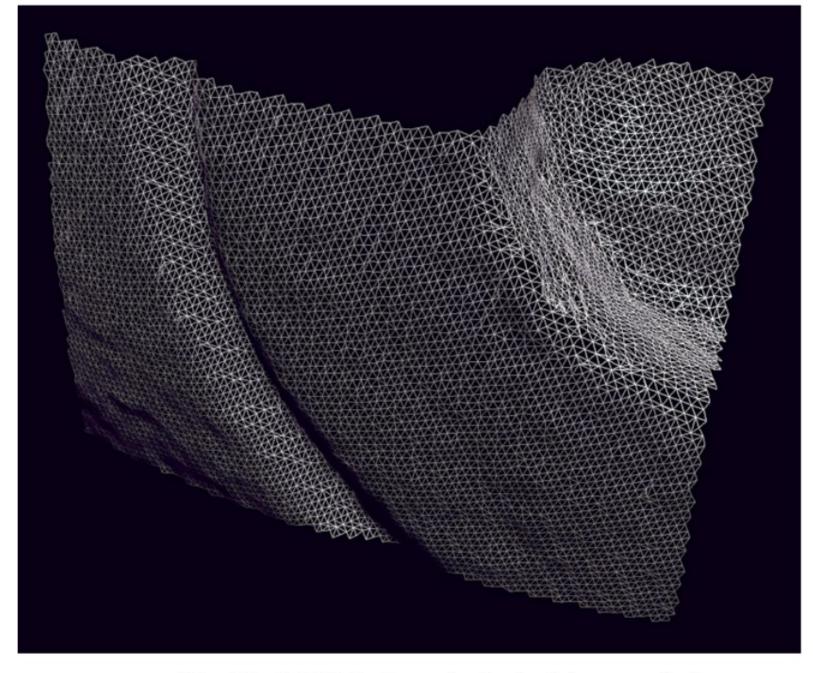
The Digital Michelangelo Project, Levoy et al.



The Digital Michelangelo Project, Levoy et al.



The Digital Michelangelo Project, Levoy et al.



The Digital Michelangelo Project, Levoy et al.

### Binary coding

### Faster Acquisition?

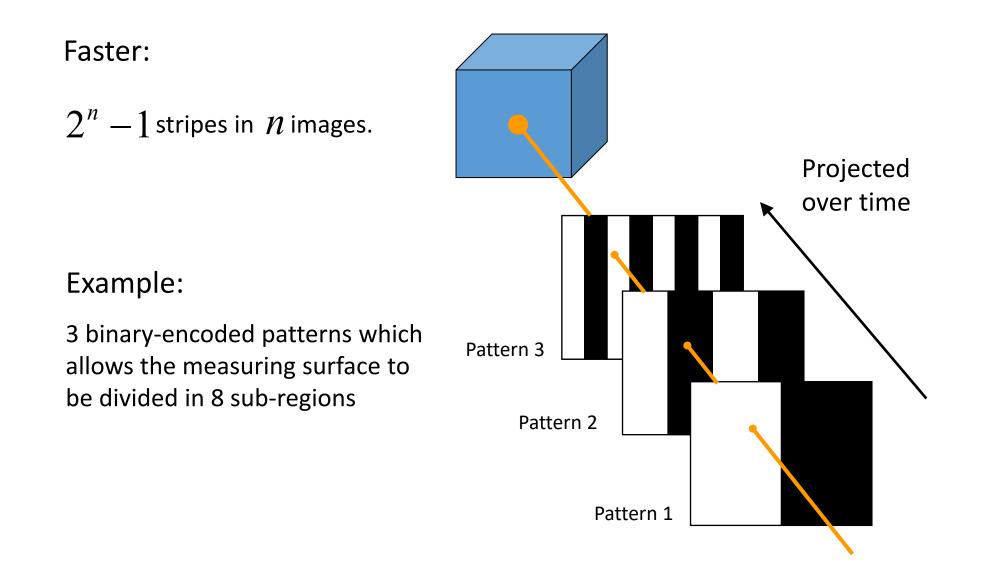
#### Faster Acquisition?

