Color





15-463, 15-663, 15-862 Computational Photography Fall 2018, Lecture 7

Course announcements

- Homework 2 is out.
 - Due September 28th.
 - Requires camera and tripod.
 - Still five cameras left if anybody needs one.
 - Start early! Large programming component and generous bonus.

Overview of today's lecture

- Leftover from lecture 6: some thoughts on HDR and tonemapping.
- Recap: color and human color perception.
- Retinal color space.
- Color matching.
- Linear color spaces.
- Chromaticity.
- Non-linear color spaces.
- Some notes about color reproduction.

Slide credits

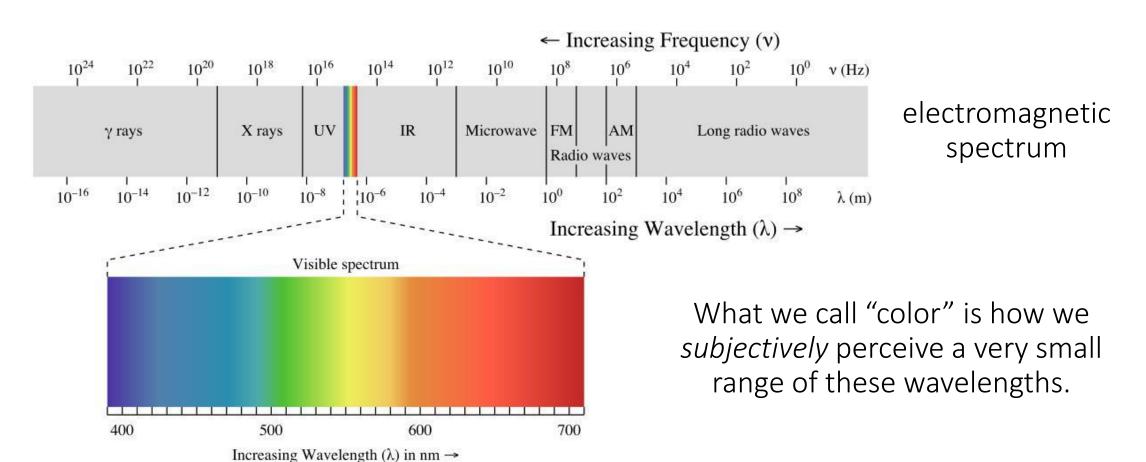
Many of these slides were inspired or adapted from:

- Todd Zickler (Harvard).
- Fredo Durand (MIT).

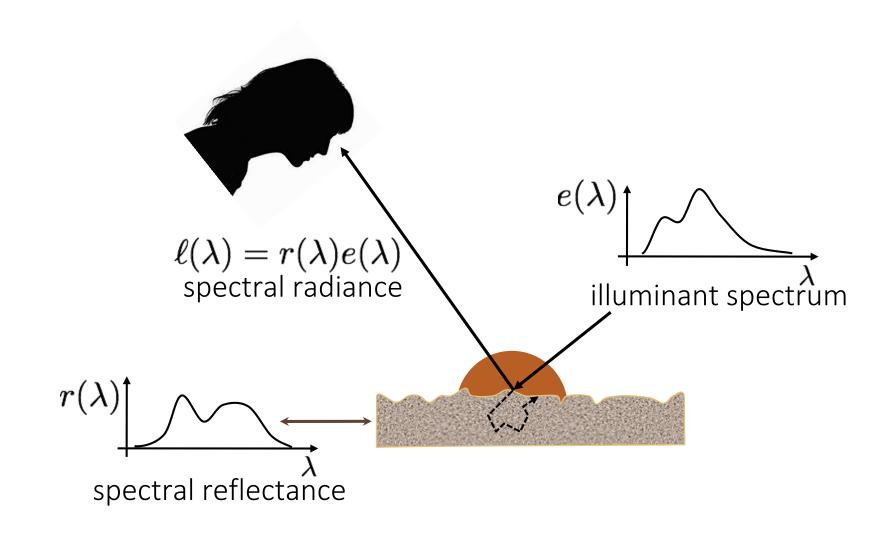
Recap: color and human color perception

Color is an artifact of human perception

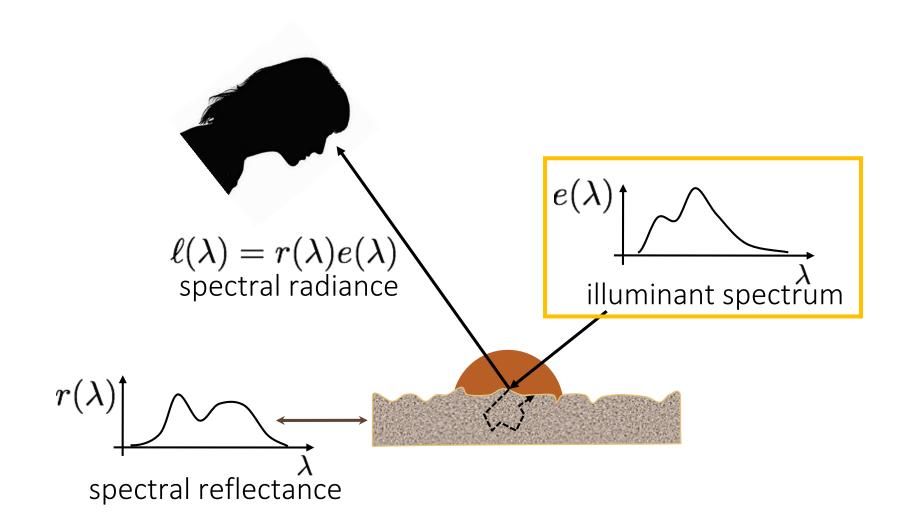
- "Color" is not an objective physical property of light (electromagnetic radiation).
- Instead, light is characterized by its wavelength.



Light-material interaction



Light-material interaction

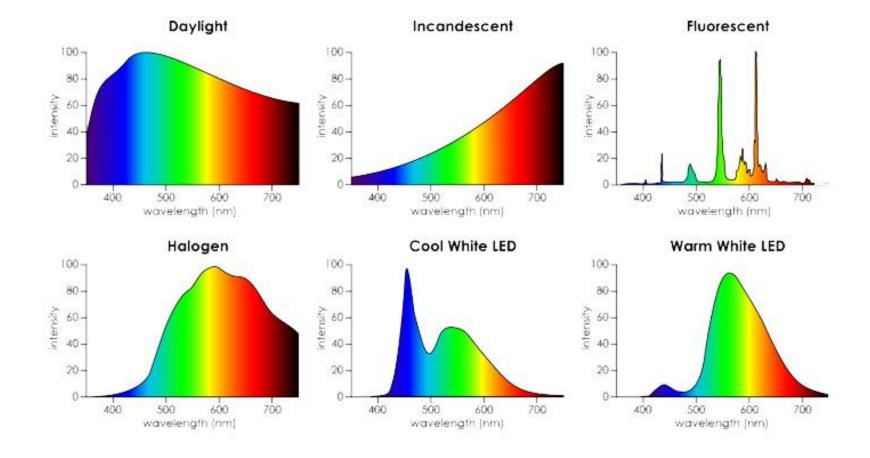


Illuminant Spectral Power Distribution (SPD)

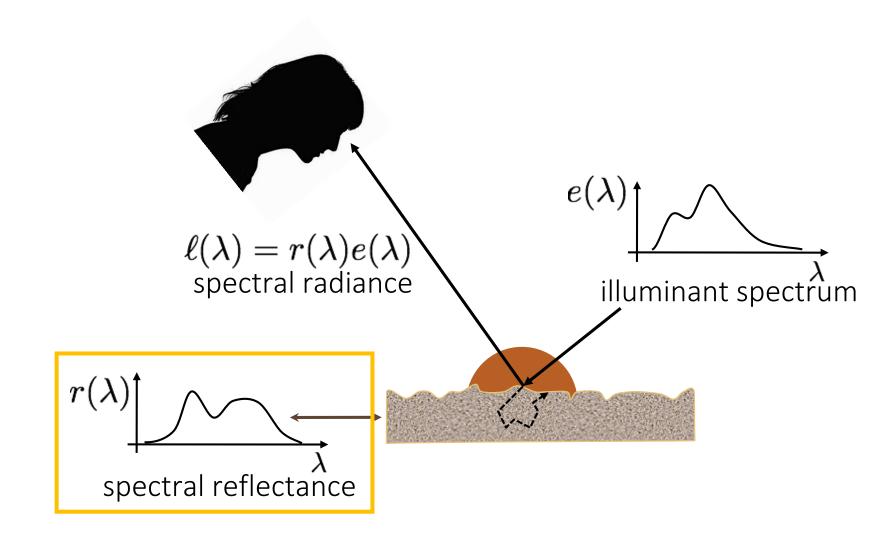
- Most types of light "contain" more than one wavelengths.
- We can describe light based on the distribution of power over different wavelengths.



We call our sensation of all of these distributions "white".



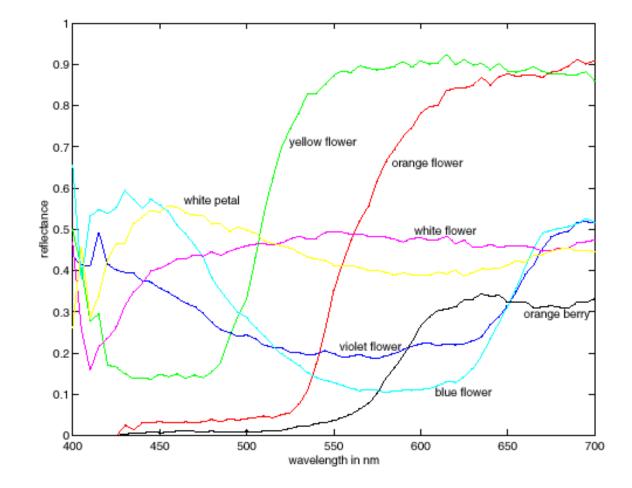
Light-material interaction



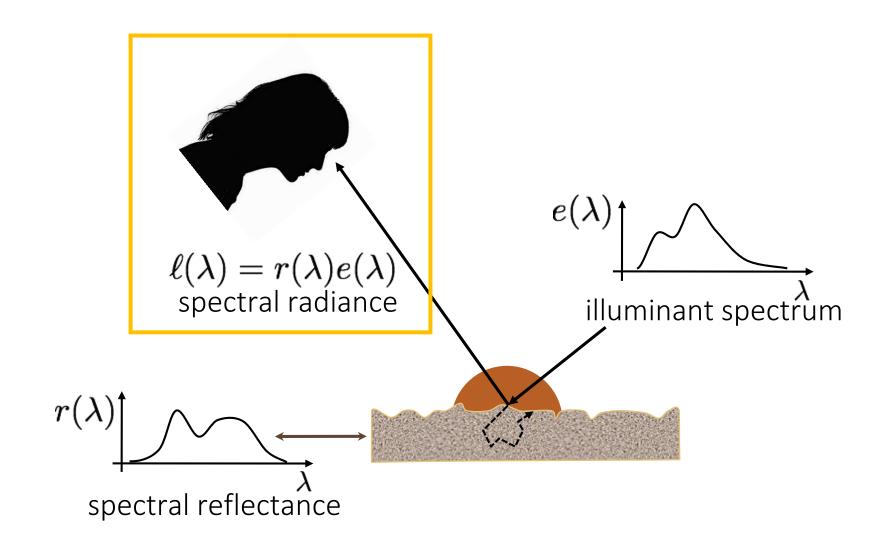
Spectral reflectance

- Most materials absorb and reflect light differently at different wavelengths.
- We can describe this as a ratio of reflected vs incident light over different wavelengths.





