

# Edge-aware and bilateral filtering



15-463, 15-663, 15-862  
Computational Photography  
Fall 2021, Lecture 9

# Course announcements

- Homework assignment 3 posted.
  - Due October 18th.
  - Start early: tricky implementation that is easy to get wrong.
- Grades for homework assignment 2 posted.
- Propose and/or vote for topics for this week's reading group.

# Overview of today's lecture

- Leftover from lecture 8.
- Back to tonemapping.
- Edge-aware filtering and bilateral filtering.
- Non-local means.
- Flash/no-flash photography.
- Joint bilateral filtering.

# Slide credits

Many of these slides were inspired or adapted from:

- James Hays (Georgia Tech).
- Fredo Durand (MIT).
- Gordon Wetzstein (Stanford).
- Sylvain Paris (MIT).
- Sam Hasinoff (Google).

Back to tonemapping

# Dealing with color

If we tonemap all channels the same, colors are washed out



Can you think of a way to deal with this?

# Intensity-only tonemapping

tonemap  
intensity



leave color  
the same



How would you implement this?

# Comparison

Color now OK, but some details are washed out due to loss of contrast

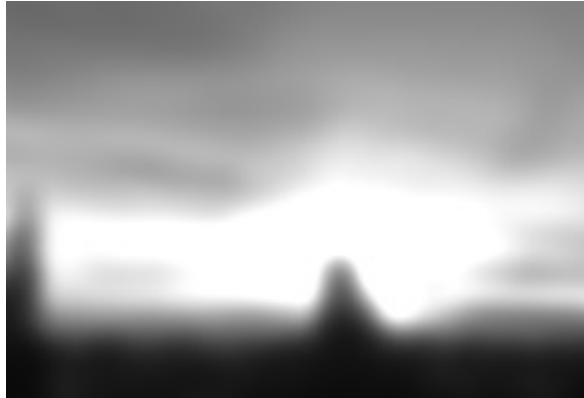


Can you think of a way to deal with this?



# Low-frequency intensity-only tonemapping

tonemap low-frequency  
intensity component



leave high-frequency  
intensity component  
the same



leave color the same



How would you implement this?

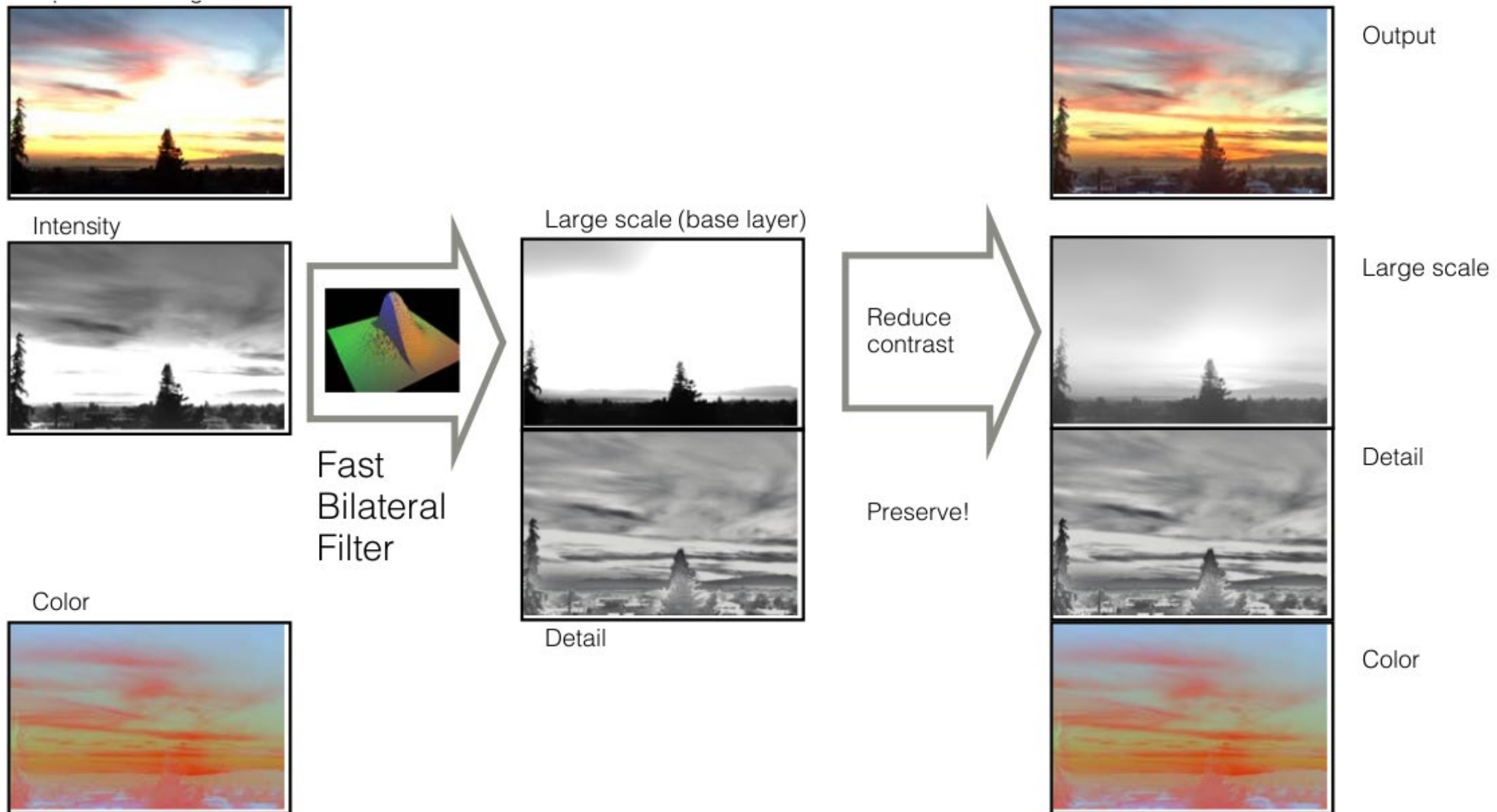
# Comparison

We got nice color and contrast, but now we've run into the halo plague



Can you think of a way to deal with this?

# Tonemapping with bilateral filtering



# Comparison

We fixed the halos without losing contrast





# Edge-aware filtering and bilateral filtering

# Motivational example



original

Let's say I want to reduce the amount of detail in this picture. What can I do?

# Motivational example



original



Gaussian filtering

What is the problem here?



# Motivational example



original



Gaussian filtering

How to smooth out the details in the image without losing the important edges?