- Project multiple stripes simultaneously
- What is the problem with this?

#### Faster Acquisition?

- Project multiple stripes simultaneously
- Correspondence problem: which stripe is which?
- Common types of patterns:
  - Binary coded light striping
  - Gray/color coded light striping

#### **Binary Coding**



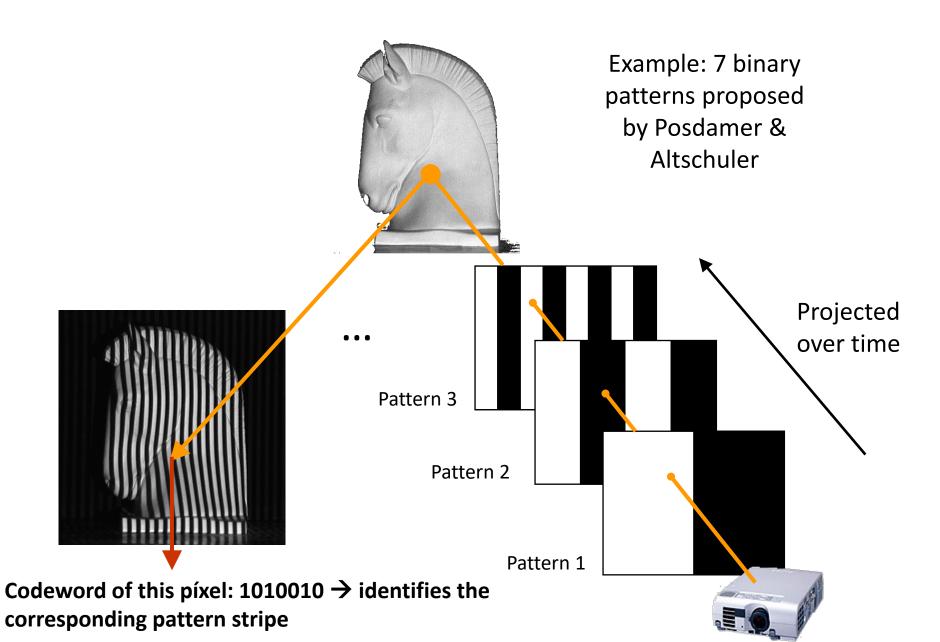
#### **Binary Coding**

• Assign each stripe a unique illumination code over time [Posdamer 82]



