

15-463, 15-663, 15-862 Computational Photography Fall 2020, Lecture 14

#### http://graphics.cs.cmu.edu/courses/15-463

#### Course announcements

- Homework assignment 4 due November 2<sup>nd</sup>.
  - Generally shorter to accommodate final project proposals.
  - Two bonus parts.
- Project logistics on Piazza and the course website.
  - Project ideas due on Piazza on October 23<sup>rd</sup> (optional).
  - Project proposals due on Gradescope on October 30<sup>th</sup>.
- Office hour logistics for this week:
  - Yannis will have extra office hours on Friday (time TBD).
- Late submissions:

 We are making an exception for homework assignment 3 and we won't count late days for submissions that are a few minutes late due to uploading delays.
 We will resume enforcing late days strictly for subsequent homeworks. One second

- We will resume enforcing late days strictly for subsequent homeworks. One second late is one late day.

## Computational photography talks this week @ CMU

• Ce Liu, Google Research (October 20<sup>th</sup>, 11 am – noon).

#### - Title: Advancing the State of the Art of Computer Vision for Billions of Users

At Google, advancing the state of the art of computer vision is very impactful as there are billions of users of Google products, many of which require high-quality, artifact-free images. I will share what we learned from successfully launching core computer vision techniques for various Google products, including PhotoScan (Photos), seamless Google Street View panorama stitching (Geo), Super Res Zoom (Pixel 4), Auto Pop-out & Uncrop (Display Ads), and Rendering4AI (Cloud AI). We also conduct academic research and publish at top-tier conferences. I will give an overview of several representative works, including seeing through obstructions (Siggraph'15), learning the depth of moving people by watching frozen people (CVPR'19), GAN-based image uncrop (ICCV'19), and supervised contrastive learning (NeurIPS'20).

- Tali Dekel, Google Research (October 20<sup>th</sup>, noon 1 pm).
  - Title: Learning to Retime People in Videos

By changing the speed of frames, or the speed of objects, we can enhance the way we perceive events or actions in videos. In this talk, I will present two of my recent works on retiming videos, and more specifically, manipulating the timings of people's actions. 1) "SpeedNet" (CVPR 2020 oral): a method for adaptively speeding up videos based on their content, allowing us to gracefully watch videos faster while avoiding jerky and unnatural motions. 2) "Layered Neural Rendering for Retiming People" (SIGGRAPH Asia): a method for speeding up, slowing down, or entirely freezing certain people in videos, while automatically re-rendering properly all the scene elements that are related to those people, like shadows, reflections, and loose clothing. Both methods are based on novel deep neural networks that learn concepts of natural motion and scene decomposition just by observing ordinary videos, without requiring any manual labels. I'll show adaptively sped-up videos of sports, of boring family events (that all of us want to watch faster), and I'll demonstrate various retiming effects of people dancing, groups running, and kids jumping on trampolines.

#### Overview of today's lecture

- Sources of blur.
- Deconvolution.
- Blind deconvolution.

#### Slide credits

Most of these slides were adapted from:

- Fredo Durand (MIT).
- Gordon Wetzstein (Stanford).

#### Why are our images blurry?

#### Why are our images blurry?

- Lens imperfections.
- Camera shake.
- Scene motion.
- Depth defocus.

• Ideal lens: An point maps to a point at a certain plane.



- Ideal lens: An point maps to a point at a certain plane.
- Real lens: A point maps to a circle that has non-zero minimum radius among all planes.



What is the effect of this on the images we capture?

- Ideal lens: An point maps to a point at a certain plane.
- Real lens: A point maps to a circle that has non-zero minimum radius among all planes.



Shift-invariant blur.

What causes lens imperfections?

What causes lens imperfections?

• Aberrations.

(Important note: Oblique aberrations like coma and distortion <u>are not shift-</u> <u>invariant</u> blur and we do not consider them here!)



• Diffraction.



small aperture



large aperture

Point spread function (PSF): The blur kernel of a lens.

• "Diffraction-limited" PSF: No aberrations, only diffraction. Determined by aperture shape.



Point spread function (PSF): The blur kernel of a lens.

• "Diffraction-limited" PSF: No aberrations, only diffraction. Determined by aperture shape.



Optical transfer function (OTF): The Fourier transform of the PSF. Equal to aperture shape.



