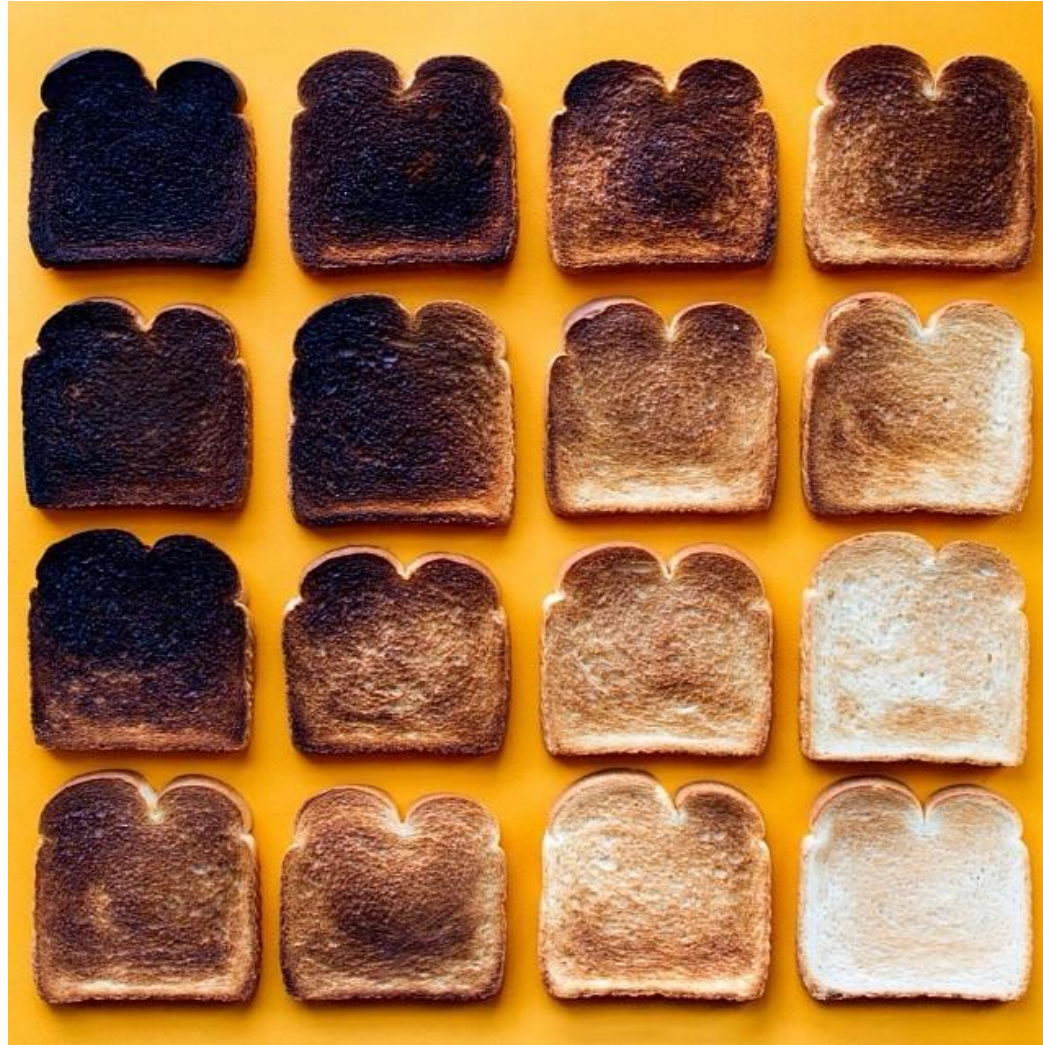


High dynamic range imaging and tonemapping



15-463, 15-663, 15-862
Computational Photography
Fall 2018, Lecture 5

Course announcements

- Homework 1 is out.
 - Due September 14th.
 - Canvas submission website is now open.
 - Make sure to sign up for a camera if you need one.
 - Drop by Yannis' office to pick up cameras any time.
- Those of you who signed up for cameras in pairs:
 - You can each pick up your own individual camera, no need to share.
- Any remaining waitlisting issues?

Overview of today's lecture

- Leftover from lecture 4: Ray transfer matrix analysis.
- Leftover from lecture 4: Other optical elements.
- Light metering.
- Our devices do not match the world.
- High dynamic range imaging.
- Tonemapping.
- Some notes about HDR and tonemapping.

Slide credits

Many of these slides were inspired or adapted from:

- James Hays (Georgia Tech).
- Fredo Durand (MIT).
- Gordon Wetzstein (Stanford).

Light metering

Camera modes

Aperture priority (“A”): you set aperture, camera sets everything else.

- Pros: Direct depth of field control.
- Cons: Can require impossible shutter speed (e.g. with f/1.4 for a bright scene).

Shutter speed priority (“S”): you set shutter speed, camera sets everything else.

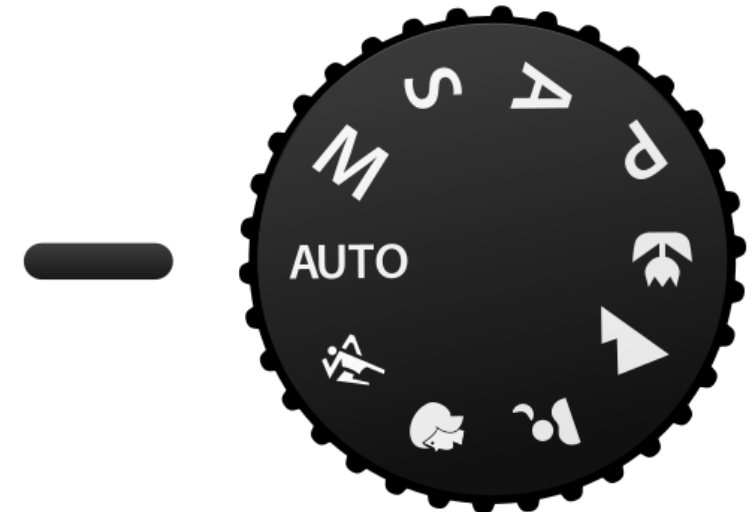
- Pros: Direct motion blur control.
- Cons: Can require impossible aperture (e.g. when requesting a 1/1000 speed for a dark scene)

Automatic (“AUTO”): camera sets everything.

- Pros: Very fast, requires no experience.
- Cons: No control.

Manual (“M”): you set everything.

- Pros: Full control.
- Cons: Very slow, requires a lot of experience.



generic camera mode dial

Camera modes

Aperture priority (“A”): you set aperture, camera sets everything else.

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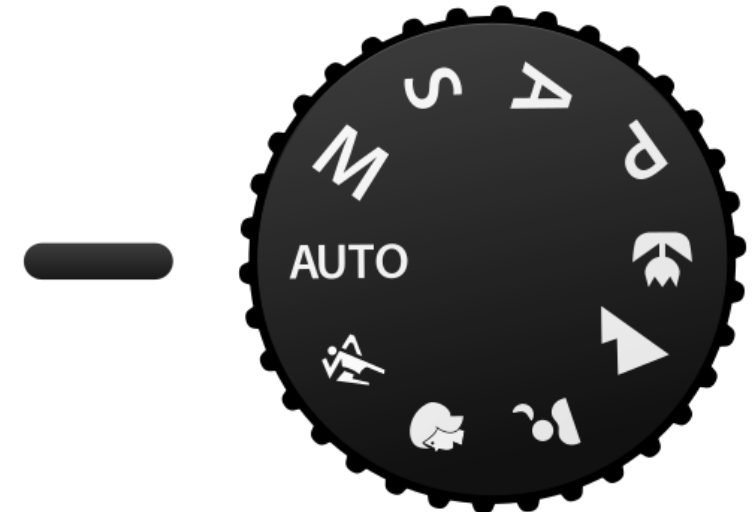
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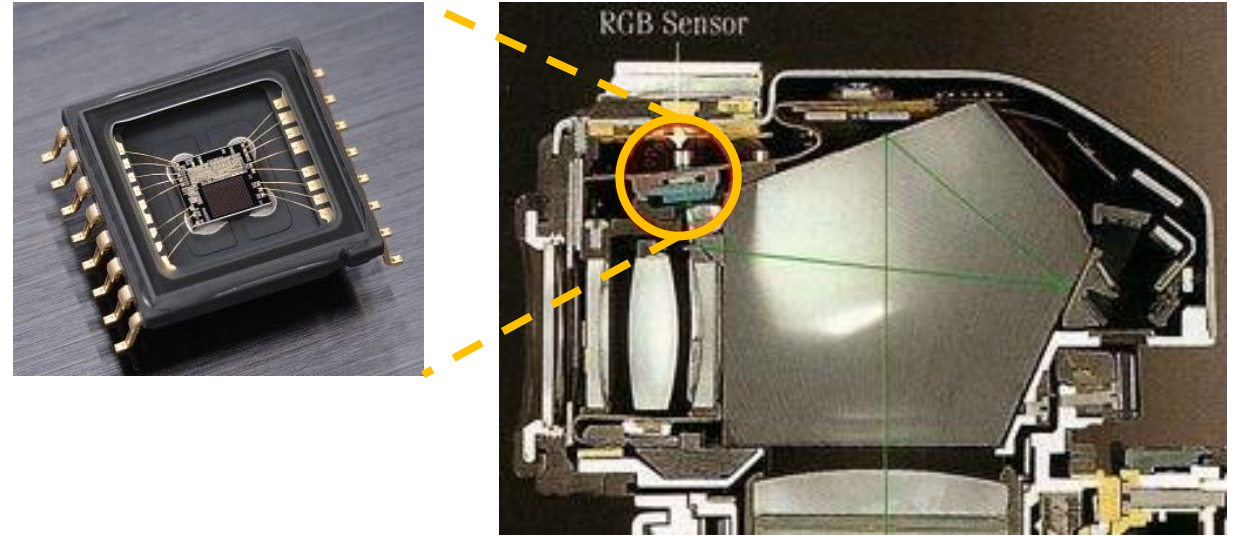
- Pros: Full control.
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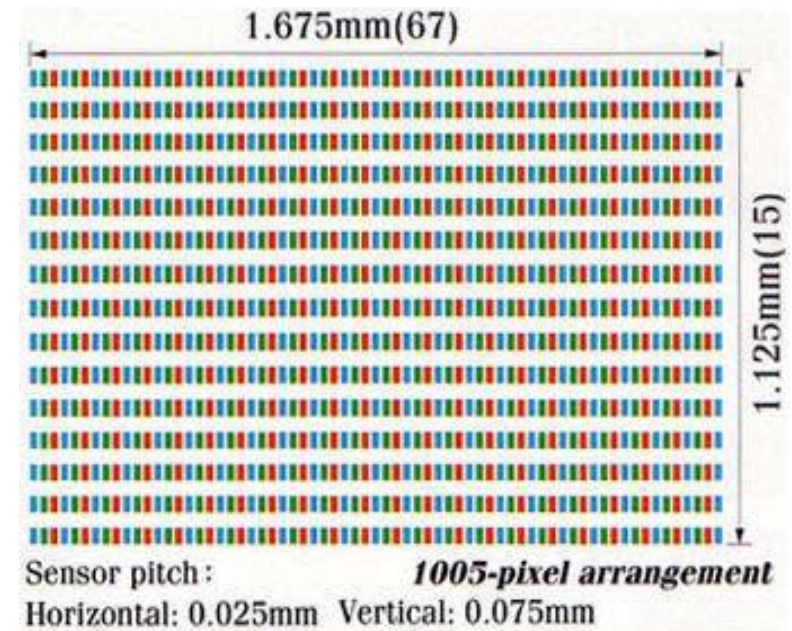
generic camera mode dial

Light metering in modern cameras

- SLR cameras use a separate low-resolution sensor that is placed at the focusing screen.

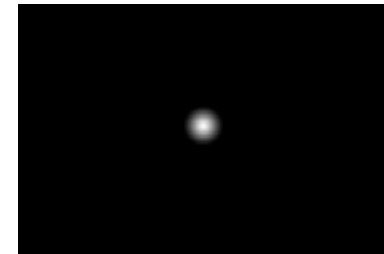
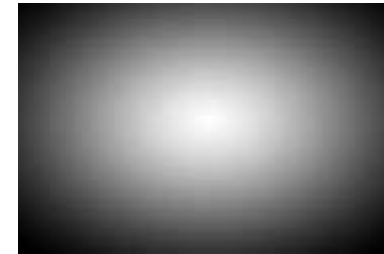


- Mirrorless cameras use measurements directly from the main sensor.



Light metering in modern cameras

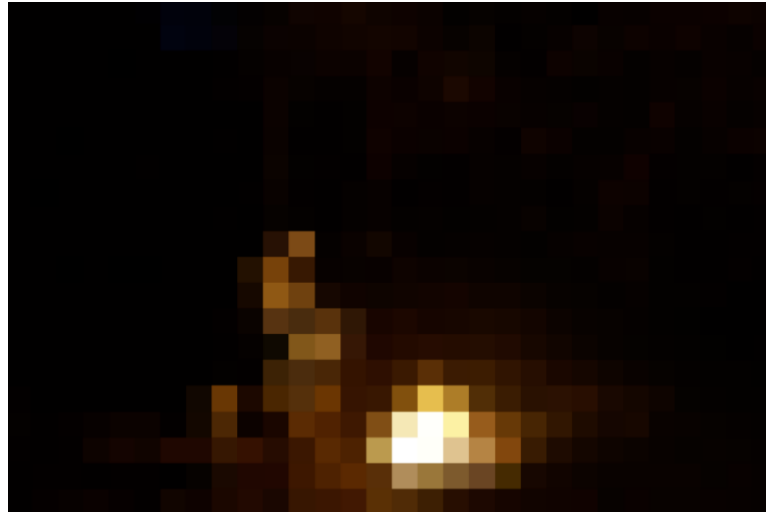
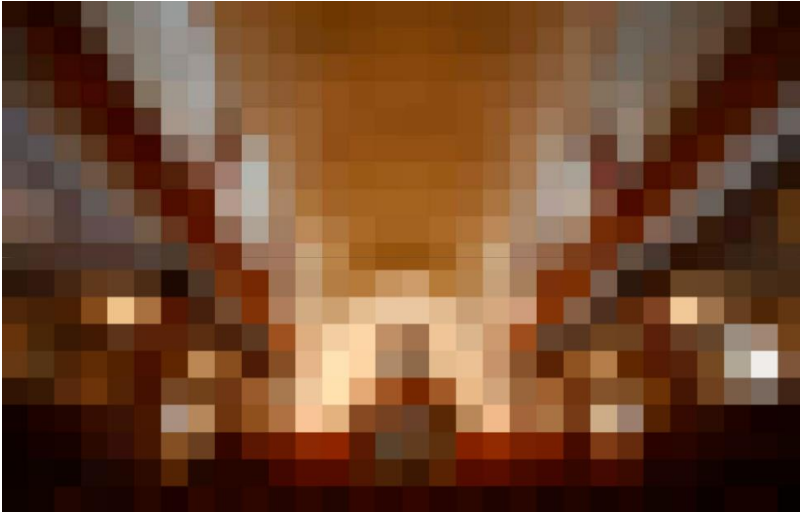
- Measurements are averaged to produce a single intensity estimate, which is assumed to correspond to a scene of 18% reflectance (the “key”).
- Exposure is set so that this average is exposed at the middle of the sensor’s dynamic range.
- Averaging can be done in many ways:
 1. Center-weighted.
 2. Spot.
 3. Scene-specific preset (portrait, landscape, horizon).
 4. “Intelligently” using proprietary algorithm.



Metering challenges: low resolution

Low-resolution can make it difficult to correctly meter the scene and set exposure.

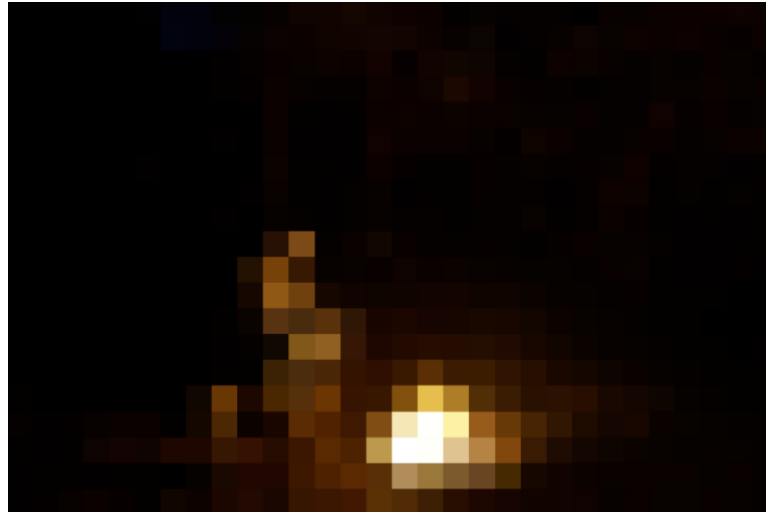
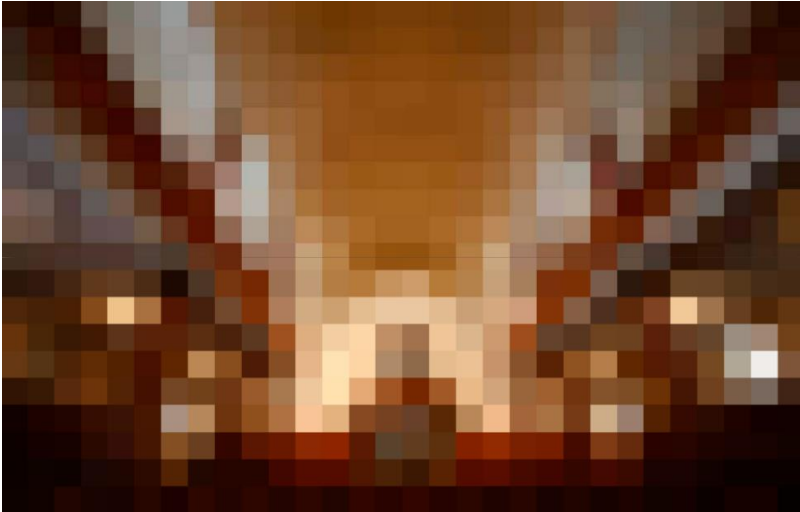
- In which of these scenes is it OK to let the brightest pixels be overexposed?



Metering challenges: low resolution

Low-resolution can make it difficult to correctly meter the scene and set exposure.

- In which of these scenes is it OK to let the brightest pixels be overexposed?