Space

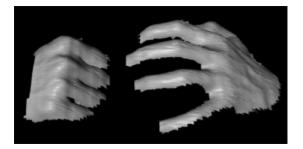
#### **Binary Coding**



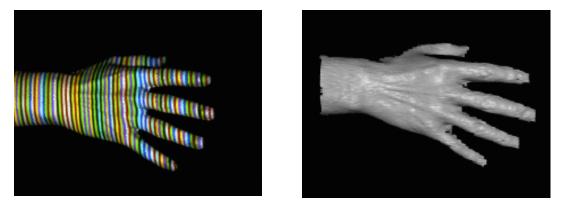
#### More complex patterns







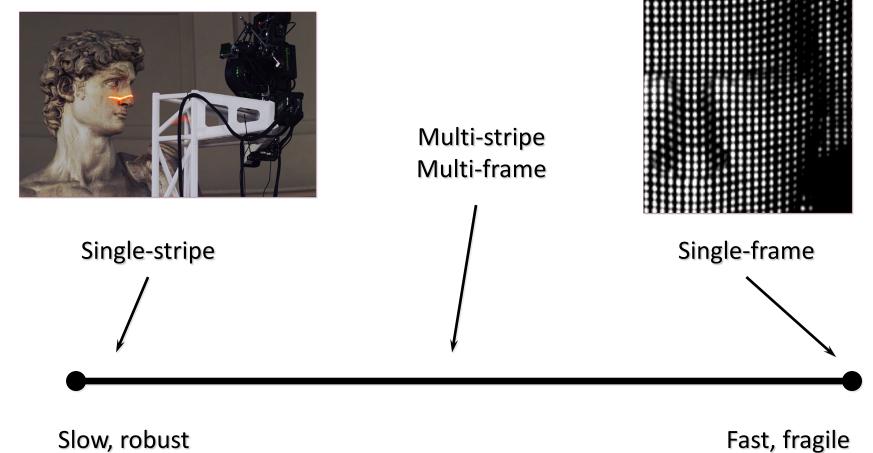
Works despite complex appearances



Works in real-time and on dynamic scenes

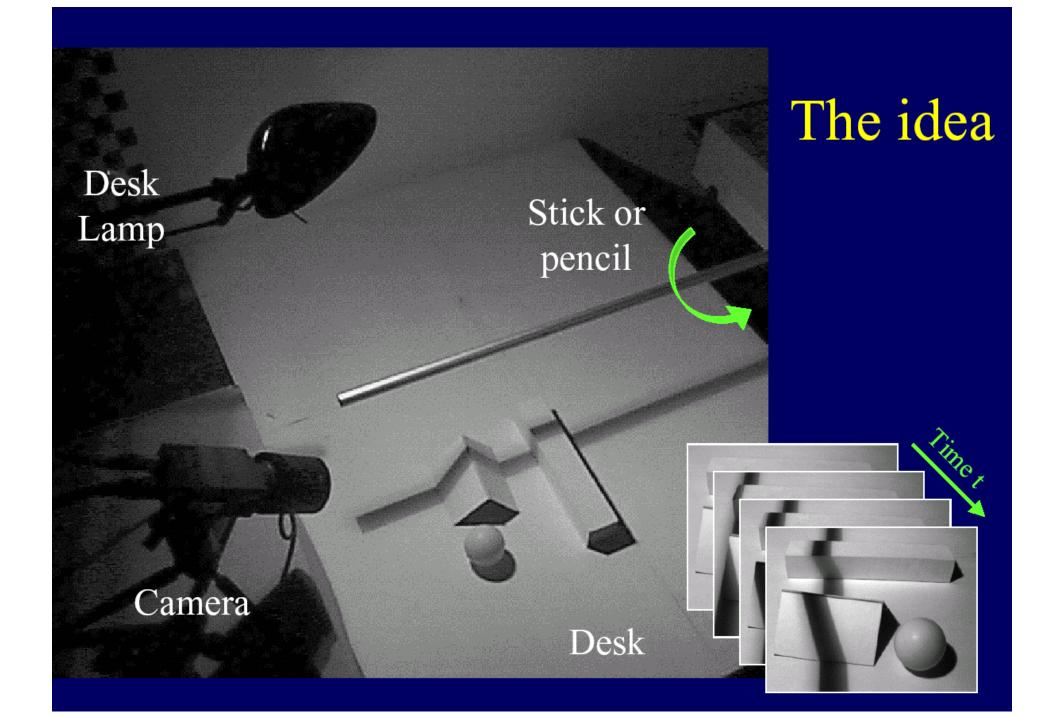
- Need very few images (one or two).
- But needs a more complex correspondence algorithm