 $( \bigcirc )$ 

imperfect lens PSF



image from imperfect lens

#### If we know c and b, can we recover x?







image from imperfect lens

image from a perfect lens

imperfect lens PSF

Lenses act as (optical) low-pass filters.

Slide from lecture 2: Basic imaging sensor design



Lenses act as (optical) smoothing filters.

- Sensors often have a lenslet array in front of them as an anti-aliasing (AA) filter.
- However, the AA filter means you also lose resolution.
- Nowadays, due the large number of sensor pixels, AA filters are becoming unnecessary.



Photographers often hack their cameras to remove the AA filter, in order to avoid the loss of resolution.

a.k.a. "hot rodding"

Example where AA filter is needed



#### without AA filter

with AA filter

Example where AA filter is unnecessary



#### without AA filter

with AA filter

#### If we know c and b, can we recover x?







image from imperfect lens

#### image from a perfect lens

imperfect lens PSF

# Deconvolution X + C = b

If we know c and b, can we recover x?

# Deconvolution x + c = b

Reminder: convolution is multiplication in Fourier domain:

## $F(x) \cdot F(c) = F(b)$

If we know c and b, can we recover x?

## Deconvolution X \* C = b

Reminder: convolution is multiplication in Fourier domain:

$$F(x) \cdot F(c) = F(b)$$

Deconvolution is division in Fourier domain:

$$F(x_{est}) = F(b) \setminus F(c)$$

After division, just do inverse Fourier transform:

$$x_{est} = F^{-1}(F(b) \setminus F(c))$$

Any problems with this approach?

• The OTF (Fourier of PSF) is a low-pass filter



zeros at high frequencies

• The measured signal includes noise

## b = c \* x + n — noise term

• The OTF (Fourier of PSF) is a low-pass filter



• The measured signal includes noise

$$b = c * x + n$$
 — noise term

• When we divide by zero, we amplify the high frequency noise

#### Naïve deconvolution

Even tiny noise can make the results awful.

• Example for Gaussian of  $\sigma = 0.05$ 







## Wiener Deconvolution

Apply inverse kernel and do not divide by zero:



- Derived as solution to maximum-likelihood problem under Gaussian noise assumption
- Requires noise of signal-to-noise ratio at each frequency

## Wiener Deconvolution

Apply inverse kernel and do not divide by zero:



Intuitively:

- When SNR is high (low or no noise), just divide by kernel.
- When SNR is low (high noise), just set to zero.

#### Deconvolution comparisons





#### naïve deconvolution

#### Wiener deconvolution

#### Deconvolution comparisons



 $\sigma = 0.01$ 

σ = 0.05

 $\sigma = 0.01$ 

Sensing model:

$$\tilde{x} = c * x + n$$

Noise n is assumed to be zeromean and independent of signal x.

Sensing model:

$$b = c * x + n$$

Noise n is assumed to be zeromean and independent of signal x.

Fourier transform:

$$B = C \cdot X + N$$

$$Mhy multiplication?$$

Sensing model:

$$b = c * x + n$$

Noise n is assumed to be *zero-mean* and *independent* of signal x.

Fourier transform:

$$B = C \cdot X + N$$

Convolution becomes multiplication.

Problem statement: Find function  $H(\omega)$  that minimizes *expected* error *in Fourier domain*.

$$\min_{H} E[\|X - HB\|^2]$$

Replace B and re-arrange loss:

$$\min_{H} E[\|(1 + HC)X - HN\|^2]$$

Expand the squares:

$$\min_{H} \|1 - HC\|^2 E[\|X\|^2] - 2(1 - HC)E[XN] + \|H\|^2 E[\|N\|^2]$$
When handling the cross terms:

• Can I write the following?

E[XN] = E[X]E[N]

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Yes, because X and N are assumed independent.

• What is this expectation product equal to?

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• Can I write the following?

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```

Yes, because X and N are assumed independent.

• What is this expectation product equal to?

Zero, because N has zero mean.

Replace B and re-arrange loss:

$$\min_{H} E[\|(1 + HC)X - HN\|^2]$$

Expand the squares:

$$\min_{H} \|1 - HC\|^{2} E[\|X\|^{2}] - 2(1 - HC)E[XN] + \|H\|^{2} E[\|N\|^{2}]$$
  
$$\swarrow \text{ cross-term is zero}$$

Simplify:

# $\min_{H} \|1 - HC\|^2 E[\|X\|^2] + \|H\|^2 E[\|N\|^2]$

How do we solve this optimization problem?