# Motivational example



original

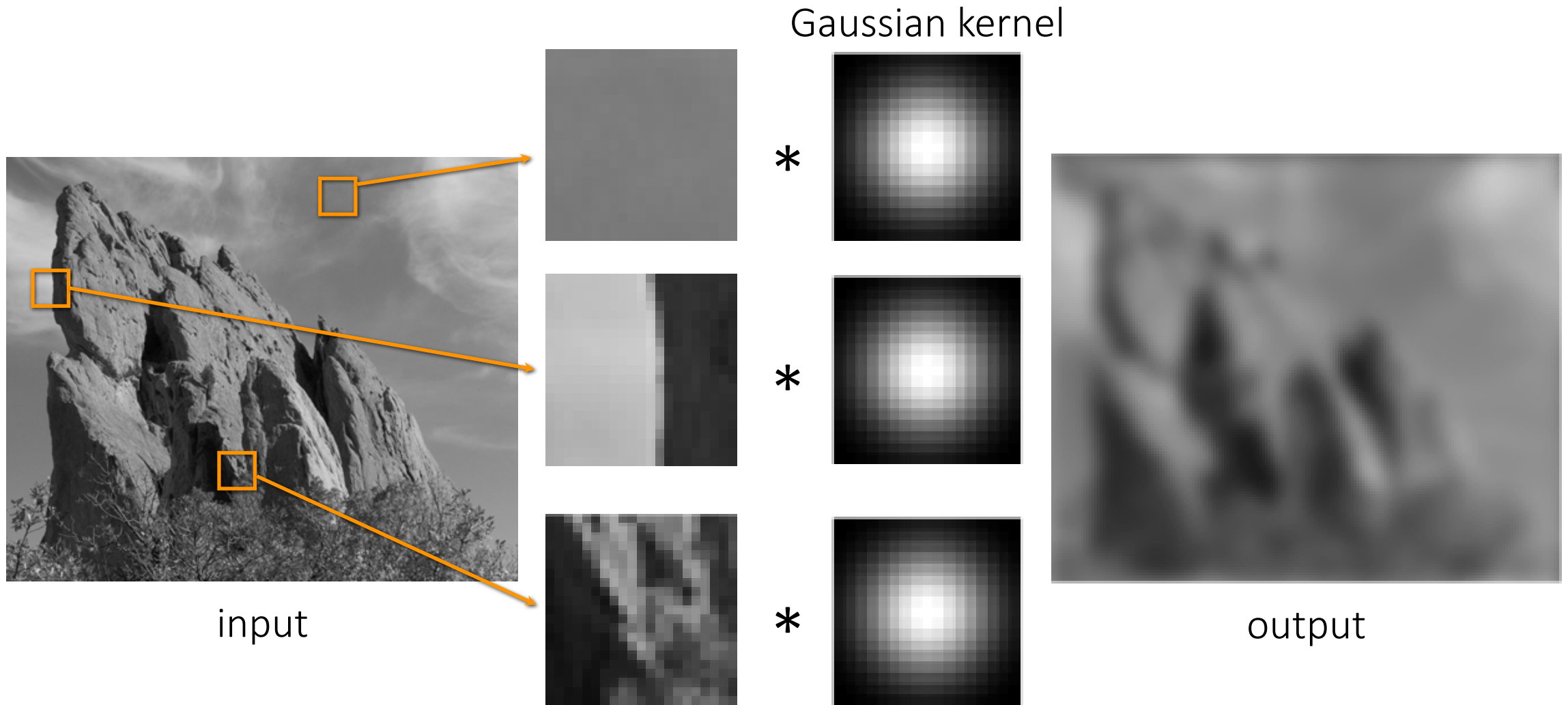


Gaussian filtering

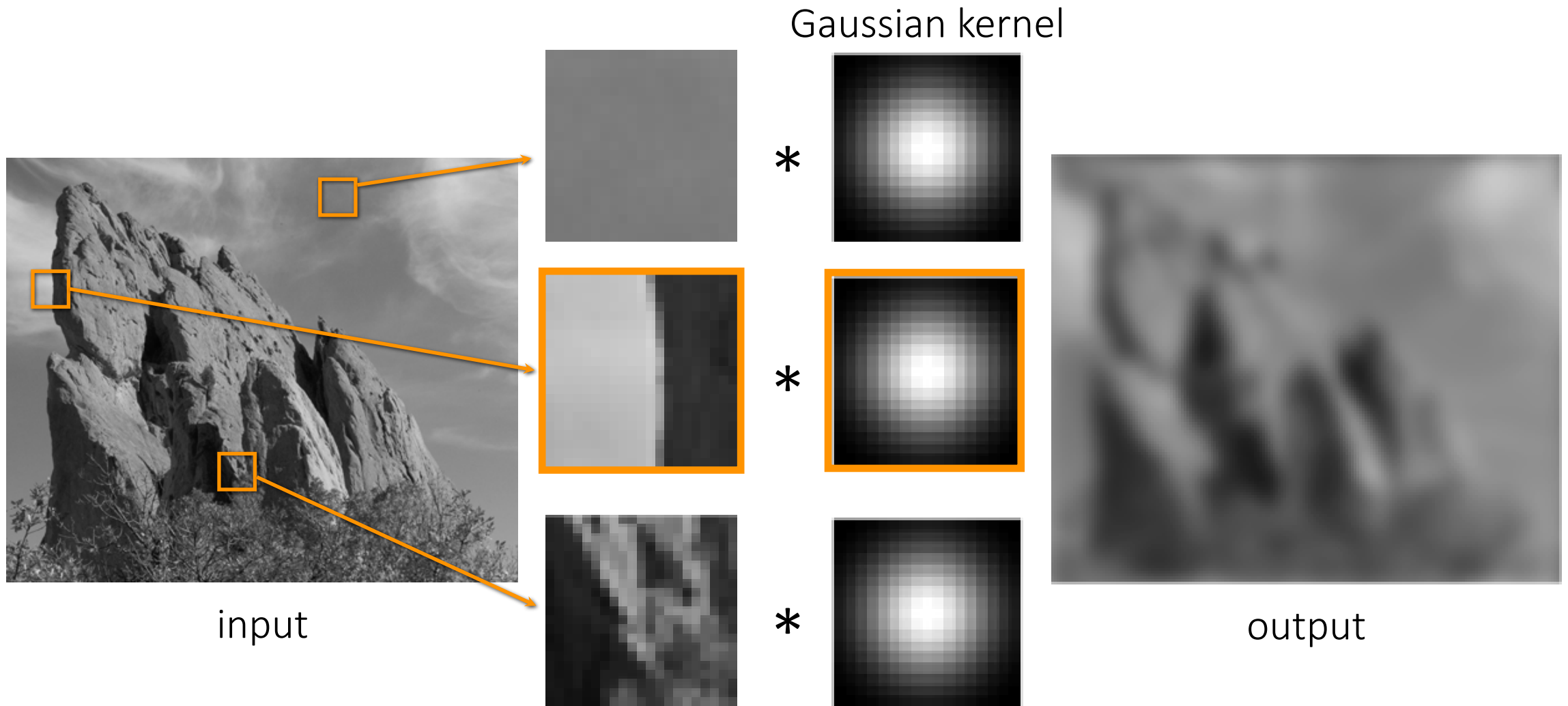


bilateral filtering

# The problem with Gaussian filtering

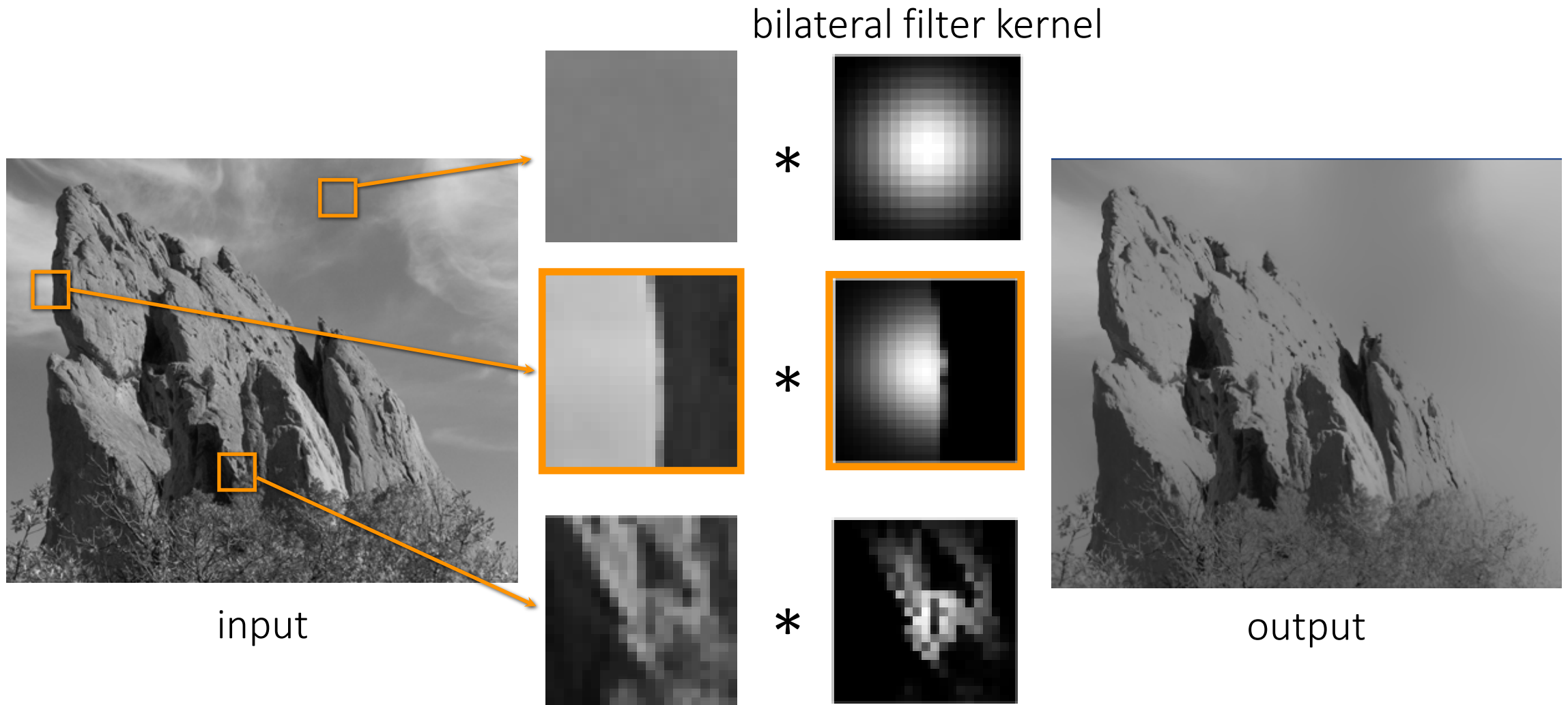


# The problem with Gaussian filtering



Blur kernel averages across edges

# The bilateral filtering solution



Do not blur if there is an edge! How does it do that?

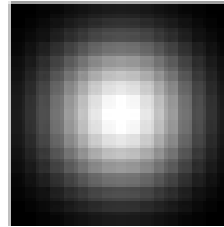
# Bilateral filtering

$$h[m, n] = \frac{1}{W_{mn}} \sum_{k,l} g[k, l] r_{mn}[k, l] f[m + k, n + l]$$

# Bilateral filtering

$$h[m, n] = \frac{1}{W_{mn}} \sum_{k,l} g[k, l] r_{mn}[k, l] f[m + k, n + l]$$

Spatial weighting



$\sigma_s$

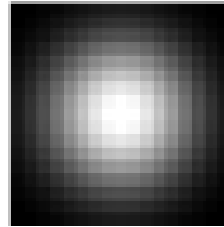
Assign a pixel a large weight if:

1) it's nearby

# Bilateral filtering

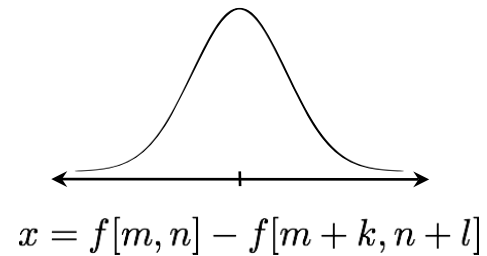
$$h[m, n] = \frac{1}{W_{mn}} \sum_{k,l} g[k, l] r_{mn}[k, l] f[m + k, n + l]$$

Spatial weighting



$\sigma_s$

Intensity range weighting



$\sigma_r$

Assign a pixel a large weight if:

1) it's nearby

and

2) it looks like me



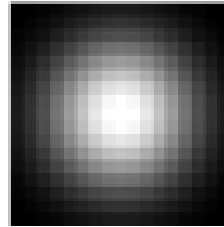
# Bilateral filtering

$$h[m, n] = \frac{1}{W_{mn}} \sum_{k,l} g[k, l] r_{mn}[k, l] f[m + k, n + l]$$

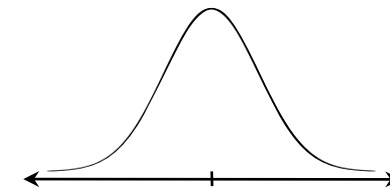
Normalization factor

Spatial weighting

Intensity range weighting



$\sigma_s$



$$x = f[m, n] - f[m + k, n + l]$$

$\sigma_r$

Assign a pixel a large weight if:

1) it's nearby

and

2) it looks like me

# Bilateral filtering vs Gaussian filtering

Which is which?

$$h[m, n] = \sum_{k, l} g[k, l] f[m + k, n + l]$$

$$h[m, n] = \frac{1}{W_{mn}} \sum_{k, l} g[k, l] r_{mn}[k, l] f[m + k, n + l]$$

# Bilateral filtering vs Gaussian filtering

Gaussian filtering

$$h[m, n] = \sum_{k, l} g[k, l] f[m + k, n + l]$$

Bilateral filtering

$$h[m, n] = \frac{1}{W_{mn}} \sum_{k, l} g[k, l] r_{mn}[k, l] f[m + k, n + l]$$

# Bilateral filtering vs Gaussian filtering

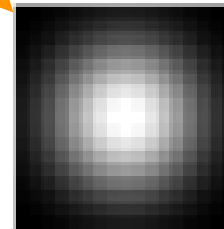
Gaussian filtering

$$h[m, n] = \sum_{k, l} g[k, l] f[m + k, n + l]$$

Bilateral filtering

$$h[m, n] = \frac{1}{W_{mn}} \sum_{k, l} g[k, l] r_{mn}[k, l] f[m + k, n + l]$$

$\sigma_s$



Spatial weighting:  
favor *nearby* pixels

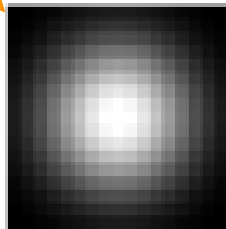
# Bilateral filtering vs Gaussian filtering

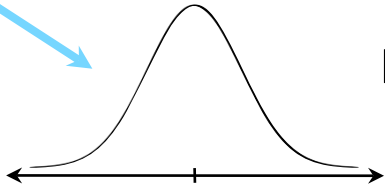
Gaussian filtering

$$h[m, n] = \sum_{k, l} g[k, l] f[m + k, n + l]$$

Bilateral filtering

$$h[m, n] = \frac{1}{W_{mn}} \sum_{k, l} g[k, l] r_{mn}[k, l] f[m + k, n + l]$$

$\sigma_s$   Spatial weighting: favor *nearby* pixels

$\sigma_r$   Intensity range weighting: favor *similar* pixels

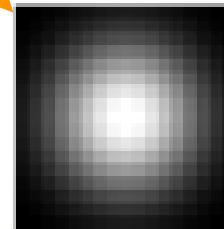
$x = f[m, n] - f[m + k, n + l]$

# Bilateral filtering vs Gaussian filtering

Gaussian filtering

$$h[m, n] = \sum_{k, l} g[k, l] f[m + k, n + l]$$

$\sigma_s$



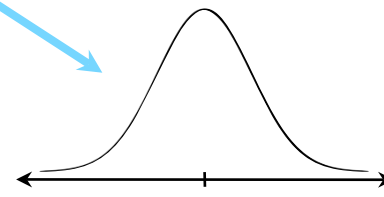
Spatial weighting:  
favor *nearby* pixels

Bilateral filtering

$$h[m, n] = \frac{1}{W_{mn}} \sum_{k, l} g[k, l] r_{mn}[k, l] f[m + k, n + l]$$

Normalization factor

$\sigma_r$



Intensity range weighting:  
favor *similar* pixels

$$x = f[m, n] - f[m + k, n + l]$$

# Bilateral filtering vs Gaussian filtering

## Gaussian filtering

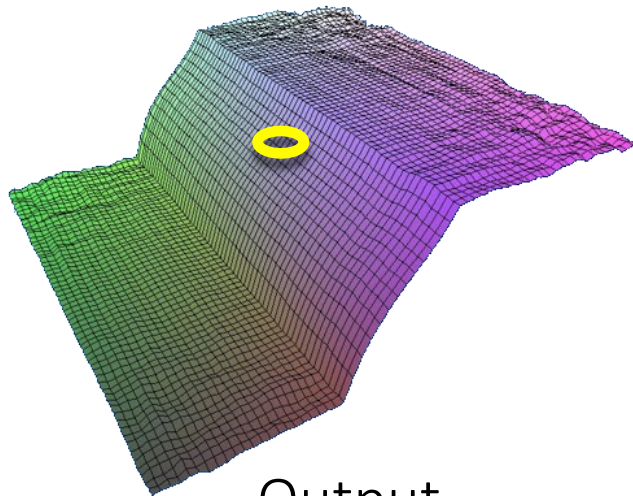
Smooths everything nearby (even edges)  
Only depends on *spatial* distance

## Bilateral filtering

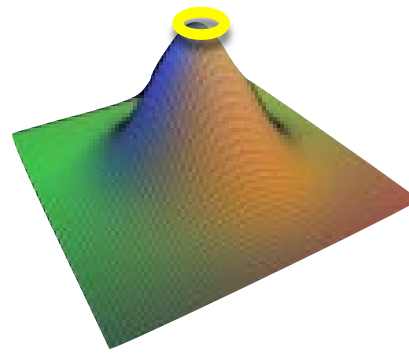
Smooths 'close' pixels in space and intensity  
Depends on *spatial* and *intensity* distance

# Gaussian filtering visualization

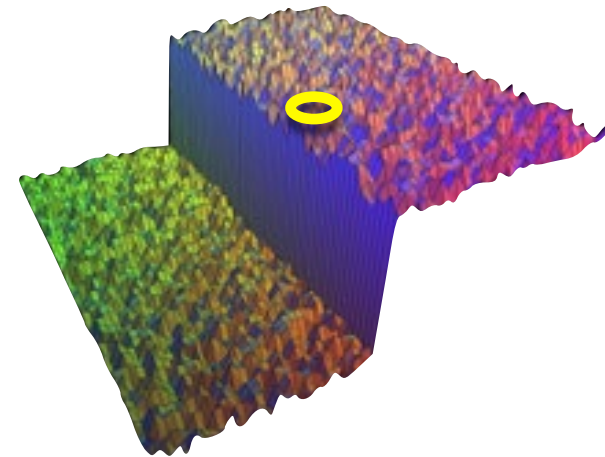
$$h[m, n] = \sum_{k, l} g[k, l] f[m + k, n + l]$$