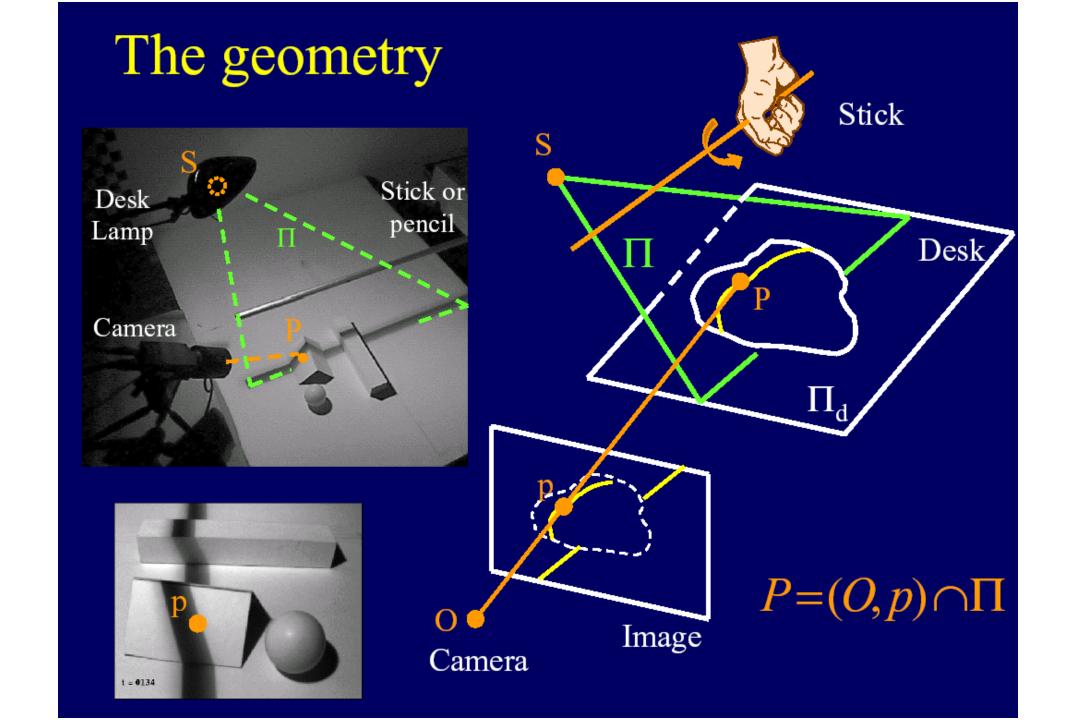
#### Continuum of Triangulation Methods

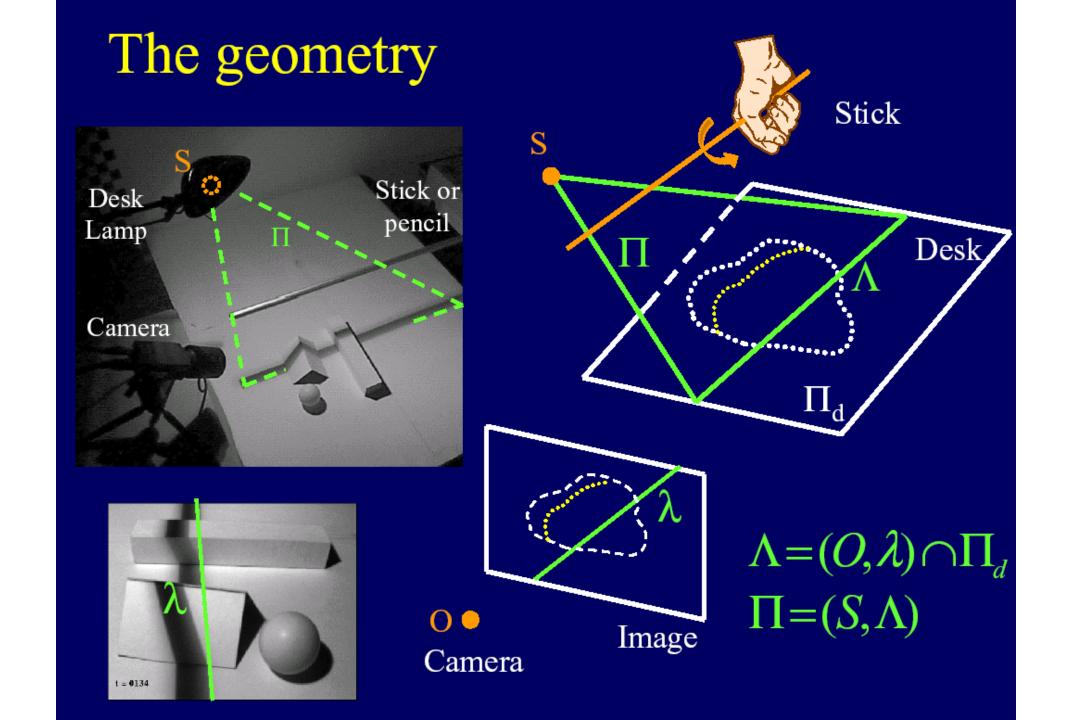


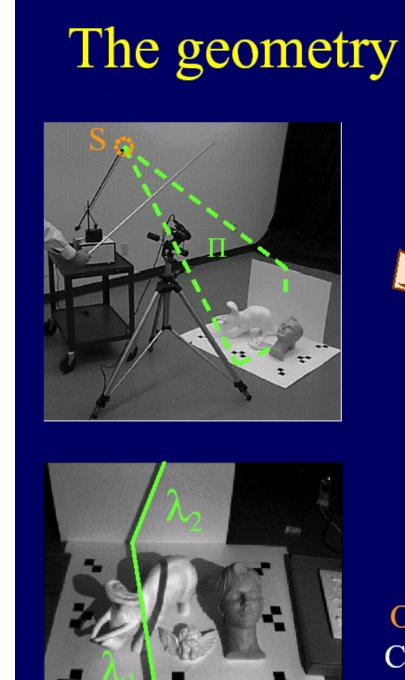
Fast, fragile

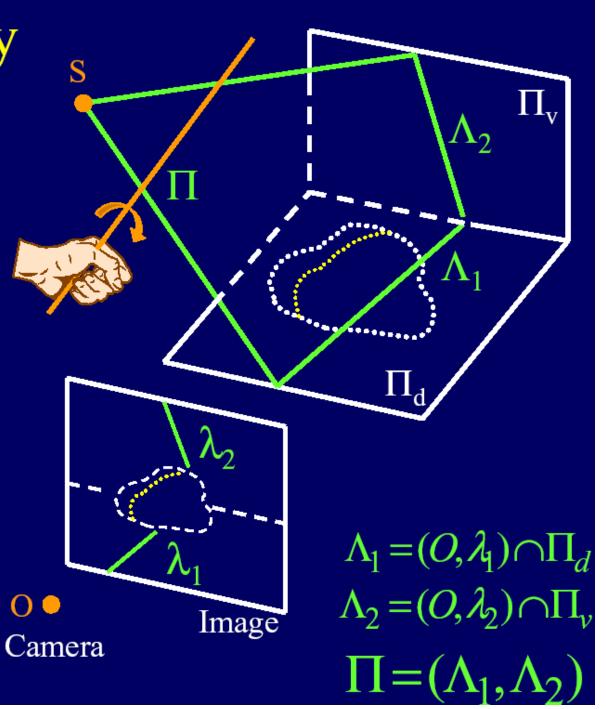
#### Using shadows











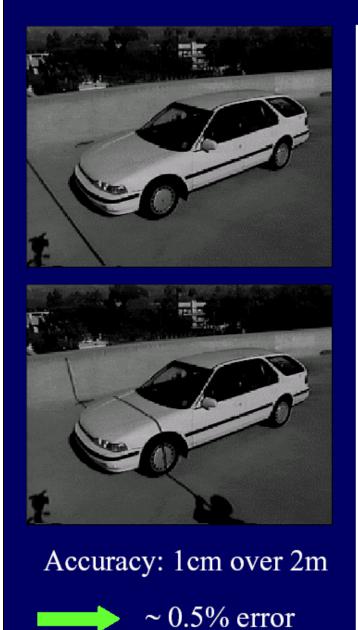