Differentiate loss with respect to H, set to zero, and solve for H:

$$\frac{\partial \text{loss}}{\partial H} = 0$$

$$\Rightarrow -2(1 - HC)E[||X||^{2}] + 2HE[||N||^{2}] = 0$$

$$\Rightarrow H = \frac{CE[\|X\|^2]}{C^2 E[\|X\|^2] + E[\|N\|^2]}$$

Divide both numerator and denominator with  $E[||X||^2]$ , extract factor 1/C, and done!

Apply inverse kernel and do not divide by zero:

$$x_{est} = F^{-1} \left( \frac{|F(c)|^2}{|F(c)|^2 + 1/SNR(\omega)} \cdot \frac{F(b)}{F(c)} \right)$$
noise-dependent damping factor

- Derived as solution to maximum-likelihood problem under Gaussian noise assumption
- Requires estimate of signal-to-noise ratio at each frequency

SNR(
$$\omega$$
) =  $\frac{1}{1000}$  signal variance at  $\omega$   
noise variance at  $\omega$ 

### Natural image and noise spectra

Natural images tend to have spectrum that scales as 1 /  $\omega^2$ 

• This is a *natural image statistic* 



# Natural image and noise spectra

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• This is a *natural image statistic* 



Noise tends to have flat spectrum,  $\sigma(\omega) = constant$ 

• We call this white noise

What is the SNR?

## Natural image and noise spectra

Natural images tend to have spectrum that scales as 1 /  $\omega^2$ 

• This is a *natural image statistic* 



Noise tends to have flat spectrum,  $\sigma(\omega) = constant$ 

• We call this white noise

Therefore, we have that:  $SNR(\omega) = 1 / \omega^2$ 

Apply inverse kernel and do not divide by zero:



- Derived as solution to maximum-likelihood problem under Gaussian noise assumption
- Requires noise of signal-to-noise ratio at each frequency

$$SNR(\omega) = \frac{1}{\omega^2}$$

For natural images and white noise, equivalent to the minimization problem:

 $min_{x} ||b - c * x||^{2} + ||\nabla x||^{2}$ 

gradient regularization

How can you prove this equivalence?

For natural images and white noise, it can be re-written as the minimization problem

$$\min_{x} ||b - c * x||^{2} + ||\nabla x||^{2}$$

gradient *regularization* 

How can you prove this equivalence?

- Convert to Fourier domain and repeat the proof for Wiener deconvolution.
- Intuitively: The  $\omega^2$  term in the denominator of the special Wiener filter is the square of the Fourier transform of  $\nabla x$ , which is  $i \cdot \omega$ .

#### Deconvolution comparisons



blurry input

naive deconvolution

gradient regularization

original

#### Deconvolution comparisons



blurry input

naive deconvolution

gradient regularization

original

#### ... and a proof-of-concept demonstration



noisy input

naive deconvolution

gradient regularization

#### Question

Can we undo lens blur by deconvolving a PNG or JPEG image without any preprocessing?

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Can we undo lens blur by deconvolving a PNG or JPEG image without any preprocessing?

- All the blur processes we discuss today happen *optically* (before capture by the sensor).
- Blur model is accurate only if our images are *linear*.

Are PNG or JPEG images linear?

### Question

Can we undo lens blur by deconvolving a PNG or JPEG image without any preprocessing?

- All the blur processes we discuss today happen *optically* (before capture by the sensor).
- Blur model is accurate only if our images are *linear*.

Are PNG or JPEG images linear?

- No, because of gamma encoding.
- Before deblurring, you must linearize your images.

How do we linearize PNG or JPEG images?

### The importance of linearity



blurry input

deconvolution without linearization

deconvolution after linearization

original

#### Can we do better than that?

# Can we do better than that?

Use different gradient regularizations:

• L<sub>2</sub> gradient regularization (Tikhonov regularization, same as Wiener deconvolution)

$$\min_{x} ||b - c * x||^{2} + ||\nabla x||^{2}$$

•  $L_1$  gradient regularization (sparsity regularization, *isotropic total variation*)

$$m_{x} ||b - c * x||^{2} + ||Vx||_{1}^{1}$$

All of these are motivated by natural image statistics. Active research area.