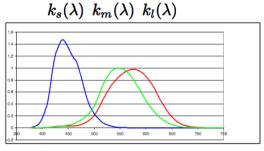
Light-material interaction



Human color vision

retinal color
$$c_s = \int k_s(\lambda)\ell(\lambda)d\lambda$$
 $\mathbf{c}(\ell(\lambda)) = (c_s, c_m, c_l)$

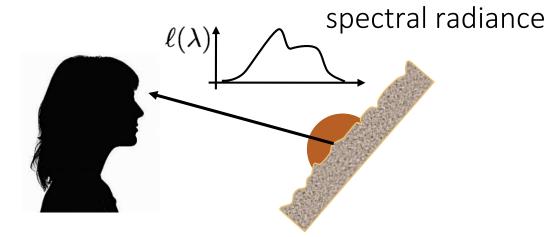
$$c_s = \int k_s(\lambda)\ell(\lambda)d\lambda$$



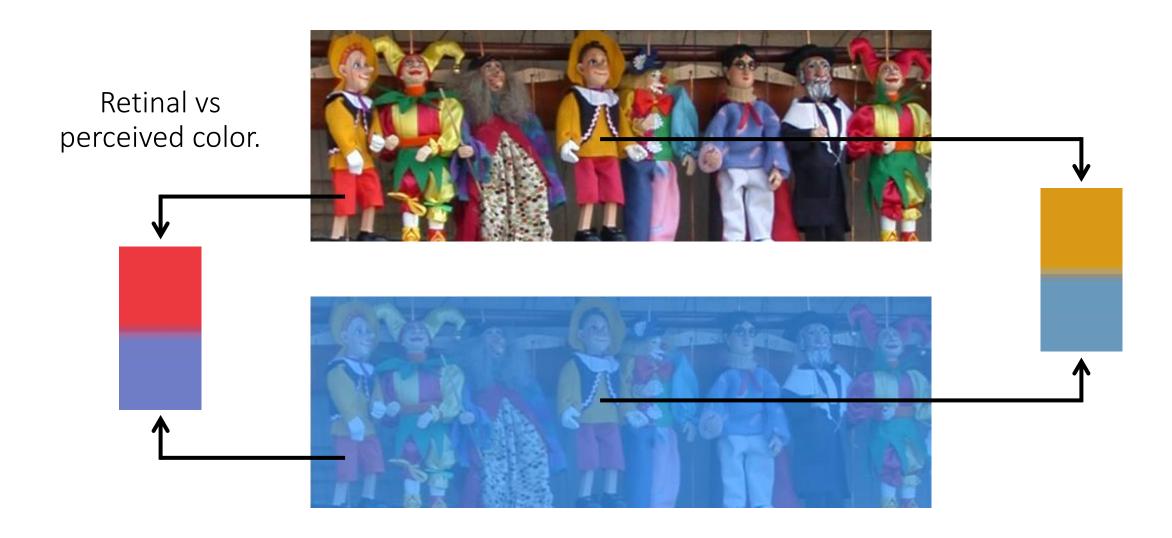
LMS senstivity functions



perceived color object color color names



Retinal vs perceived color



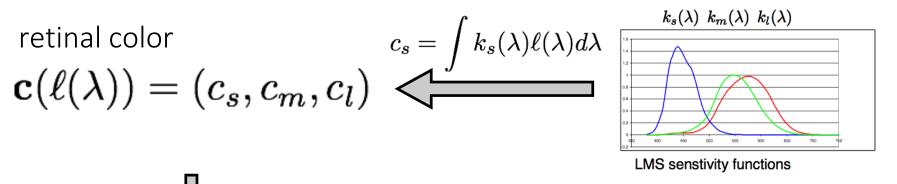
Retinal vs perceived color

- Our visual system tries to "adapt" to illuminant.
- We may interpret the same retinal color very differently.



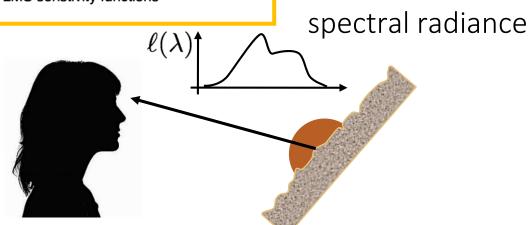
Human color vision

We will exclusively discuss retinal color in this course



 \forall

perceived color object color color names



Retinal color space

Spectral Sensitivity Function (SSF)

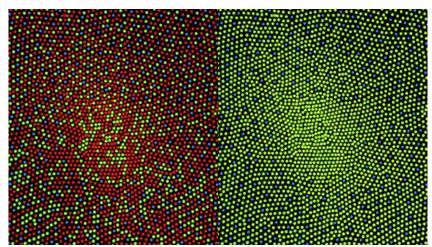
- Any light sensor (digital or not) has different sensitivity to different wavelengths.
- This is described by the sensor's spectral sensitivity function $f(\lambda)$.
- When measuring light of a some SPD $\Phi(\lambda)$, the sensor produces a *scalar* response:

$$\stackrel{\text{sensor}}{\longrightarrow} R = \int_{\lambda}^{\text{light SPD}} \Phi(\lambda) f(\lambda) d\lambda$$

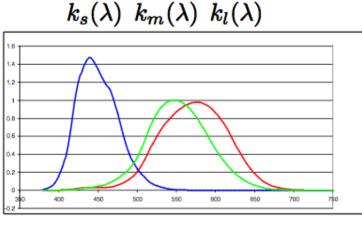
Weighted combination of light's SPD: light contributes more at wavelengths where the sensor has higher sensitivity.

Spectral Sensitivity Function of Human Eye

- The human eye is a collection of light sensors called cone cells.
- There are three types of cells with different spectral sensitivity functions.
- Human color perception is three-dimensional (tristimulus color).



"short"
$$S=\int_{\lambda}\Phi(\lambda)S(\lambda)d\lambda$$
 "medium" $M=\int_{\lambda}\Phi(\lambda)M(\lambda)d\lambda$ "long" $L=\int_{\lambda}\Phi(\lambda)L(\lambda)d\lambda$

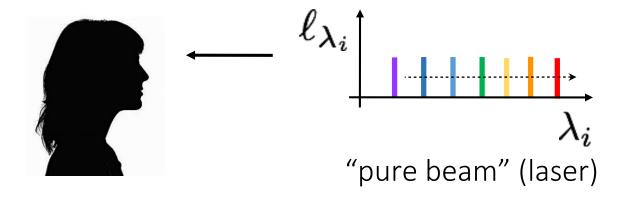


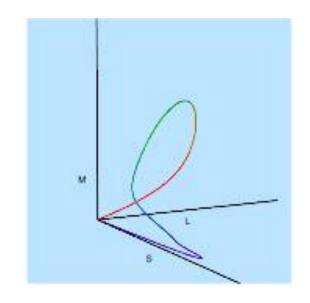
LMS senstivity functions

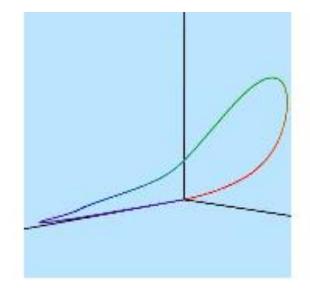
$$\mathbf{c}(\ell_{\lambda_i}) = (c_s, c_m, c_l)$$

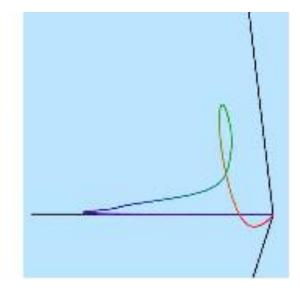
$$\downarrow \\ k_s(\lambda) \ k_m(\lambda) \ k_l(\lambda)$$

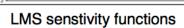
LMS senstivity functions

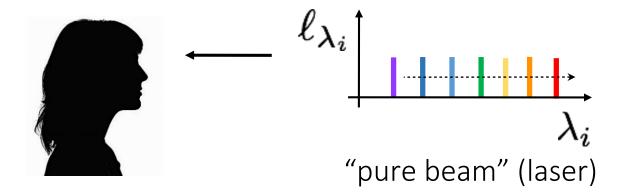








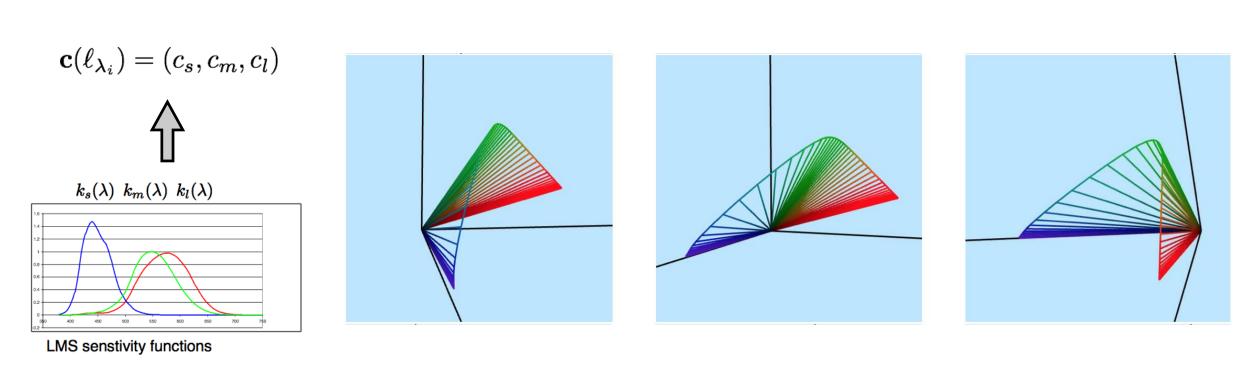


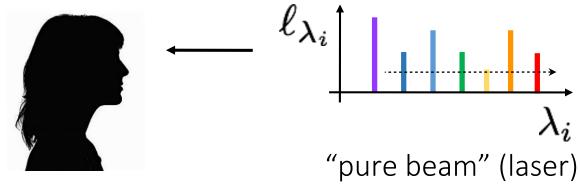


- "lasso curve"
- contained in positive octant
- parameterized by wavelength
- starts and ends at origin
- never comes close to M axis

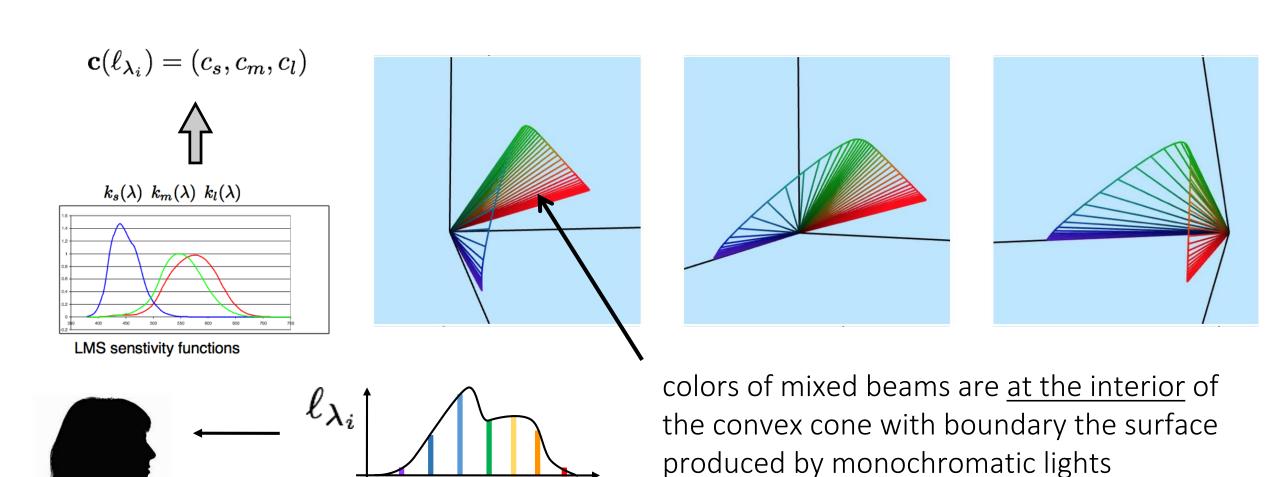


← why?



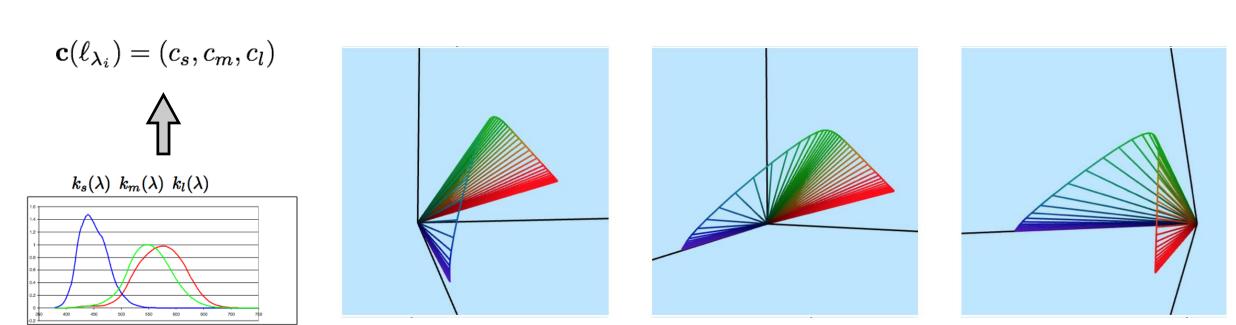


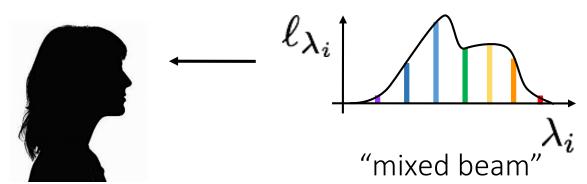
if we also consider variations in the *strength* of the laser this "lasso" turns into (convex!) radial cone with a "horse-shoe shaped" radial cross-section



= convex combination of pure colors

"mixed beam"