Our devices do not match the world

The world has a high dynamic range



1



1500

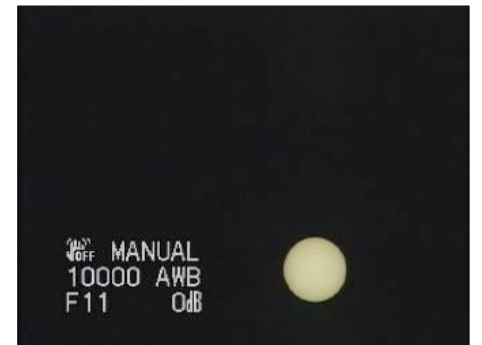


25,000

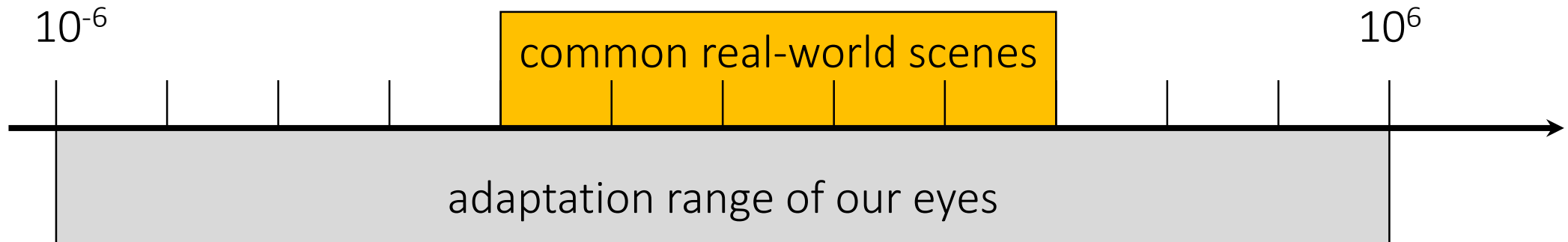


400,000

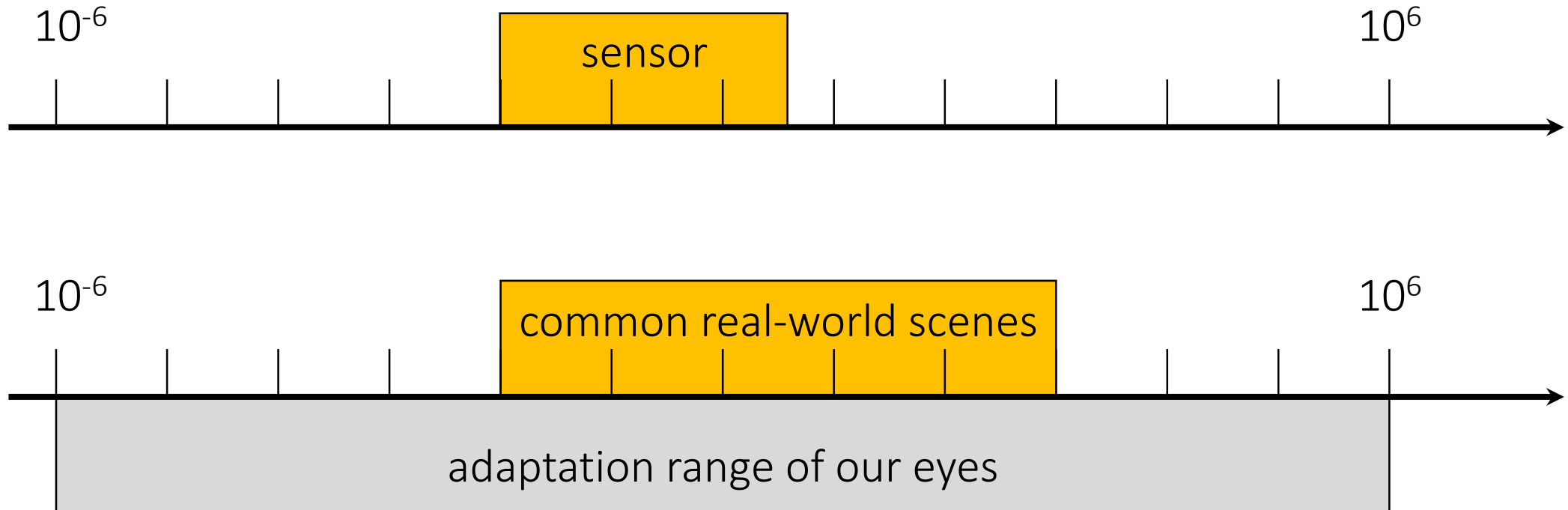
2,000,000,000



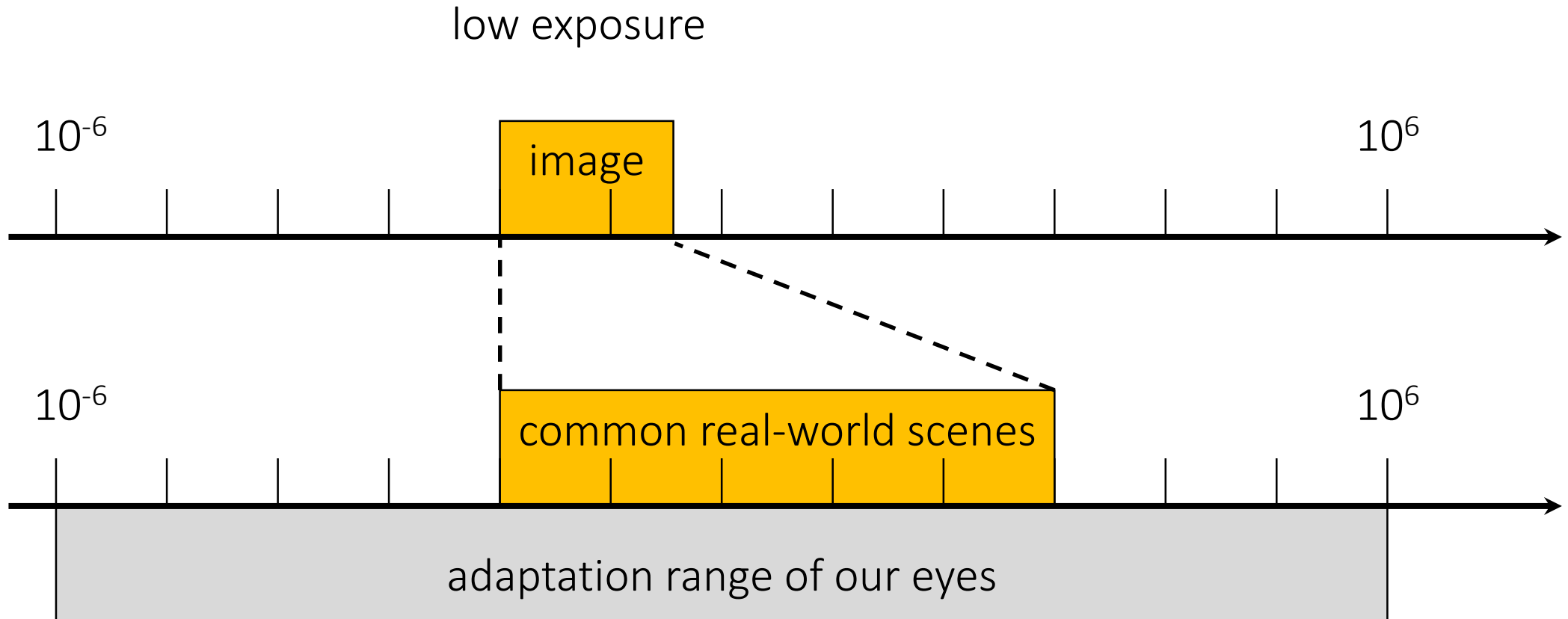
The world has a high dynamic range



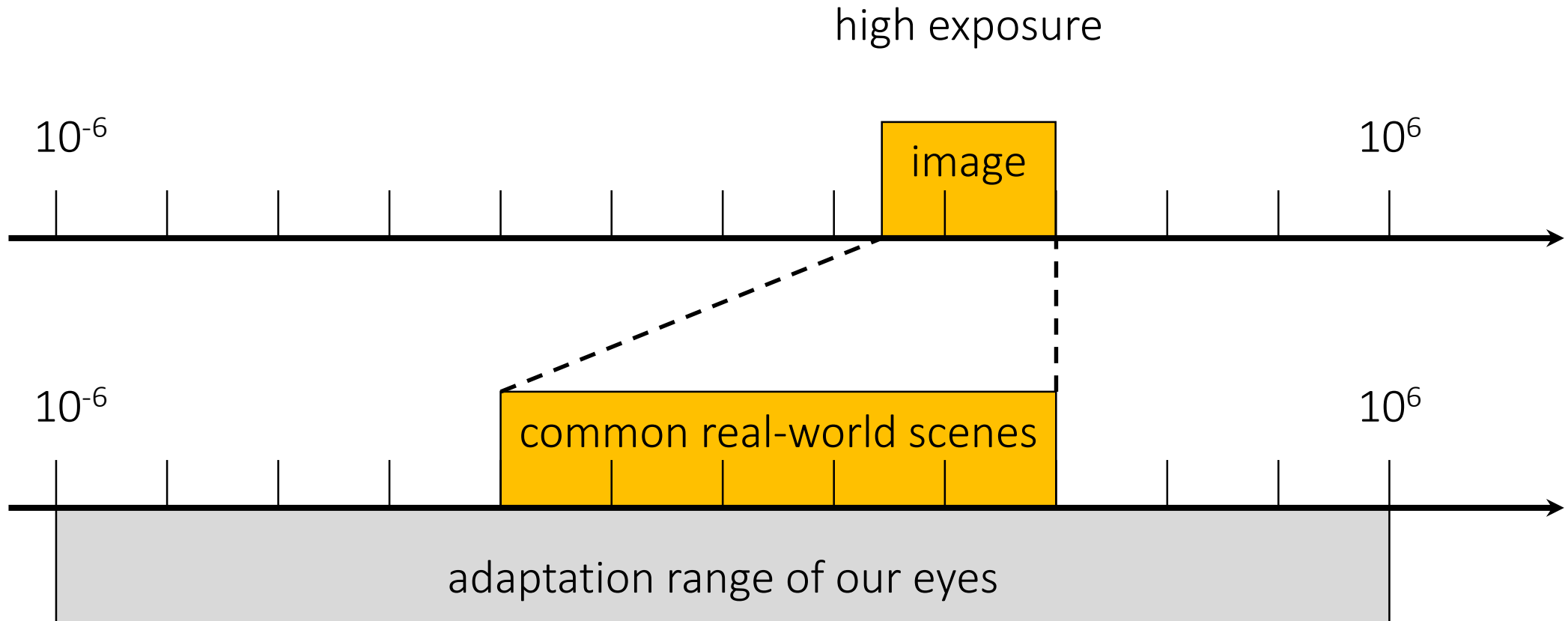
(Digital) sensors also have a low dynamic range



(Digital) images have an even lower dynamic range

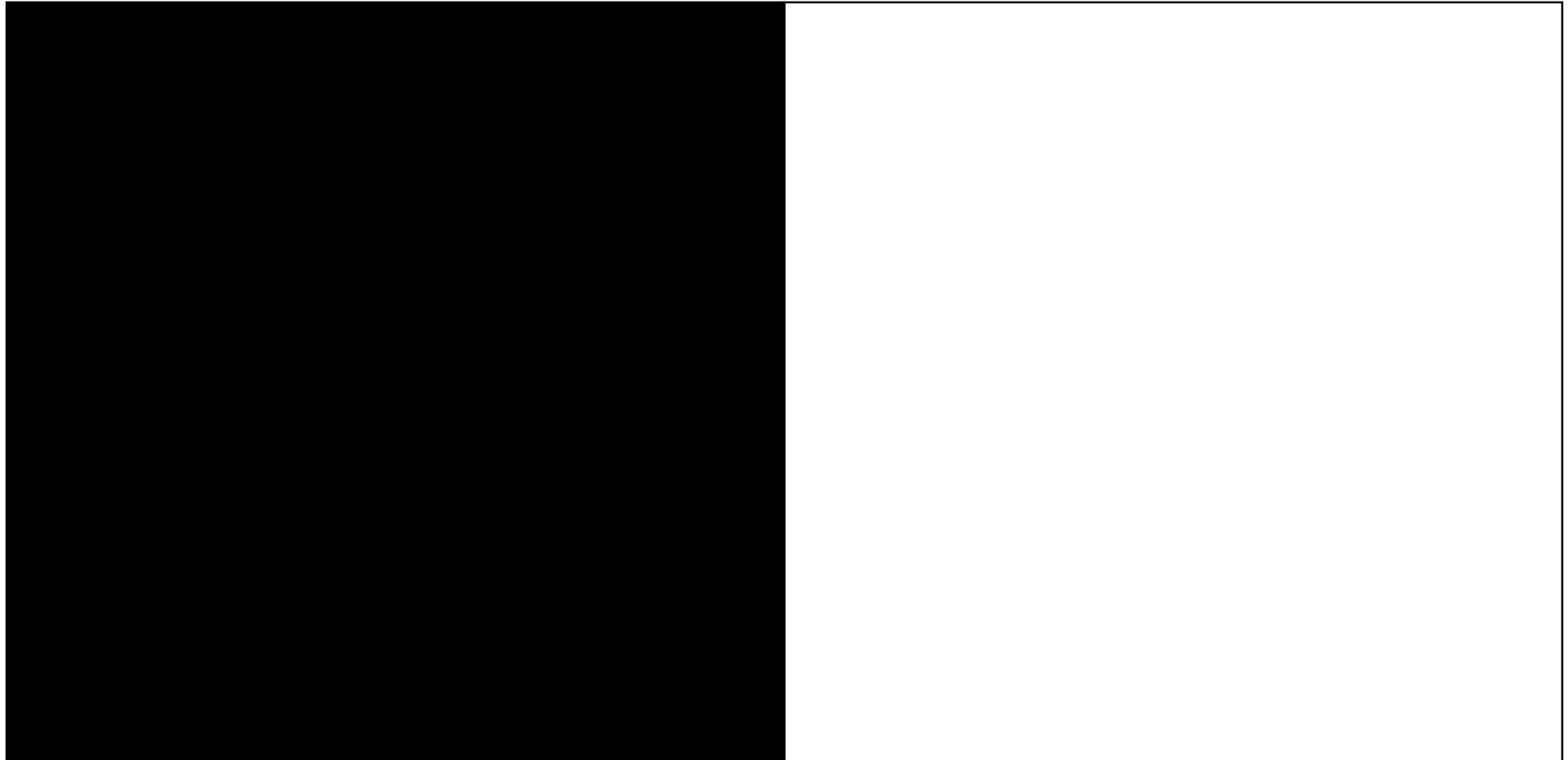


(Digital) images have an even lower dynamic range



(Digital) images have an even lower dynamic range

Any guesses about the dynamic range of a standard 0-255 image?

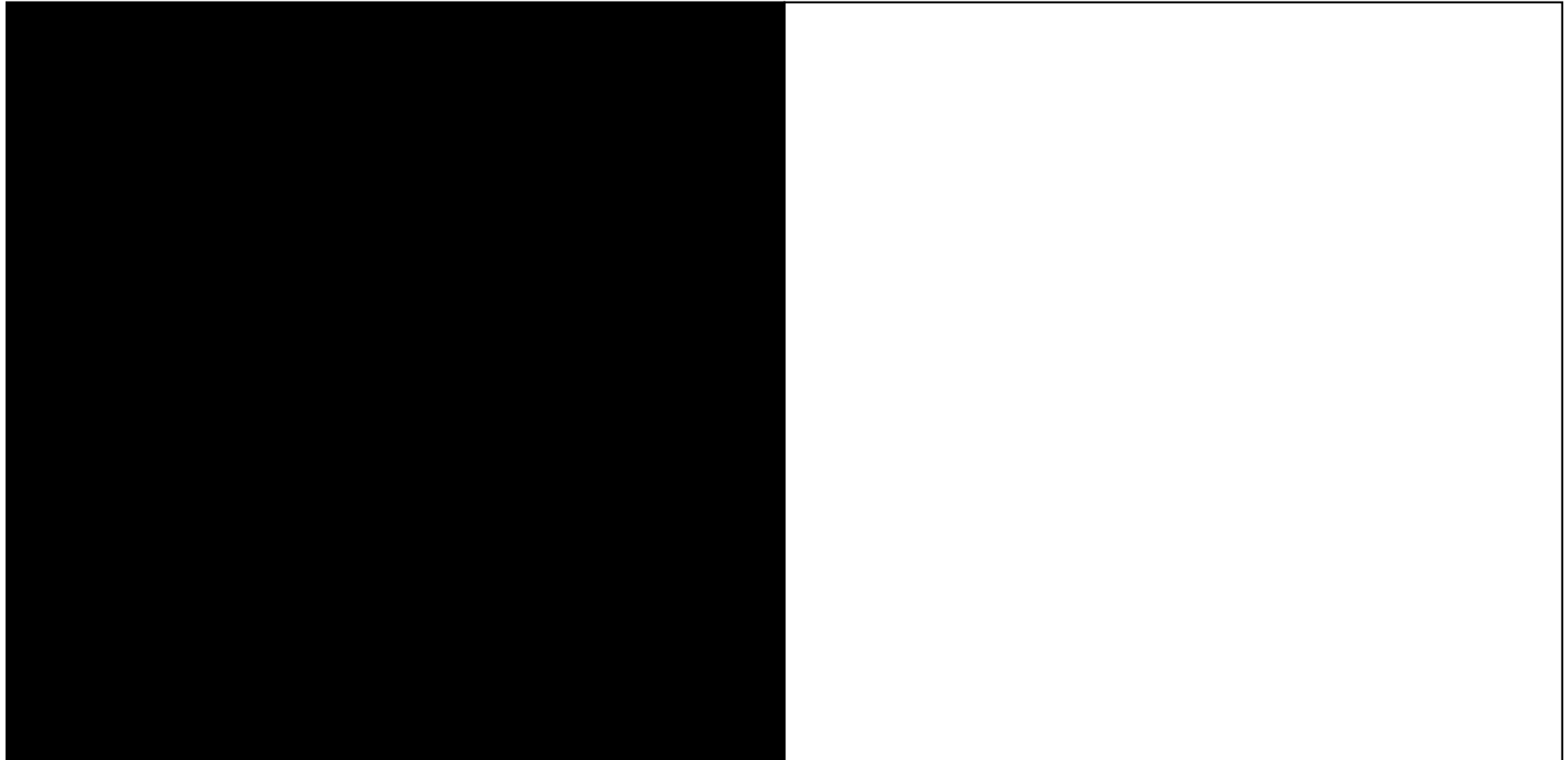


pure black

pure white

(Digital) images have an even lower dynamic range

Any guesses about the dynamic range of a standard 0-255 image?