Output



Gaussian Filter

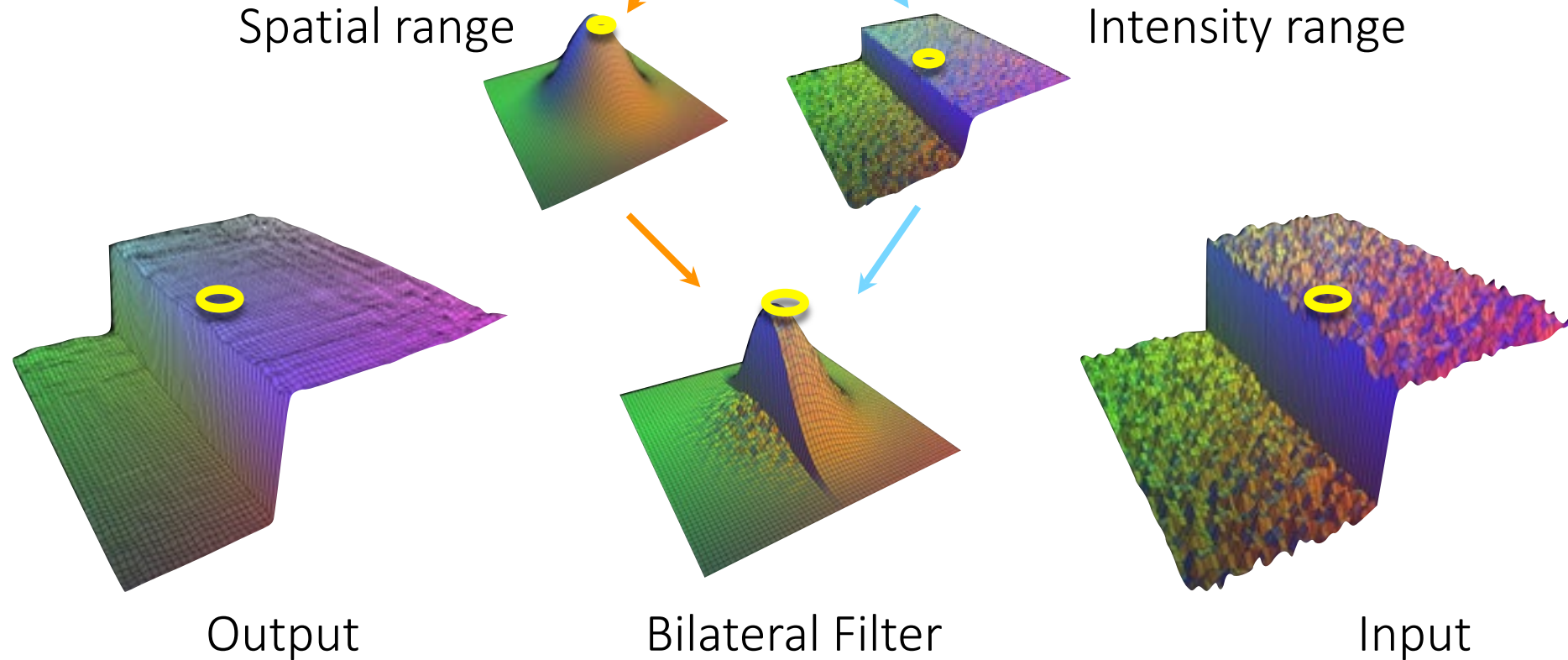


Input

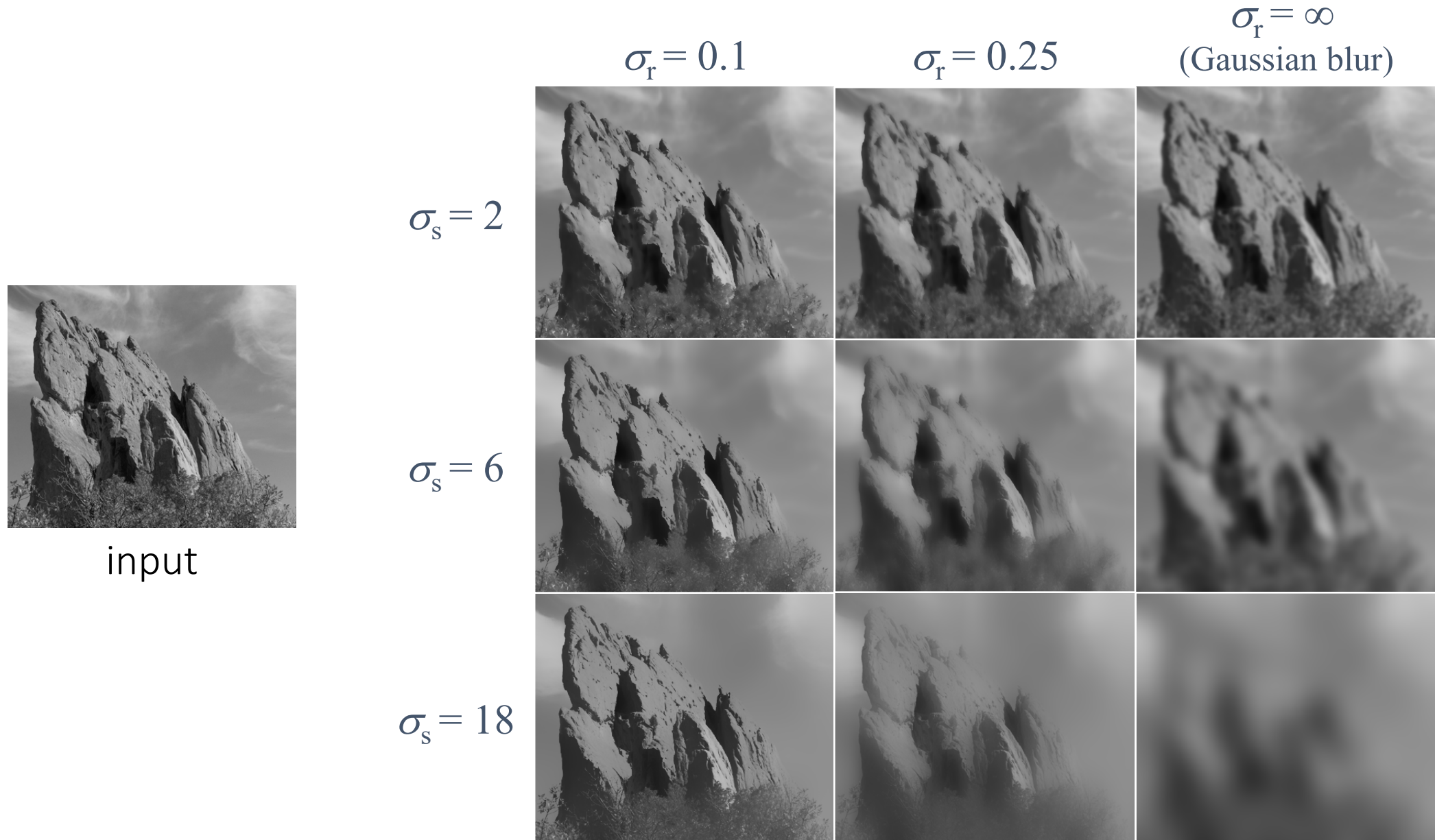


# Bilateral filtering visualization

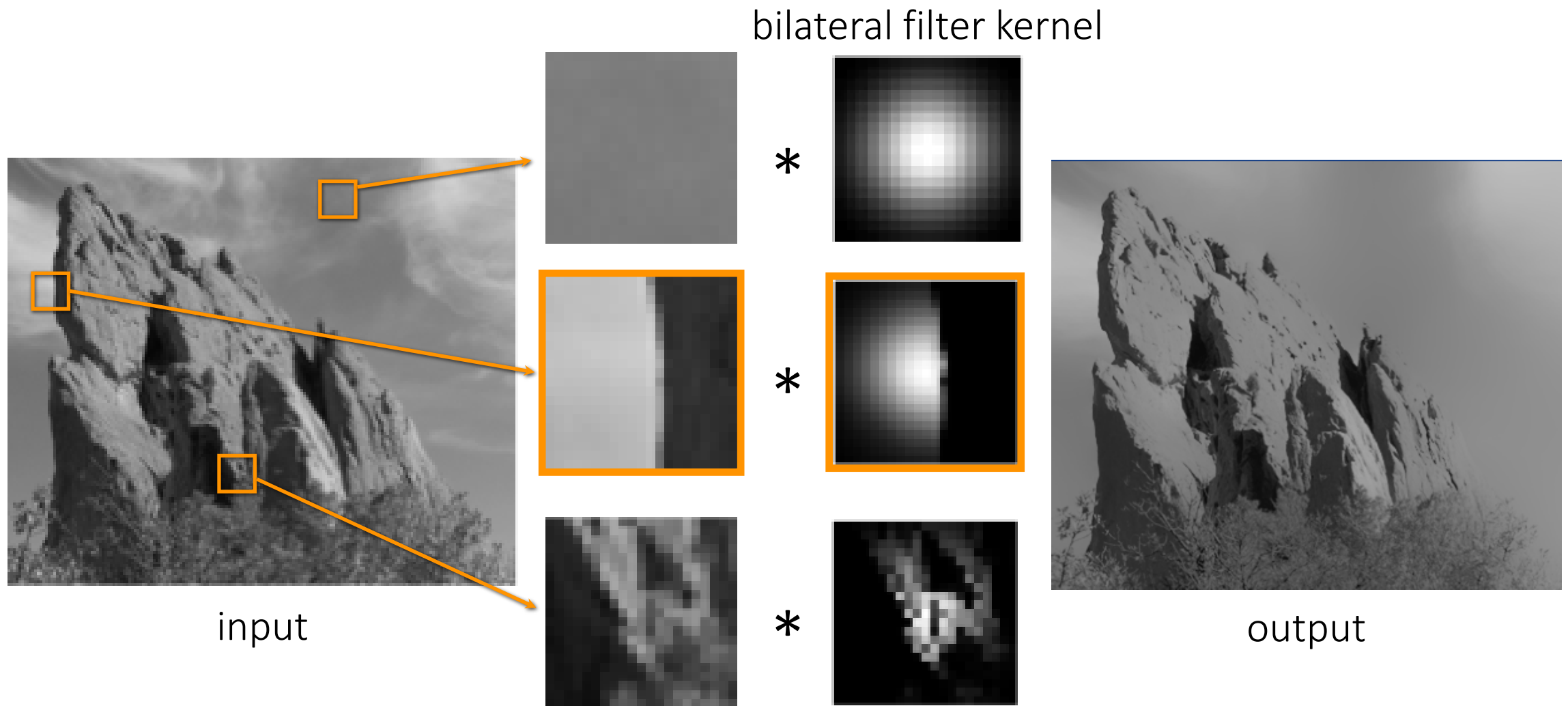
$$h[m, n] = \frac{1}{W_{mn}} \sum_{k, l} g[k, l] r_{mn}[k, l] f[m + k, n + l]$$



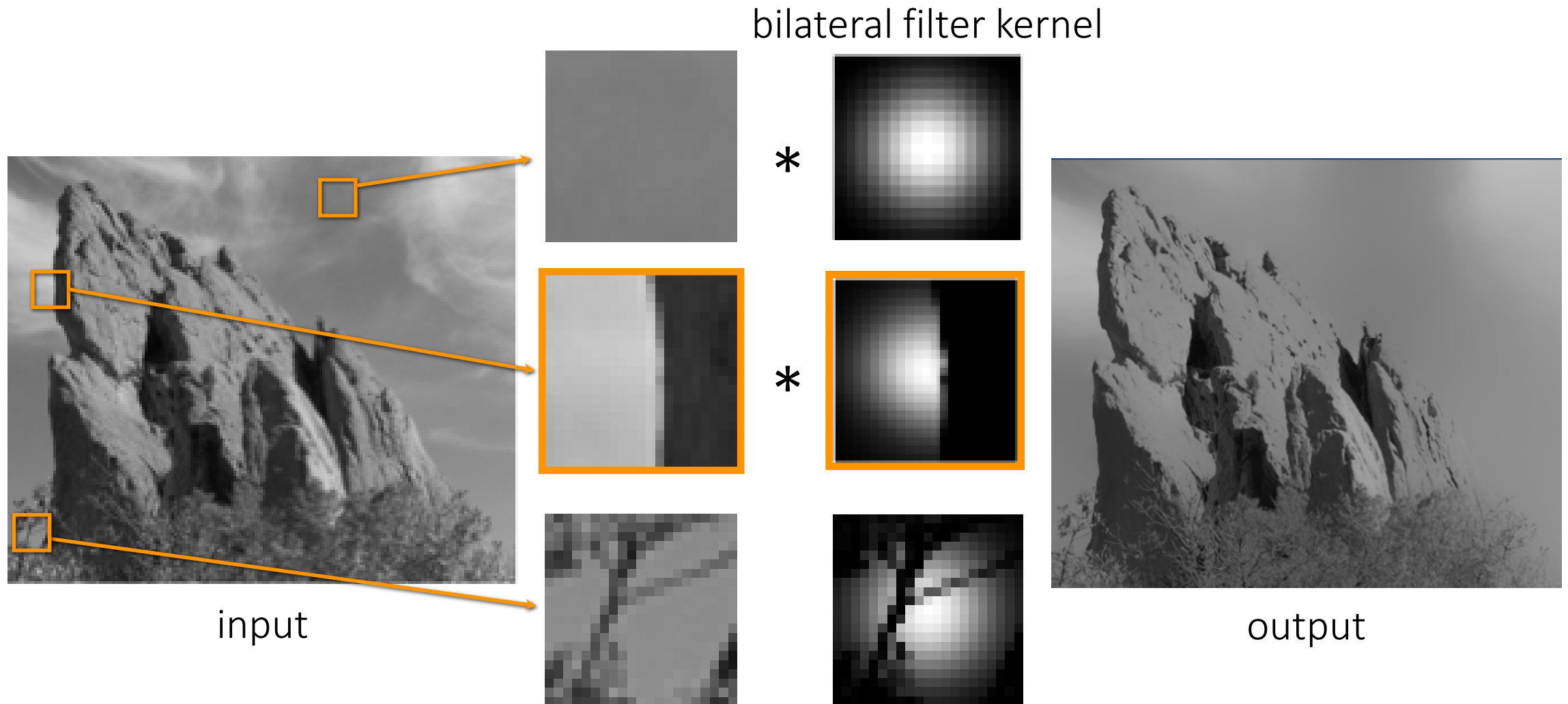
# Exploring the bilateral filter parameter space