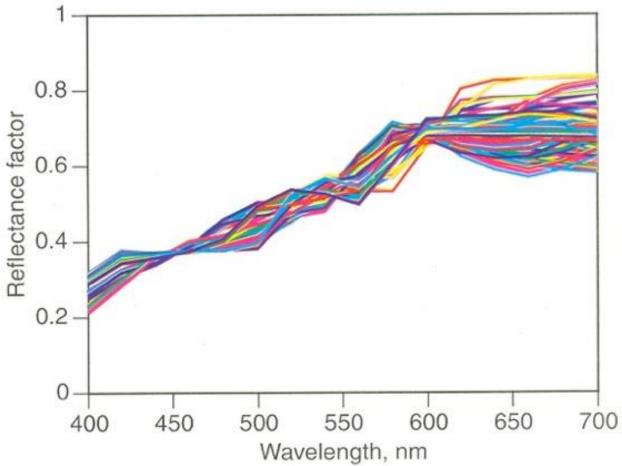


LMS senstivity functions

= convex combination of pure colors

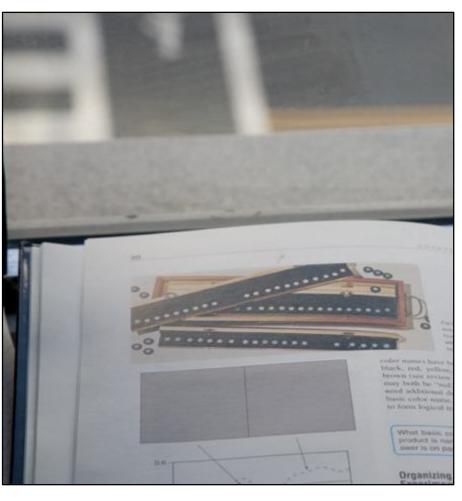
- distinct mixed beams can produce the same retinal color
- These beams are called *metamers*

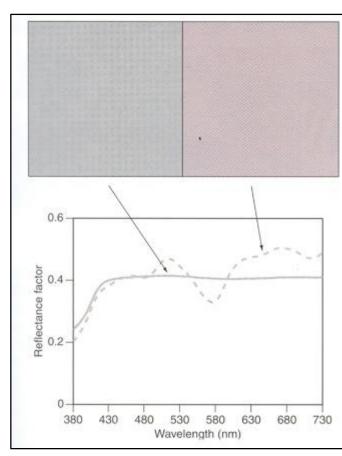
There is an infinity of metamers

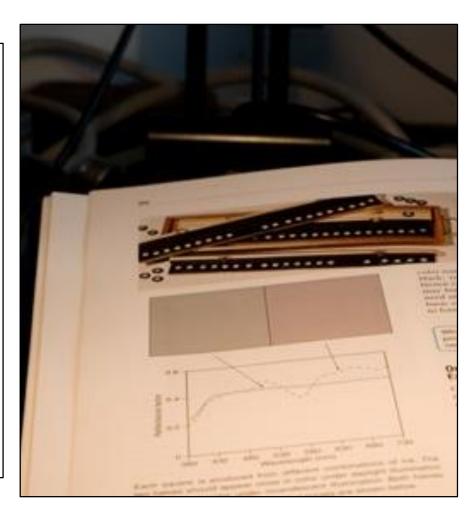


Ensemble of spectral reflectance curves corresponding to three chromatic-pigment recipes all matching a tan material when viewed by an average observer under daylight illumination. [Based on Berns (1988b).]

Example: illuminant metamerism



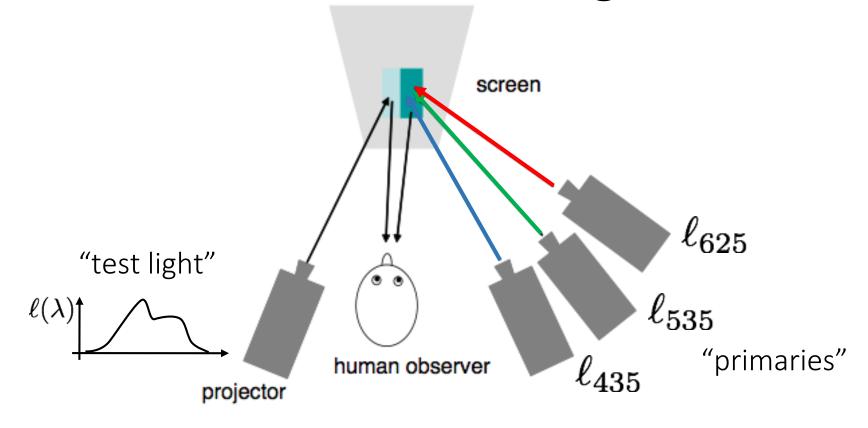




day light scanned copy hallogen light

Color matching

CIE color matching

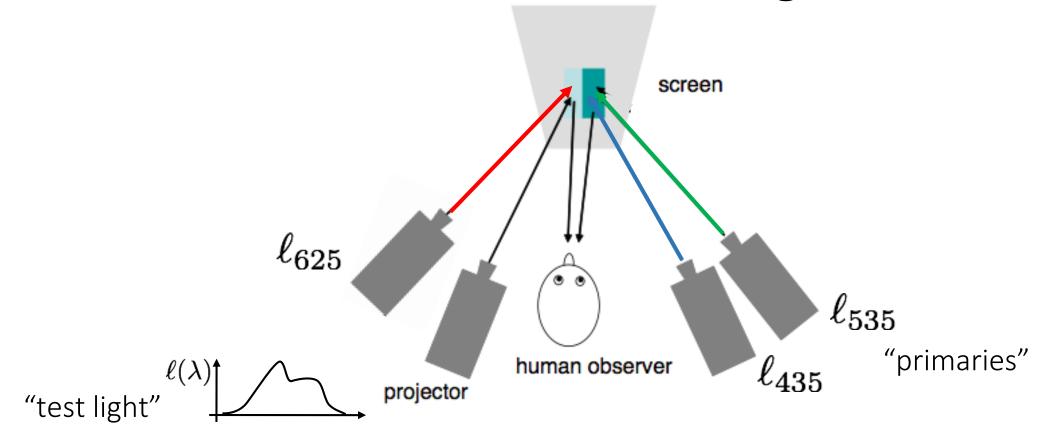


Adjust the strengths of the primaries until they re-produce the test color. Then:

$$\mathbf{c}(\ell(\lambda)) = \alpha \mathbf{c}(\ell_{435}) + \beta \mathbf{c}(\ell_{535}) + \gamma \mathbf{c}(\ell_{625})$$

equality symbol means "has the same retinal color as" or "is metameric to"

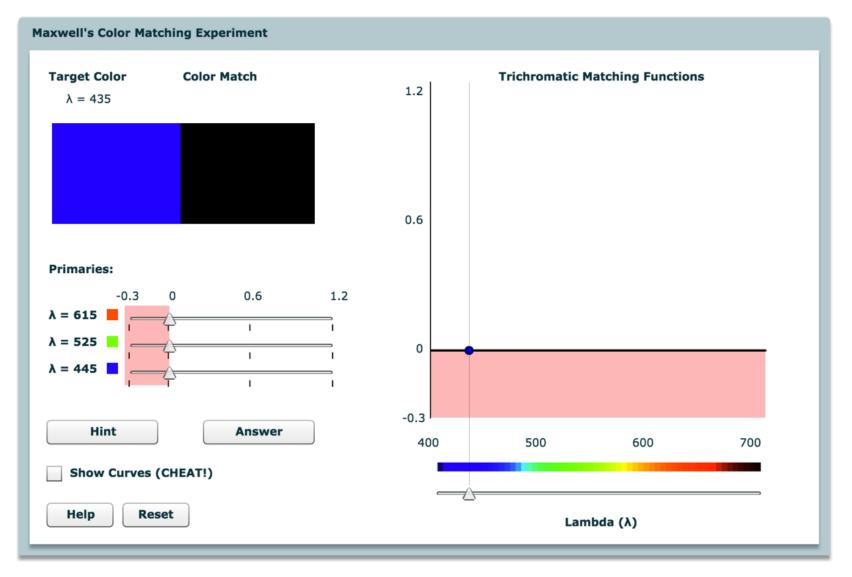
CIE color matching



To match some test colors, you need to add some primary beam on the left (same as "subtracting light" from the right)

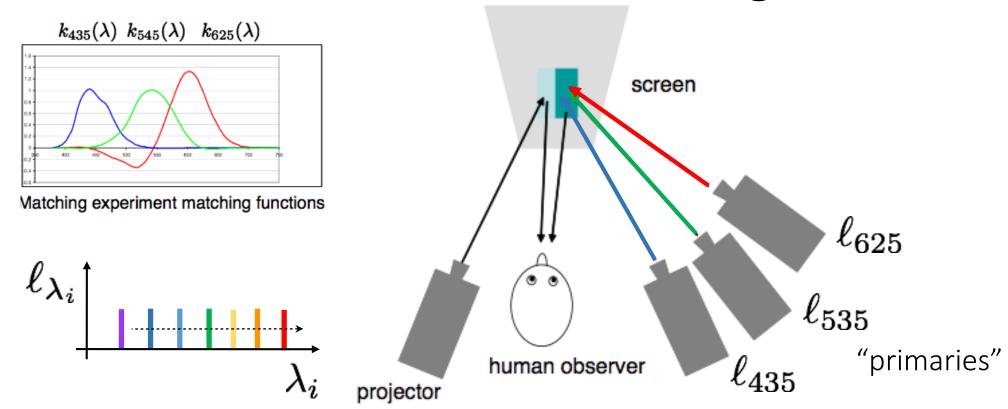
$$\mathbf{c}(\ell(\lambda)) + \gamma \mathbf{c}(\ell_{625}) = \alpha \mathbf{c}(\ell_{435}) + \beta \mathbf{c}(\ell_{535})$$
$$\longrightarrow \mathbf{c}(\ell(\lambda)) = \alpha \mathbf{c}(\ell_{435}) + \beta \mathbf{c}(\ell_{535}) - \gamma \mathbf{c}(\ell_{625})$$

Color matching demo



http://graphics.stanford.edu/courses/cs178/applets/colormatching.html

CIE color matching

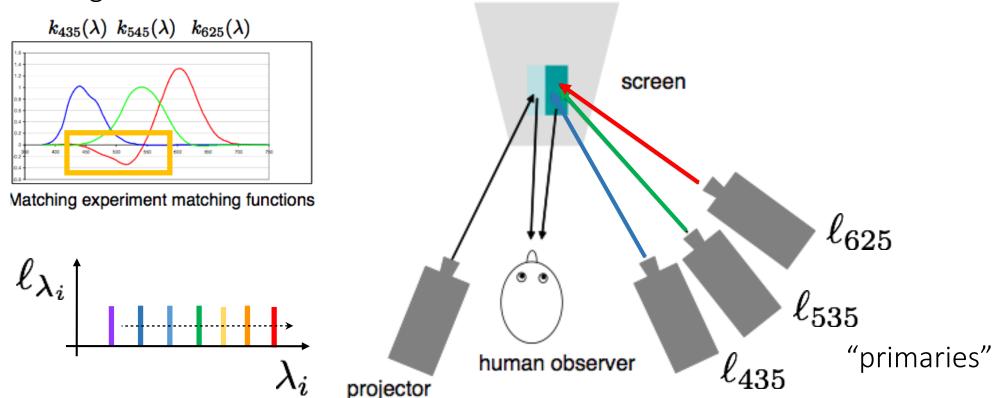


Repeat this matching experiments for pure test beams at wavelengths λ_i and keep track of the coefficients (negative or positive) required to reproduce each pure test beam.

$$\mathbf{c}(\lambda_i) = k_{435}(\lambda)\mathbf{c}(\ell_{435}) + k_{535}(\lambda)\mathbf{c}(\ell_{535}) + k_{625}(\lambda)\mathbf{c}(\ell_{625})$$

note the negative values

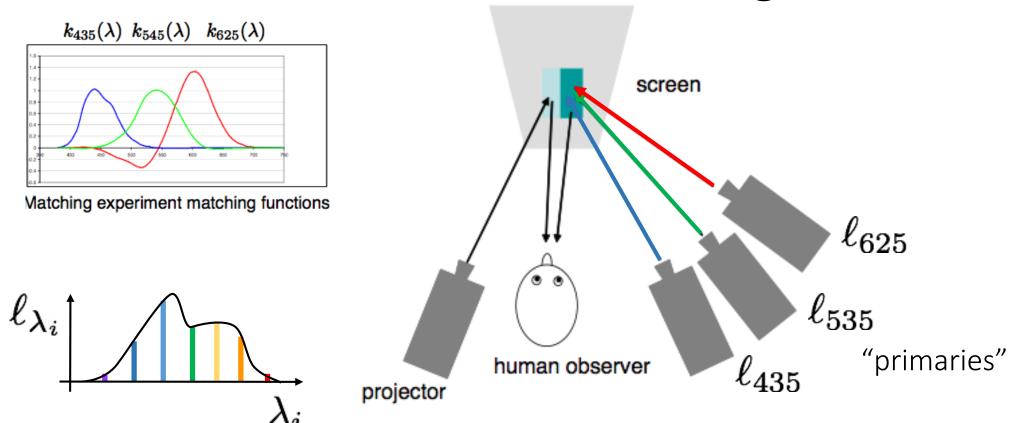
CIE color matching



Repeat this matching experiments for pure test beams at wavelengths λ_i and keep track of the coefficients (negative or positive) required to reproduce each pure test beam.