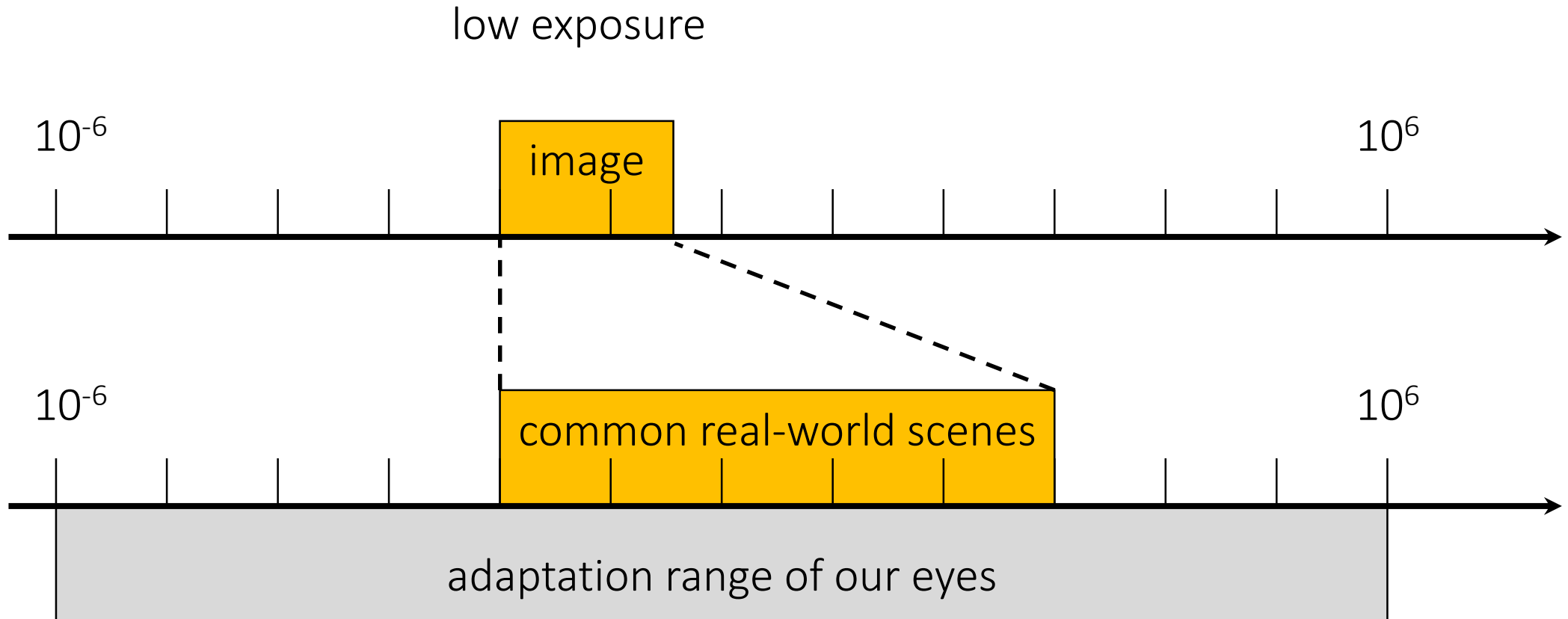


pure black

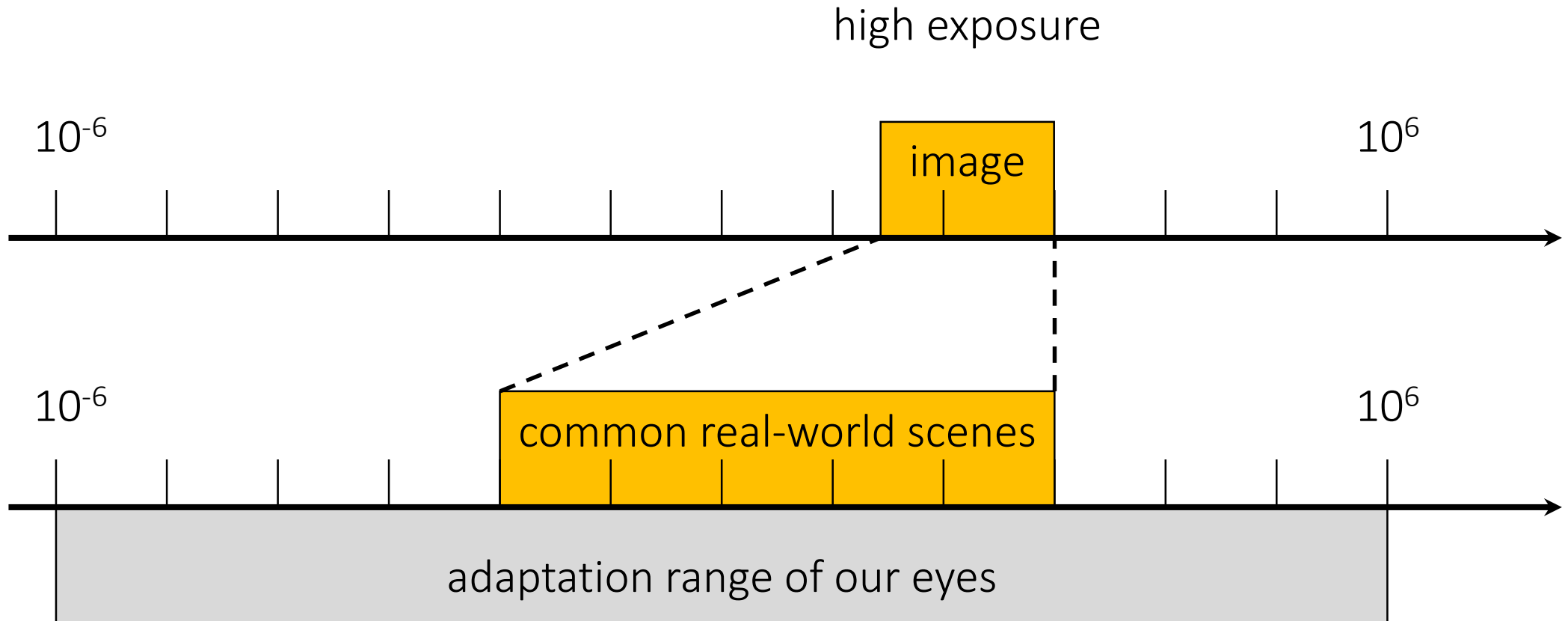
pure white

about 50x
brighter

(Digital) images have an even lower dynamic range



(Digital) images have an even lower dynamic range



Our devices do not match the real world

- 10:1 photographic print (higher for glossy paper)
- 20:1 artist's paints
- 200:1 slide film
- 500:1 negative film
- 1000:1 LCD display
- 2000:1 digital SLR (at 12 bits)
- 100000:1 real world

Two challenges:

1. HDR imaging – which parts of the world do we include in the 8-14 bits available to our device?
2. Tonemapping – which parts of the world do we display in the 4-10 bits available to our device?

High dynamic range imaging







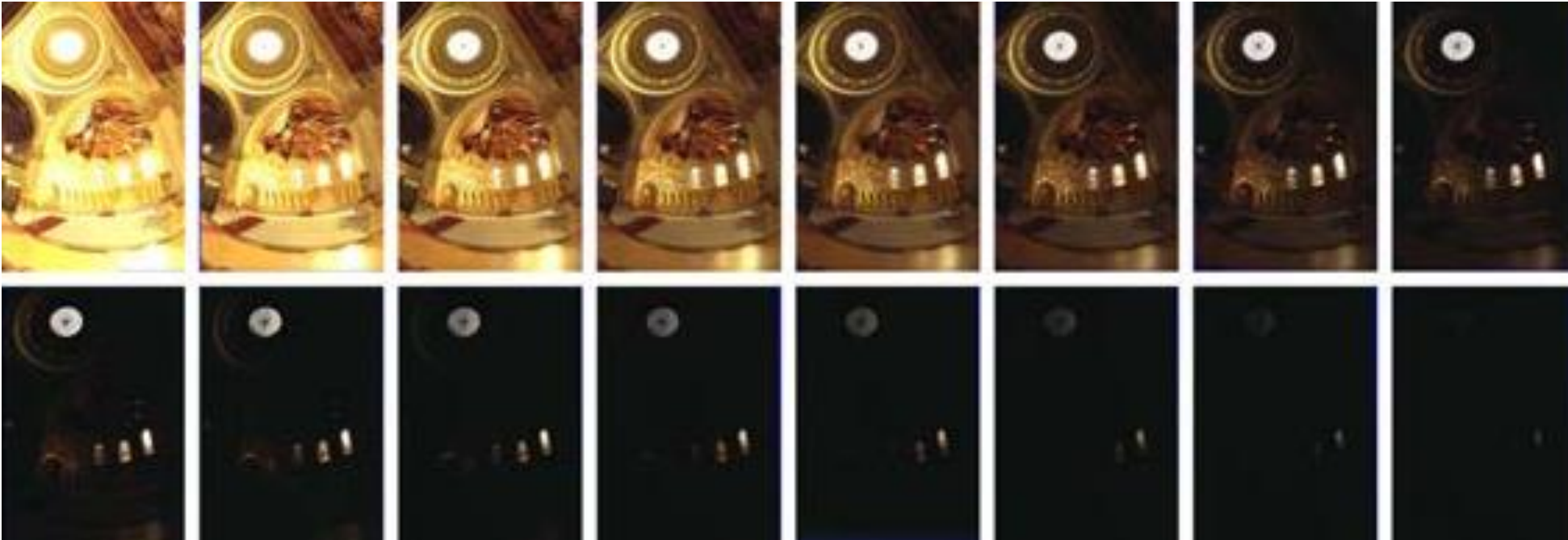




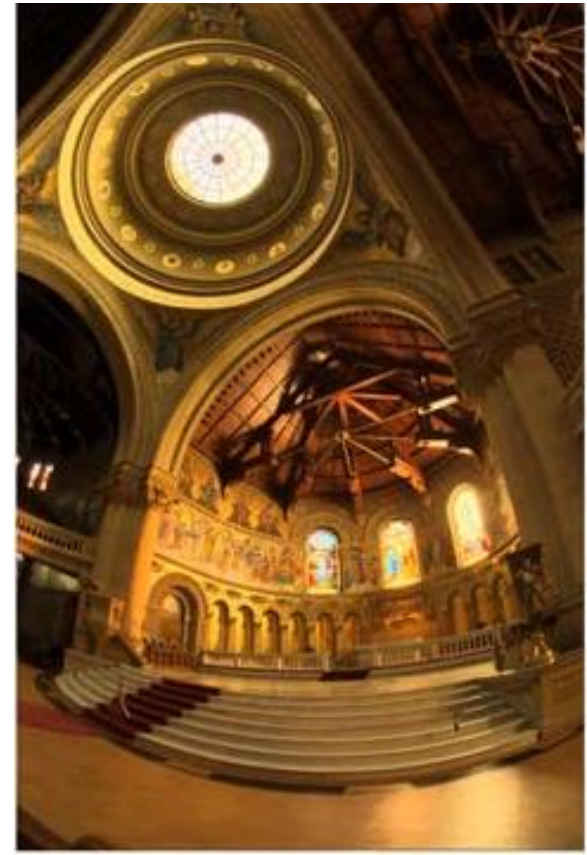


Key idea

1. Exposure bracketing: Capture multiple LDR images at different exposures

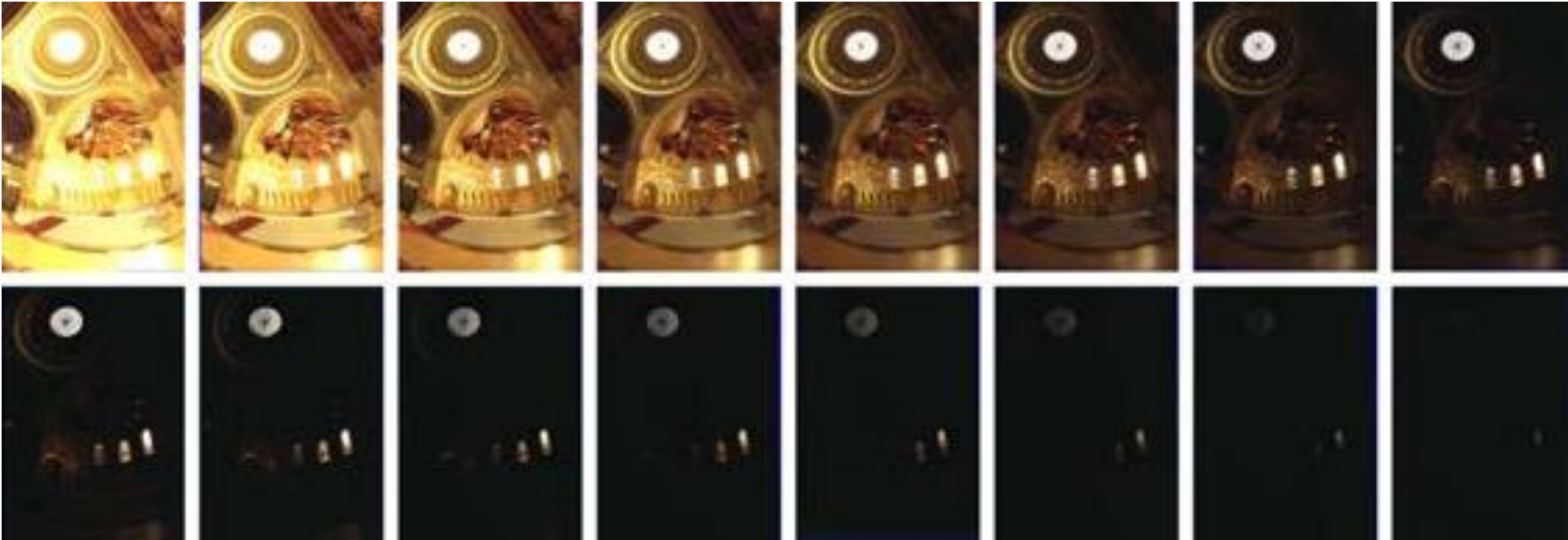


2. Merging: Combine them into a single HDR image

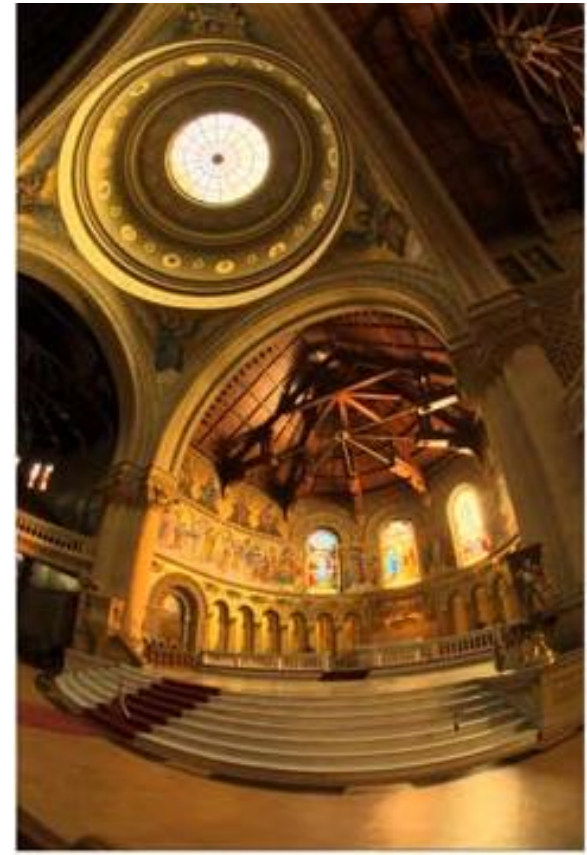


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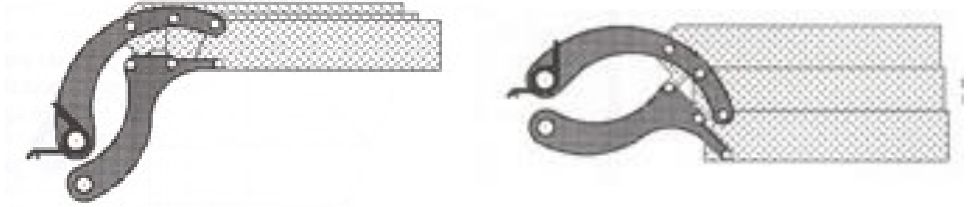


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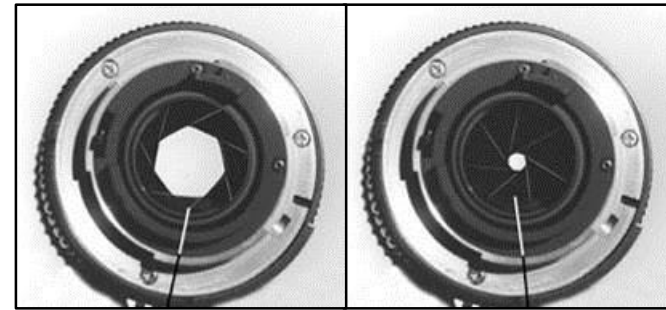


Ways to vary exposure

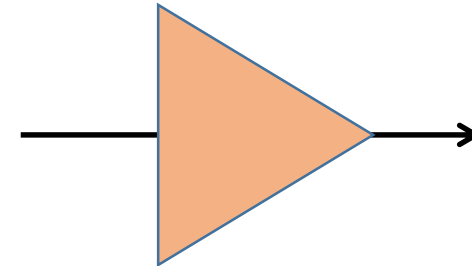
1. Shutter speed



2. F-stop (aperture, iris)



3. ISO



4. Neutral density (ND) filters



Pros and cons of each for HDR?

Ways to vary exposure

1. Shutter speed

- Range: about 30 sec to 1/4000 sec (6 orders of magnitude)
- Pros: repeatable, linear
- Cons: noise and motion blur for long exposure

2. F-stop (aperture, iris)

- Range: about f/0.98 to f/22 (3 orders of magnitude)
- Pros: fully optical, no noise
- Cons: changes depth of field

3. ISO

- Range: about 100 to 1600 (1.5 orders of magnitude)
- Pros: no movement at all
- Cons: noise

4. Neutral density (ND) filters

- Range: up to 6 densities (6 orders of magnitude)
- Pros: works with strobe/flash
- Cons: not perfectly neutral (color shift), extra glass (interreflections, aberrations), need to touch camera (shake)

Exposure bracketing with shutter speed

Note: shutter times usually obey a power series – each “stop” is a factor of 2

1/4, 1/8, 1/15, 1/30, 1/60, 1/125, 1/250, 1/500, 1/1000 sec

usually really is

1/4, 1/8, 1/16, 1/32, 1/64, 1/128, 1/256, 1/512, 1/1024 sec

Questions:

1. How many exposures?
2. What exposures?

Exposure bracketing with shutter speed

Note: shutter times usually obey a power series – each “stop” is a factor of 2

1/4, 1/8, 1/15, 1/30, 1/60, 1/125, 1/250, 1/500, 1/1000 sec

usually really is

1/4, 1/8, 1/16, 1/32, 1/64, 1/128, 1/256, 1/512, 1/1024 sec

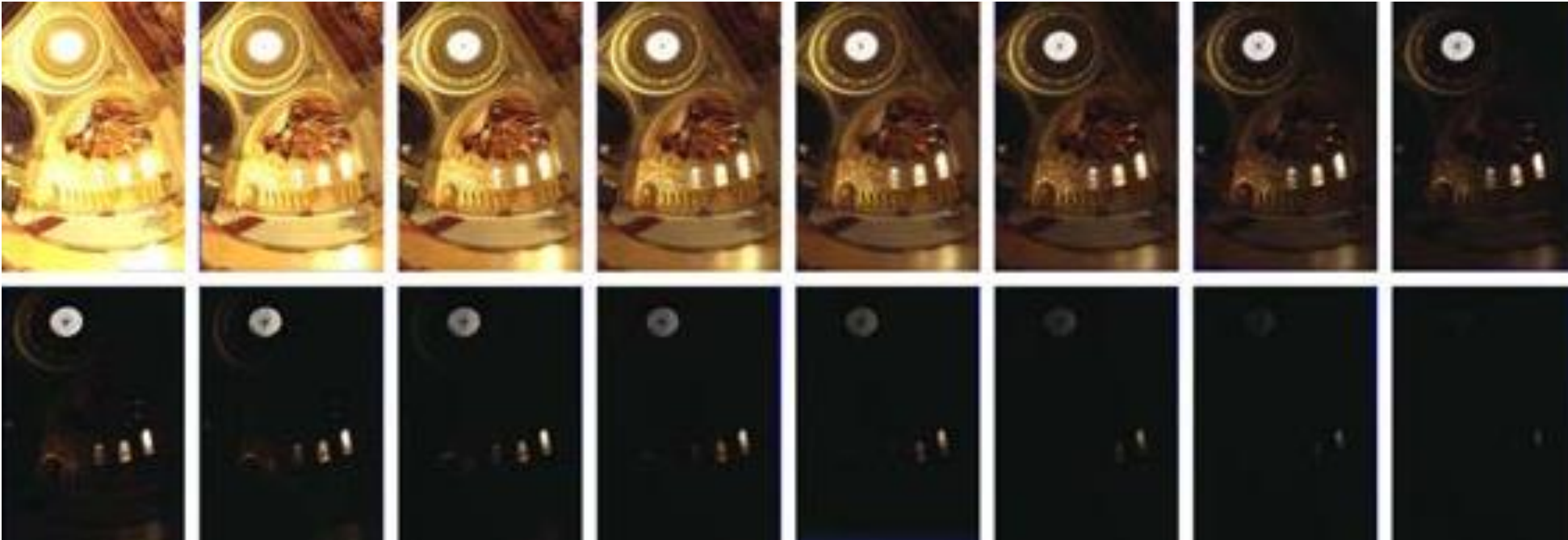
Questions:

1. How many exposures?
2. What exposures?

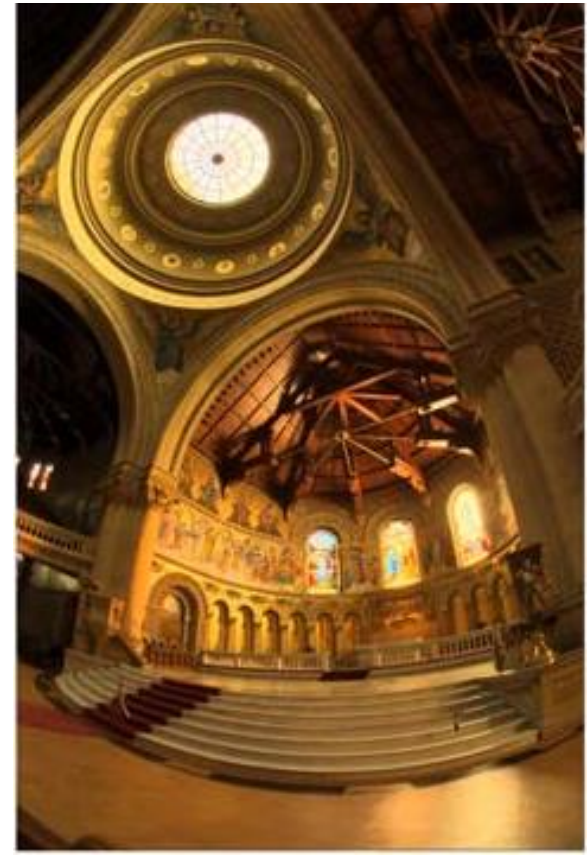
Answer: Depends on the scene, but a good default is 5 exposures, the metered exposure and +/- 2 stops around that.