### Angel experiment

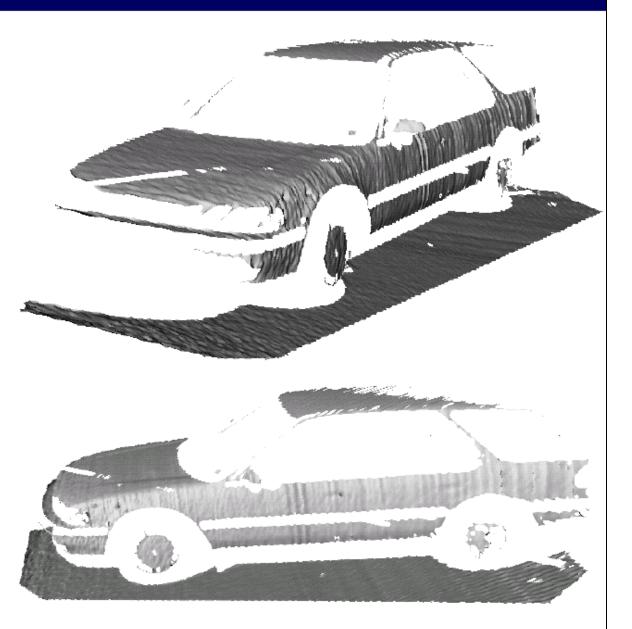




Accuracy: 0.1mm over 10cm  $\rightarrow$  ~ 0.1% error

### Scanning with the sun





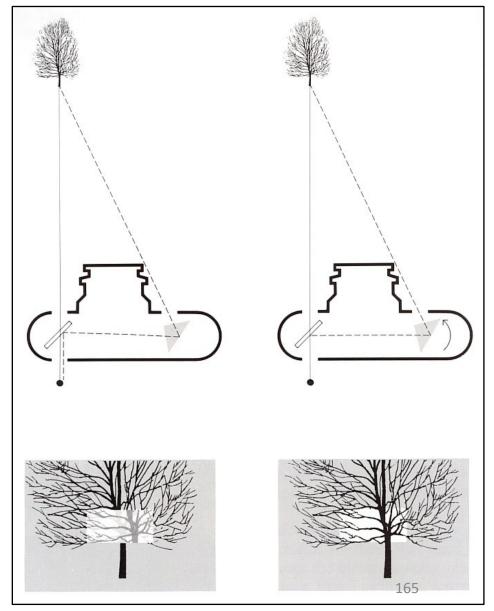
### Revisiting auto-focusing

### Why does this work in rangefinder cameras?