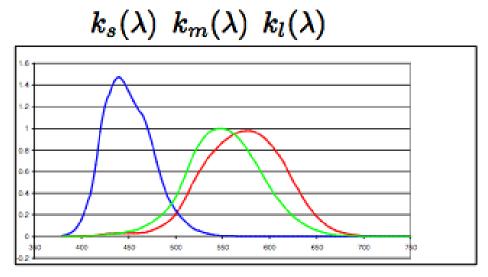
$$\mathbf{c}(\lambda_i) = k_{435}(\lambda)\mathbf{c}(\ell_{435}) + k_{535}(\lambda)\mathbf{c}(\ell_{535}) + k_{625}(\lambda)\mathbf{c}(\ell_{625})$$

CIE color matching



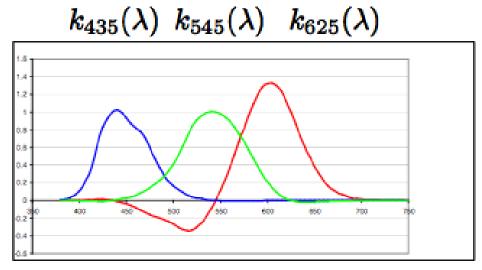
What about "mixed beams"?

Two views of retinal color



LMS senstivity functions

Analytic: Retinal color is produced by analyzing spectral power distributions using the color sensitivity functions.

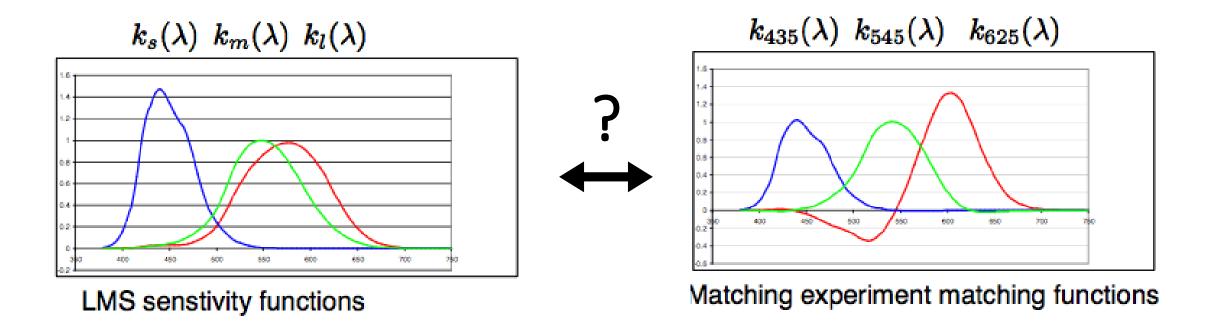


Matching experiment matching functions

<u>Synthetic:</u> Retinal color is produced by synthesizing color primaries using the color matching functions.

What is each view of retinal color best suited for?

Two views of retinal color

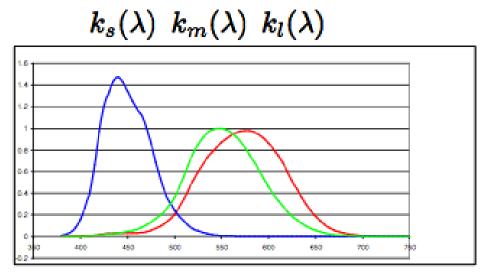


<u>Analytic:</u> Retinal color is produced by analyzing spectral power distributions using the color sensitivity functions.

<u>Synthetic:</u> Retinal color is produced by synthesizing color primaries using the color matching functions.

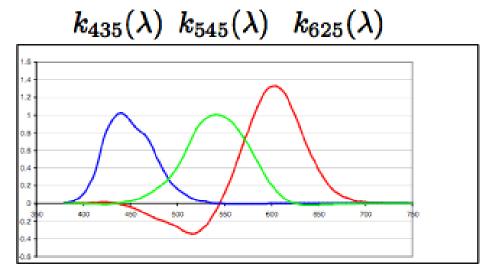
How do they relate to each other?

Two views of retinal color



LMS senstivity functions

Analytic: Retinal color is produced by analyzing spectral power distributions using the color sensitivity functions.



Matching experiment matching functions

<u>Synthetic:</u> Retinal color is produced by synthesizing color primaries using the color matching functions.

The two views are equivalent: Color matching functions are also color sensitivity functions. For each set of color sensitivity functions, there are corresponding color primaries.

1) Color matching experimental outcome:

$$\mathbf{c}(\lambda_i) = k_{435}(\lambda)\mathbf{c}(\ell_{435}) + k_{535}(\lambda)\mathbf{c}(\ell_{535}) + k_{625}(\lambda)\mathbf{c}(\ell_{625})$$

same in matrix form:

$$\begin{bmatrix} | \\ \mathbf{c}(\lambda_{\mathbf{i}}) \\ | \end{bmatrix} = \begin{bmatrix} | & | & | \\ \mathbf{c}(\ell_{\mathbf{435}}) & \mathbf{c}(\ell_{\mathbf{545}}) & \mathbf{c}(\ell_{\mathbf{625}}) \\ | & | \end{bmatrix} \begin{bmatrix} k_{435} \\ k_{535} \\ k_{625} \end{bmatrix}$$

how is this matrix formed?

1) Color matching experimental outcome:

$$\mathbf{c}(\lambda_i) = k_{435}(\lambda)\mathbf{c}(\ell_{435}) + k_{535}(\lambda)\mathbf{c}(\ell_{535}) + k_{625}(\lambda)\mathbf{c}(\ell_{625})$$

same in matrix form:

$$\begin{bmatrix} | \\ \mathbf{c}(\lambda_{\mathbf{i}}) \\ | \end{bmatrix} = \begin{bmatrix} | & | & | \\ \mathbf{c}(\ell_{\mathbf{435}}) & \mathbf{c}(\ell_{\mathbf{545}}) & \mathbf{c}(\ell_{\mathbf{625}}) \\ | & | \end{bmatrix} \begin{bmatrix} k_{435} \\ k_{535} \\ k_{625} \end{bmatrix}$$

2) Implication for arbitrary mixed beams:

$$\begin{bmatrix} \mathbf{c}(\ell(\lambda)) \\ \mathbf{c}(\ell(\lambda)) \end{bmatrix} = \begin{bmatrix} \mathbf{c}(\ell_{\mathbf{435}}) & \mathbf{c}(\ell_{\mathbf{545}}) & \mathbf{c}(\ell_{\mathbf{625}}) \\ \mathbf{c}(\ell_{\mathbf{435}}) & \mathbf{c}(\ell_{\mathbf{545}}) \end{bmatrix} \begin{bmatrix} \int k_{435}(\lambda)\ell(\lambda)d\lambda \\ \int k_{535}(\lambda)\ell(\lambda)d\lambda \\ \int k_{625}(\lambda)\ell(\lambda)d\lambda \end{bmatrix}$$



where do these terms come from?

1) Color matching experimental outcome:

$$\mathbf{c}(\lambda_i) = k_{435}(\lambda)\mathbf{c}(\ell_{435}) + k_{535}(\lambda)\mathbf{c}(\ell_{535}) + k_{625}(\lambda)\mathbf{c}(\ell_{625})$$

same in matrix form:

$$\begin{bmatrix} | \\ \mathbf{c}(\lambda_{\mathbf{i}}) \end{bmatrix} = \begin{bmatrix} | & | & | \\ \mathbf{c}(\ell_{\mathbf{435}}) & \mathbf{c}(\ell_{\mathbf{545}}) & \mathbf{c}(\ell_{\mathbf{625}}) \end{bmatrix} \begin{bmatrix} k_{435} \\ k_{535} \\ k_{625} \end{bmatrix}$$

2) Implication for arbitrary mixed beams:

$$\begin{bmatrix} \mathbf{c}(\ell(\lambda)) \\ \mathbf{c}(\ell(\lambda)) \end{bmatrix} = \begin{bmatrix} \mathbf{c}(\ell_{\mathbf{435}}) & \mathbf{c}(\ell_{\mathbf{545}}) & \mathbf{c}(\ell_{\mathbf{625}}) \\ \mathbf{c}(\ell_{\mathbf{435}}) & \mathbf{c}(\ell_{\mathbf{545}}) \end{bmatrix} \begin{bmatrix} \int k_{435}(\lambda)\ell(\lambda)d\lambda \\ \int k_{535}(\lambda)\ell(\lambda)d\lambda \\ \int k_{625}(\lambda)\ell(\lambda)d\lambda \end{bmatrix}$$



what is this similar to?

1) Color matching experimental outcome:

$$\mathbf{c}(\lambda_i) = k_{435}(\lambda)\mathbf{c}(\ell_{435}) + k_{535}(\lambda)\mathbf{c}(\ell_{535}) + k_{625}(\lambda)\mathbf{c}(\ell_{625})$$

same in matrix form:

$$\begin{bmatrix} | \\ \mathbf{c}(\lambda_{\mathbf{i}}) \\ | \end{bmatrix} = \begin{bmatrix} | & | & | \\ \mathbf{c}(\ell_{\mathbf{435}}) & \mathbf{c}(\ell_{\mathbf{545}}) & \mathbf{c}(\ell_{\mathbf{625}}) \\ | & | & | \end{bmatrix} \begin{bmatrix} k_{435} \\ k_{535} \\ k_{625} \end{bmatrix}$$

2) Implication for arbitrary mixed beams:

$$\begin{bmatrix} \mathbf{c}(\ell(\lambda)) \\ \mathbf{c}(\ell(\lambda)) \end{bmatrix} = \begin{bmatrix} \mathbf{c}(\ell_{\mathbf{435}}) & \mathbf{c}(\ell_{\mathbf{545}}) & \mathbf{c}(\ell_{\mathbf{625}}) \\ \mathbf{c}(\ell_{\mathbf{545}}) & \mathbf{c}(\ell_{\mathbf{625}}) \end{bmatrix} \begin{bmatrix} \int k_{435}(\lambda)\ell(\lambda)d\lambda \\ \int k_{535}(\lambda)\ell(\lambda)d\lambda \\ \int k_{625}(\lambda)\ell(\lambda)d\lambda \end{bmatrix}$$

representation of retinal color in LMS space

change of basis matrix

representation of retinal color in space of primaries

basis for retinal color ⇔ color matching functions ⇔ primary colors ⇔ color space

$$\begin{bmatrix} \mathbf{c}(\ell(\lambda)) \\ \mathbf{c}(\ell(\lambda)) \end{bmatrix} = \begin{bmatrix} \mathbf{c}(1 & \mathbf{c}_1 & \mathbf{c}_2 & \mathbf{c}_3 \\ \mathbf{c}_1 & \mathbf{c}_2 & \mathbf{c}_3 \\ \mathbf{c}(1 & \mathbf{c}_1 & \mathbf{c}_2) \end{bmatrix} \begin{bmatrix} \int k_1(\lambda)\ell(\lambda)d\lambda \\ \int k_2(\lambda)\ell(\lambda)d\lambda \\ \int k_3(\lambda)\ell(\lambda)d\lambda \end{bmatrix}$$
$$\begin{bmatrix} \mathbf{c}(\ell_{\mathbf{435}}) & \mathbf{c}(\ell_{\mathbf{545}}) \\ \mathbf{c}(\ell_{\mathbf{545}}) & \mathbf{c}(\ell_{\mathbf{625}}) \end{bmatrix} \mathbf{M}^{-1}$$
$$\begin{bmatrix} k_1(\lambda) \\ k_2(\lambda) \\ k_3(\lambda) \end{bmatrix} = \mathbf{M} \begin{bmatrix} k_{435}(\lambda) \\ k_{545}(\lambda) \\ k_{625}(\lambda) \end{bmatrix}$$

 $\mathbf{M}^{-1}\mathbf{M}$ can insert any invertible M

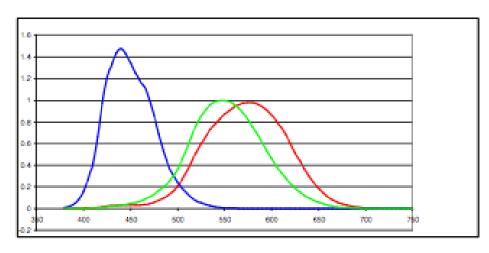
$$\begin{bmatrix} \mathbf{c}(\ell(\lambda)) \\ \mathbf{c}(\ell(\lambda)) \end{bmatrix} = \begin{bmatrix} \mathbf{c}(\ell_{\mathbf{435}}) & \mathbf{c}(\ell_{\mathbf{545}}) & \mathbf{c}(\ell_{\mathbf{625}}) \\ \mathbf{c}(\ell_{\mathbf{545}}) & \mathbf{c}(\ell_{\mathbf{625}}) \end{bmatrix} \begin{bmatrix} \int k_{435}(\lambda)\ell(\lambda)d\lambda \\ \int k_{535}(\lambda)\ell(\lambda)d\lambda \\ \int k_{625}(\lambda)\ell(\lambda)d\lambda \end{bmatrix}$$

representation of retinal color in LMS space

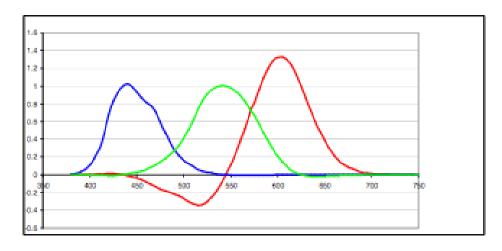
change of basis matrix

representation of retinal color in space of primaries

A few important color spaces



LMS color space



CIE RGB color space



not the "usual" RGB color space encountered in practice

Two views of retinal color

Analytic: Retinal color is three numbers formed by taking the dot product of a power spectral distribution with three color matching/sensitivity functions.