How are

# **Total Variation**



 $\sqrt{\left(\nabla_x x\right)^2 + \left(\nabla_y x\right)^2}$ 

X

easier: anisotropic

 $\sqrt{\left(\nabla_{x} x\right)^{2}} + \sqrt{\left(\nabla_{y} x\right)^{2}}$ 



# **Total Variation**

$$\underset{x}{\text{minimize}} \|Cx - b\|_{2}^{2} + \lambda TV(x) = \underset{x}{\text{minimize}} \|Cx - b\|_{2}^{2} + \lambda \|\nabla x\|_{1}$$

 $||x||_1 = \sum_i |x_i|$ 

• idea: promote sparse gradients (edges)

•  $\nabla$  is finite differences operator, i.e. matrix



Rudin et al. 1992

# **Total Variation**

• for simplicity, this lecture only discusses anisotropic TV:

$$TV(x) = \left\| \nabla_{x} x \right\|_{1} + \left\| \nabla_{y} x \right\|_{1} = \left\| \begin{bmatrix} \nabla_{x} \\ \nabla_{y} \end{bmatrix} x \right\|_{1}$$

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• problem: I1-norm is not differentiable, can't use inverse filtering

• however: simple solution for data fitting along and simple solution for TV alone  $\rightarrow$  split problem!

# Deconvolution with ADMM

• split deconvolution with TV prior:

minimize 
$$||Cx - b||_2^2 + \lambda ||z||_1$$
  
subject to  $\nabla x = z$ 

• general form of ADMM (alternating direction method of multiplies):

minimize f(x) + g(z)subject to Ax + Bz = c

$$f(x) = ||Cx - b||_{2}^{2}$$
$$g(z) = \lambda ||z||_{1}$$
$$A = \nabla, B = -I, c = 0$$

• Lagrangian (bring constraints into objective = penalty method):

$$L(x,y,z) = f(x) + g(z) + y^{T}(Ax + Bz - c)$$

$$\uparrow$$
dual variable or Lagrange multiplier

 augmented Lagrangian is differentiable under mild conditions (usually better convergence etc.)

$$L_{\rho}(x, y, z) = f(x) + g(z) + y^{T} (Ax + Bz - c) + (\rho / 2) ||Ax + Bz - c||_{2}^{2}$$

• ADMM consists of 3 steps per iteration k:

$$x^{k+1} \coloneqq \arg\min_{x} L_{\rho}(x, z^{k}, y^{k})$$

$$z^{k+1} \coloneqq \arg\min_{z} L_{\rho}(x^{k+1}, z, y^{k})$$

$$y^{k+1} \coloneqq y^{k} + \rho(Ax^{k+1} + Bz^{k+1} - c)$$

• ADMM consists of 3 steps per iteration k:

$$x^{k+1} \coloneqq \arg\min_{x} \left( f(x) + (\rho/2) ||Ax + Bz^{k} - c + u^{k}|| \right)$$

$$z^{k+1} \coloneqq \arg\min_{z} \left( g(z) + (\rho/2) ||Ax^{k+1} + Bz - c + u^{k}|| \right)$$

$$u^{k+1} \coloneqq u^{k} + Ax^{k+1} + Bz^{k+1} - c$$

scaled dual variable:  $u = (1 / \rho)y$ 

• ADMM consists of 3 steps per iteration k:

split f(x) and g(x) into independent problems!

$$x^{k+1} := \arg \min_{x} \left( f(x) + (\rho/2) ||Ax + Bz^{k} - c + u^{k}||_{2}^{2} \right)^{(\text{u connects them})}$$
  

$$z^{k+1} := \arg \min_{z} \left( g(z) + (\rho/2) ||Ax^{k+1} + Bz - c + u^{k}||_{2}^{2} \right)$$
  

$$u^{k+1} := u^{k} + Ax^{k+1} + Bz^{k+1} - c$$

scaled dual variable:  $u = (1 / \rho)y$ 

minimize 
$$\frac{1}{2} ||Cx - b||_2^2 + \lambda ||z||_1$$
 Deconvolution with ADMM

subject to  $\nabla x - z = 0$ 

• ADMM consists of 3 steps per iteration k:

$$x^{k+1} \coloneqq \arg\min_{x} \left( \frac{1}{2} ||Cx - b||_{2}^{2} + (\rho/2) ||\nabla x - z^{k} + u^{k}||_{2}^{2} \right)$$
$$z^{k+1} \coloneqq \arg\min_{z} \left( \lambda ||z||_{1} + (\rho/2) ||\nabla x^{k+1} - z + u^{k}||_{2}^{2} \right)$$
$$u^{k+1} \coloneqq u^{k} + \nabla x^{k+1} - z^{k+1}$$

minimize 
$$\frac{1}{2} ||Cx - b||_2^2 + \lambda ||z||_1$$
 Deconvolution with ADMM  
subject to  $\nabla x - z = 0$  constant, say  $v = z^k - u^k$   
1. x-update:  $x^{k+1} \coloneqq \underset{x}{\operatorname{arg\,min}} \left( \frac{1}{2} ||Cx - b||_2^2 + (\rho/2) ||\nabla x - z^k + u^k||_2^2 \right)$ 

solve normal equations 
$$(C^T C + \rho \nabla^T \nabla) x = (C^T b + \rho \nabla^T v)$$
  
 $\nabla^T v = \begin{bmatrix} \nabla_x \\ \nabla_y \end{bmatrix}^T v = \nabla_x^T v_1 + \nabla_y^T v_2$ 

minimize 
$$\frac{1}{2} ||Cx - b||_2^2 + \lambda ||z||_1$$
 Deconvolution with ADMM  
subject to  $\nabla x - z = 0$  constant, say  $v = z^k - u^k$   
1. x-update:  $x^{k+1} \coloneqq \operatorname*{arg\,min}_x \left( \frac{1}{2} ||Cx - b||_2^2 + (\rho/2) ||\nabla x - z^k + u^k||_2^2 \right)$ 

$$x = \left(C^T C + \rho \nabla^T \nabla\right)^{-1} \left(C^T b + \rho \nabla^T v\right)$$

• inverse filtering: 
$$x^{k+1} = F^{-1} \left\{ F\{c\}^* \cdot F\{b\} + \rho \left[F\{\nabla_x\}^* \cdot F\{v_1\} + F\{\nabla_y\}^* \cdot F\{v_2\}\right] \\ F\{c\}^* \cdot F\{c\} + \rho \left[F\{\nabla_x\}^* \cdot F\{\nabla_y\} + F\{\nabla_y\}^* \cdot F\{\nabla_y\}\right] \right\}$$

precompute!

minimize 
$$\frac{1}{2} ||Cx - b||_2^2 + \lambda ||z||_1$$
 Deconvolution with ADMM  
subject to  $\nabla x - z = 0$  constant, say  $a = \nabla x^{k+1} + u^k$   
2. z-update:  $z^{k+1} \coloneqq \arg\min_{z} \left(\lambda ||z||_1 + (\rho/2) ||\nabla x^{k+1} - z + u^k||_2^2\right)$ 

minimize 
$$\frac{1}{2} ||Cx - b||_2^2 + \lambda ||z||_1$$
 Deconvolution with ADMM  
subject to  $\nabla x - z = 0$ 

for k=1:max\_iters

$$x^{k+1} \coloneqq \arg\min_{x} \left( \frac{1}{2} \left\| \begin{bmatrix} C \\ \rho \nabla \end{bmatrix} x - \begin{bmatrix} b \\ \rho \nu \end{bmatrix} \right\|_{2}^{2} \right) \text{ inverse filtering}$$

$$z^{k+1} \coloneqq S_{\lambda/\rho} (\nabla x^{k+1} + u^{k}) \qquad \text{element-wise threshold}$$

$$u^{k+1} \coloneqq u^{k} + \nabla x^{k+1} - z^{k+1} \qquad \text{trivial}$$

#### Deconvolution comparisons



#### Wiener deconvolution

#### ADMM + TV, $\lambda = 0.01$

#### ADMM + TV, $\lambda = 0.1$

- image becomes too flat as we increase weight of TV prior
- Image becomes too noisy as we decrease weight of TV prior
#### Deconvolution comparisons



Wiener deconvolution

#### ADMM + TV, $\lambda = 0.01$

#### ADMM + TV, $\lambda = 0.1$

- image becomes too flat as we increase weight of TV prior
- Image becomes too noisy as we decrease weight of TV prior