# Does the bilateral filter respect all edges?



# Does the bilateral filter respect all edges?



# Denoising



noisy input



bilateral filtering



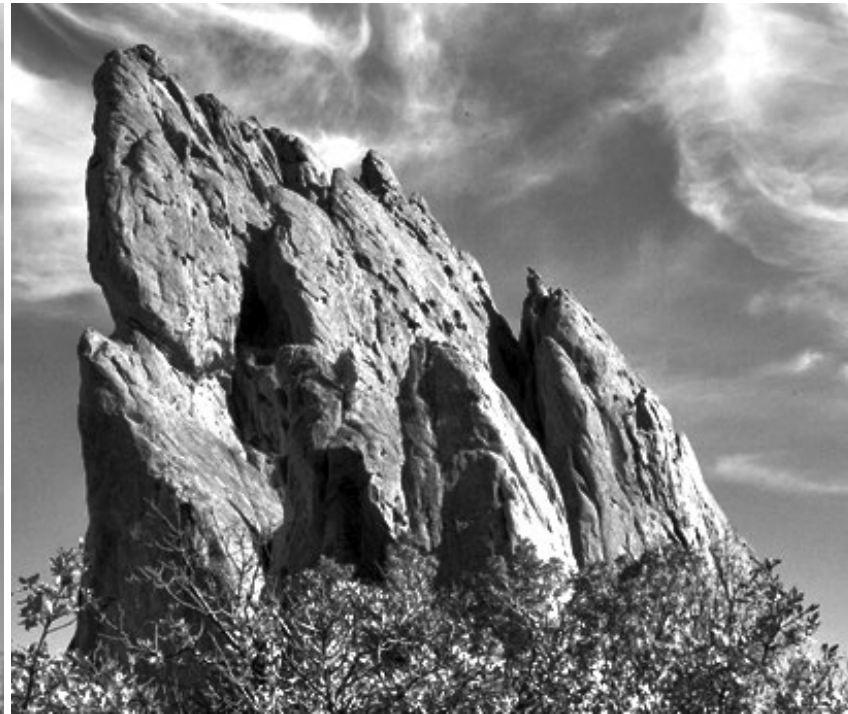
median filtering

# Contrast enhancement

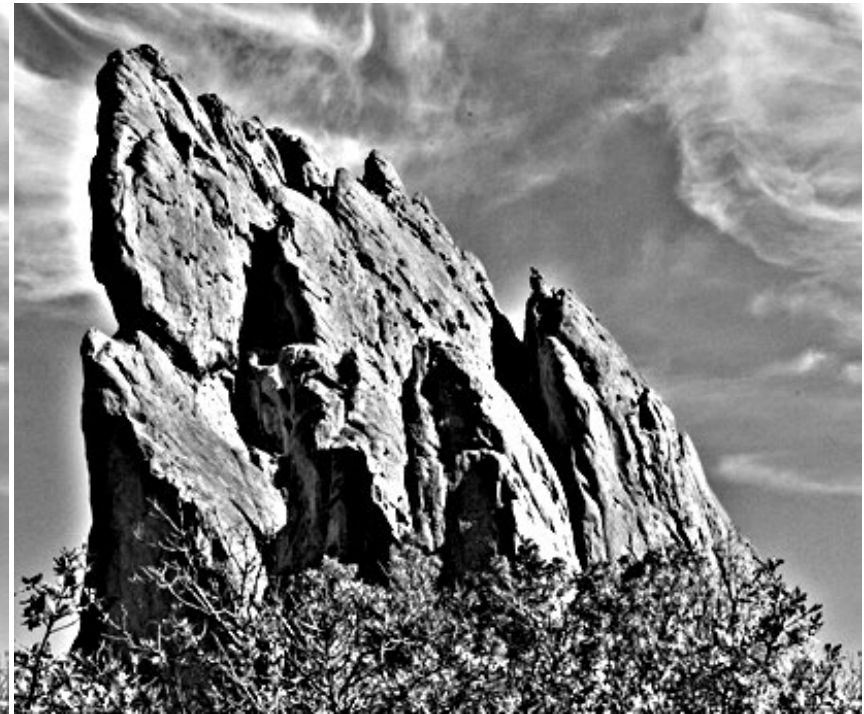
How would you use Gaussian or bilateral filtering for sharpening?



input



sharpening based on  
bilateral filtering



sharpening based on  
Gaussian filtering

# Photo retouching



# Photo retouching



original



digital pore removal (aka bilateral filtering)



# Before



# After



# Close-up comparison



original

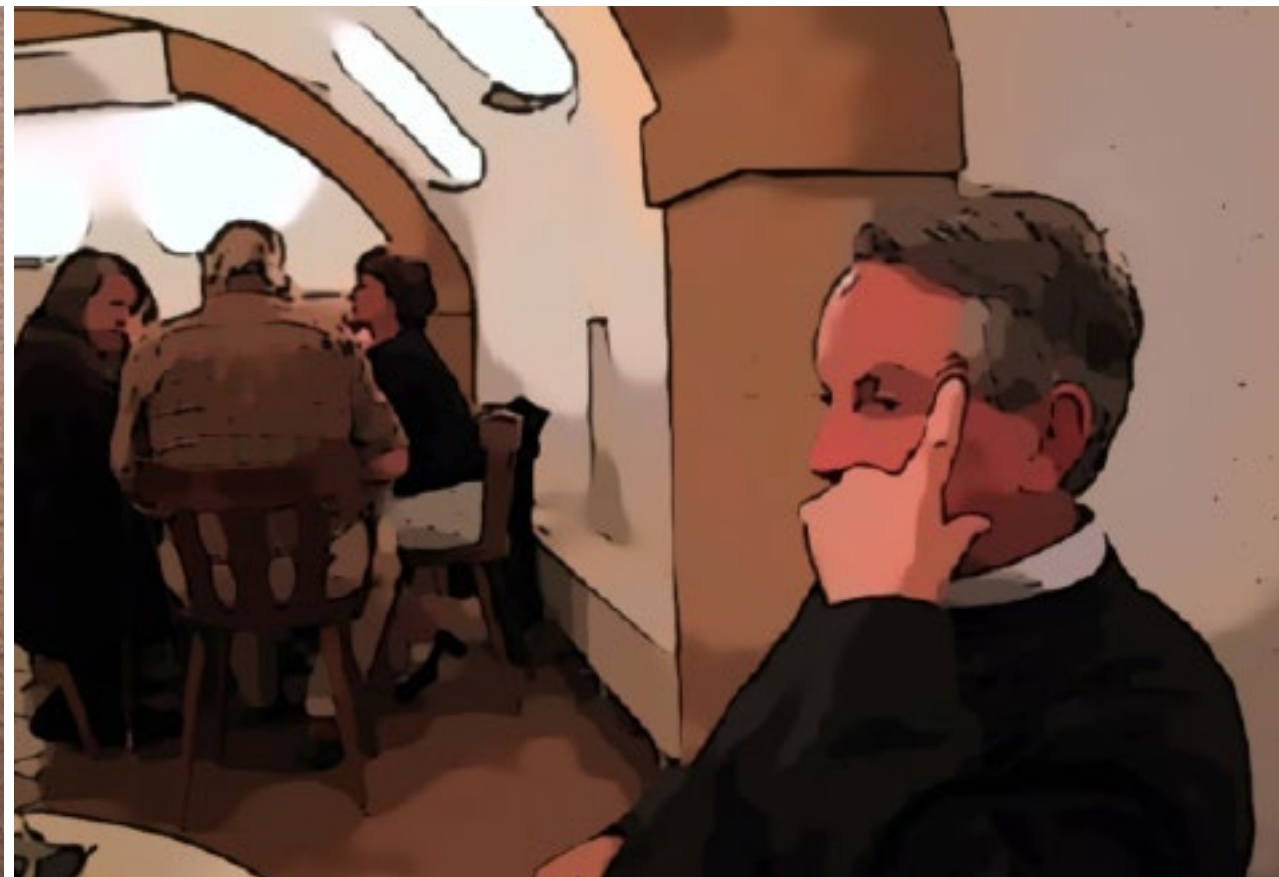


digital pore removal (aka bilateral filtering)

# Cartoonization

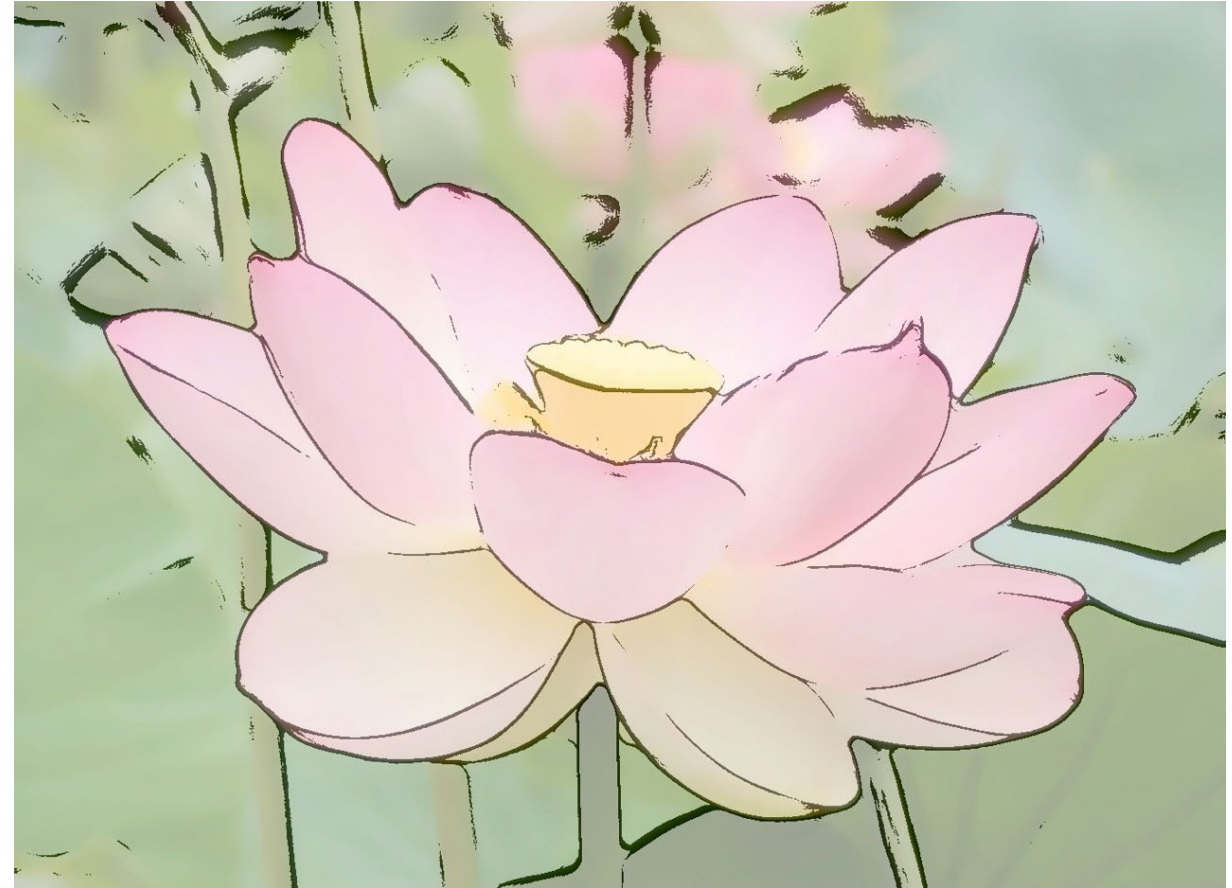


input



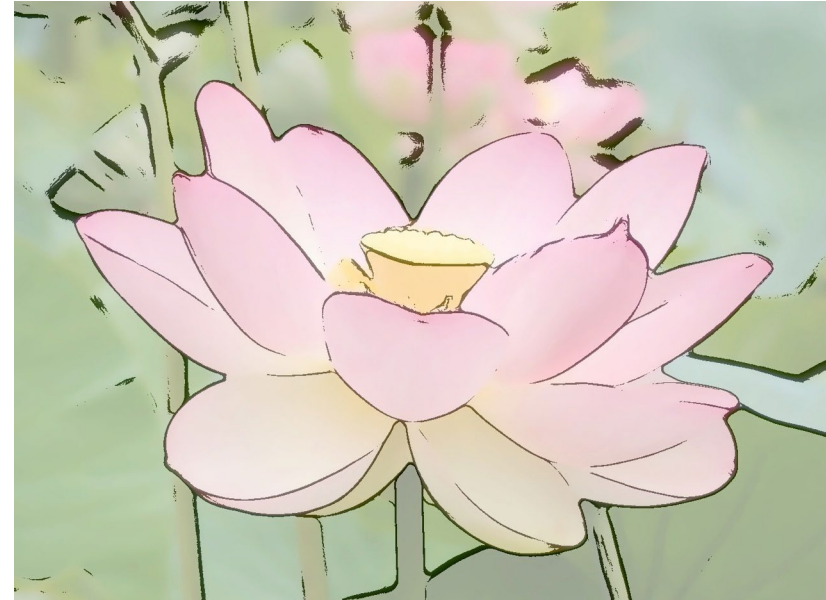
cartoon rendition

# Cartoonization



How would you create this effect?