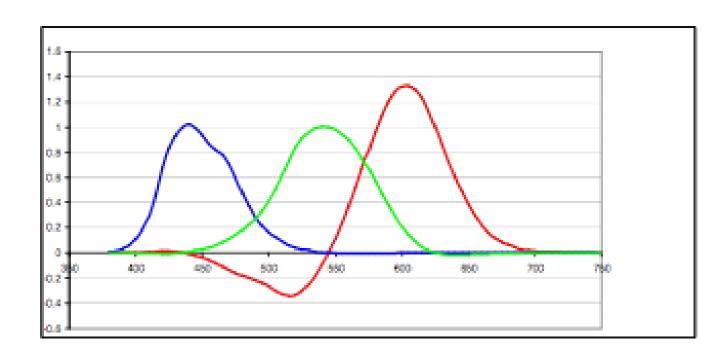
Synthetic: Retinal color is three numbers formed by assigning weights to three color primaries to match the perception of a power spectral distribution.

How would you make a color measurement device?

Do what the eye does:

- Select three spectral filters (i.e., three color matching functions.).
- Capture three measurements.

Can we use the CIE RGB color matching functions?



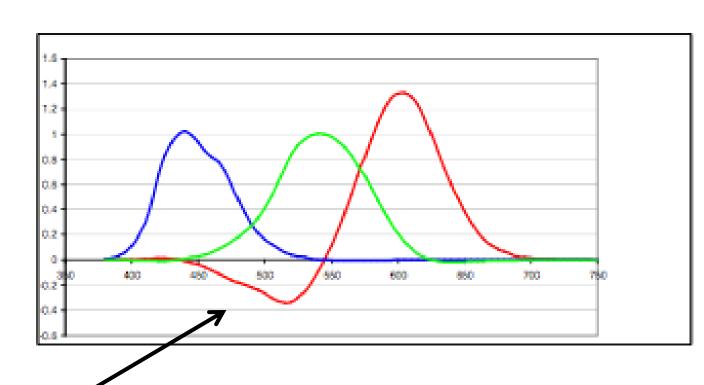
CIE RGB color space

Do what the eye does:

- Select three spectral filters (i.e., three color matching functions.).
- Capture three measurements.

Can we use the CIE RGB color matching functions?

Negative values are an issue (we can't "subtract" light at a sensor)

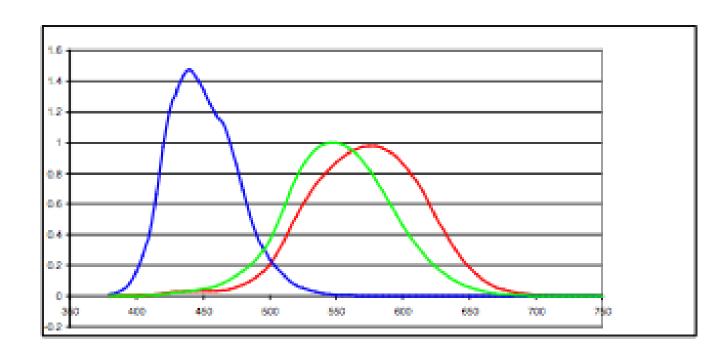


CIE RGB color space

Do what the eye does:

- Select three spectral filters (i.e., three color matching functions).
- Capture three measurements.

Can we use the LMS color matching functions?



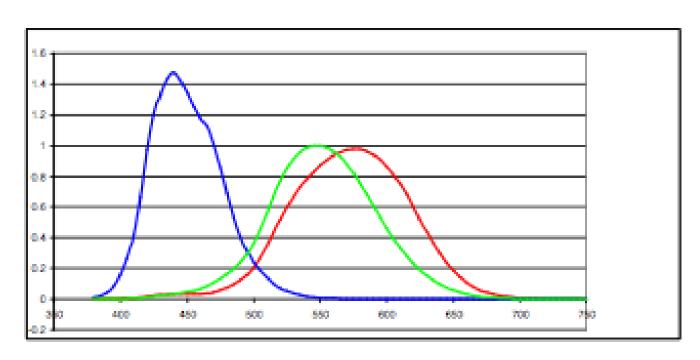
LMS color space

Do what the eye does:

- Select three spectral filters (i.e., three color matching functions).
- Capture three measurements.

Can we use the LMS color matching functions?

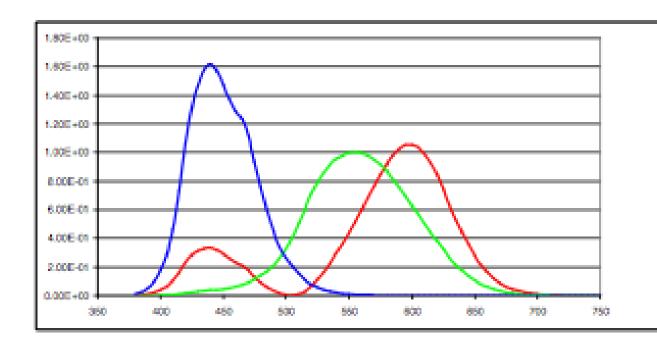
• They weren't known when CIE was doing their color matching experiments.



LMS color space

The CIE XYZ color space

- Derived from CIE RGB by adding enough blue and green to make the red positive.
- Probably the most important *reference* (i.e., device independent) color space.



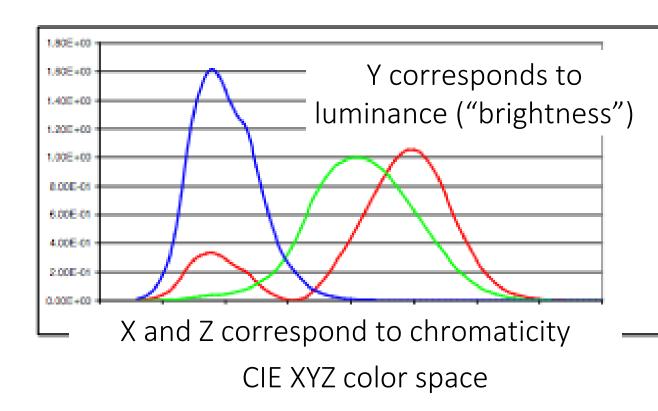
Remarkable and/or scary: 80+ years of CIE XYZ is all down to color matching experiments done with 12 "standard observers".

CIE XYZ color space

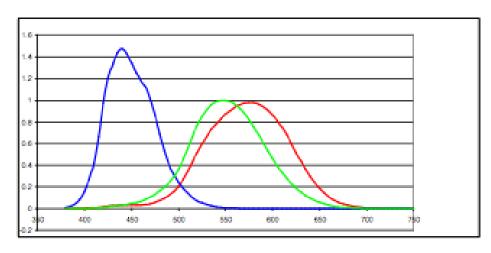
The CIE XYZ color space

- Derived from CIE RGB by adding enough blue and green to make the red positive.
- Probably the most important *reference* (i.e., device independent) color space.

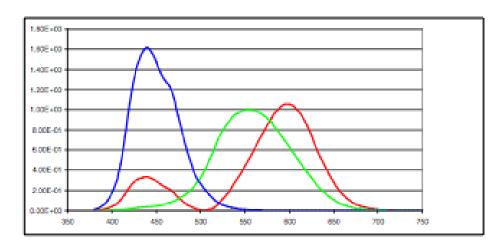
How would you convert a color image to grayscale?



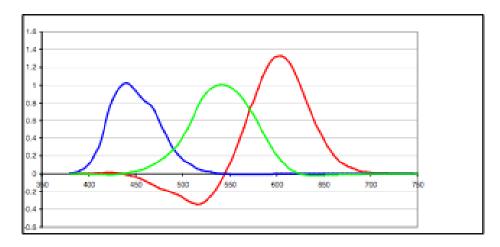
A few important color spaces



LMS color space



CIE XYZ color space



CIE RGB color space

Two views of retinal color

Analytic: Retinal color is three numbers formed by taking the dot product of a power spectral distribution with three color matching/sensitivity functions.

Synthetic: Retinal color is three numbers formed by assigning weights to three color primaries to match the perception of a power spectral distribution.

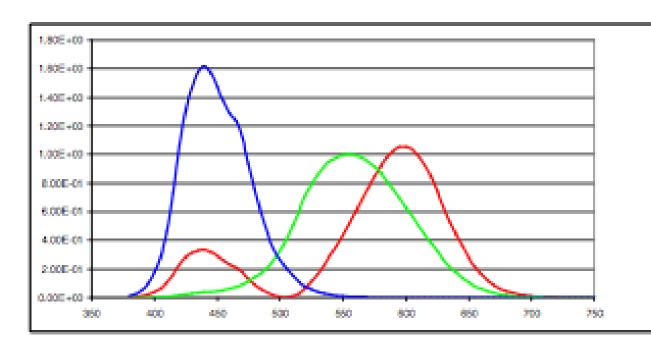
How would you make a color reproduction device?

How would you make a color reproduction device?

Do what color matching does:

- Select three color primaries.
- Represent all colors as mixtures of these three primaries.

Can we use the XYZ color primaries?



CIE XYZ color space

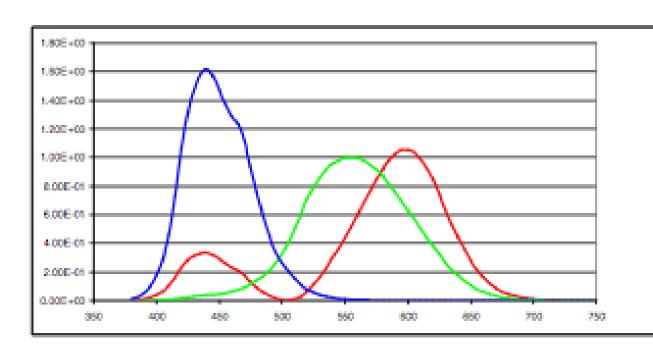
How would you make a color reproduction device?

Do what color matching does:

- Select three color primaries.
- Represent all colors as mixtures of these three primaries.

Can we use the XYZ color primaries?

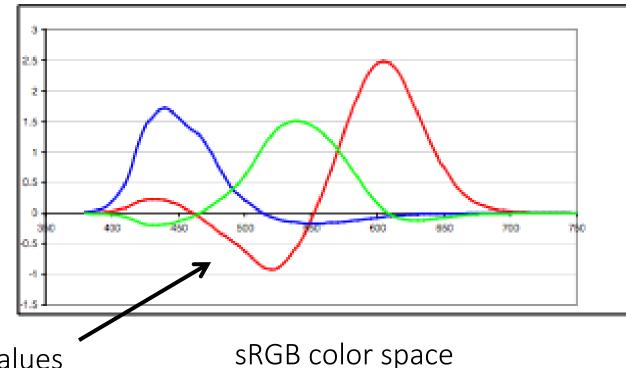
- No, because they are not "real" colors (they require an SPD with negative values).
- Same goes for LMS color primaries.



CIE XYZ color space

The Standard RGB (sRGB) color space

- Derived by Microsoft and HP in 1996, based on CRT displays used at the time.
- Similar but not equivalent to CIE RGB.



Note the negative values

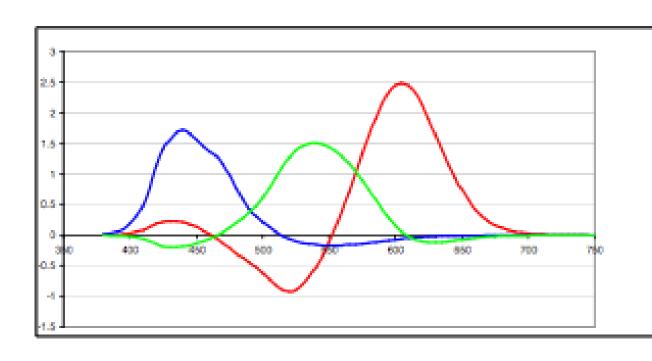
While it is called "standard", when you grab an "RGB" image, it is highly likely it is in a different RGB color space...

The Standard RGB (sRGB) color space

- Derived by Microsoft and HP in 1996, based on CRT displays used at the time.
- Similar but not equivalent to CIE RGB.

There are really two kinds of sRGB color spaces: linear and non-linear.

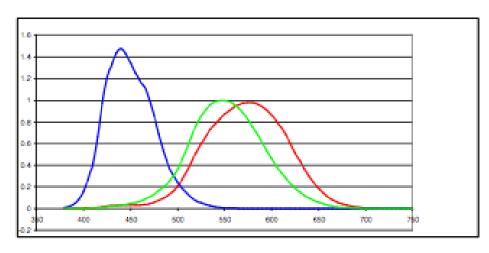
 Non-linear sRGB images have the following tone reproduction curve applied to them.