# Outlook ADMM

- powerful tool for many computational imaging problems
- include generic prior in g(z), just need to derive proximal operator



- example priors: noise statistics, sparse gradient, smoothness, ...
- weighted sum of different priors also possible
- anisotropic TV is one of the easiest priors

# Can we do better than that?

Use different gradient regularizations:

• L<sub>2</sub> gradient regularization (Tikhonov regularization, same as Wiener deconvolution)

$$min_{x} ||b - c * x||^{2} + ||\nabla x||_{2}^{2}$$

• L<sub>1</sub> gradient regularization (sparsity regularization, same as *total variation*)

$$\min_{x} ||b - c * x||^{2} + ||\nabla x||_{1}^{1}$$

• L<sub>n<1</sub> gradient regularization (fractional regularization)

$$\min_{x} ||b - c * x||^{2} + ||\nabla x||_{0.8}^{0.8}$$

All of these are motivated by natural image statistics. Active research area.

# Comparison of gradient regularizations



input

squared gradient regularization

fractional gradient regularization

## Derivation

Sensing model:

$$\tilde{x} = c * x + n$$

Noise **n** is assumed to be zeromean and independent of signal **x**.

Is this a reasonable noise model?

# $\begin{aligned} & \text{Richardson-Lucy Algorithm + TV} \\ & \cdot \quad \text{log-likelihood function:} \\ & \log\left(L_{TV}\left(\mathbf{x}\right)\right) = \log\left(p\left(\mathbf{b}|\mathbf{x}\right)\right) + \log\left(p\left(\mathbf{x}\right)\right) = \log\left(\mathbf{A}\mathbf{x}\right)^{T}\mathbf{b} - (\mathbf{A}\mathbf{x})^{T}\mathbf{1} - \sum_{i=1}^{M}\log\left(\mathbf{b}_{i}!\right) - \lambda \|\mathbf{D}\mathbf{x}\|_{1} \end{aligned}$

• gradient:

$$\nabla \log \left( L_{TV} \left( \mathbf{x} \right) \right) = \mathbf{A}^{T} \operatorname{diag} \left( \mathbf{A} \mathbf{x} \right)^{-1} \mathbf{b} - \mathbf{A}^{T} \mathbf{1} + \nabla \lambda \left\| \nabla \mathbf{x} \right\|_{1} = \mathbf{A}^{T} \left( \frac{\mathbf{b}}{\mathbf{A} \mathbf{x}} \right) - \mathbf{A}^{T} \mathbf{1} - \nabla \lambda \left\| \mathbf{D} \mathbf{x} \right\|_{1}$$

- recover signal by setting gradient to zero
- generally challenging

# High quality images using cheap lenses





[Heide et al., "High-Quality Computational Imaging Through Simple Lenses," TOG 2013]

# Deconvolution

If we know b and c, can we recover x?



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How do we measure this?

\*

\*



## PSF calibration



Image of PSF

Image with sharp lens

Image with cheap lens

# Deconvolution

#### If we know b and c, can we recover x?



Х



\*





# Blind deconvolution

#### If we know b, can we recover x and c?



Х



\*

\*



#### Camera shake

#### Removing Camera Shake from a Single Photograph

Rob Fergus<sup>1</sup> Barun Singh<sup>1</sup> Aaron Hertzmann<sup>2</sup> Sam T. Roweis<sup>2</sup> William T. Freeman<sup>1</sup> <sup>1</sup>MIT CSAIL <sup>2</sup>University of Toronto



Figure 1: Left: An image spoiled by camera shake. Middle: result from Photoshop "unsharp mask". Right: result from our algorithm.

## Camera shake as a filter

If we know b, can we recover x and c?



image from static camera

Х

PSF from camera motion

image from shaky camera

## Multiple possible solutions



How do we detect this one?

#### Use prior information

Among all the possible pairs of images and blur kernels, select the ones where:

• The image "looks like" a natural image.

• The kernel "looks like" a motion PSF.

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# Shake kernel statistics

Gradients in natural images follow a characteristic "heavy-tail" distribution.





sharp natural image

blurry natural image

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Gradients in natural images follow a characteristic "heavy-tail" distribution.





sharp natural image

blurry natural image

# Use prior information

Among all the possible pairs of images and blur kernels, select the ones where:

• The image "looks like" a natural image.