Key idea

1. Exposure bracketing: Capture multiple LDR images at different exposures

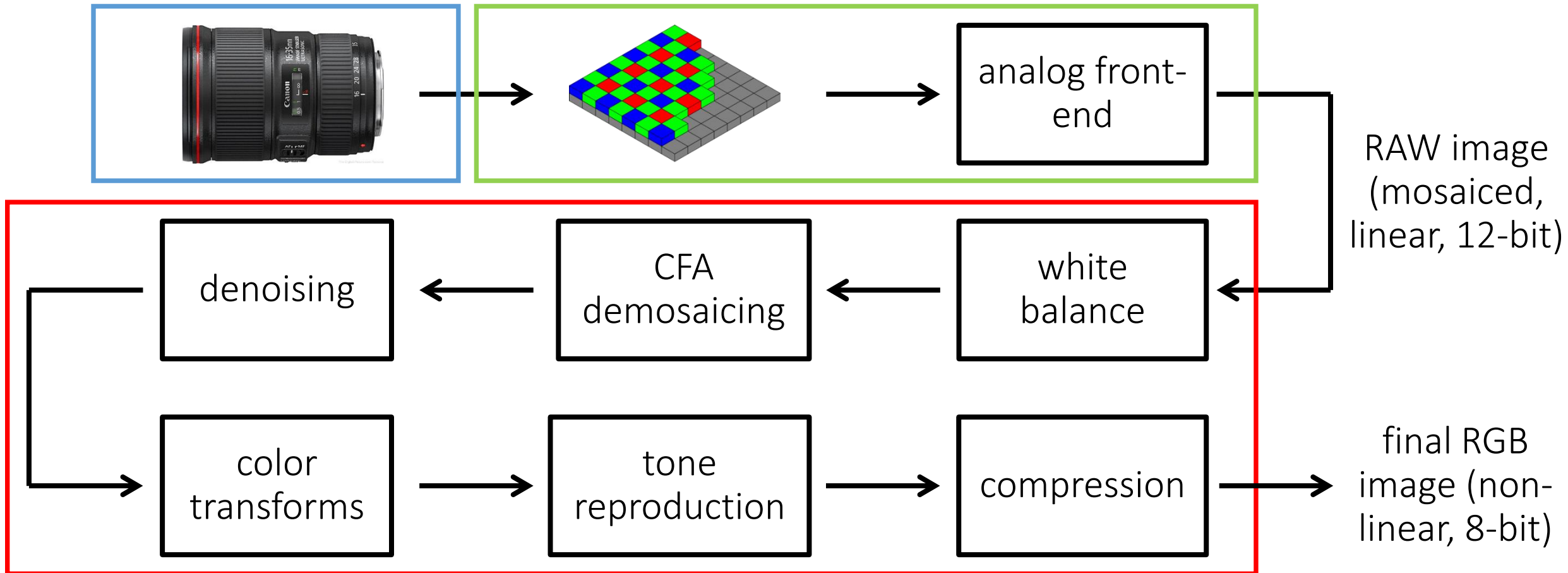


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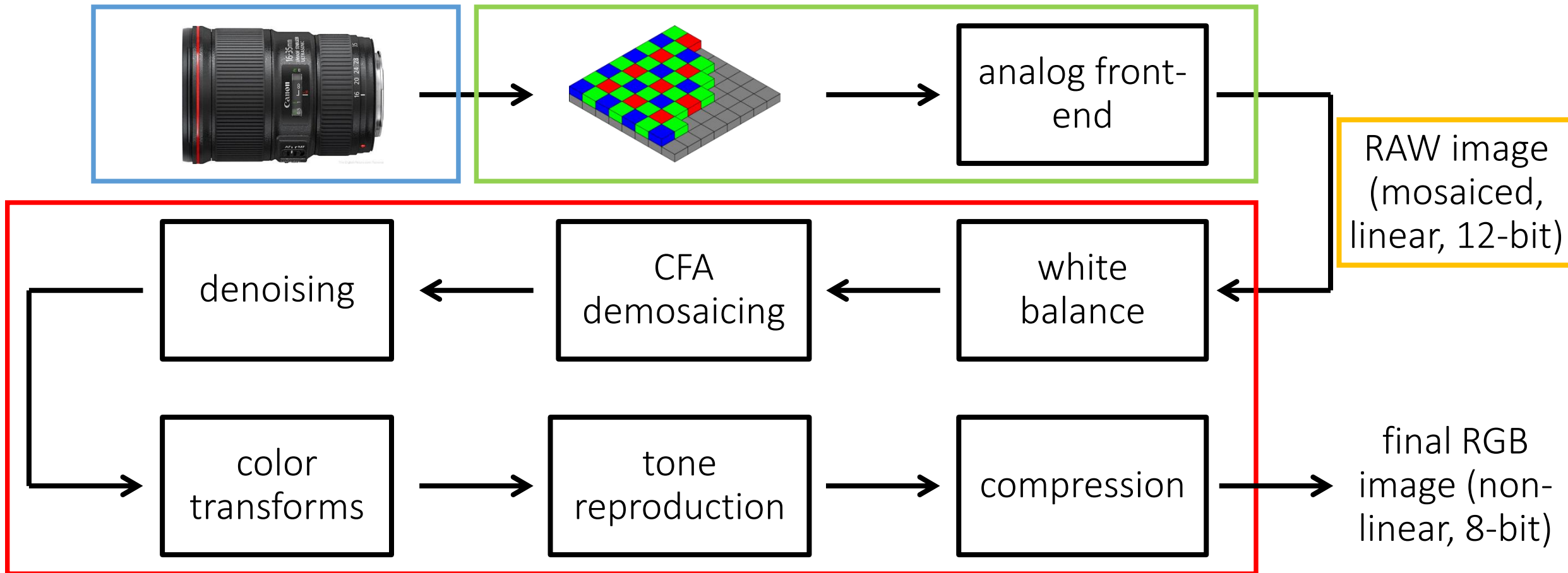
The image processing pipeline

The sequence of image processing operations applied by the camera's image signal processor (ISP) to convert a RAW image into a "conventional" image.



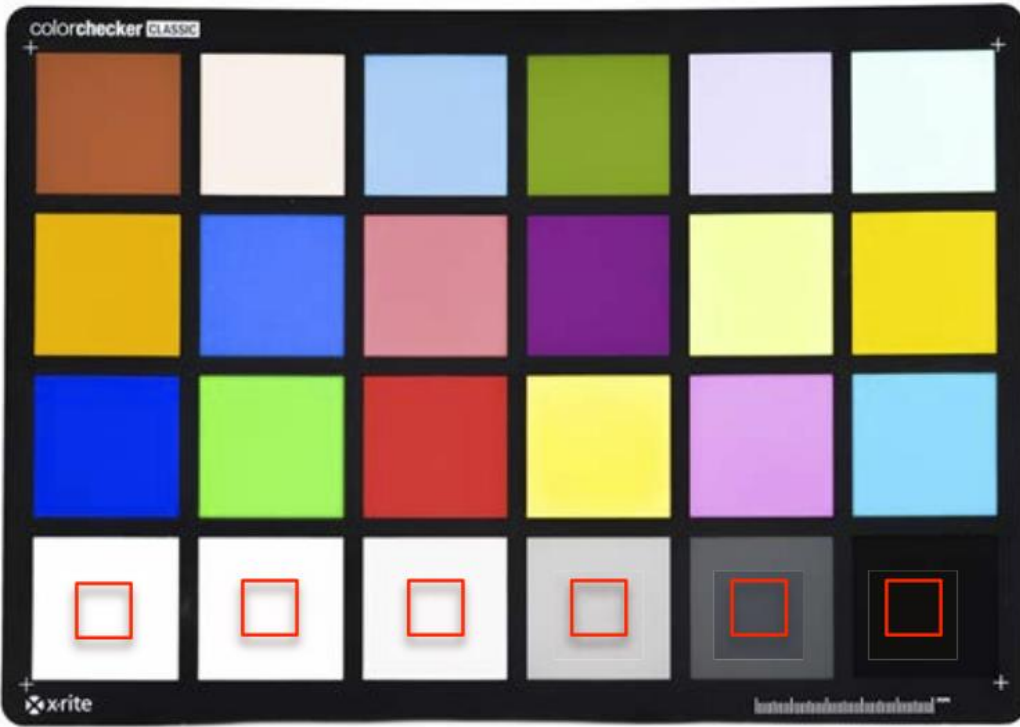
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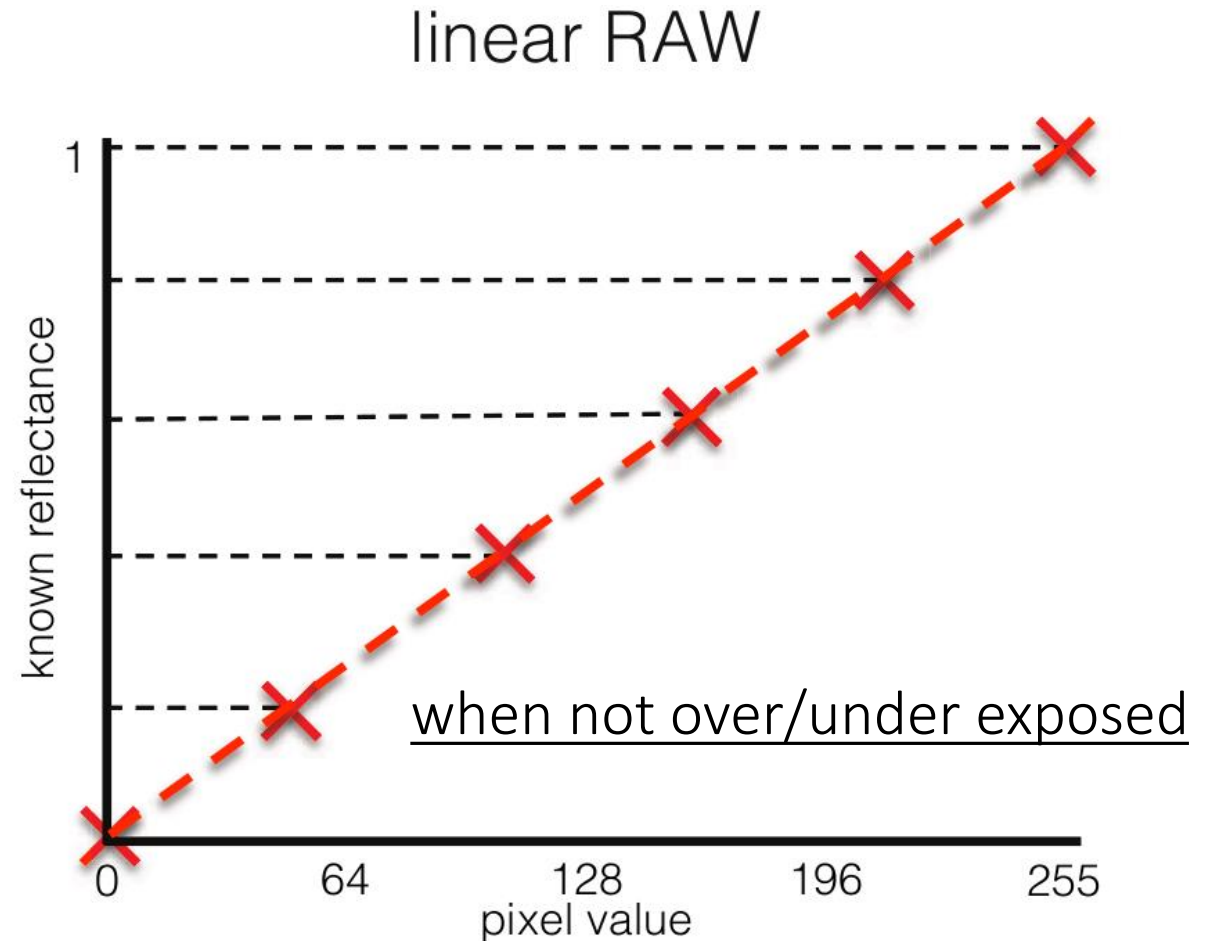


RAW images have a linear response curve

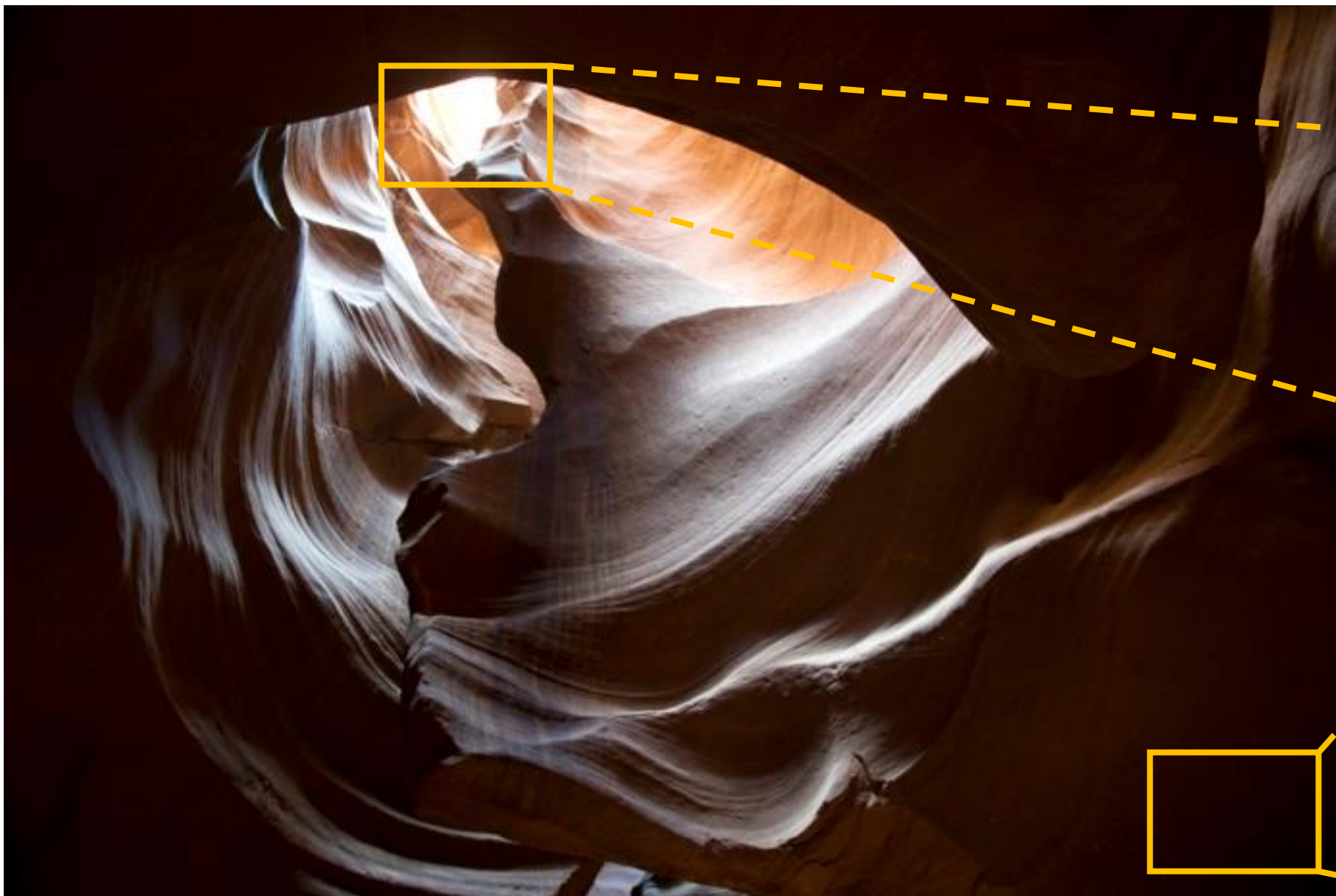
Colorchecker: Great tool for radiometric and color calibration.



Patches at bottom row have reflectance that increases linearly.



Over/under exposure



in highlights we are limited by clipping



in shadows we are limited by noise



RAW (linear) image formation model

Real scene radiance for image pixel (x,y) : $L(x, y)$

Exposure time:

t_5



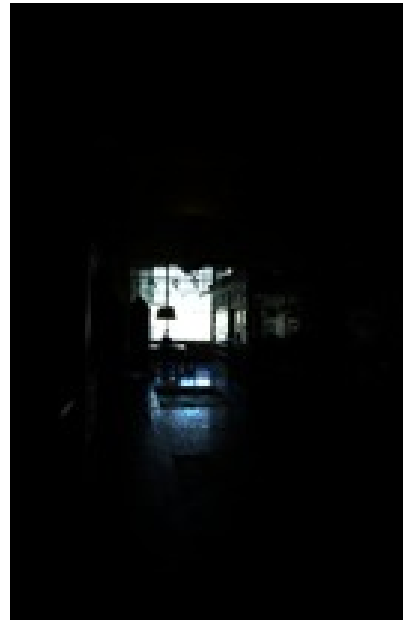
t_4



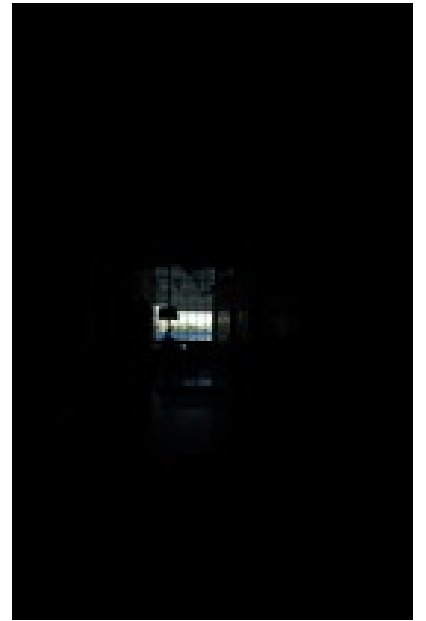
t_3



t_2



t_1



What is an expression for the image $I_{\text{linear}}(x,y)$ as a function of $L(x,y)$?