- Focusing based on triangulation: when the image is in focus, you will see the two copies aligned.
- Very accurate but very painstaking.
- Different perspective than that of the main lens.

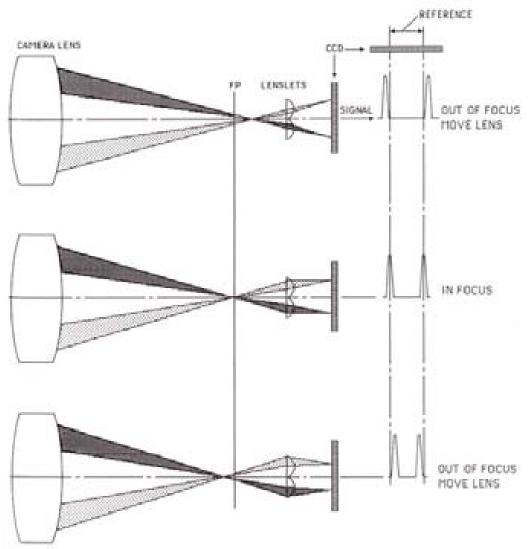
standard in Leica cameras





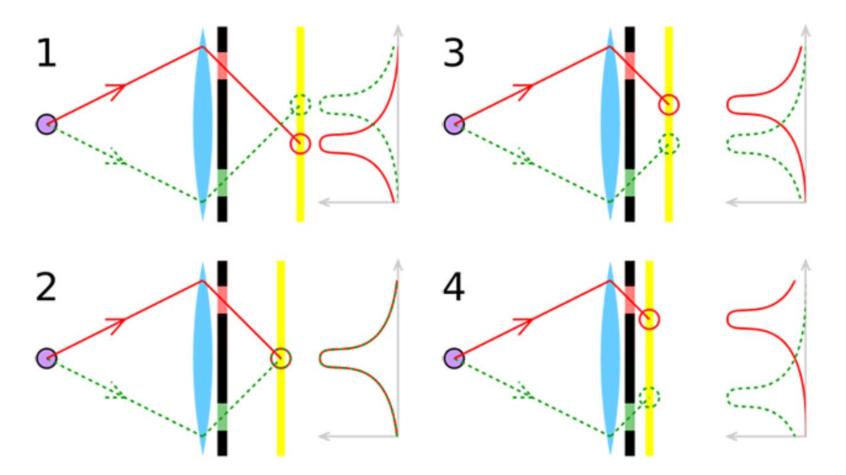
# Why does this work for phase detection?