Gradients in natural images follow a characteristic "heavy-tail" distribution.

• The kernel "looks like" a motion PSF.

Shake kernels are very sparse, have continuous contours, and are always positive

How do we use this information for blind deconvolution?





Solve regularized least-squares optimization

$$\min_{x,b} ||b - c * x||^2 + ||\nabla x||^{0.8} + ||c||_1$$

What does each term in this summation correspond to?

Solve regularized least-squares optimization

$$\begin{array}{c} \min_{x,b} \|b - c * x\|^2 + \|\nabla x\|^{0.8} + \|c\|_1 \\ \downarrow & \downarrow & \uparrow \\ \text{data term} & \text{natural image prior} & \text{shake kernel prior} \end{array}$$

Note: Solving such optimization problems is complicated (no longer *linear* least squares).

Gradient

#### A demonstration

input



#### deconvolved image and kernel





#### A demonstration

input



#### deconvolved image and kernel



This image looks worse than the original...



This doesn't look like a plausible shake kernel...

Solve regularized least-squares optimization

$$\min_{x,b} ||b - c * x||^2 + ||\nabla x||^{0.8} + ||c||_1$$

loss function

Solve regularized least-squares optimization

$$\min_{x,b} ||b - c * x||^{2} + ||\nabla x||^{0.8} + ||c||_{1}$$
inverse loss function  
Where in this graph is the solution we find?

Solve regularized least-squares optimization

$$\min_{x,b} ||b - c * x||^2 + ||\nabla x||^{0.8} + ||c||_1$$
inverse loss function
$$\max_{b \in S} ||b - c * x||^2 + ||\nabla x||^{0.8} + ||c||_1$$

$$\max_{b \in S} ||b - c * x||^2 + ||\nabla x||^{0.8} + ||c||_1$$

$$\max_{b \in S} ||b - c * x||^2 + ||\nabla x||^{0.8} + ||c||_1$$

## A demonstration

input

#### maximum-only









# More examples





























#### More advanced motion deblurring



[Shah et al., High-quality Motion Deblurring from a Single Image, SIGGRAPH 2008]

# Why are our images blurry?

- Lens imperfections. Can we solve all of these problems using (blind) deconvolution?
- Camera shake.
- Scene motion.
- Depth defocus.

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- Lens imperfections.
- Camera shake.
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- Depth defocus.

Can we solve all of these problems using (blind) deconvolution?

- We can deal with (some) lens imperfections and camera shake, because their blur is shift invariant.
- We cannot deal with scene motion and depth defocus, because their blur is not shift invariant.
- See coded photography lecture.

# References

Basic reading:

- Szeliski textbook, Sections 3.4.3, 3.4.4, 10.1.4, 10.3.
- Fergus et al., "Removing camera shake from a single image," SIGGRAPH 2006. the main motion deblurring and blind deconvolution paper we covered in this lecture.

Additional reading:

- Heide et al., "High-Quality Computational Imaging Through Simple Lenses," TOG 2013. the paper on high-quality imaging using cheap lenses, which also has a great discussion of all matters relating to blurring from lens aberrations and modern deconvolution algorithms.
- Levin, "Blind Motion Deblurring Using Image Statistics," NIPS 2006.
- Levin et al., "Image and depth from a conventional camera with a coded aperture," SIGGRAPH 2007.
- Levin et al., "Understanding and evaluating blind deconvolution algorithms," CVPR 2009 and PAMI 2011.
- Krishnan and Fergus, "Fast Image Deconvolution using Hyper-Laplacian Priors," NIPS 2009.
- Levin et al., "Efficient Marginal Likelihood Optimization in Blind Deconvolution," CVPR 2011.

   a sequence of papers developing the state of the art in blind deconvolution of natural images, including the use Laplacian (sparsity) and hyper-Laplacian priors on gradients, analysis of different loss functions and maximum a-posteriori versus Bayesian estimates, the use of variational inference, and efficient optimization algorithms.
- Minskin and MacKay, "Ensemble Learning for Blind Image Separation and Deconvolution," AICA 2000. the paper explaining the mathematics of how to compute Bayesian estimators using variational inference.
- Shah et al., "High-quality Motion Deblurring from a Single Image," SIGGRAPH 2008. a more recent paper on motion deblurring.