# Cartoonization



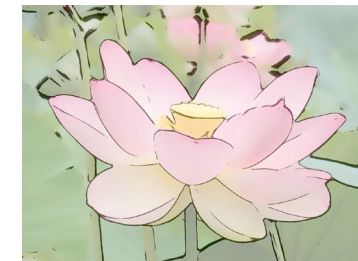
edges from bilaterally filtered image    bilaterally filtered image    cartoon rendition



+



=



Note: image cartoonization and abstraction are very active research areas.

# Is the bilateral filter:

Linear?

Shift-invariant?

# Is the bilateral filter:

Linear?

- No.

Shift-invariant?

- No.

Does this have any bad implications?



# The bilateral grid

## Real-time Edge-Aware Image Processing with the Bilateral Grid

Jiawen Chen      Sylvain Paris      Frédo Durand

Computer Science and Artificial Intelligence Laboratory  
Massachusetts Institute of Technology



**Figure 1:** The bilateral grid enables edge-aware image manipulations such as local tone mapping on high resolution images in real time. This 15 megapixel HDR panorama was tone mapped and locally refined using an edge-aware brush at 50 Hz. The process used about 1 MB of texture memory. The inset shows the original input.

Data structure for fast edge-aware image processing.

# Modern edge-aware filtering: local Laplacian pyramids

## Local Laplacian Filters: Edge-aware Image Processing with a Laplacian Pyramid

Sylvain Paris  
Adobe Systems, Inc.

Samuel W. Hasinoff  
Toyota Technological Institute at Chicago and MIT CSAIL

Jan Kautz  
University College London



(a) input HDR image tone-mapped with a simple gamma curve (details are compressed)



(b) our pyramid-based tone mapping, set to preserve details without increasing them



(c) our pyramid-based tone mapping, set to strongly enhance the contrast of details

**Figure 1:** We demonstrate edge-aware image filters based on the direct manipulation of Laplacian pyramids. Our approach produces high-quality results, without degrading edges or introducing halos, even at extreme settings. Our approach builds upon standard image pyramids and enables a broad range of effects via simple point-wise nonlinearities (shown in corners). For an example image (a), we show results of tone mapping using our method, creating a natural rendition (b) and a more exaggerated look that enhances details as well (c). Laplacian pyramids have previously been considered unsuitable for such tasks, but our approach shows otherwise.

# Modern edge-aware filtering: local Laplacian pyramids



# Modern edge-aware filtering: local Laplacian pyramids

input



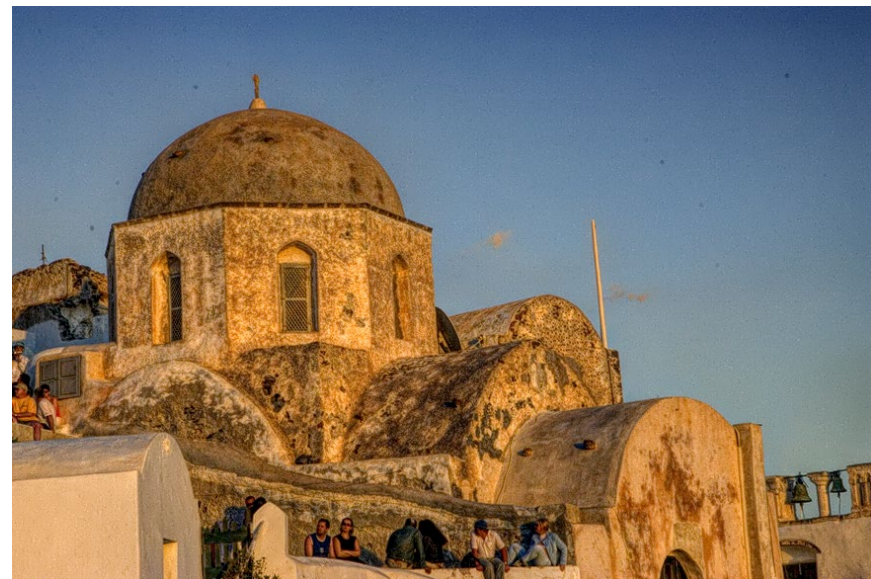
texture  
increase



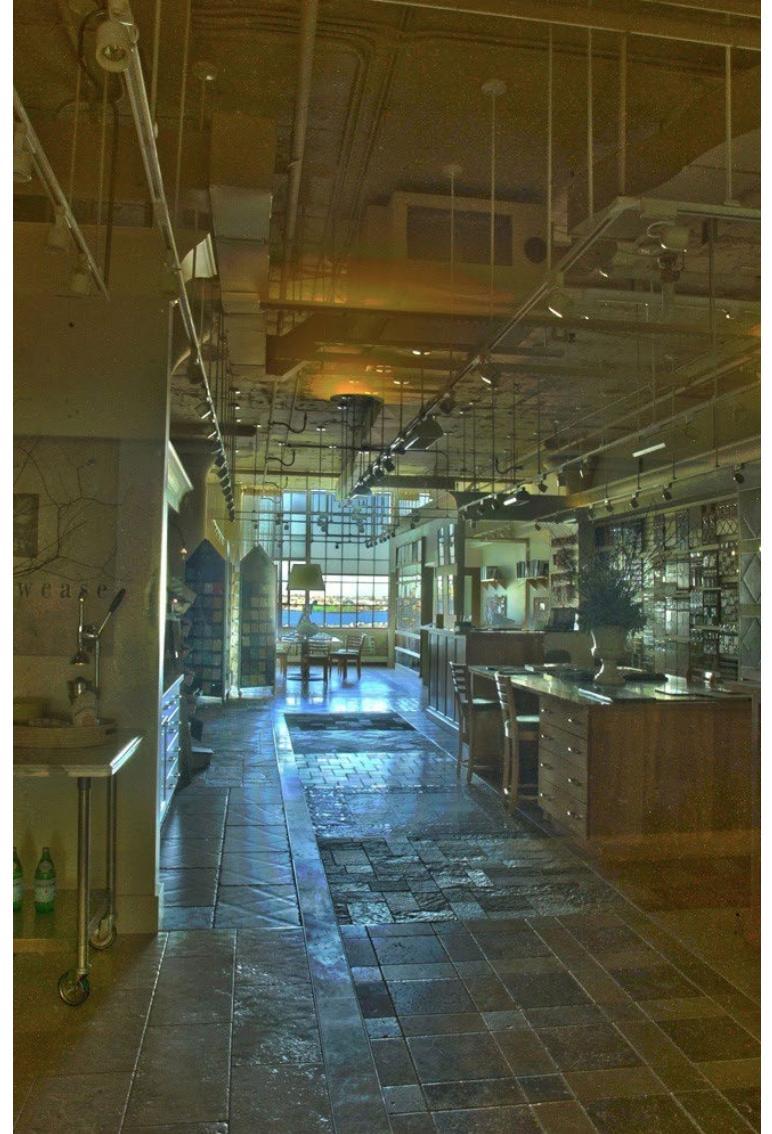
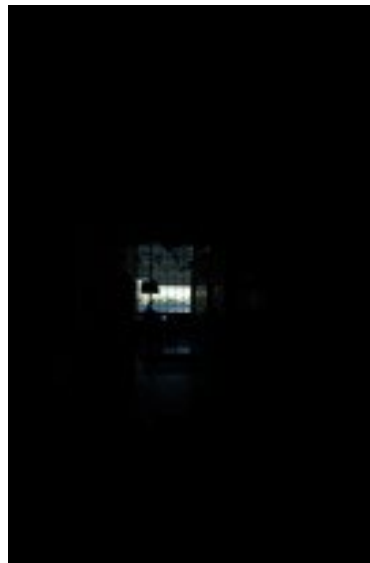
texture  
decrease



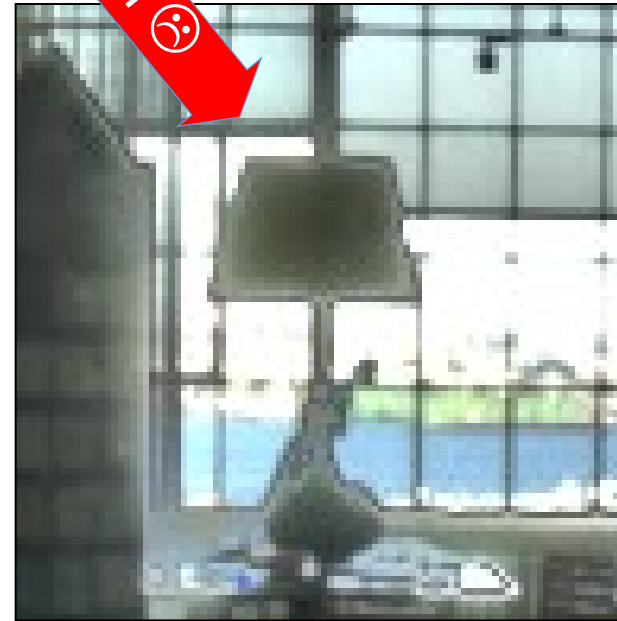
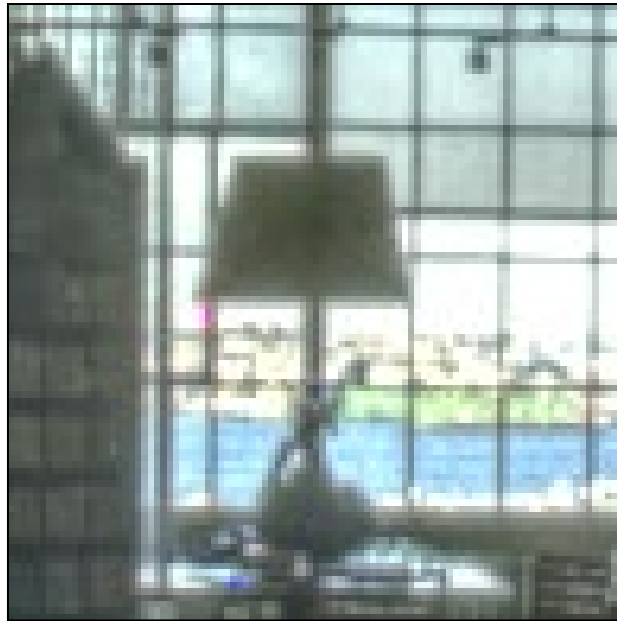
large texture  
increase



# Tonemapping with edge-aware filtering



# Tonemapping with edge-aware filtering



local Laplacian pyramids

bilateral filter

# Modern edge-aware filtering: local Laplacian pyramids



# Modern edge-aware filtering: domain transform

## Domain Transform for Edge-Aware Image and Video Processing

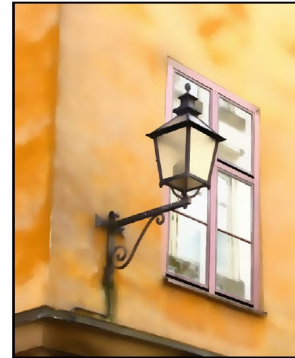
Eduardo S. L. Gastal\*

Manuel M. Oliveira†

Instituto de Informática – UFRGS



(a) *Photograph*



(b) *Edge-aware smoothing*



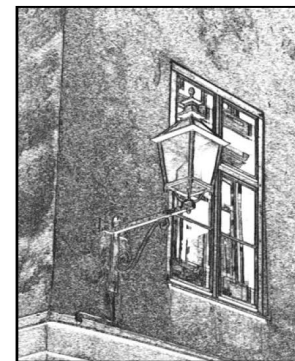
(c) *Detail enhancement*



(d) *Stylization*



(e) *Recoloring*



(f) *Pencil drawing*



(g) *Depth-of-field*

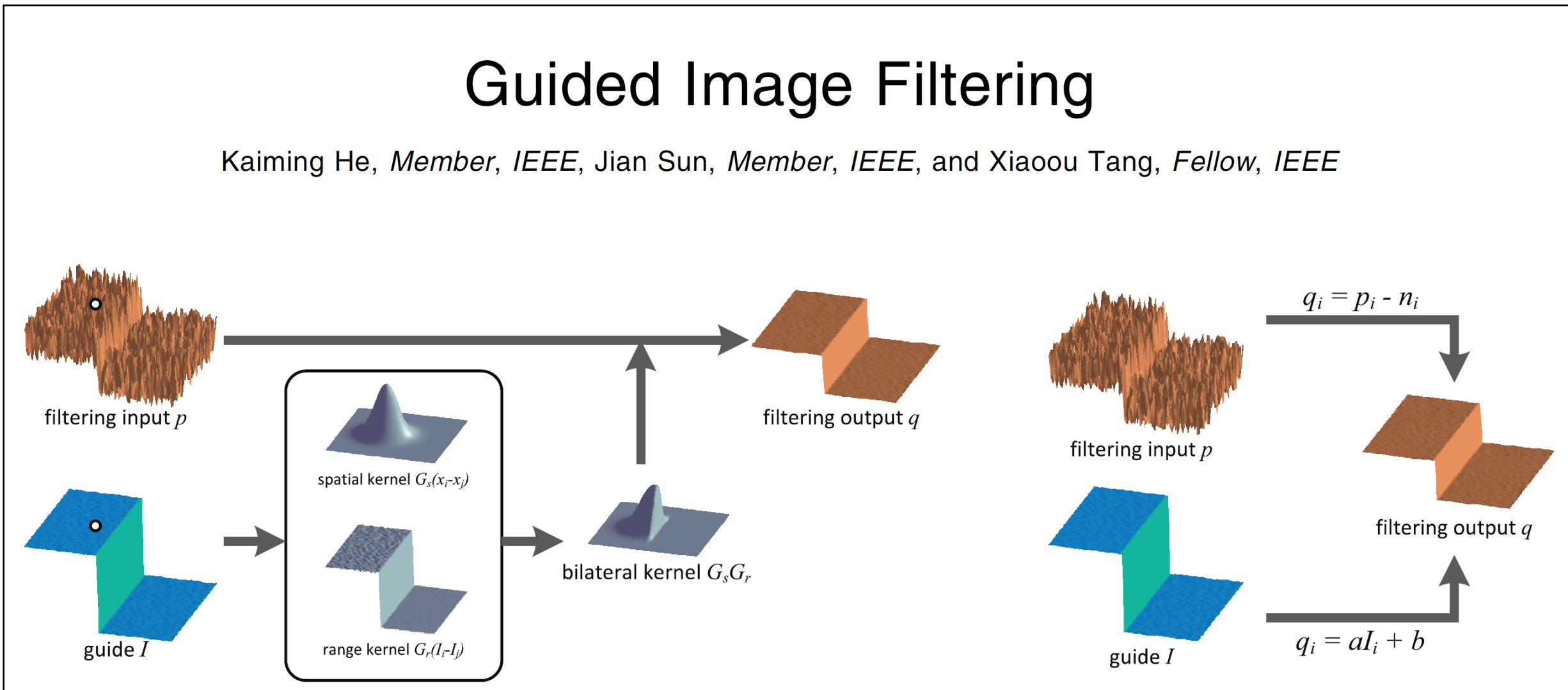
Lots of great examples at: <https://www.inf.ufrgs.br/~eslgastal/DomainTransform/>