- As the lens moves, ray bundles from an object converge to a different point in the camera and change in angle.
- This change in angle causes them to refocus through two lenslets to different positions on a separate AF sensor.
- A certain spacing between these double images indicates that the object is "in focus".



Demo: http://graphics.stanford.edu/courses/cs178/applets/autofocuspd.html

### Why does this work for phase detection?



Each yellow box indicates *two* sensors, each measuring light from different parts of the aperture.

- Which one is correct focusing?
- How do you need to move the lens or sensor to get correct focusing?

## Dual-pixels: disparity with incredibly small baseline

Pixels dedicated to

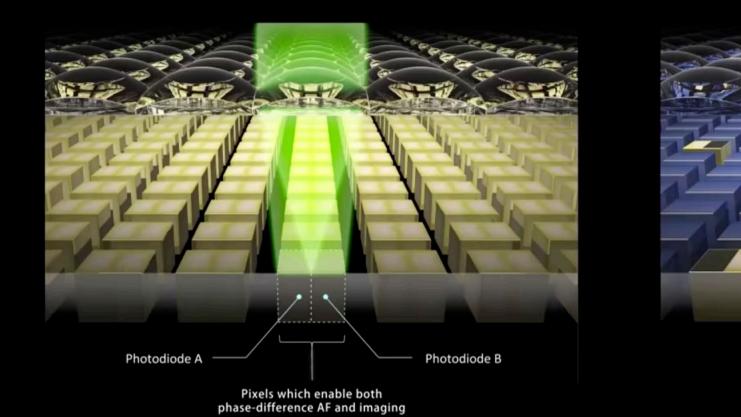
phase-difference AF

Pixels for

imaging

- Split each pixel into two independent photodiodes—like a two-view lightfield.
- Use different pixels for phase detection.
- Many other interesting opportunities (depth from stereo/lightfield with a tiny baseline).

All pixels are configured to be used for imaging as well as phase-difference AF\*



Basic reading:

- Szeliski textbook, Sections 7.1, 8.1, Chapter 11, Sections 11.1, 12.2.
- Hartley and Zisserman, Section 11.12.
- Boles et al., "Epipolar-plane image analysis: An approach to determining structure from motion," IJCV 1987.
  - This classical paper introduces EPIs, and discusses how they can be used to infer depth.
- Lanman and Taubin, "Build Your Own 3D Scanner: Optical Triangulation for Beginners," SIGGRAPH course 2009.

- This very comprehensive course has everything you need to know about 3D scanning using structured light, including details on how to build your own.

• Bouguet and Perona, "3D Photography Using Shadows in Dual-Space Geometry," IJCV 1999.

- This paper introduces the idea of using shadows to do structured light 3D scanning, and shows an implementation using just a camera, desk lamp, and a stick.

Additional reading:

• Gupta et al., "A Practical Approach to 3D Scanning in the Presence of Interreflections, Subsurface Scattering and Defocus," IJCV 2013.

- This paper has a very detailed treatment of standard patterns used for structured light, problems arising due to global illumination, and robust patterns for dealing with these patterns.

- Barron et al., "Fast bilateral-space stereo for synthetic defocus," CVPR 2015.
- Barron and Poole, "The fast bilateral solver," ECCV 2016.

- The above two papers show how to combine edge-aware filtering (and bilateral filtering in particular) with disparity matching for robust stereo. The first paper also shows how the resulting depth maps can be used to create synthetic defocus blur.

- Wanner and Goldluecke, "Globally Consistent Depth Labeling of 4D Light Fields," CVPR 2012.
- Kim et al., "Scene reconstruction from high spatio-angular resolution light fields," SIGGRAPH 2013.

- These two papers show detailed systems for using EPIs to extract depth.

• Levin et al., "Understanding camera trade-offs through a Bayesian analysis of light field projections," ECCV 2008.

- This paper uses EPIs to show how different types of imaging systems (pinhole cameras, plenoptic cameras, stereo pairs, lens-based systems, and so on) relate to each other, and analyze their pros and cons for 3D imaging.