RAW (linear) image formation model

Real scene radiance for image pixel (x,y) : $L(x, y)$

Exposure time:

t_5



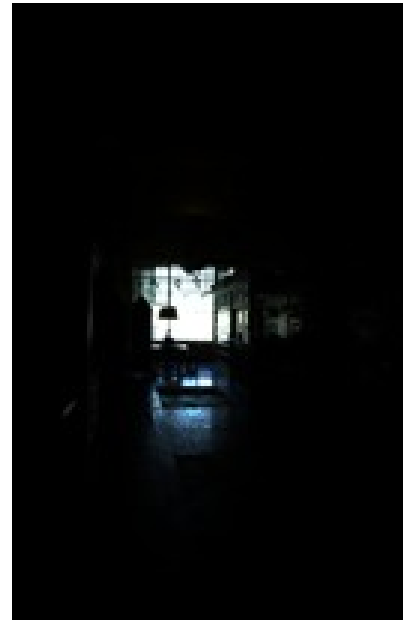
t_4



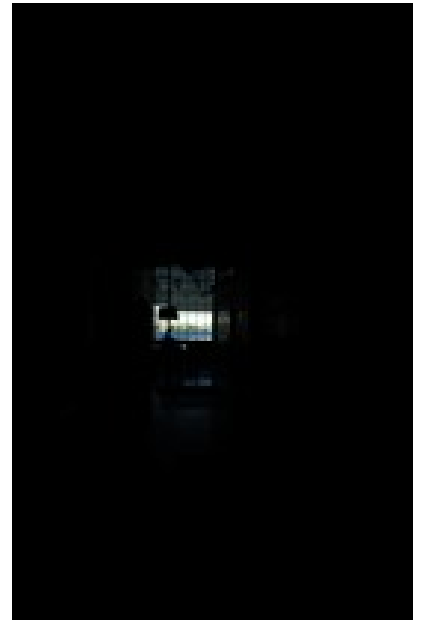
t_3



t_2



t_1



What is an expression for the image $I_{\text{linear}}(x,y)$ as a function of $L(x,y)$?

$$I_{\text{linear}}(x,y) = \text{clip}[t_i \cdot L(x,y) + \text{noise}]$$

How would you merge these images into an HDR one?

Merging RAW (linear) exposure stacks

For each pixel:

1. Find “valid” images
2. Weight valid pixel values appropriately
3. Form a new pixel value as the weighted average of valid pixel values

How would you
implement steps 1-2?

t_5



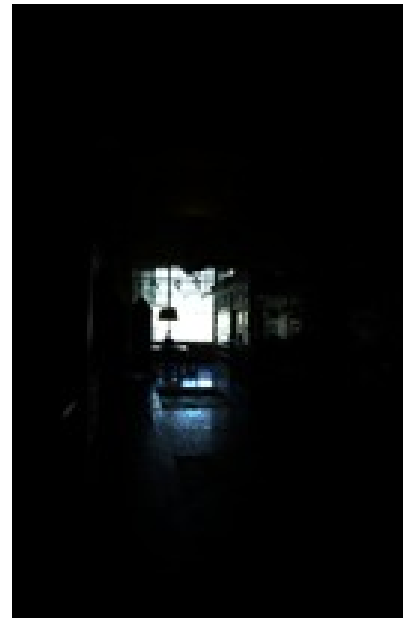
t_4



t_3



t_2



t_1



Merging RAW (linear) exposure stacks

For each pixel:

1. Find “valid” images

← (noise) $0.05 < \text{pixel} < 0.95$ (clipping)

2. Weight valid pixel values appropriately

● noise

● valid

3. Form a new pixel value as the weighted average of valid pixel values

● clipped

t_5



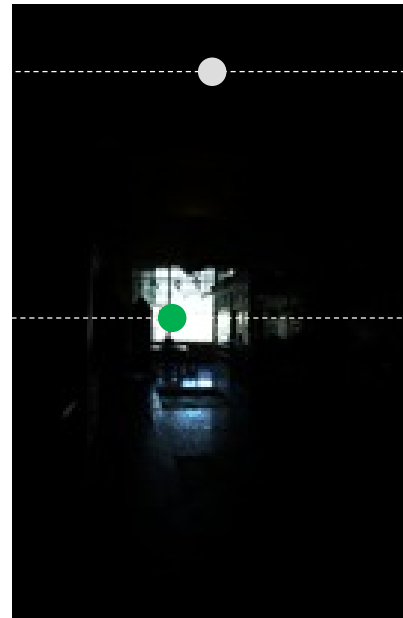
t_4



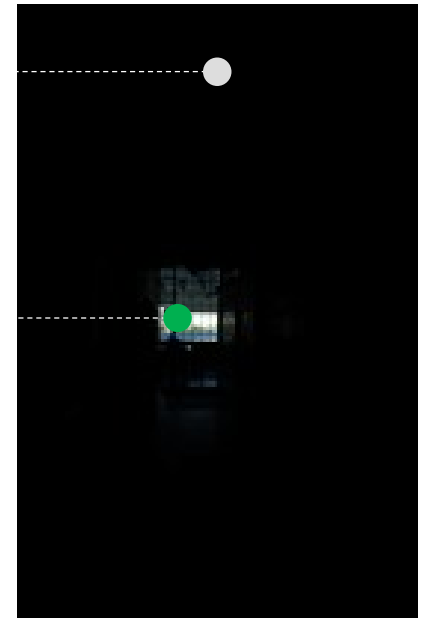
t_3



t_2



t_1



Merging RAW (linear) exposure stacks

For each pixel:

1. Find “valid” images \longleftarrow (noise) $0.05 < \text{pixel} < 0.95$ (clipping)
2. Weight valid pixel values appropriately \longleftarrow (pixel value) / t_i
3. Form a new pixel value as the weighted average of valid pixel values

t_5



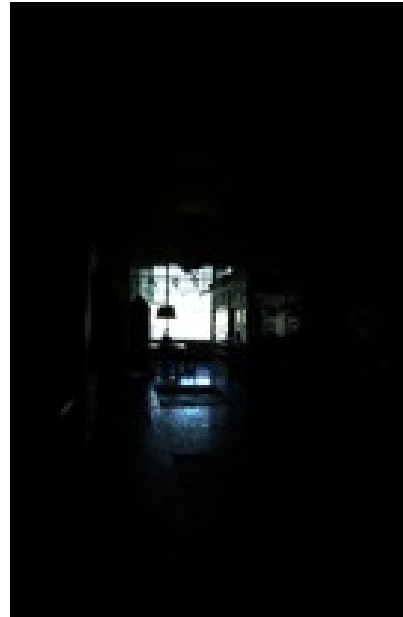
t_4



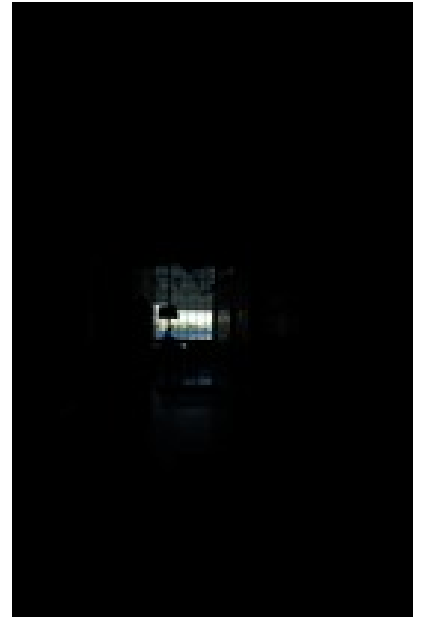
t_3



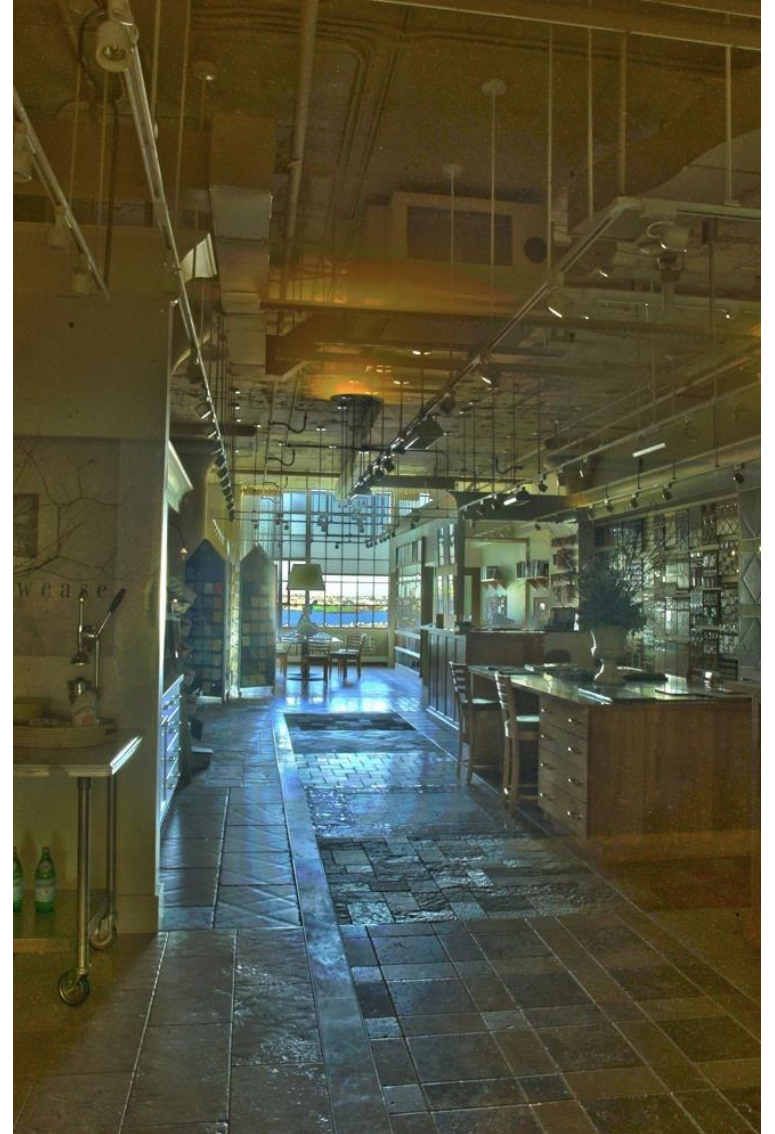
t_2



t_1



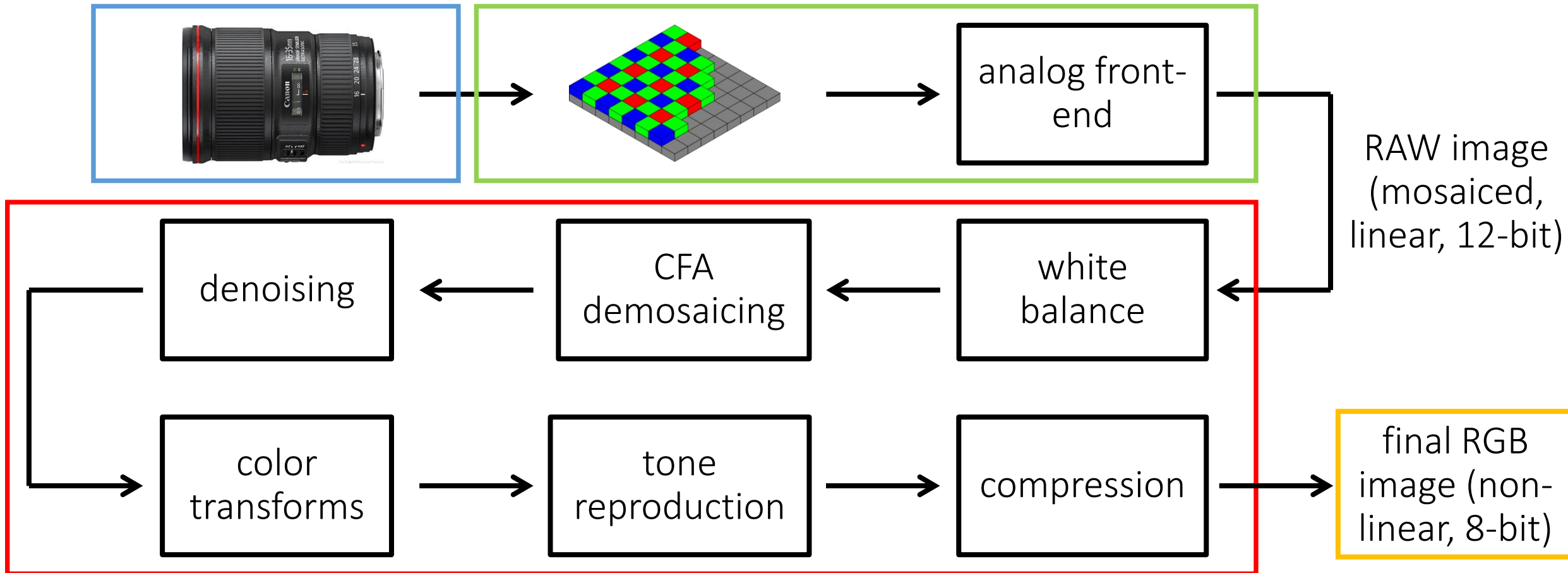
Merging result (after tonemapping)



What if I cannot use raw?

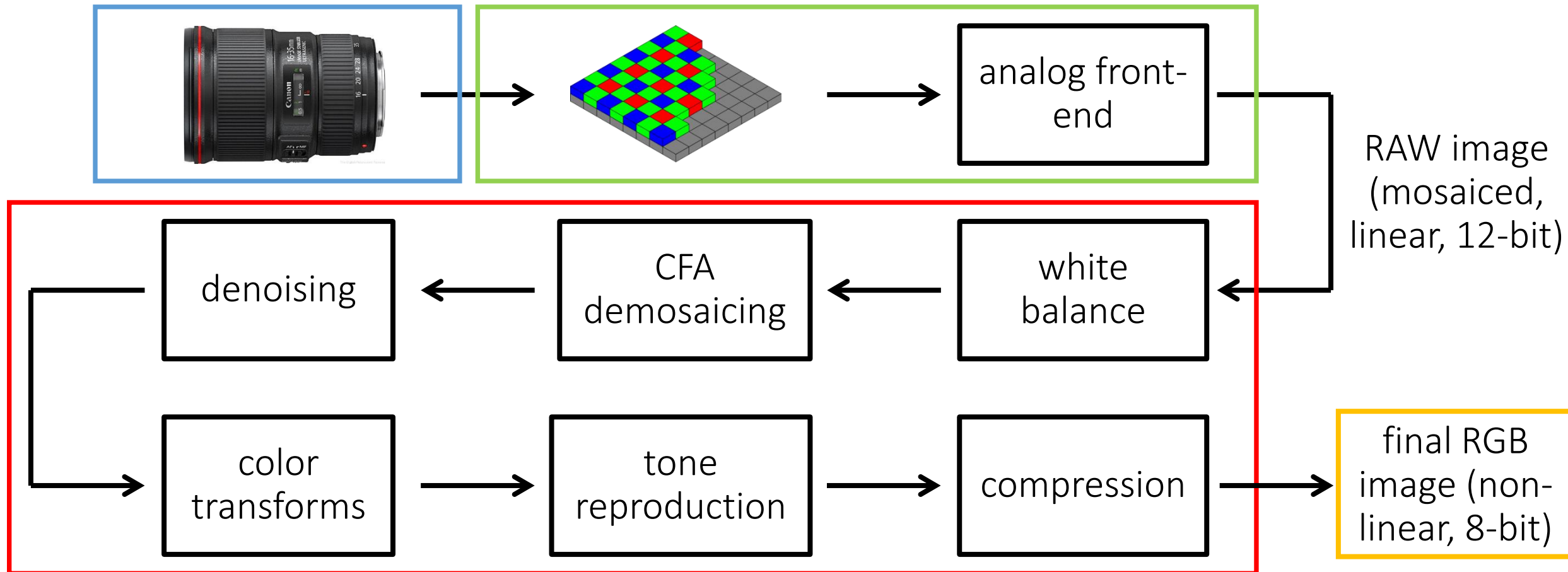
The image processing pipeline

- Can you foresee any problem when we switch from RAW to rendered images?



The image processing pipeline

- Can you foresee any problem when we switch from RAW to rendered images?
- How do we deal with the nonlinearities?



Radiometric calibration

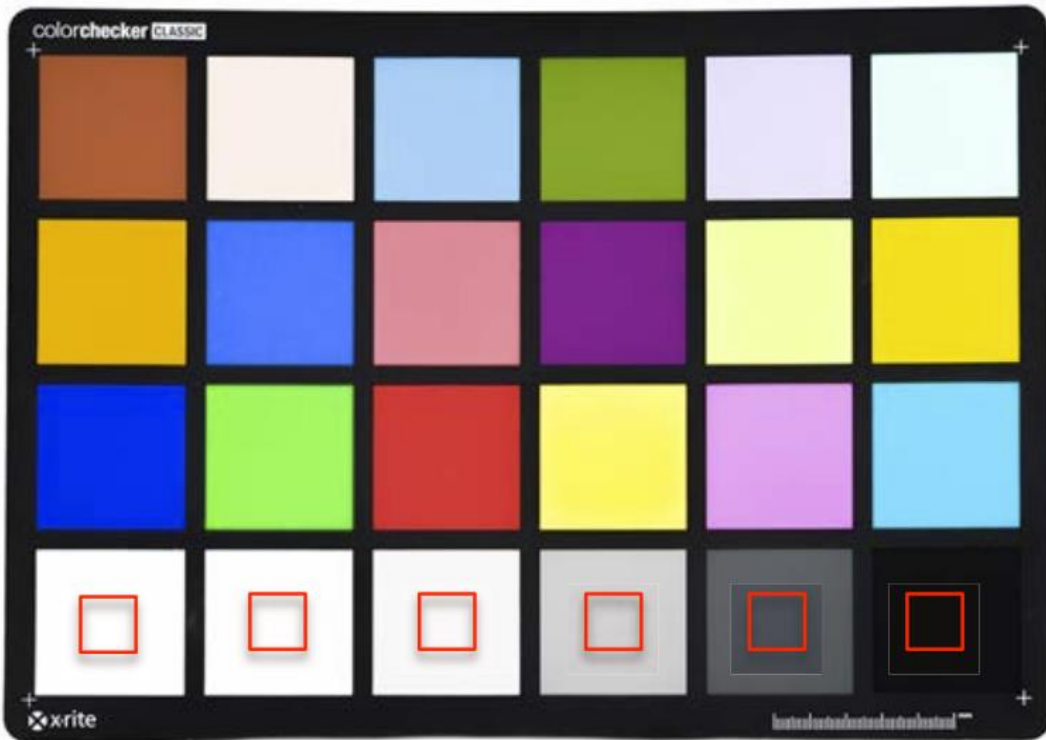
The process of measuring the camera's response curve. Can be two in three ways:

- Take images of scenes with different irradiance while keeping exposure the same.
- Takes images under different exposures while keeping irradiance the same.
- Takes images of scenes with different irradiance and under different exposures.

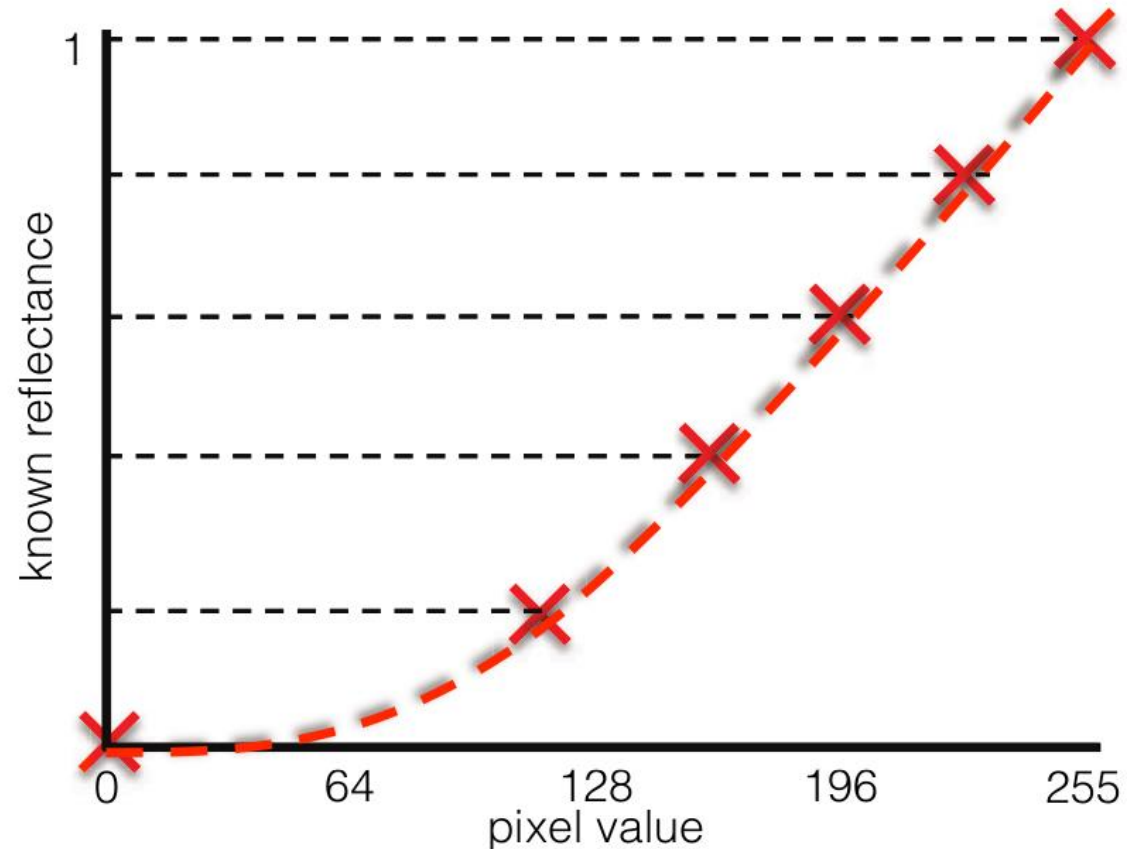
Same camera exposure, varying scene irradiance

Colorchecker: Great tool for radiometric and color calibration.

e.g. JPEG



Patches at bottom row have reflectance that increases linearly.