# Modern edge-aware filtering: guided filter

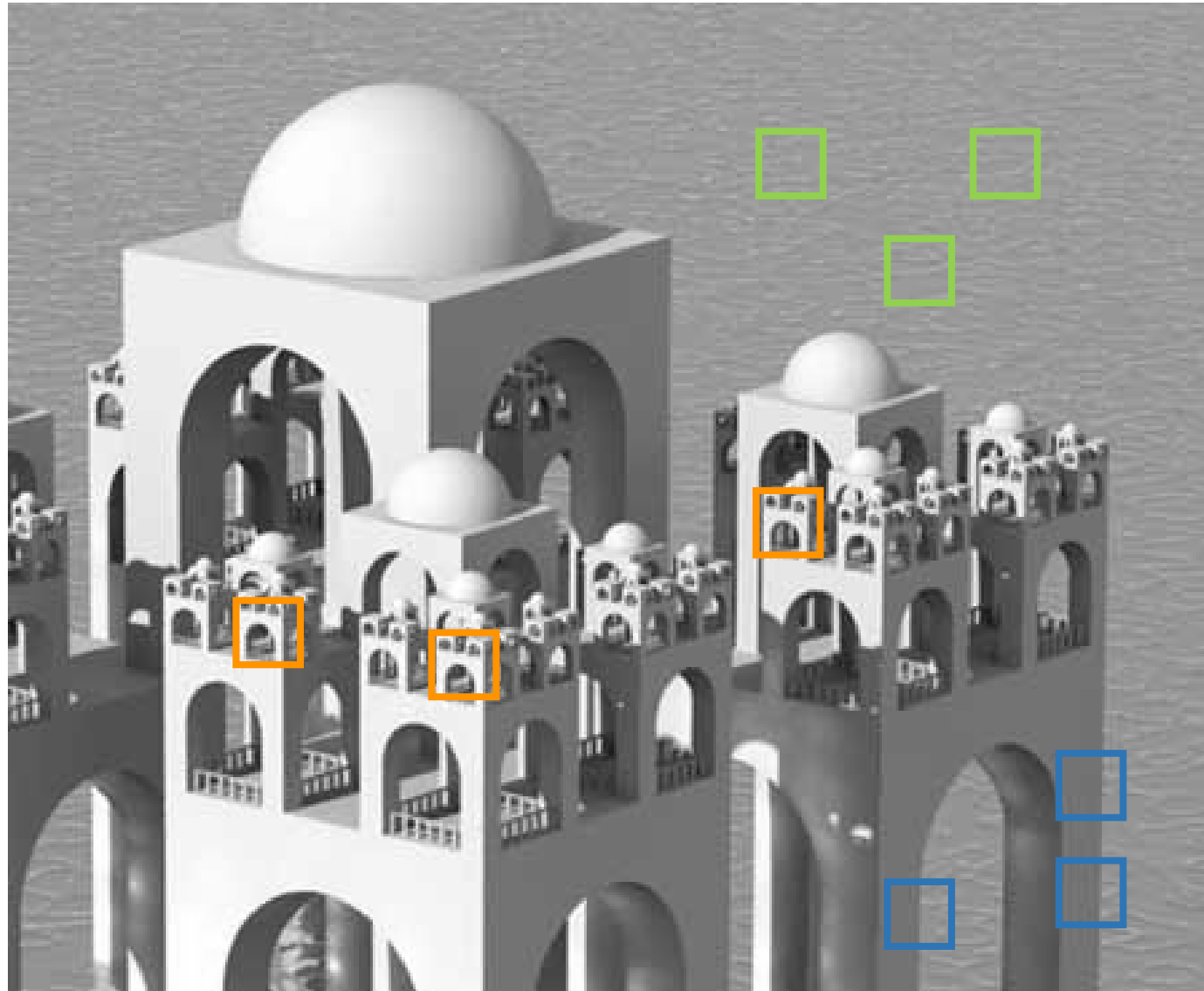
## Guided Image Filtering

Kaiming He, *Member, IEEE*, Jian Sun, *Member, IEEE*, and Xiaoou Tang, *Fellow, IEEE*



Non-local means

# Redundancy in natural images

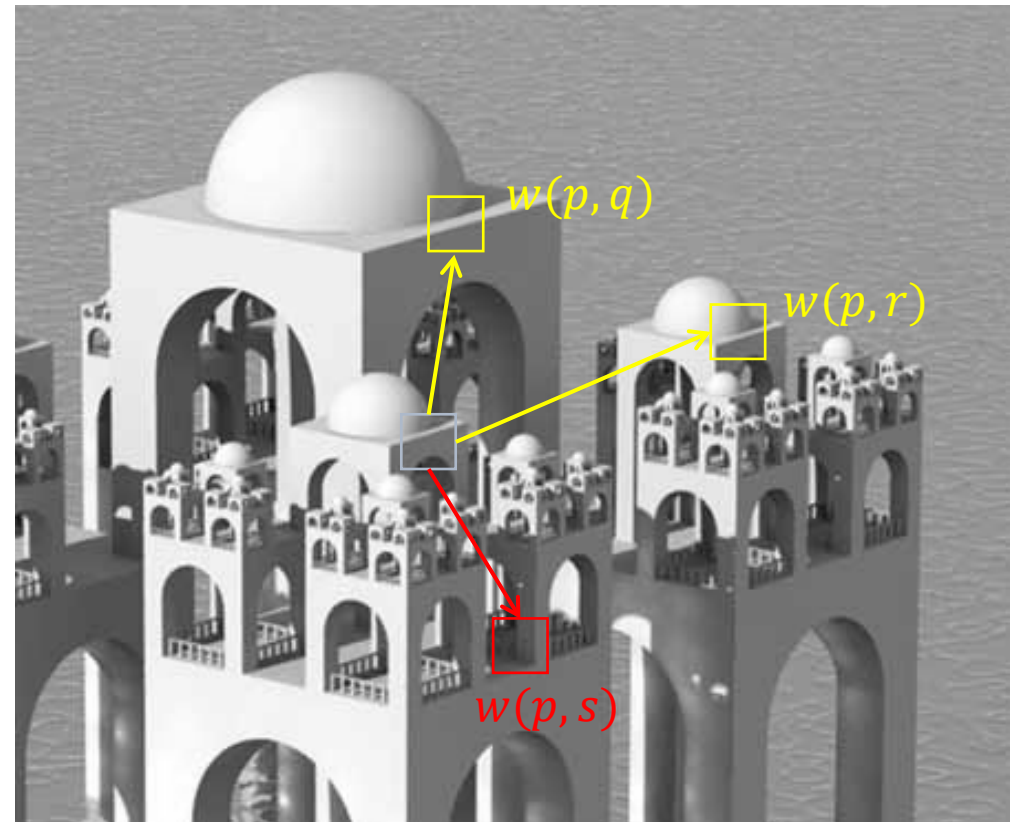


# Non-local means

No need to stop at neighborhood. Instead search *everywhere* in the image.

$$\hat{x}(i) = \frac{1}{C_i} \sum_j y(j) e^{-\frac{SSD(y(N_i)-y(N_j))}{2\sigma^2}}$$

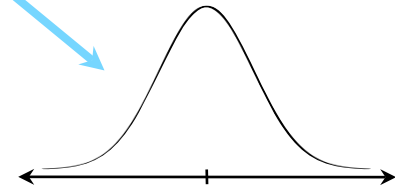
$w(i, j)$



# Non-local means vs bilateral filtering

Non-local means filtering

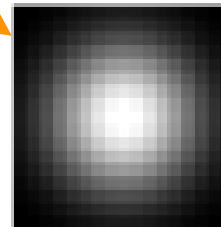
$$h[m, n] = \frac{1}{W_{mn}} \sum_{k,l} r_{mn}[k, l] f[m+k, n+l]$$



Intensity range weighting:  
favor *similar* pixels (patches  
in case of non-local means)

Bilateral filtering

$$h[m, n] = \frac{1}{W_{mn}} \sum_{k,l} g[k, l] r_{mn}[k, l] f[m+k, n+l]$$



Spatial weighting:  
favor *nearby* pixels

# Everything put together

## Gaussian filtering

Smooths everything nearby (even edges)  
Only depends on *spatial* distance

## Bilateral filtering

Smooths 'close' pixels in space and intensity  
Depends on *spatial* and *intensity* distance

## Non-local means

Smooths similar patches no matter how far away  
Only depends on *intensity* distance

# Denoising example



noisy input



Gaussian filtering



bilateral filtering



non-local means

# Very general forms of “structural” filtering



We will see more in later lectures.



# Is non-local means:

Linear?

Shift-invariant?

# Is non-local means:

Linear?

- No.

Shift-invariant?

- No.

Non-local means is not a convolution, and is generally very very challenging to implement efficiently.

Efficient algorithms for non-local means are an active research area.