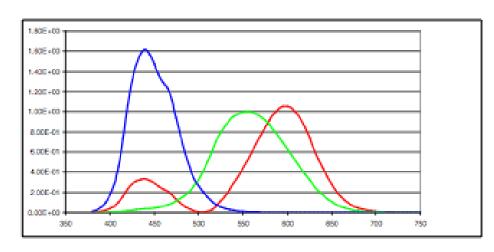
sRGB color space

$$C_{\text{non-linear}} = \begin{cases} 12.92 \cdot C_{\text{linear}}, & C_{\text{linear}} \leq 0.0031308 \\ (1 + 0.055) \cdot C_{\text{linear}}^{\frac{1}{2.4}} - 0.055, & C_{\text{linear}} \geq 0.0031308 \end{cases}$$

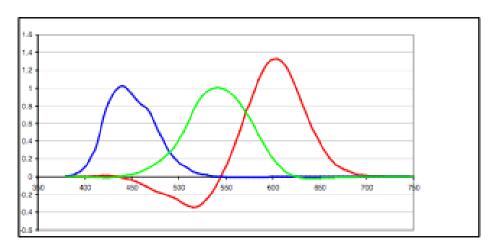
A few important color spaces



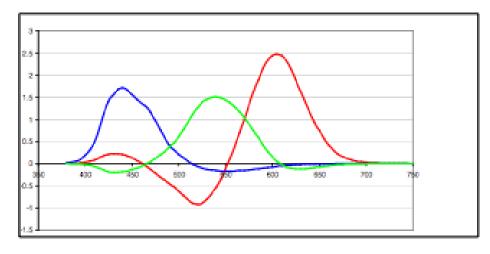
LMS color space



CIE XYZ color space

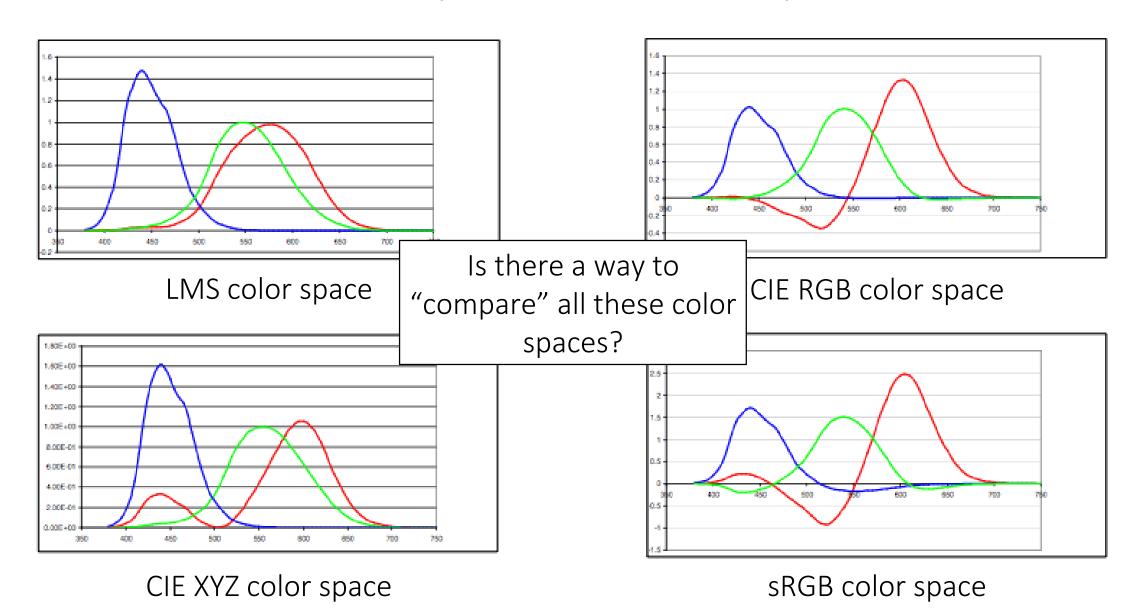


CIE RGB color space



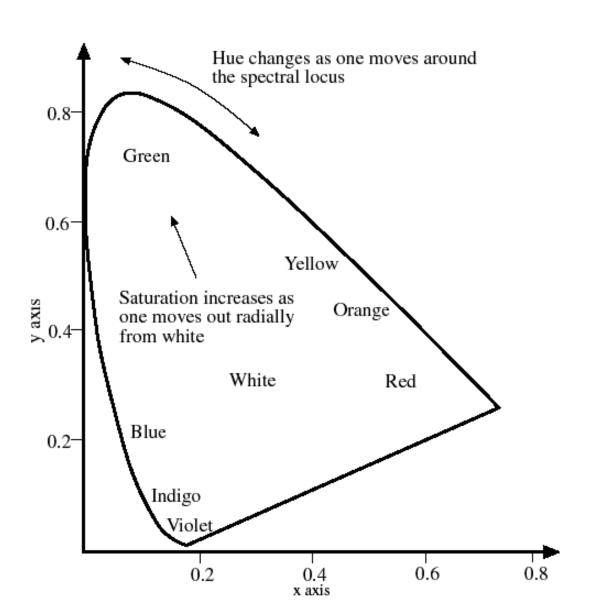
sRGB color space

A few important color spaces



Chromaticity

CIE xy (chromaticity)



$$x = \frac{X}{X + Y + Z}$$

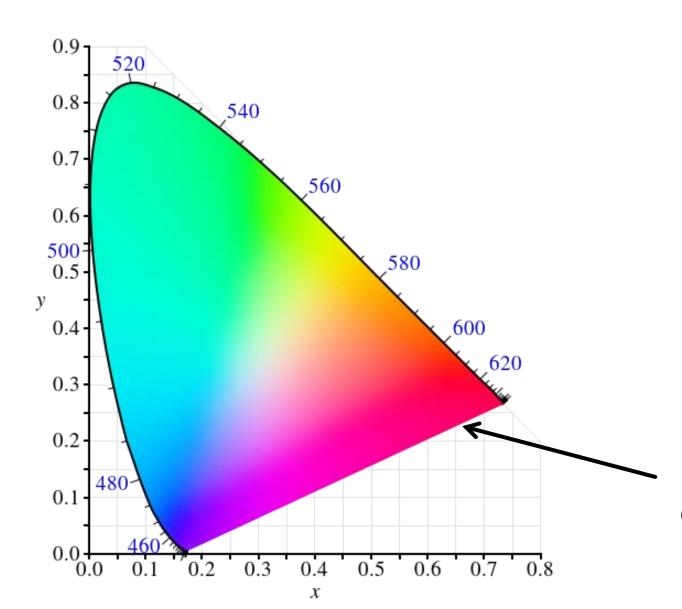
$$y = \frac{Y}{X + Y + Z}$$

$$(X,Y,Z)\longleftrightarrow (\underline{x,y},Y)$$
 chromaticity

luminance/brightness

Perspective projection of 3D retinal color space to two dimensions.

CIE xy (chromaticity)



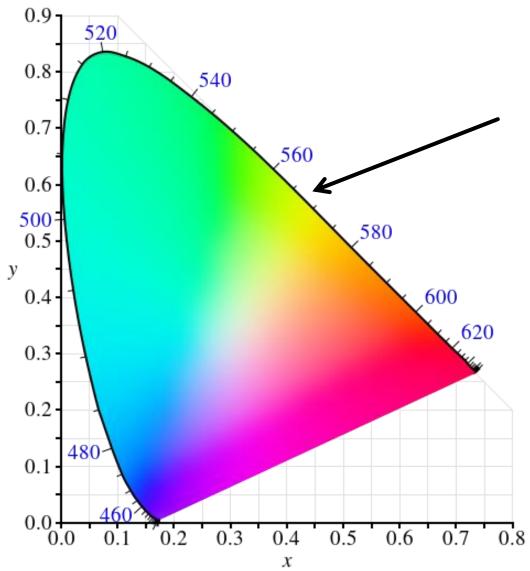
$$x = \frac{X}{X + Y + Z}$$

$$y = \frac{Y}{X + Y + Z}$$

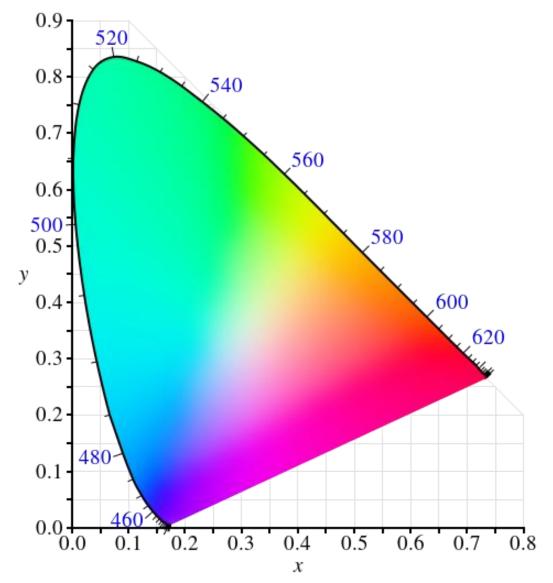
$$(X,Y,Z)\longleftrightarrow (x,y,Y)$$

Note: These colors can be extremely misleading depending on the file origin and the display you are using

CIE xy (chromaticity)

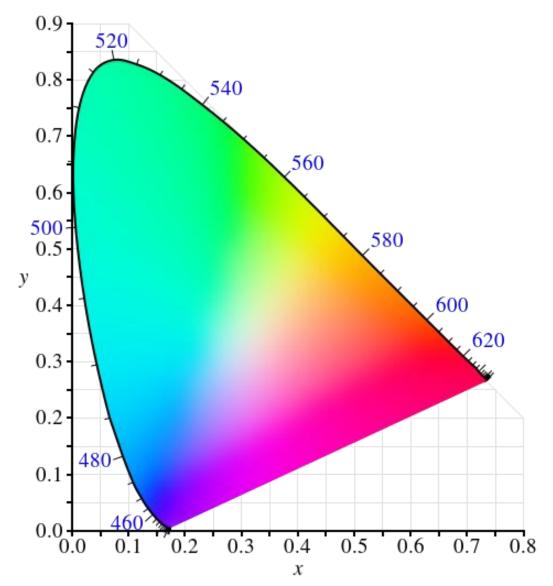


What does the boundary of the chromaticity diagram correspond to?



We can compare color spaces by looking at what parts of the chromaticity space they can reproduce with their primaries.

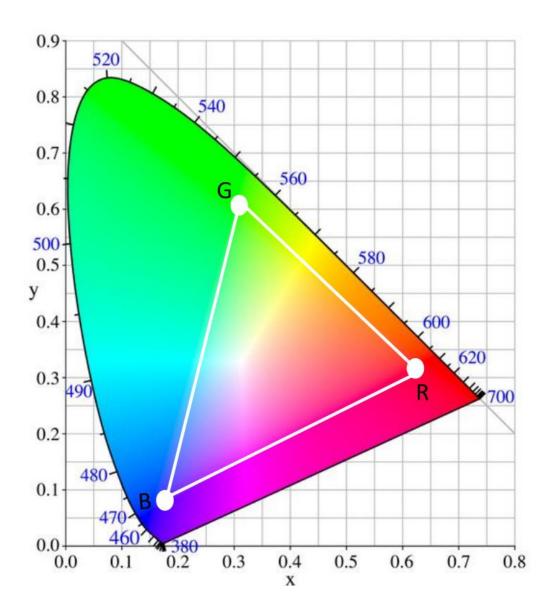
But why would a color space not be able to reproduce all of the chromaticity space?



We can compare color spaces by looking at what parts of the chromaticity space they can reproduce with their primaries.

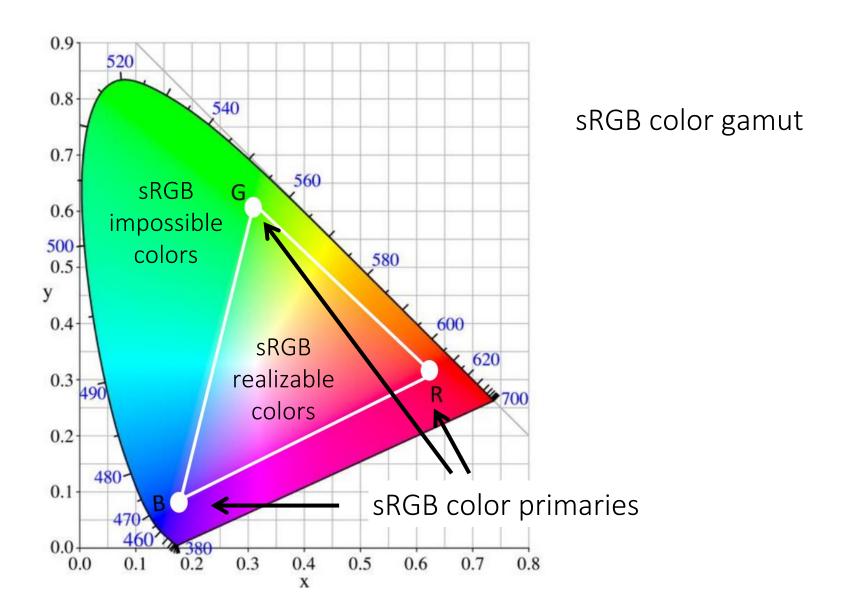
But why would a color space not be able to reproduce all of the chromaticity space?