Different values correspond to patches of increasing reflected irradiance.

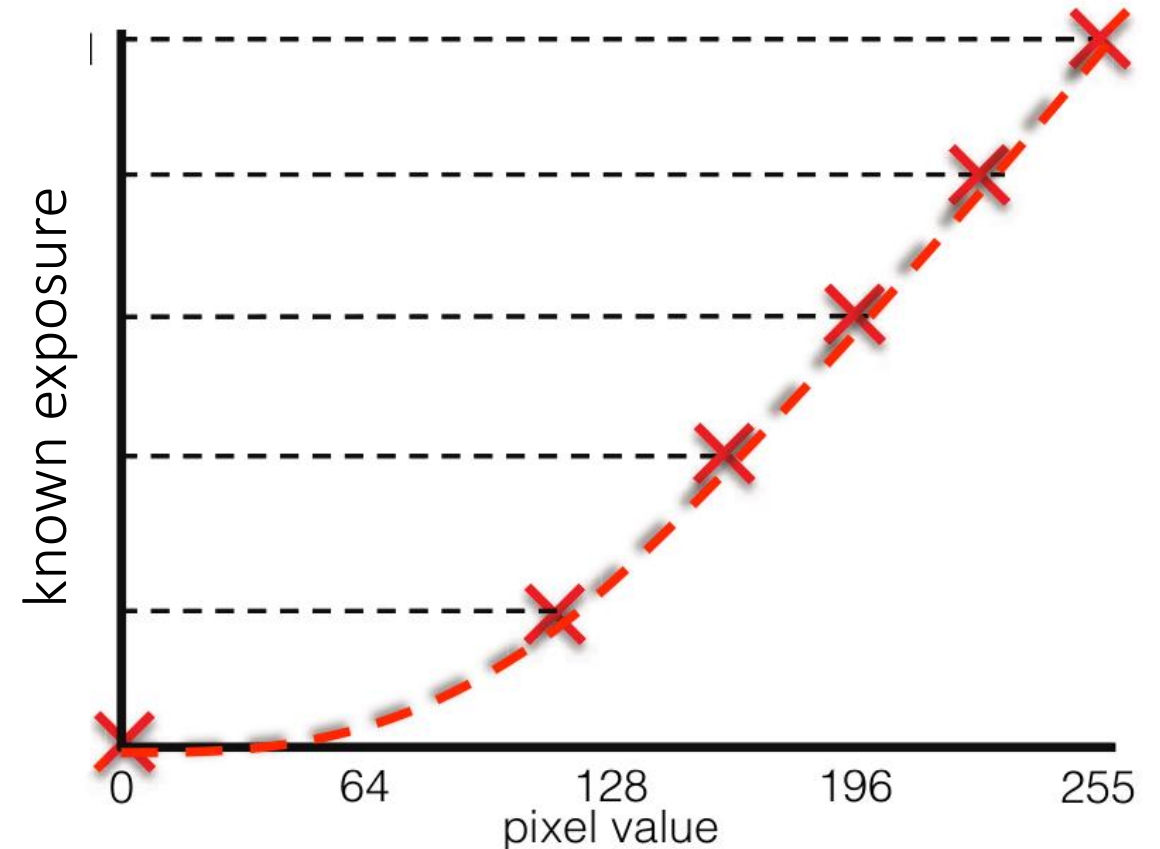
Same scene irradiance, varying camera exposure

Colorchecker: Great tool for white balancing and radiometric calibration.



All points on (the white part of) the target have the same reflectance.

e.g. JPEG



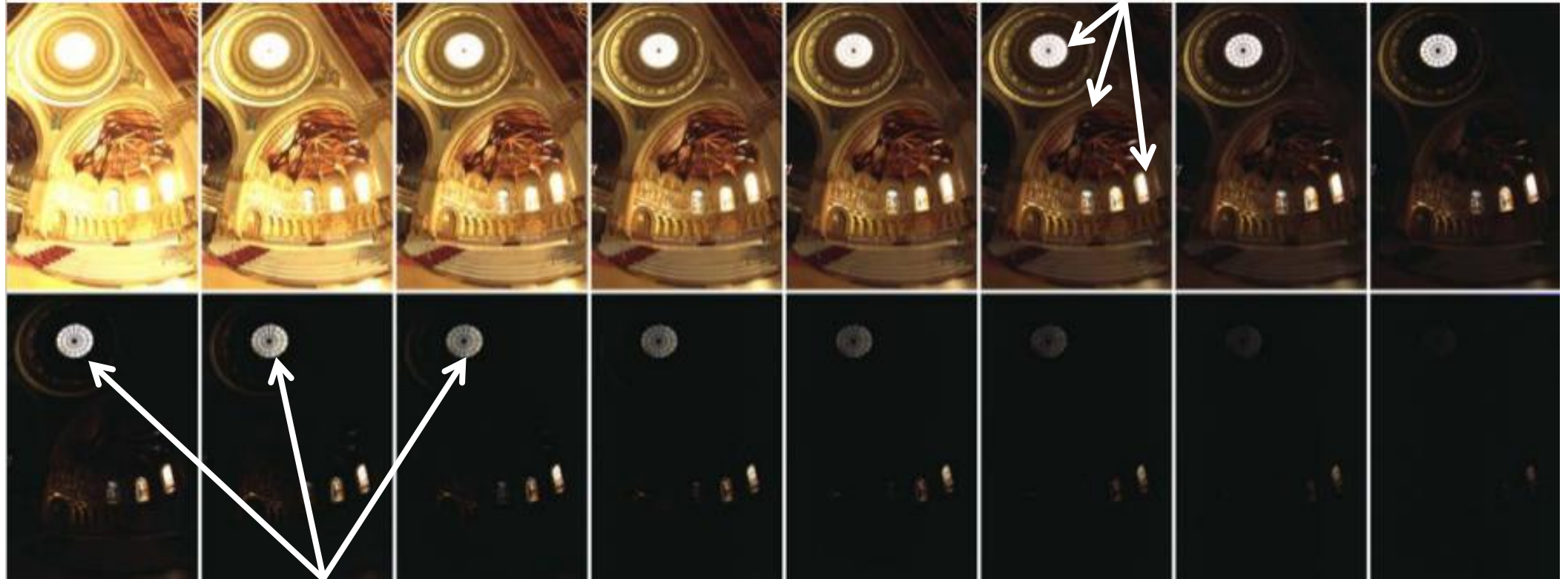
Different values correspond to images taken under increasing camera exposure.

Varying both scene irradiance and camera exposure

You can do this using the LDR exposure stack itself

- More information in Homework 2

Same scene irradiance, different camera exposure

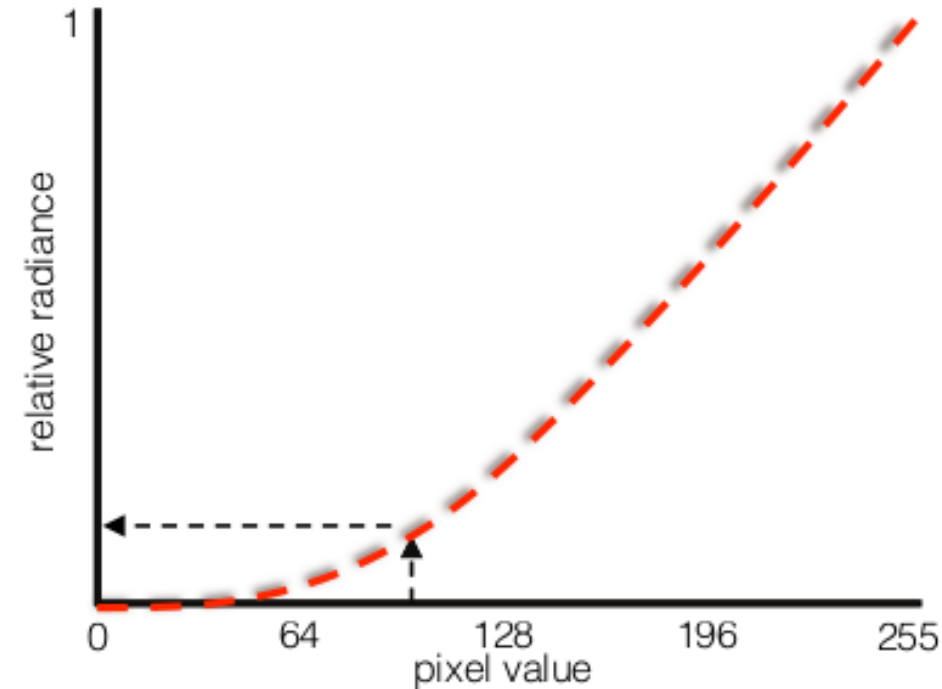


Same scene irradiance, different camera exposure

Non-linear image formation model

Real scene radiance for image pixel (x,y) : $L(x, y)$

Exposure time: t_i



$$I_{\text{linear}}(x,y) = \text{clip}[t_i \cdot L(x,y) + \text{noise}]$$

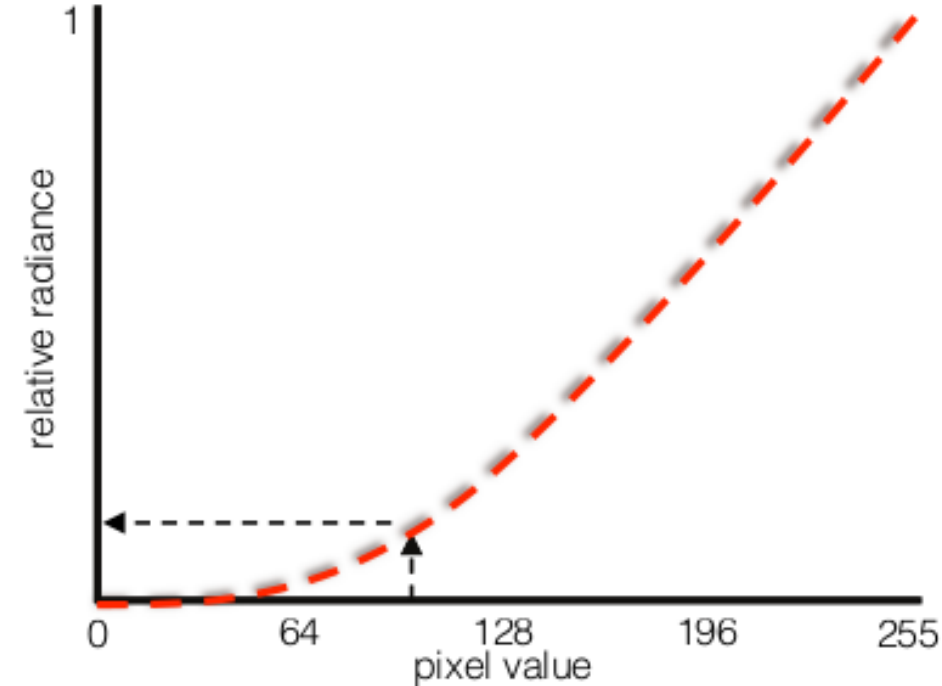
$$I_{\text{non-linear}}(x,y) = f[I_{\text{linear}}(x,y)]$$

How would you merge the non-linear images into an HDR one?

Non-linear image formation model

Real scene radiance for image pixel (x,y) : $L(x, y)$

Exposure time: t_i



$$I_{\text{linear}}(x,y) = \text{clip}[t_i \cdot L(x,y) + \text{noise}]$$

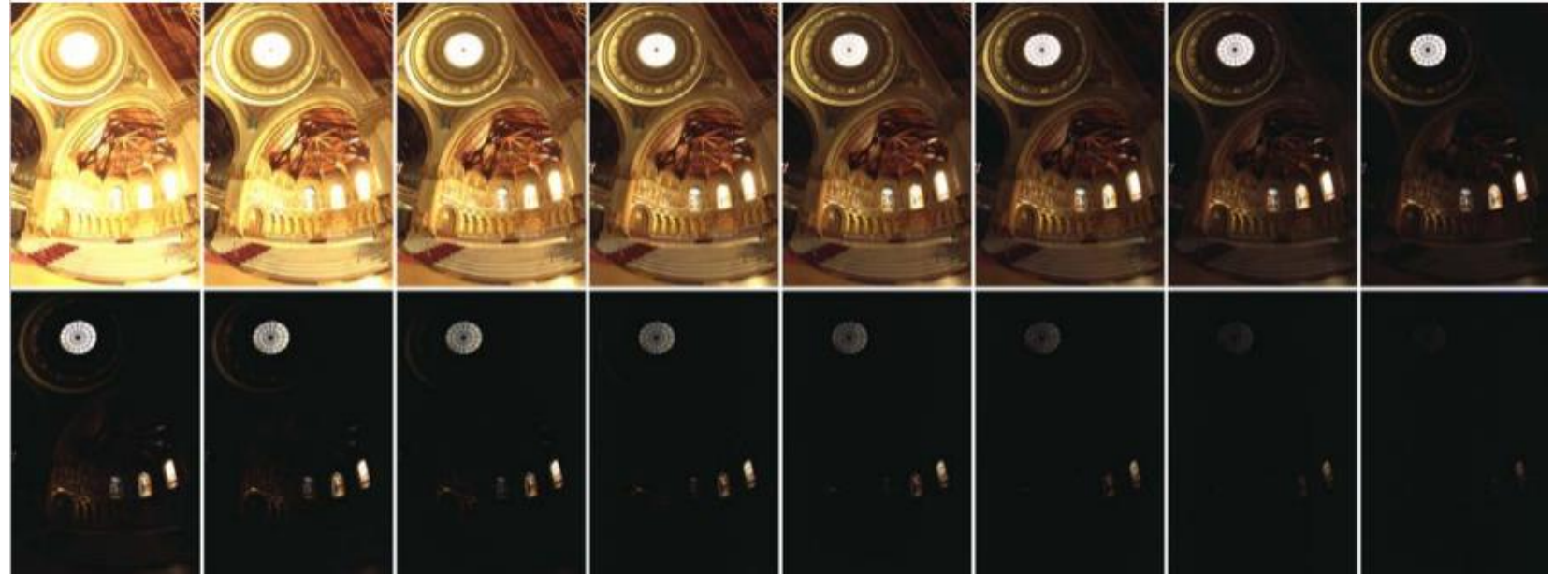
$$I_{\text{non-linear}}(x,y) = f[I_{\text{linear}}(x,y)]$$

$$I_{\text{est}}(x,y) = f^{-1}[I_{\text{non-linear}}(x,y)]$$

Use inverse transform to estimate linear image, then proceed as before

Linearization

$$I_{\text{non-linear}}(x,y) = f[I_{\text{linear}}(x,y)]$$



$$I_{\text{est}}(x,y) = f^{-1}[I_{\text{non-linear}}(x,y)]$$



Merging non-linear exposure stacks

1. Calibrate response curve

2. Linearize images

For each pixel:

3. Find “valid” images

← (noise) $0.05 < \text{pixel} < 0.95$ (clipping)

4. Weight valid pixel values appropriately

← (pixel value) / t_i

5. Form a new pixel value as the weighted average of valid pixel values

→ Same steps as in the RAW case.

Merging non-linear exposure stacks

1. Calibrate response curve

2. Linearize images

For each pixel:

3. Find “valid” images

← (noise) $0.05 < \text{pixel} < 0.95$ (clipping)

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→ Same steps as in the RAW case.

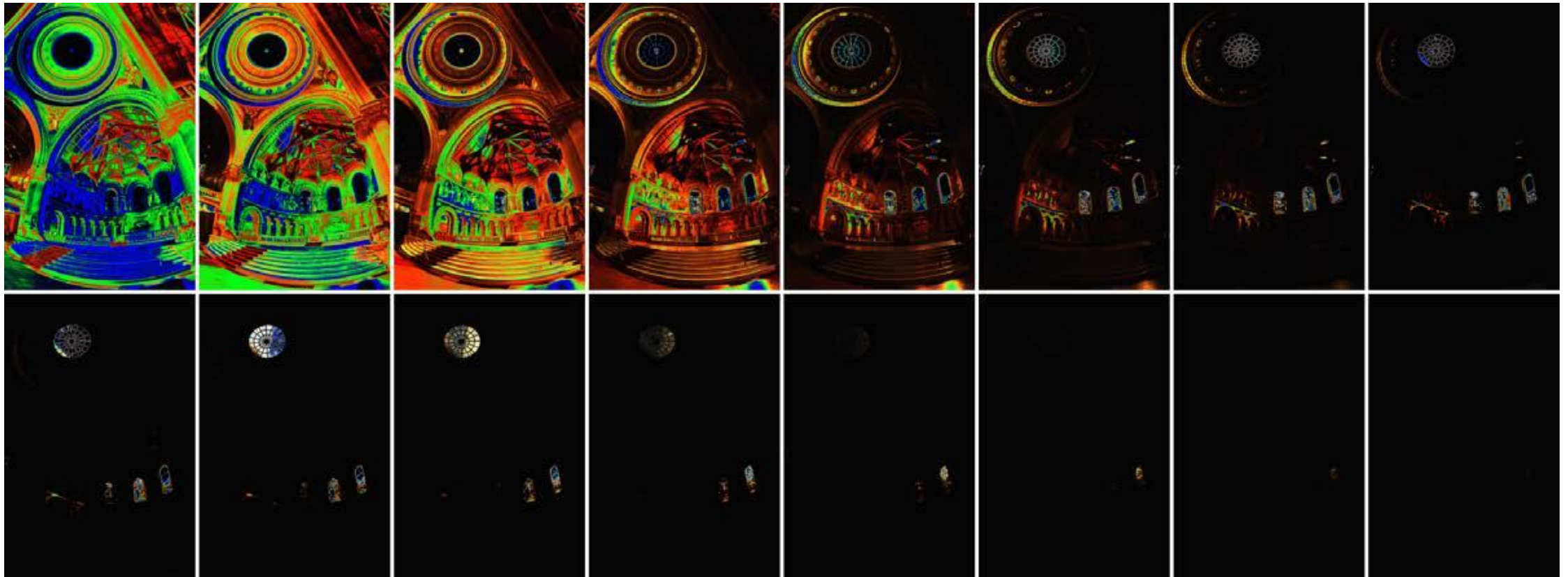
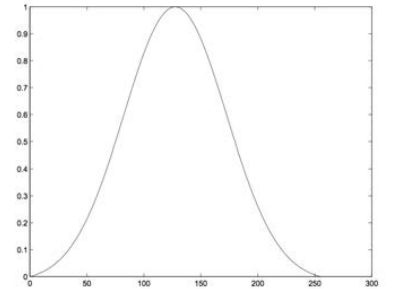
Note: many possible weighting schemes

Many possible weighting schemes

- We can derive optimal weights by modeling the sensor noise.
- More details in Homework 2.