Flash/no-flash photography



Red Eye



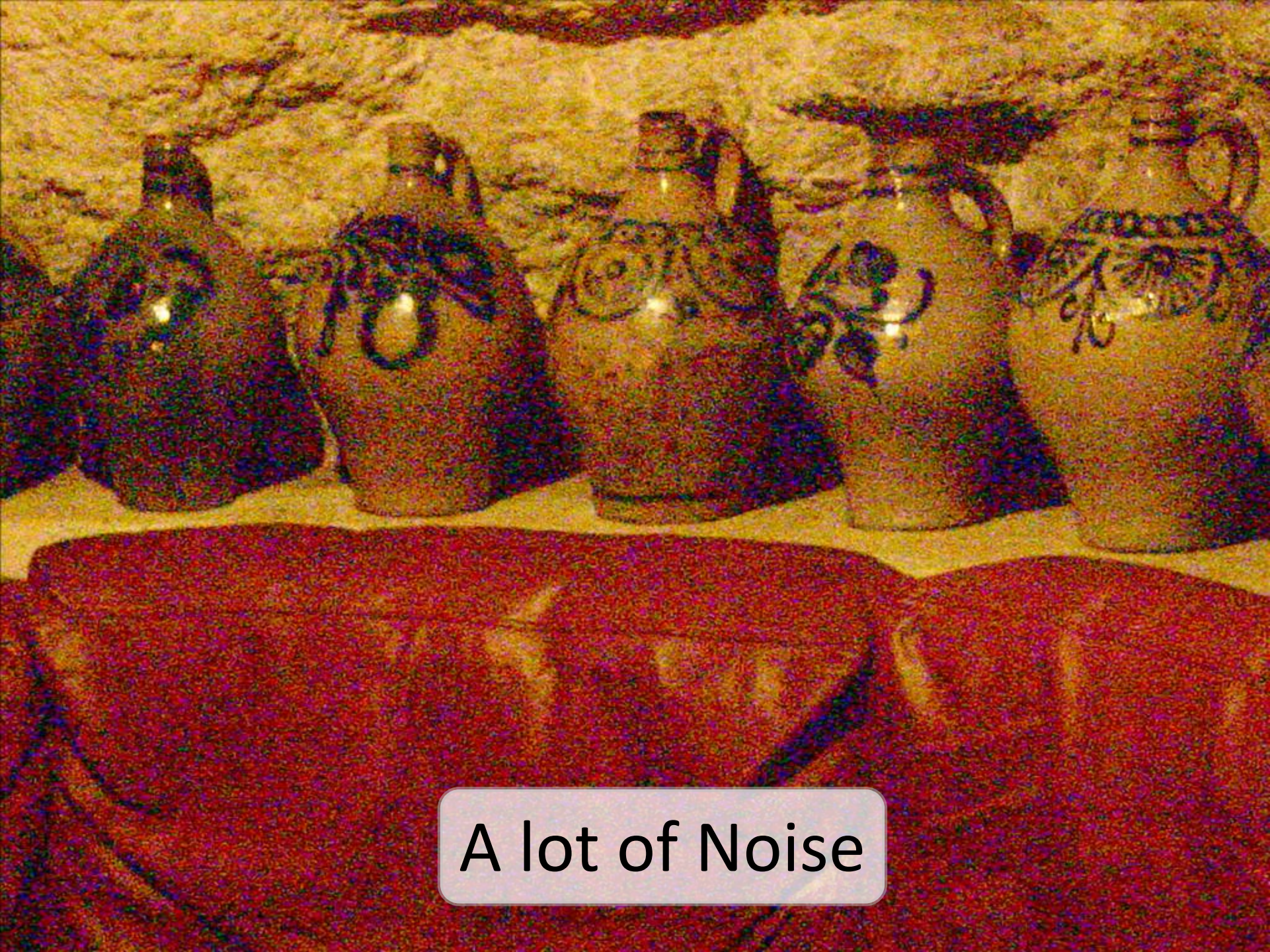
**Unflattering Lighting**



Motion Blur



Noise



A lot of Noise





Ruined Ambiance

# Flash

# No-Flash

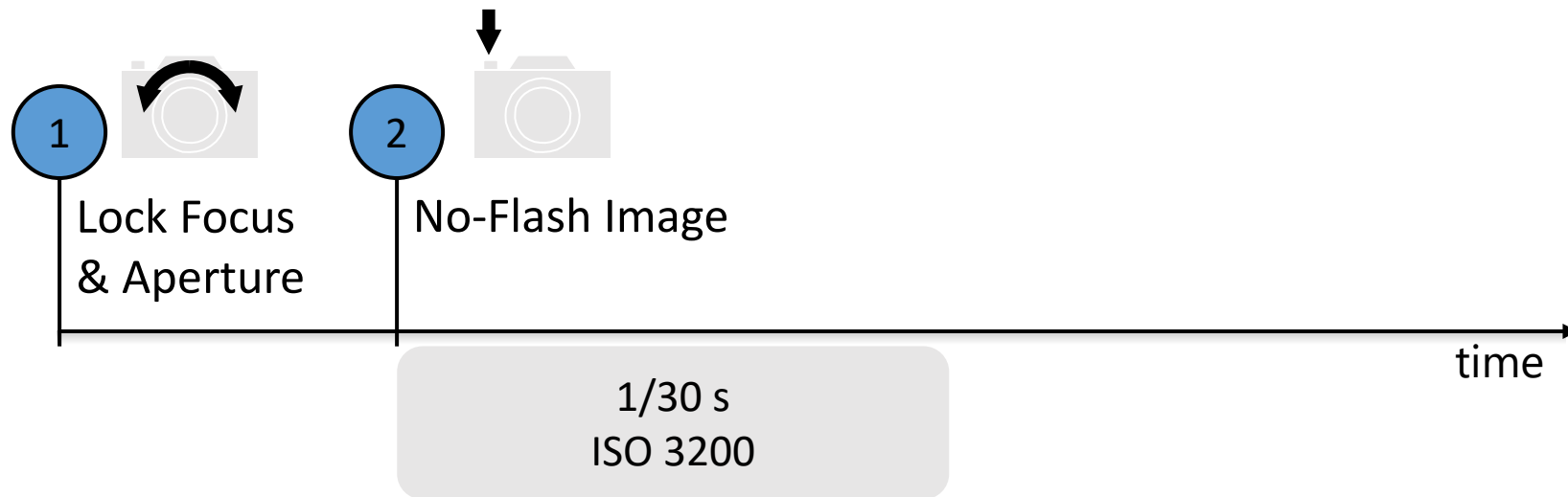
- + Low Noise
- + Sharp
- Artificial Light
- Jarring Look

- High Noise
- Lacks Detail
- + Ambient Light
- + Natural Look

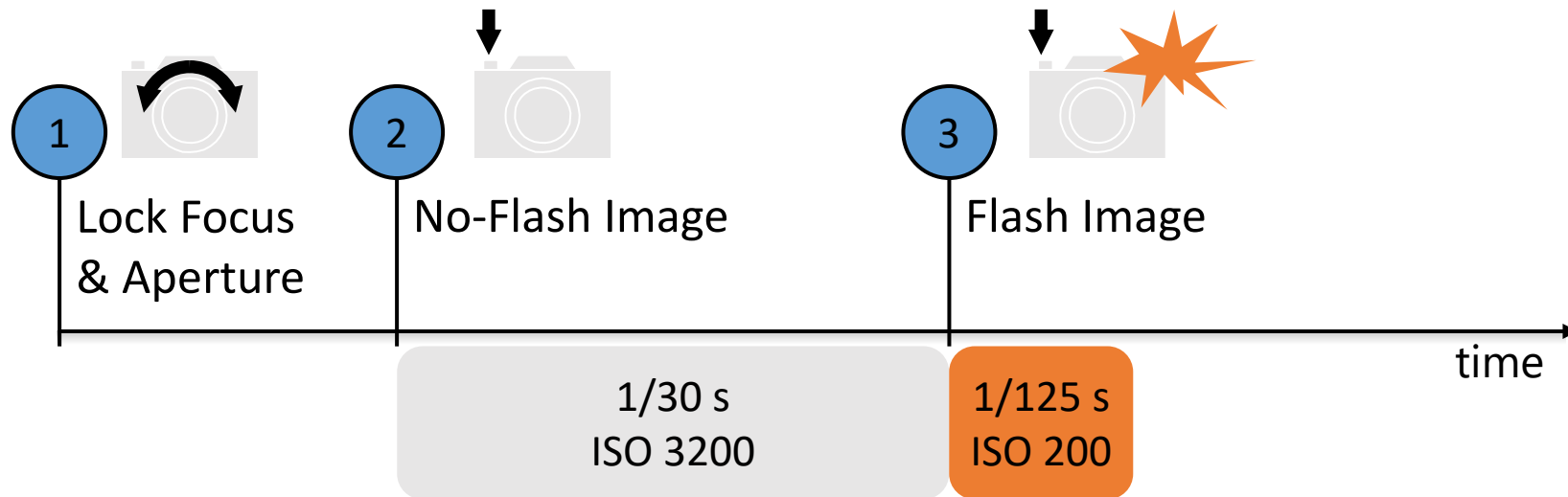
# Image acquisition



# Image acquisition



# Image acquisition





Denoising Result



No-Flash



Denoising Result



# Key idea

Denoise the no-flash image while maintaining the edge structure of the flash image

- How would you do this using the image editing techniques we've learned about?

# Joint bilateral filtering

# Denoising with bilateral filtering



noisy input



bilateral filtering



median filtering

# Denoising with bilateral filtering

$$A_{p(col)}^{Base} = \frac{1}{k(p(col))} \sum_{p' \in \Omega} \overset{\text{spatial kernel}}{g_d(|p - p'|)} \overset{\text{intensity kernel}}{g_r(A_{p(col)} - A_{p'(col)})} A_{p'(col)}$$

- However, results still have noise or blur (or both)



# Denoising with joint bilateral filtering

$$A_{p(col)}^{NR} = \frac{1}{k(p(col))} \sum_{p' \in \Omega} g_d(|p - p'|) g_r(F_{p(col)} - F_{p'(col)}) A_{p'(col)}$$

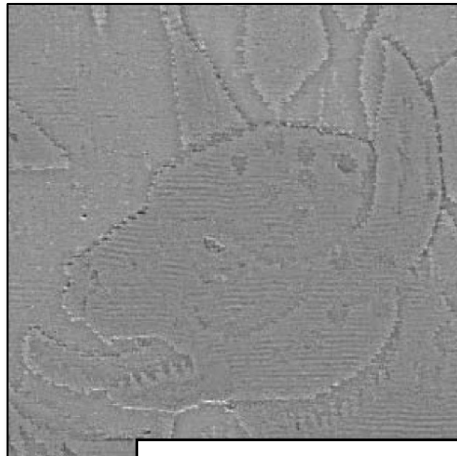
- In the flash image there are many more *details*
- Use the flash image F to find edges

# Denoising with joint bilateral filtering

$$A_{p(col)}^{NR} = \frac{1}{k(p(col))} \sum_{p' \in \Omega} g_d(|p - p'|) g_r(\mathbf{F}_{p(col)} - \mathbf{F}_{p'(col)}) A_{p'(col)}$$



Bilateral filter



The difference

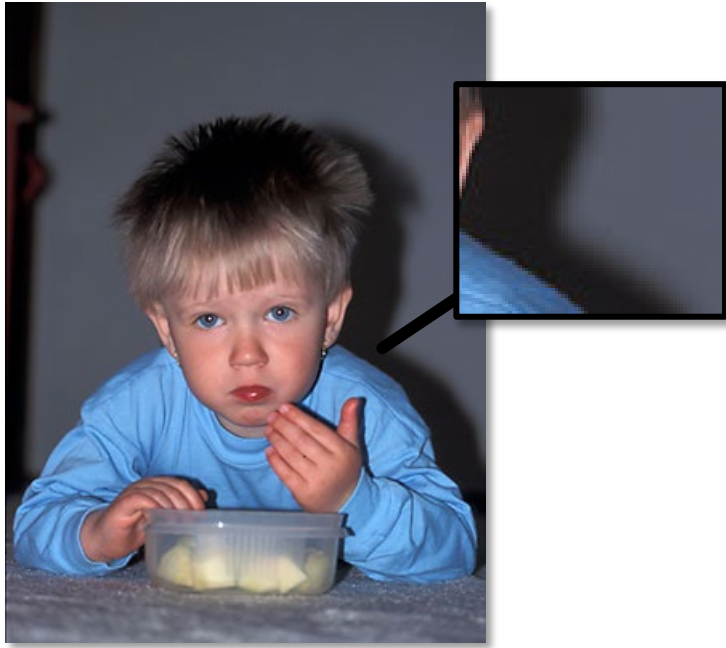


Joint Bilateral filter

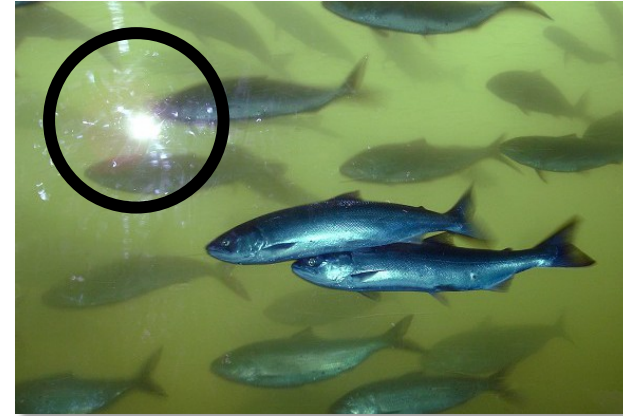
# Not all edges in the flash image are real

Can you think of any types of edges that may exist in the flash image but not the ambient one?

# Not all edges in the flash image are real



shadows



specularities

- May cause over- or under-blur in joint bilateral filter
- We need to eliminate their effect



# Detecting shadows

- **Observation:** the pixels in the flash shadow should be similar to the ambient image.
- Not identical:
  1. Noise.
  2. Inter-reflected flash.
- Compute a *shadow mask*.
- Take pixel  $p$  if  $F_{p(col)}^{Lin} - A_{p(col)}^{Lin} \leq \tau_{Shadow}$
- $\tau_{Shadow}$  is manually adjusted
- Mask is *smoothed* and *dilated*

# Detecting specularities

- Take pixels where sensor input is close to maximum (very bright).
  - Over fixed threshold  $\tau_{spec}$
- Create a *specularity mask*.
- Also smoothed.
- **M** – the combination of shadow and specularity masks:

Where  $M_p=1$ , we use  $A^{Base}$ . For other pixels we use  $A^{NR}$ .

# Detail transfer

- Denoising cannot add details *missing* in the ambient image
- Exist in flash image because of high SNR
- We use a *quotient image*:

$$F_{p(col)}^{Detail} = \frac{F_{p(col)} + \varepsilon}{F_{p(col)}^{Base} + \varepsilon}$$

Reduces the effect of noise in F

Bilateral filtered

- Multiply with  $A^{NR}$  to add the details
- Masked in the same way

Why does this quotient image make sense for detail?