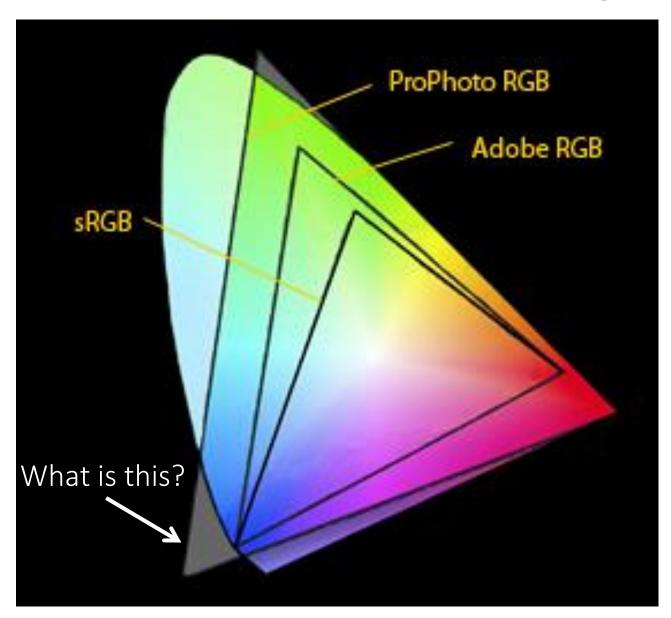
• Many colors require negative weights to be reproduced, which are not realizable.



sRGB color gamut:

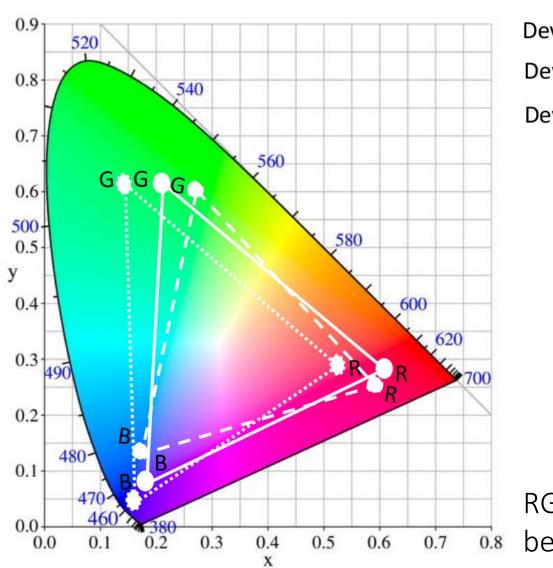
- What are the three triangle corners?
- What is the interior of the triangle?
- What is the exterior of the triangle?





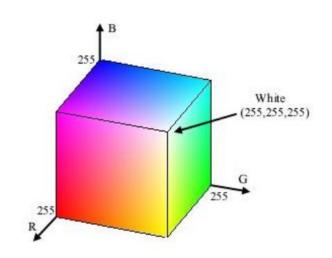
Gamuts of various common industrial RGB spaces

The problem with RGBs visualized in chromaticity space

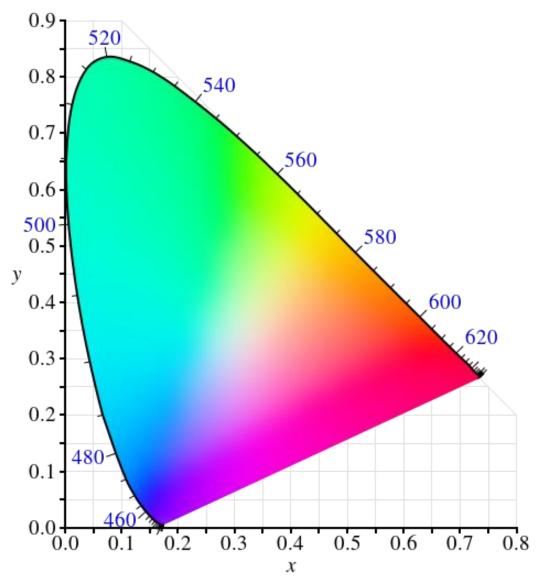


Device 2

Device 3 --

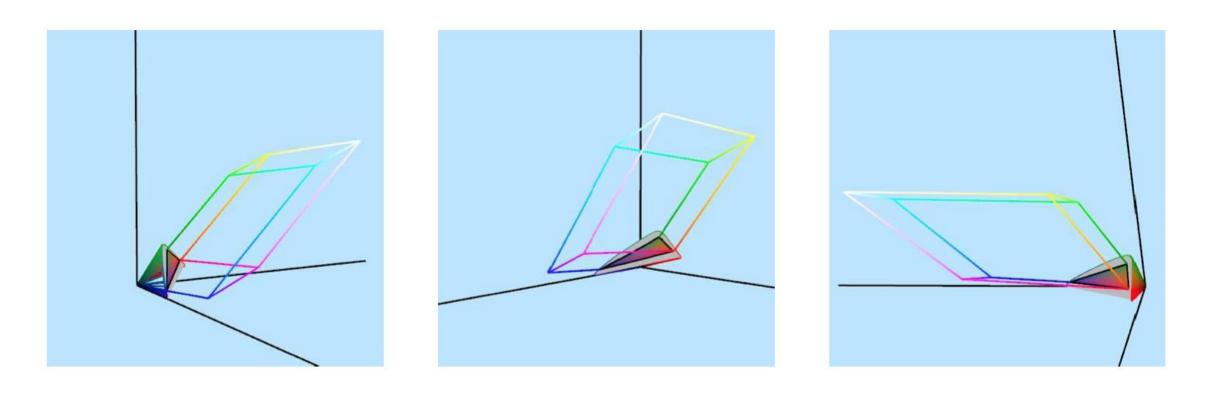


RGB values have no meaning if the primaries between devices are not the same!



- Can we create an RGB color space that reproduces the entire chromaticity diagram?
- What would be the pros and cons of such a color space?
- What devices would you use it for?

Chromaticity diagrams can be misleading



Different gamuts may compare very differently when seen in full 3D retinal color space.

Some take-home messages about color spaces

Analytic: Retinal color is three numbers formed by taking the dot product of a power spectral distribution with three color matching/sensitivity functions.

Synthetic: Retinal color is three numbers formed by assigning weights to three color primaries to match the perception of a power spectral distribution.

<u>Fundamental problem:</u> Analysis spectrum (camera, eyes) cannot be the same as synthesis one (display) - impossible to encode all possible colors without something becoming negative

- CIE XYZ only needs positive coordinates, but need primaries with negative light.
- RGB must use physical (non-negative) primaries, but needs negative coordinates for some colors.

<u>Problem with current practice:</u> Many different RGB color spaces used by different devices, without clarity of what exactly space a set of RGB color values are in.

• Huge problem for color reproduction from one device to another.

See for yourself



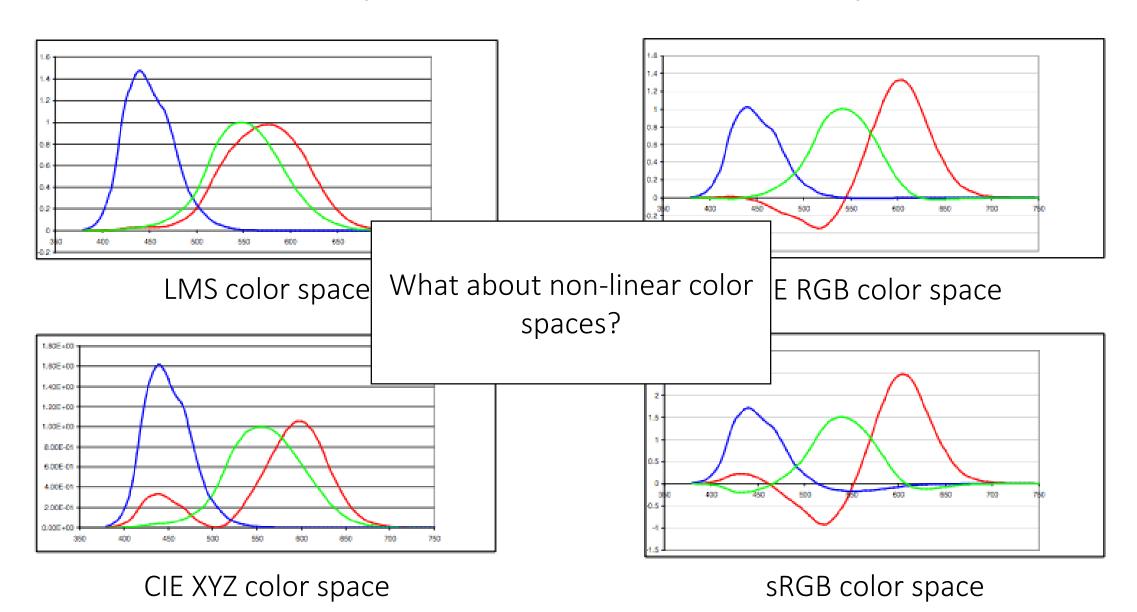




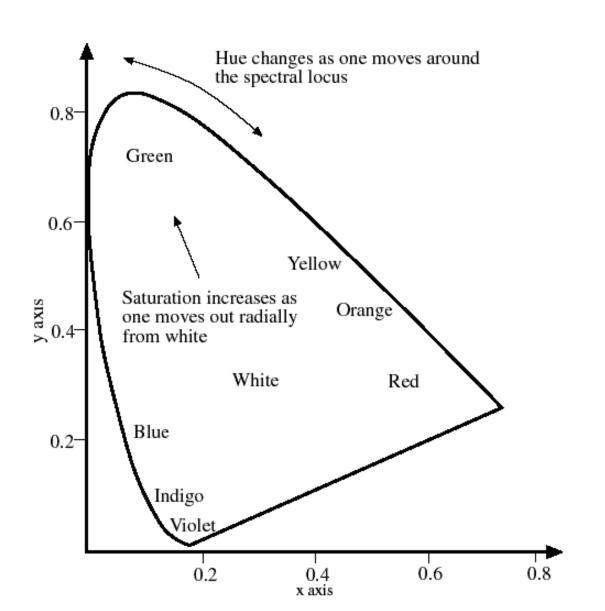
Images of the same scene captured using 3 different cameras with identical settings, supposedly in sRGB space.

Non-linear color spaces

A few important linear color spaces



CIE xy (chromaticity)



$$x = \frac{X}{X + Y + Z}$$

$$y = \frac{Y}{X + Y + Z}$$

$$(X,Y,Z)\longleftrightarrow (\underline{x,y},Y)$$
 chromaticity

luminance/brightness

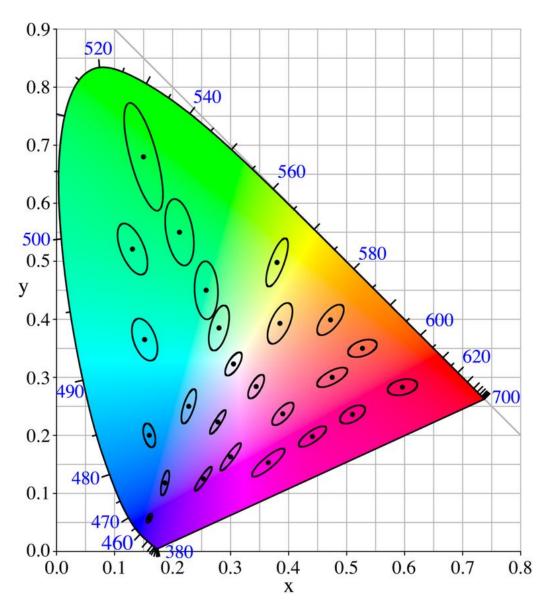
CIE xyY is a non-linear color space.

Uniform color spaces

Find map $F: \mathbb{R}^3 \to \mathbb{R}^3$ such that perceptual distance can be well approximated using Euclidean distance:

$$d(\vec{c}, \vec{c}') \approx ||F(\vec{c}) - F(\vec{c}')||_2$$

MacAdam ellipses

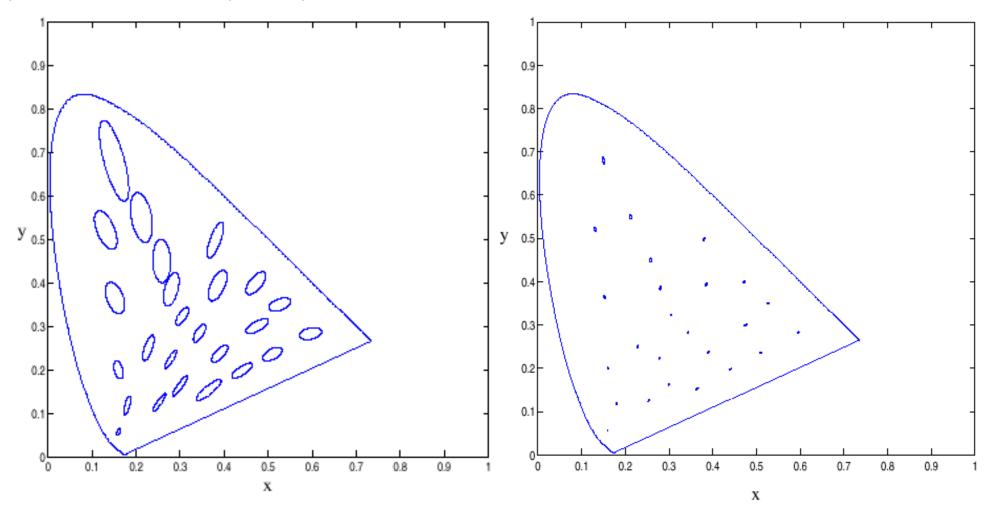


Areas in chromaticity space of imperceptible change:

- They are ellipses instead of circles.
- They change scale and direction in different parts of the chromaticity space.