“Confidence” that pixel is noisy/clipped

$$w_{ij} = \exp \left(-4 \frac{(I_{lin_{ij}} - 0.5)^2}{0.5^2} \right)$$

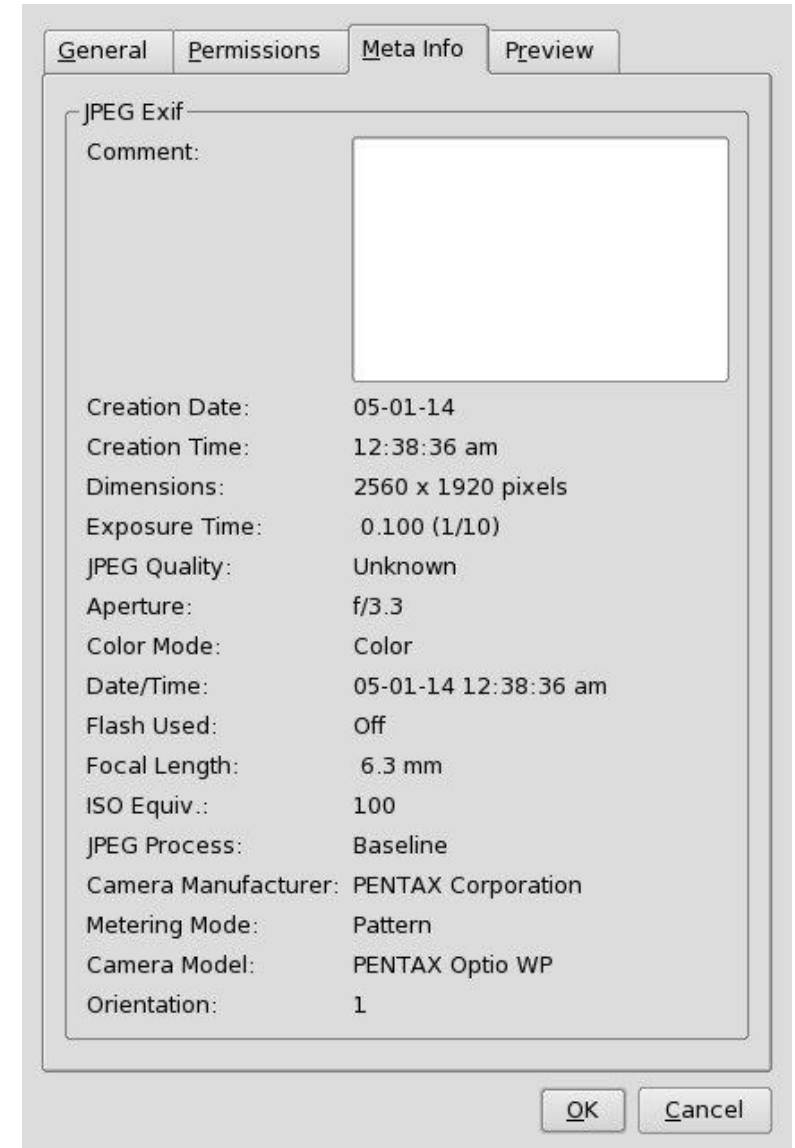


What if I cannot measure response curve?

You may find information in the image itself

If you cannot do calibration, take a look at the image's EXIF data (if available).

Often contains information about tone reproduction curve and color space.



Tone reproduction curves

The exact tone reproduction curve depends on the camera.

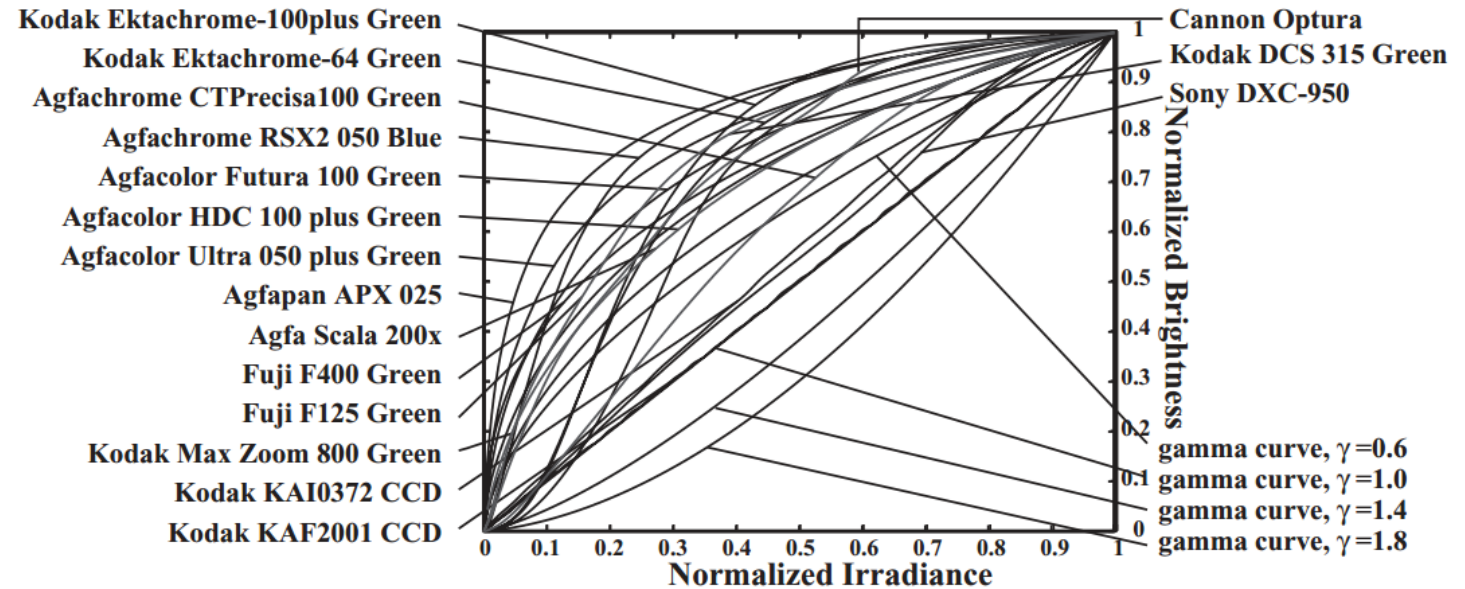
- Often well approximated as L^γ , for different values of the power γ (“gamma”).
- A good default is $\gamma = 1 / 2.2$.



before gamma



after gamma

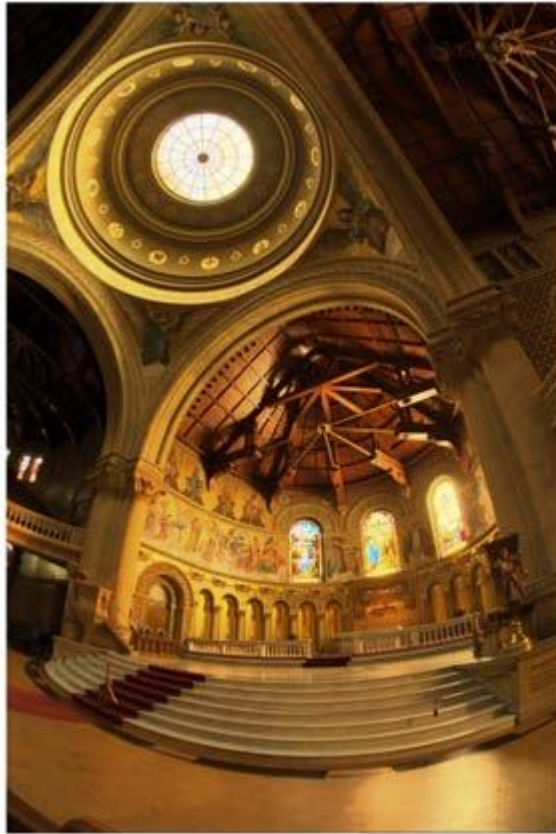


If nothing else, take the square of your image to approximately remove effect of tone reproduction curve.

Relative vs absolute radiance

Final fused HDR image gives radiance only up to a global scale

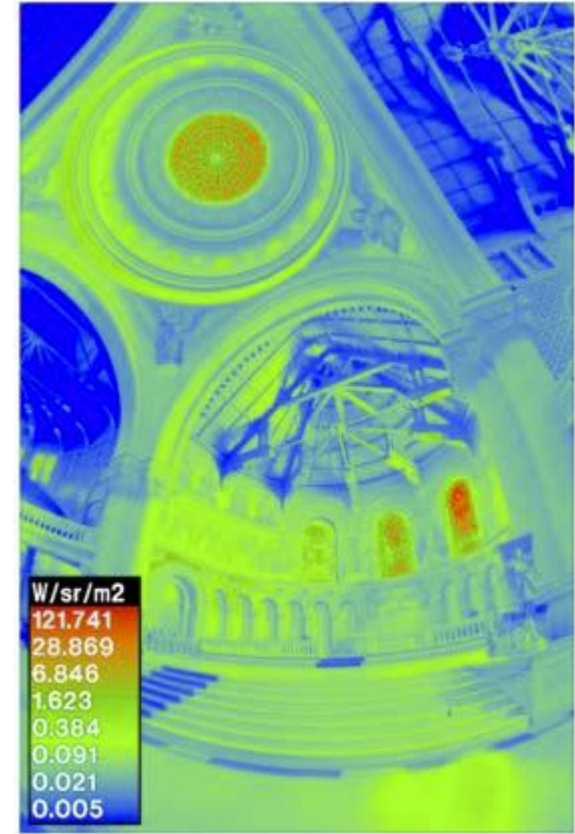
- If we know exact radiance at one point, we can convert relative HDR image to absolute radiance map



HDR image
(relative radiance)



spotmeter (absolute
radiance at one point)



absolute
radiance map

W/sr/m2
121.741
28.869
6.846
1.623
0.384
0.091
0.021
0.005

Basic HDR approach

1. Capture multiple LDR images at different exposures
2. Merge them into a single HDR image

Any problems with this approach?

Basic HDR approach

1. Capture multiple LDR images at different exposures
2. Merge them into a single HDR image

Problem: Very sensitive to movement

- Scene must be completely static
- Camera must not move

Most modern automatic HDR solutions include an alignment step before merging exposures

How do we store HDR images?

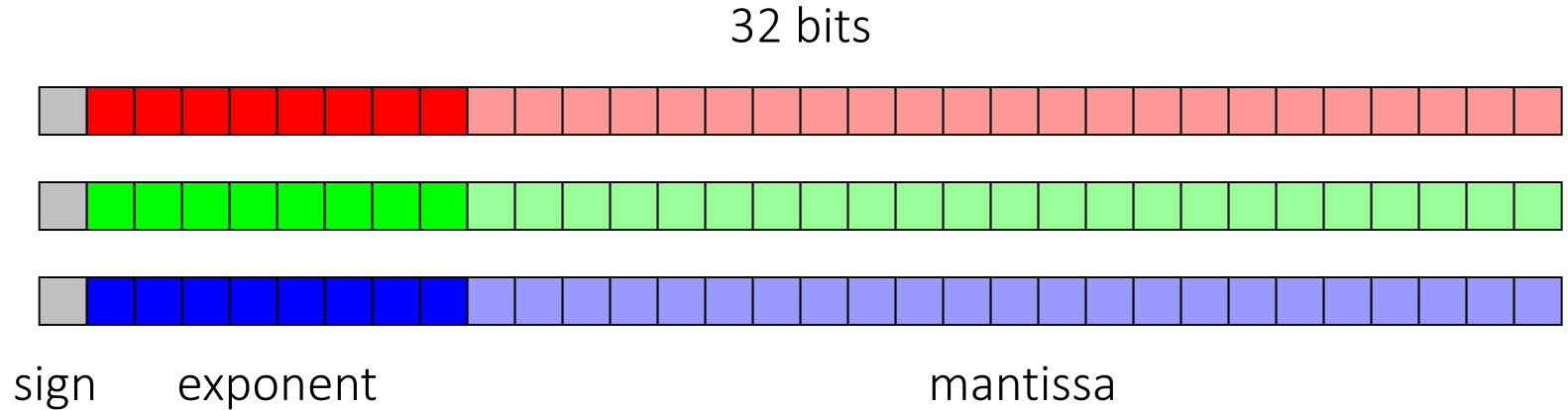
- Most standard image formats store integer 8-bit images
- Some image formats store integer 12-bit or 16-bit images
- HDR images are floating point 32-bit or 64-bit images

How do we store HDR images?

Use specialized image formats for HDR images

portable float map (.pfm)

- very simple to implement



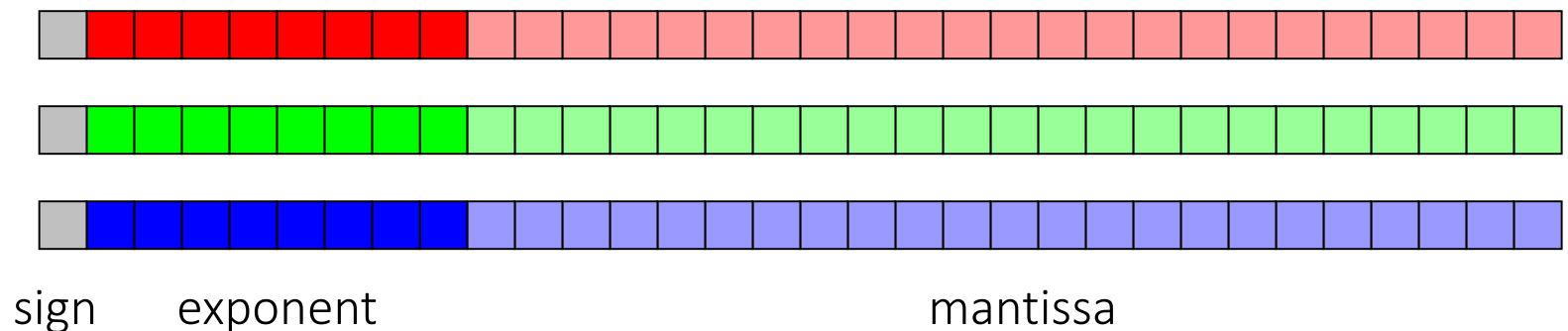
Radiance format (.hdr)

- supported by Matlab



OpenEXR format (.exr)

- multiple extra features



Another type of HDR images

Light probes: place a chrome sphere in the scene and capture an HDR image

- Used to measure real-world illumination environments (“environment maps”)

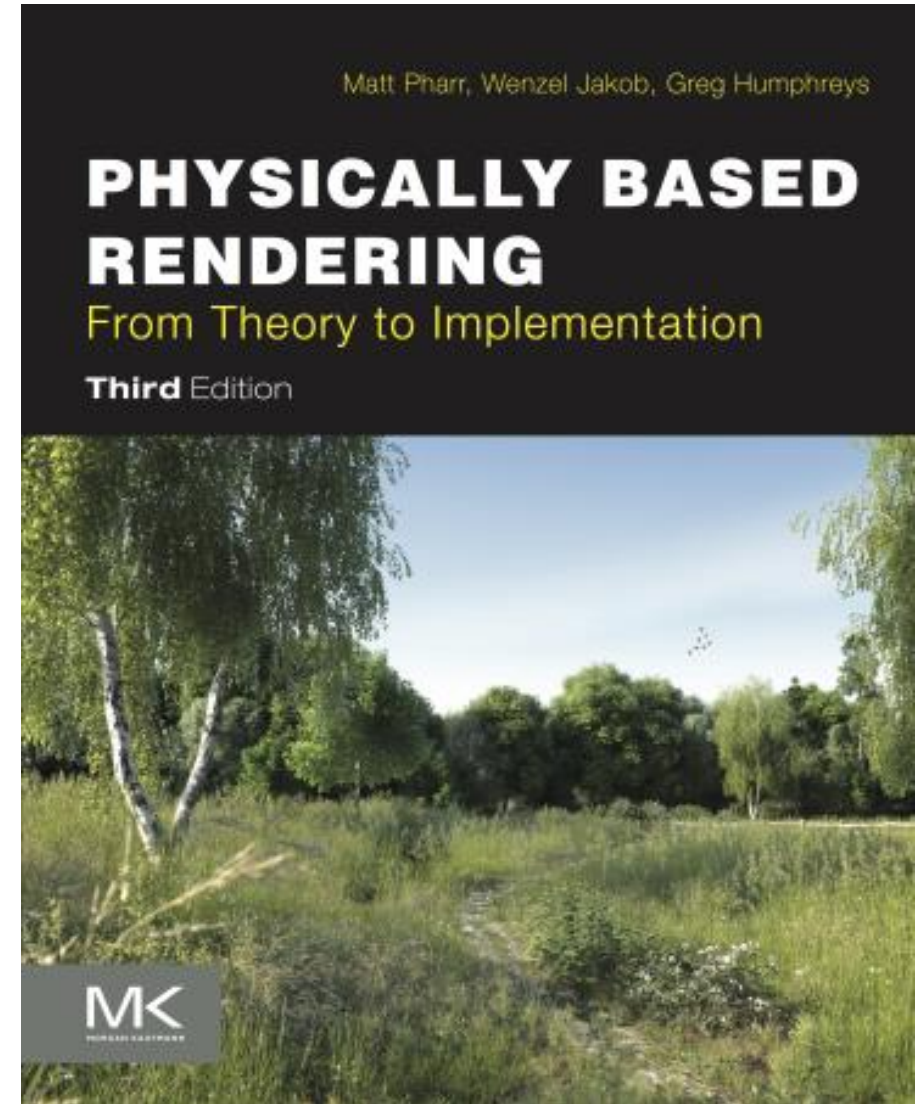


Application: image-based relighting
(later lecture)

Another way to create HDR images

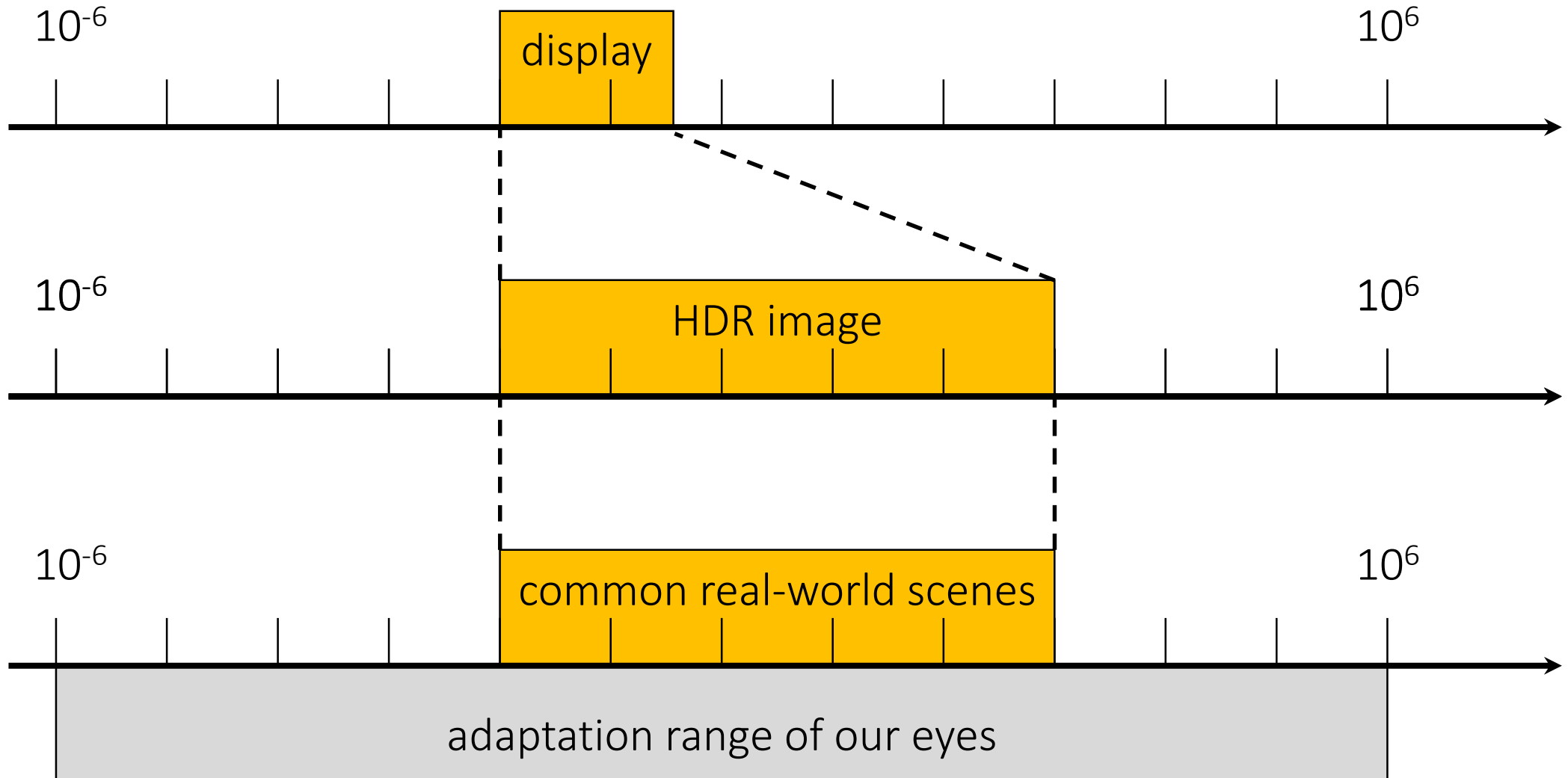
Physics-based renderers simulate radiance maps (relative or absolute)