# Detail transfer

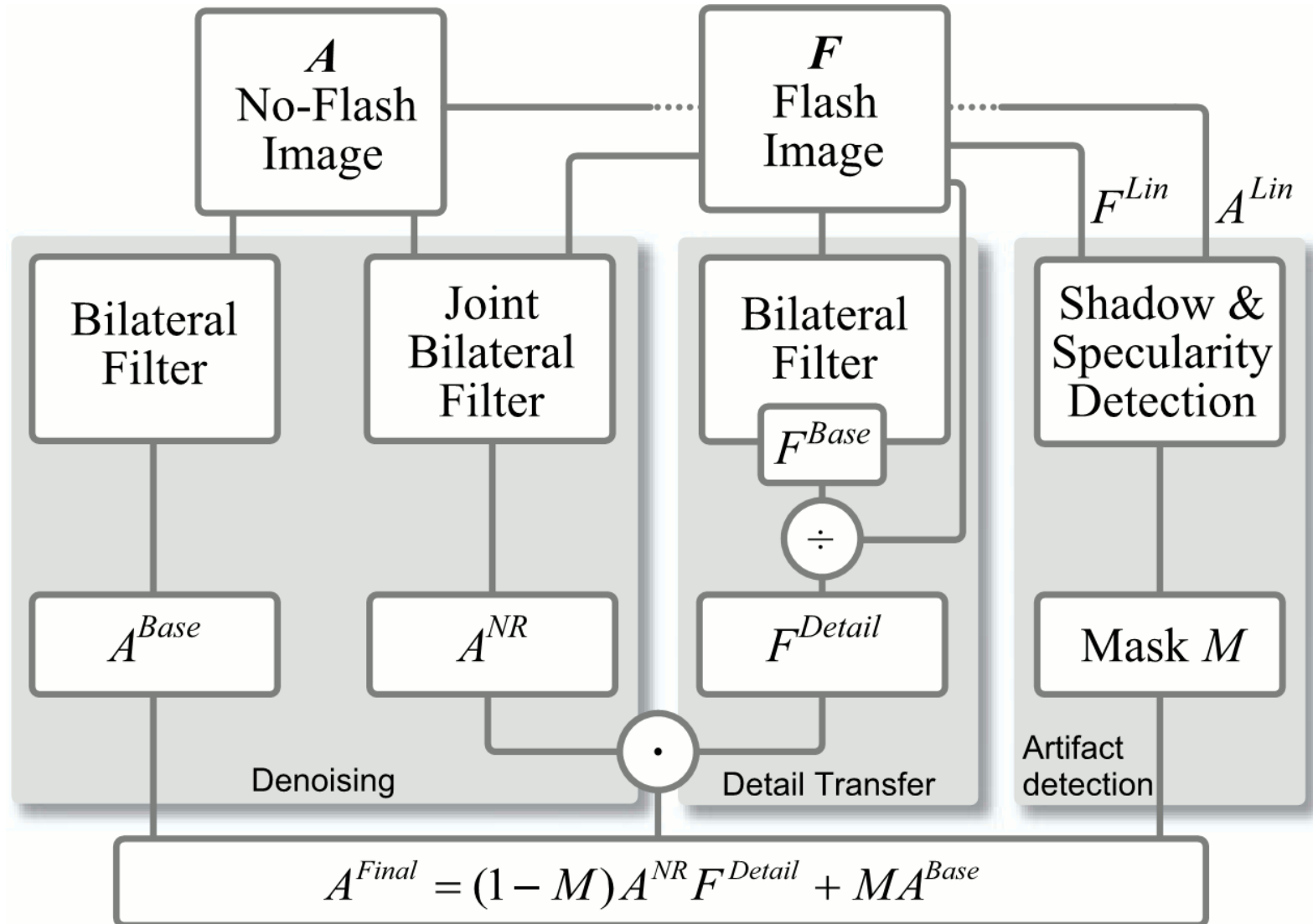
- Denoising cannot add details *missing* in the ambient image
- Exist in flash image because of high SNR
- We use a *quotient image*:

$$F_{p(col)}^{Detail} = \frac{F_{p(col)} + \varepsilon}{F_{p(col)}^{Base} + \varepsilon}$$

Reduces the  
effect of  
noise in F



# Full pipeline



# Demonstration



ambient-only



joint bilateral and detail transfer



Flash




No-Flash





No-Flash



Result



Flash



No-Flash



No-Flash



Result



Flash



No-Flash





Flash



No-Flash



Result

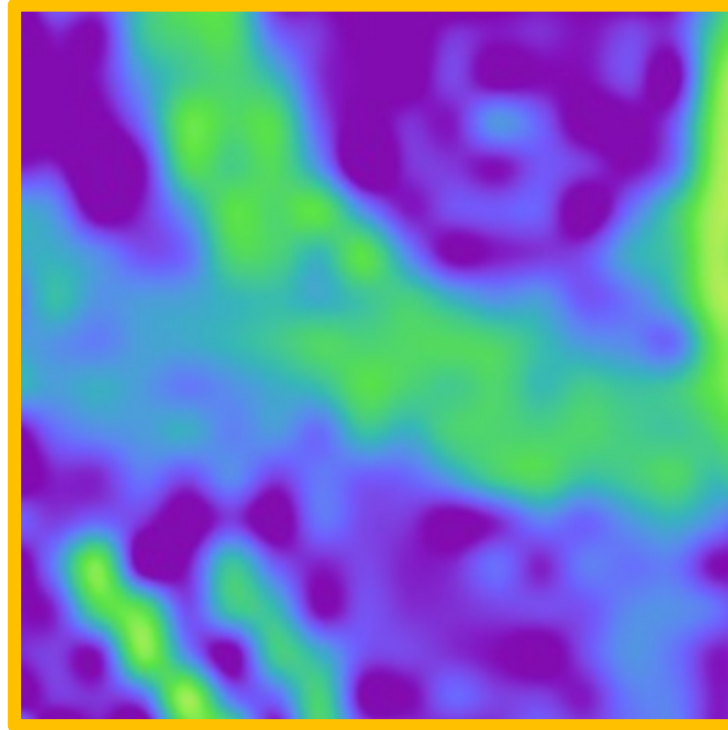
# Edge-aware depth denoising

$$A_{p(col)} = \frac{1}{k(p(col))} \sum_{p' \in \Omega} g_d(|p - p'|) g_r(F_{p(col)} - F_{p'(col)}) A_{p'(col)}$$

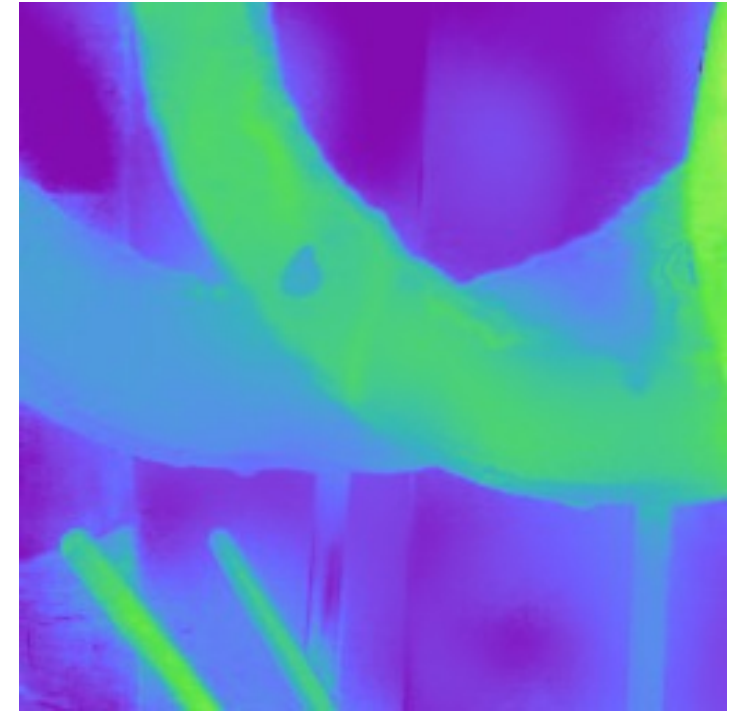
Use joint bilateral filtering, with the input image as guide.



One of two input images



Depth from disparity



Guided filtering

# Other applications of joint bilateral filtering

## Deep Bilateral Learning for Real-Time Image Enhancement

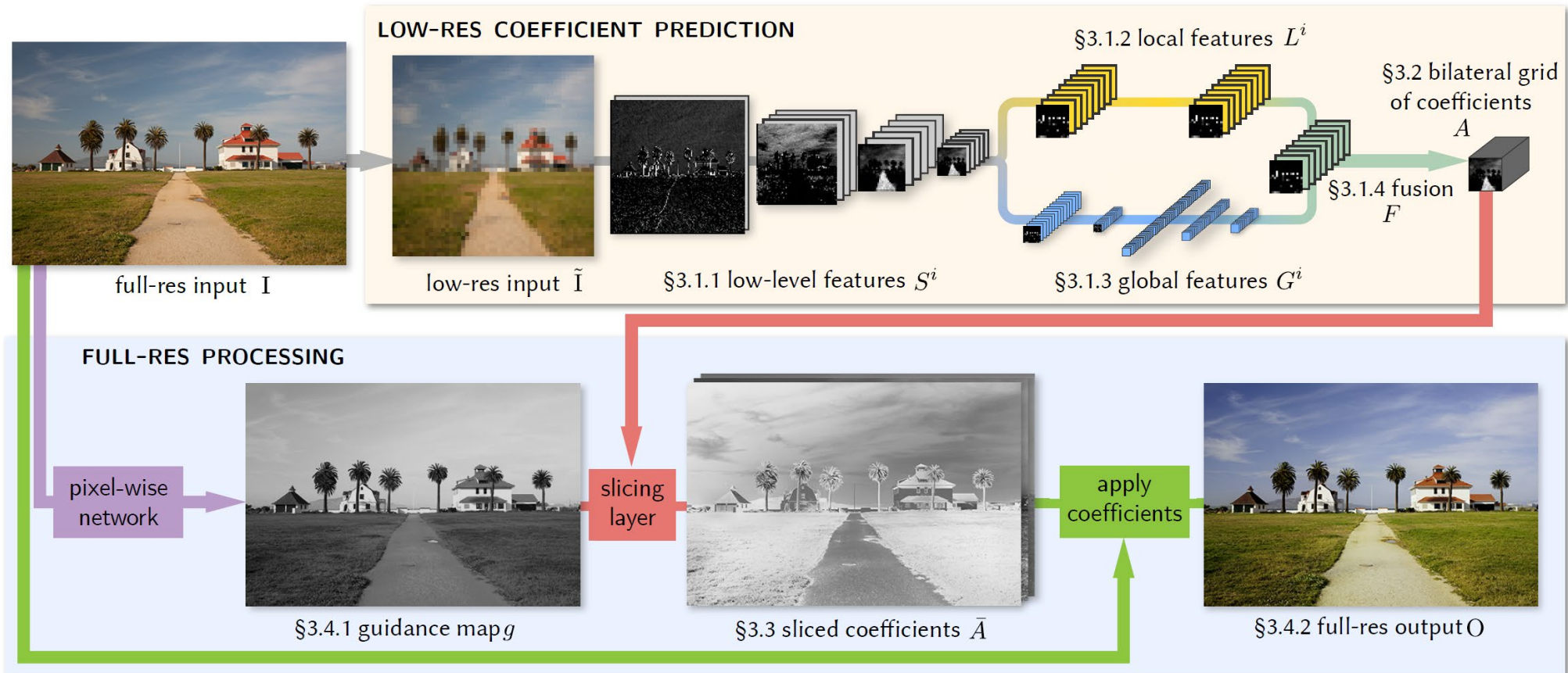
MICHAËL GHARBI, MIT CSAIL

JIAWEN CHEN, Google Research

JONATHAN T. BARRON, Google Research

SAMUEL W. HASINOFF, Google Research

FRÉDO DURAND, MIT CSAIL / Inria, Université Côte d'Azur



# References

## Basic reading:

- Durand and Dorsey, “Fast bilateral filtering for the display of high-dynamic-range images,” SIGGRAPH 2002.  
The paper on tonemapping using bilateral filtering.
- Paris et al., “Bilateral Filtering: Theory and Applications,” Foundations and Trends® in Computer Graphics and Vision 2009.  
A comprehensive review of bilateral filtering.
- Paris et al., “A Gentle Introduction to the Bilateral Filter and Its Applications,” SIGGRAPH 2007-08, CVPR 2008, [https://people.csail.mit.edu/sparis/bf\\_course/](https://people.csail.mit.edu/sparis/bf_course/)  
Short course on the bilateral filter, including discussion of fast implementations.
- Petschnigg et al., “Digital photography with flash and no-flash image pairs,” SIGGRAPH 2004.
- Eisemann and Durand, “Flash Photography Enhancement via Intrinsic Relighting,” SIGGRAPH 2004.  
The first two papers exploring the idea of photography with flash and no-flash pairs using the joint bilateral filter.

## Additional reading:

- Chen et al., “Real-time edge-aware image processing with the bilateral grid,” SIGGRAPH 2007.
- Paris and Durand, “A Fast Approximation of the Bilateral Filter Using a Signal Processing Approach,” IJCV 2009.  
Two papers on acceleration techniques for the bilateral filter.
- Paris et al., “Local Laplacian Filters: Edge-aware Image Processing with a Laplacian Pyramid,” SIGGRAPH 2011 and CACM 2015.  
The paper on local Laplacian pyramids.
- Buades et al., “Nonlocal Image and Movie Denoising,” IJCV 2008.  
The journal version of the original non-local means paper.
- Barnes et al., “PatchMatch: A Randomized Correspondence Algorithm for Structural Image Editing,” SIGGRAPH 2009.  
A paper on a very efficient implementation of non-local means, including a few amazing applications focusing on creative manipulation of images.
- He et al., “Guided image filtering,” PAMI 2013.
- Gastal and Oliveira, “Domain Transform for Edge-Aware Image and Video Processing,” SIGGRAPH 2011.  
The papers introducing the two different types of edge-aware filtering we mentioned.
- Gharbi et al., “Deep Bilateral Learning for Real-Time Image Enhancement,” SIGGRAPH 2017.  
Learning image transformations using bilateral filtering.
- Barron et al., “Fast bilateral-space stereo for synthetic defocus,” CVPR 2015.
- Barron and Poole, “The fast bilateral solver,” ECCV 2016.  
The above two papers show how to combine edge-aware filtering (and bilateral filtering in particular) with disparity matching for robust stereo. The first paper also shows how the resulting depth maps can be used to create synthetic defocus blur.