MacAdam ellipses

Note: MacAdam ellipses are almost always shown at 10x scale for visualization. In reality, the areas of imperceptible difference are much smaller.



The Lab (aka L*ab, aka L*a*b*) color space

The L* component of *lightness* is defined as

$$L^* = 116f\left(\frac{Y}{Y_n}\right),\tag{2.105}$$

where Y_n is the luminance value for nominal white (Fairchild 2005) and

$$f(t) = \begin{cases} t^{1/3} & t > \delta^3 \\ t/(3\delta^2) + 2\delta/3 & \text{else,} \end{cases}$$
 (2.106)

is a finite-slope approximation to the cube root with $\delta = 6/29$. The resulting 0...100 scale roughly measures equal amounts of lightness perceptibility.

In a similar fashion, the a* and b* components are defined as

$$a^* = 500 \left[f\left(\frac{X}{X_n}\right) - f\left(\frac{Y}{Y_n}\right) \right] \text{ and } b^* = 200 \left[f\left(\frac{Y}{Y_n}\right) - f\left(\frac{Z}{Z_n}\right) \right],$$
 (2.107)

where again, (X_n, Y_n, Z_n) is the measured white point. Figure 2.32i–k show the L*a*b* representation for a sample color image.

The Lab (aka L*ab, aka L*a*b*) color space

The L* component of *lightness* is defined as

$$L^* = 116f\left(\frac{Y}{Y_n}\right),\tag{2.105}$$

where Y_n is the luminance value for nominal white (Fairchild 2005) and

What is this?
$$f(t) = \begin{cases} t^{1/3} & t > \delta^3 \\ t/(3\delta^2) + 2\delta/3 & \text{else,} \end{cases}$$
 (2.106)

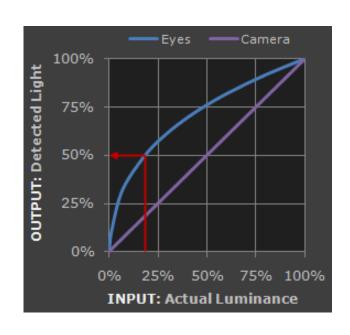
is a finite-slope approximation to the cube root with $\delta = 6/29$. The resulting 0...100 scale roughly measures equal amounts of lightness perceptibility.

In a similar fashion, the a* and b* components are defined as

$$a^* = 500 \left[f\left(\frac{X}{X_n}\right) - f\left(\frac{Y}{Y_n}\right) \right] \text{ and } b^* = 200 \left[f\left(\frac{Y}{Y_n}\right) - f\left(\frac{Z}{Z_n}\right) \right],$$
 (2.107)

where again, (X_n, Y_n, Z_n) is the measured white point. Figure 2.32i–k show the L*a*b* representation for a sample color image.

Perceived vs measured brightness by human eye

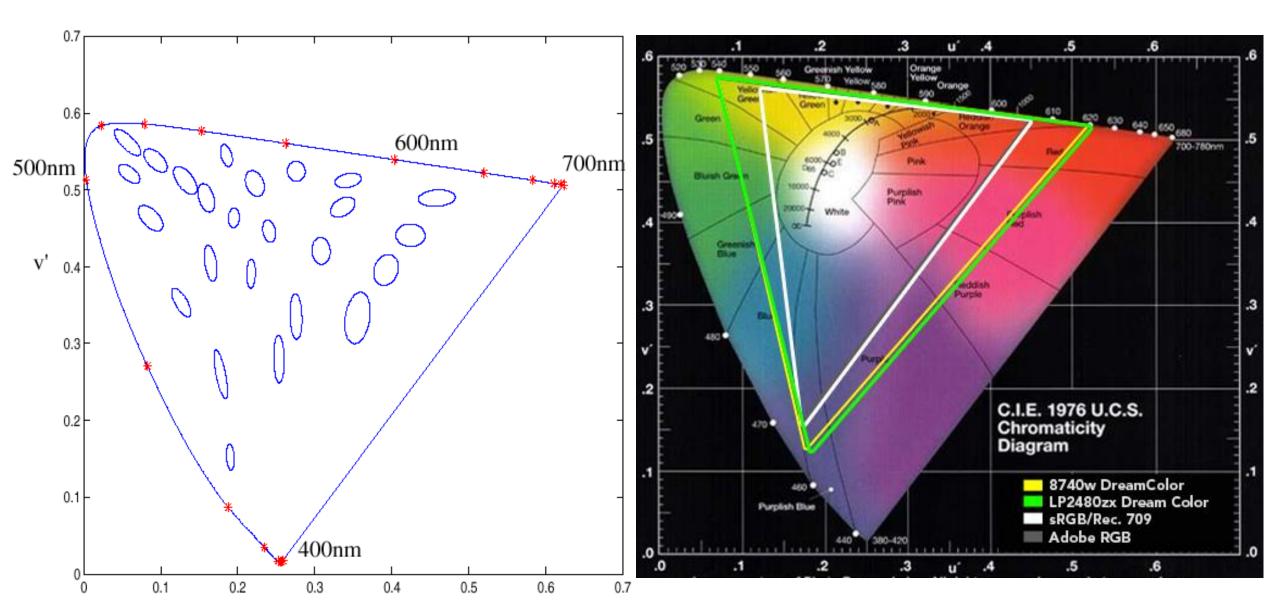


Human-eye response (measured brightness) is linear.

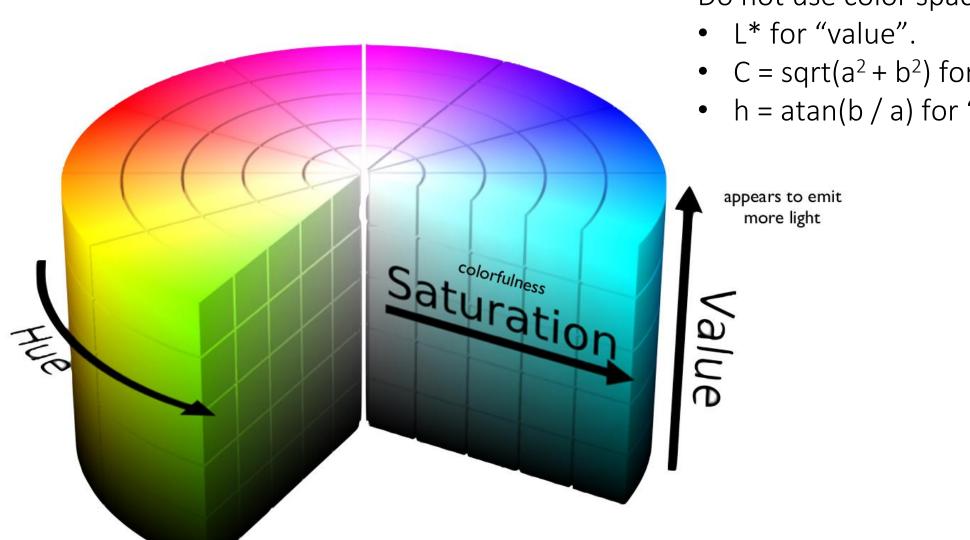
However, human-eye *perception* (perceived brightness) is *non-linear*:

- More sensitive to dark tones.
- Approximately a Gamma function.

The Lab (aka L*ab, aka L*a*b*) color space



Hue, saturation, and value



Do not use color space HSV! Use <u>LCh</u>:

• $C = sqrt(a^2 + b^2)$ for "saturation" (chroma).

• h = atan(b/a) for "hue".

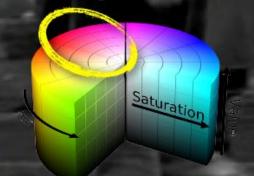


How could you make an image like this from a color image?

Zero saturation

Higher saturation

Control saturation with red-pass filter

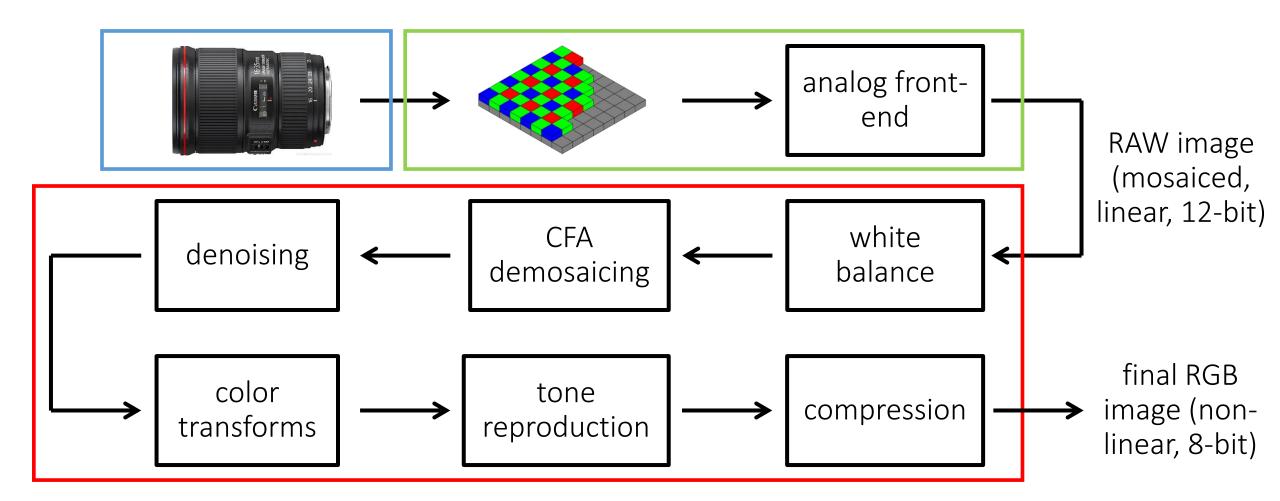


Easier to do color processing in HSV

Some thoughts about color reproduction

The image processing pipeline

The sequence of image processing operations applied by the camera's <u>image signal</u> <u>processor</u> (ISP) to convert a RAW image into a "conventional" image.



Color reproduction notes

To properly reproduce the color of an image file, you need to?

Color reproduction notes

To properly reproduce the color of an image file, you need to convert it from the color space it was stored in, to a reference color space, and then to the color space of your display.

On the camera side:

- If the file is RAW, it *often* has EXIF tags with information about the RGB color space corresponding to the camera's color sensitivity functions.
- If the file is not RAW, you may be lucky and still find accurate information in the EXIF tags about what color space the image was converted in during processing.
- If there is no such information and you own the camera that shot the image, then you can do color calibration for the camera.
- If all of the above fails, assume sRGB.

On the display side:

- If you own a high-end display, it likely has accurate color profiles provided by the manufacturer.
- If not, you can use a spectrometer to do color profiling (not color calibration).
- Make sure your viewer does not automatically do color transformations.

Be careful to account for any gamma correction!

Amazing resource for color management and photography: https://ninedegreesbelow.com/

How do you convert an image to grayscale?

How do you convert an image to grayscale?

First, you need to answer two questions:

- 1) Is your image linear or non-linear?
- If the image is linear (RAW, HDR, or otherwise radiometrically calibrated), skip this step.
- If the image is nonlinear (PNG, JPEG, etc.), you must undo the tone reproduction curve.
 - i. If you can afford to do radiometric calibration, do that.
 - ii. If your image has EXIF tags, check there about the tone reproduction curve.
 - iii. If your image is tagged as non-linear sRGB, use the inverse of the sRGB tone reproduction curve.
 - iv. If none of the above, assume sRGB and do as in (iii).

2) What is the color space of your image?

- If it came from an original RAW file, read the color transform matrix from there (e.g., dcraw).
- If not, you need to figure out the color space.
 - i. If you can afford to do color calibration, use that.
 - ii. If your image has EXIF tags, check there about the color space.
 - iii. If your image is tagged as non-linear sRGB, use the color transform matrix for linear sRGB.
 - iv. If none of the above, assume sRGB and do (iii).

With this information in hand:

- Transform your image into the XYZ color space.
- Extract the Y channel.
- If you want brightness instead of luminance, apply the Lab brightness non-linearity.

References

Basic reading:

- Szeliski textbook, Section 2.3.2, 3.1.2
- Michael Brown, "Understanding the In-Camera Image Processing Pipeline for Computer Vision," CVPR 2016, very detailed discussion of issues relating to color photography and management, slides available at: http://www.comp.nus.edu.sg/~brown/CVPR2016 Brown.html
- Gortler, "Foundations of 3D Computer Graphics," MIT Press 2012.

 Chapter 19 of this book has a great coverage of color spaces and the theory we discussed in class, it is available in PDF form from the CMU library.

Additional reading:

- Reinhard et al., "Color Imaging: Fundamentals and Applications," A.K Peters/CRC Press 2008.
- Koenderink, "Color Imaging: Fundamentals and Applications," MIT Press 2010.
- Fairchild, "Color Appearance Models," Wiley 2013. all of the above books are great references on color photography, reproduction, and management
- Nine Degrees Below, https://ninedegreesbelow.com/

 amazing resource for color photography, reproduction, and management