- Their outputs are very often HDR images



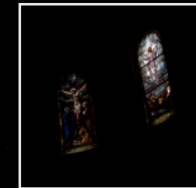
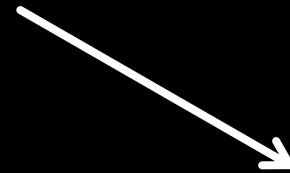
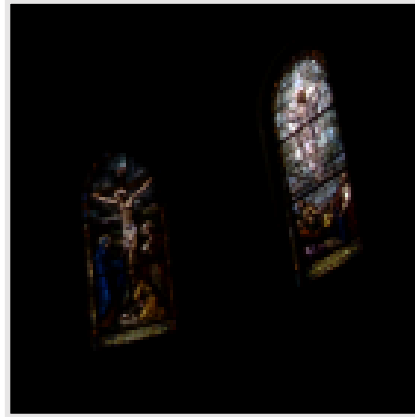
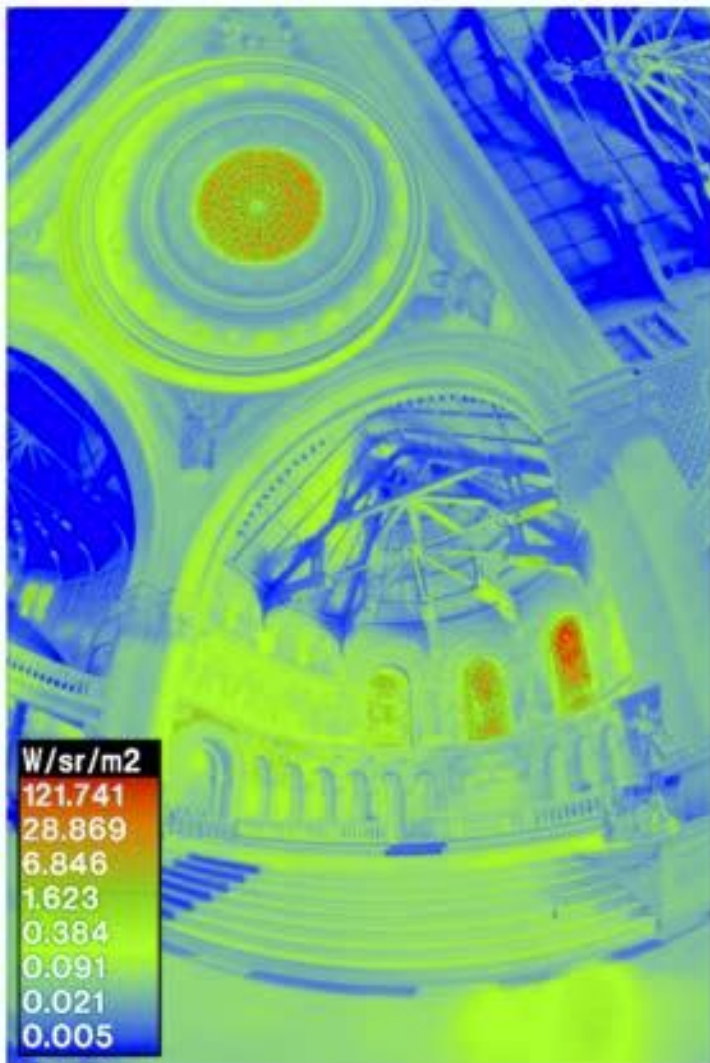
Tonemapping

How do we display our HDR images?



Linear scaling

Scale image so that maximum value equals 1

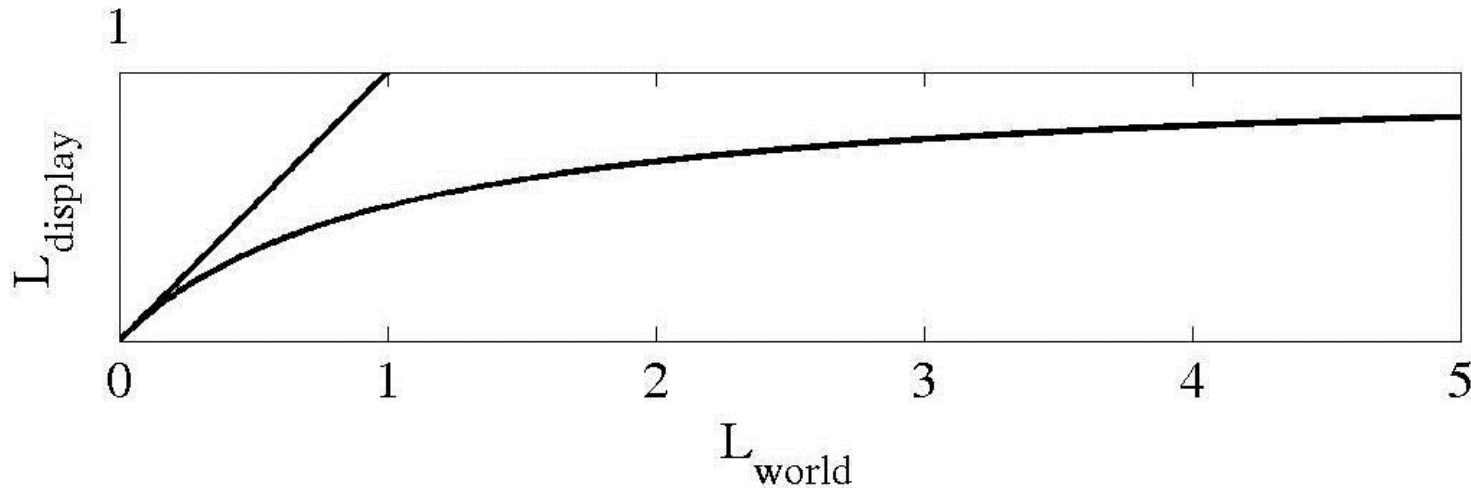


Can you think of something better?

Photographic tonemapping

Apply the same non-linear scaling to all pixels in the image so that:

- Bring everything within range \rightarrow asymptote to 1
- Leave dark areas alone \rightarrow slope = 1 near 0



$$I_{display} = \frac{I_{HDR}}{1 + I_{HDR}}$$

(exact formula more complicated)

- Photographic because designed to approximate film zone system.
- Perceptually motivated, as it approximates our eye's response curve.

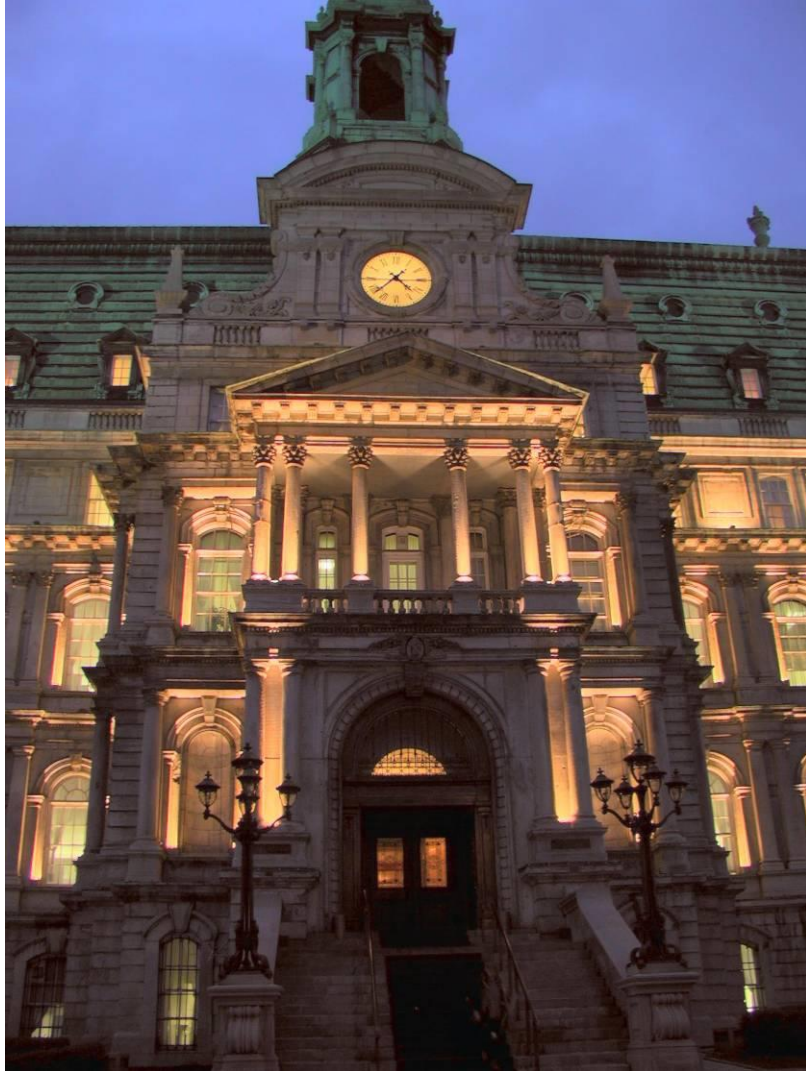
What is the zone system?

- Technique formulated by Ansel Adams for film development.
- Still used with digital photography.

		Zone	Description
		0	Pure black
		I	Near black, with slight tonality but no texture
		II	Textured black; the darkest part of the image in which slight detail is recorded
		III	Average dark materials and low values showing adequate texture
		IV	Average dark foliage, dark stone, or landscape shadows
		V	Middle gray: clear north sky; dark skin, average weathered wood
		VI	Average Caucasian skin; light stone; shadows on snow in sunlit landscapes
		VII	Very light skin; shadows in snow with acute side lighting
		VIII	Lightest tone with texture: textured snow
		IX	Slight tone without texture; glaring snow
		X	Pure white: light sources and specular reflections

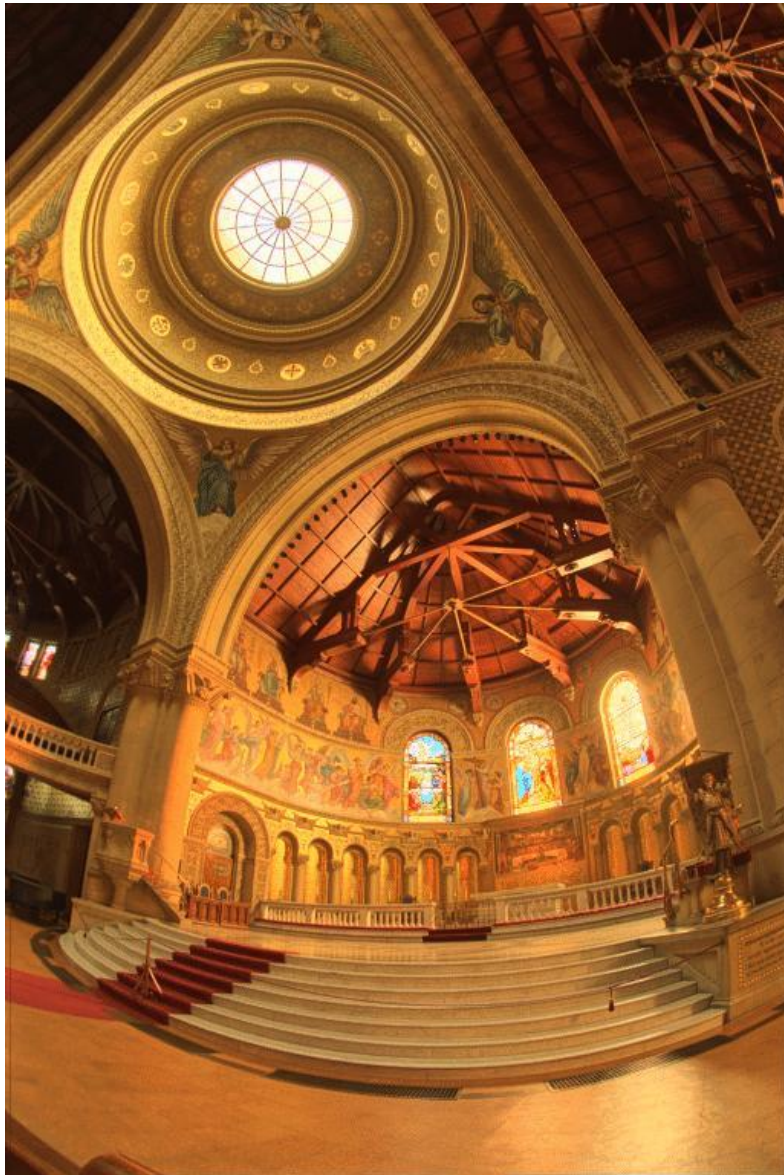


Examples

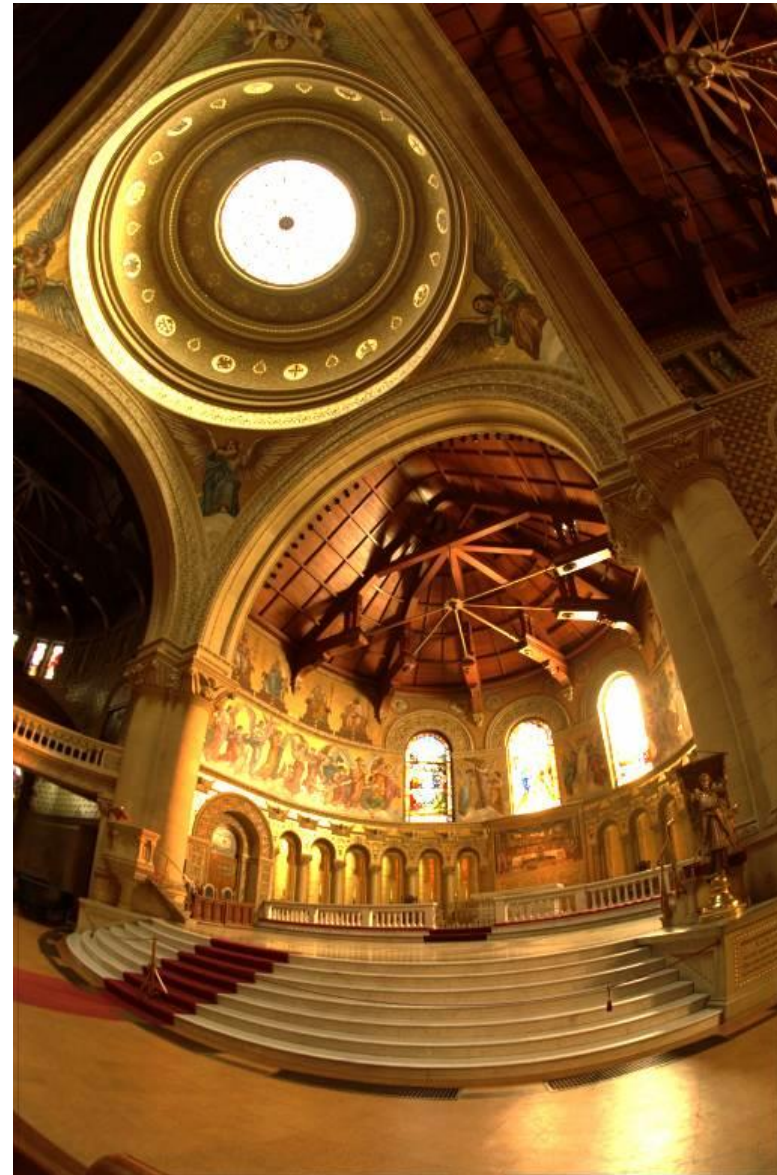


Examples

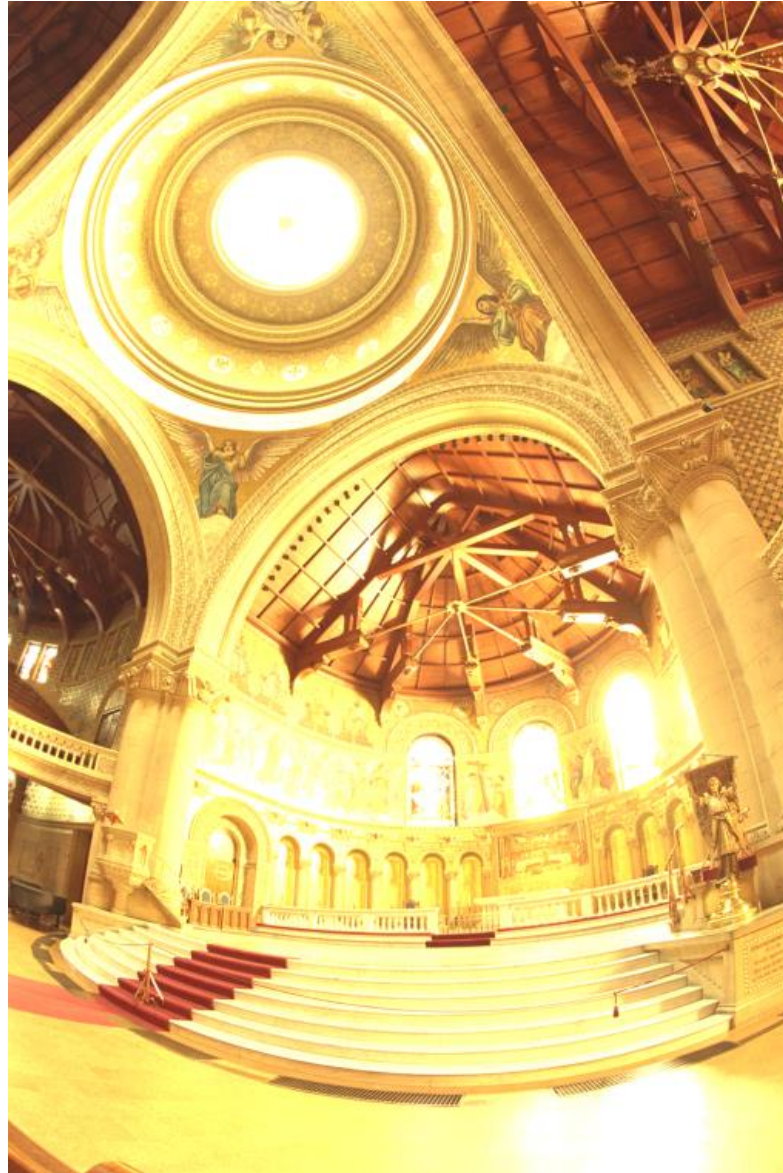
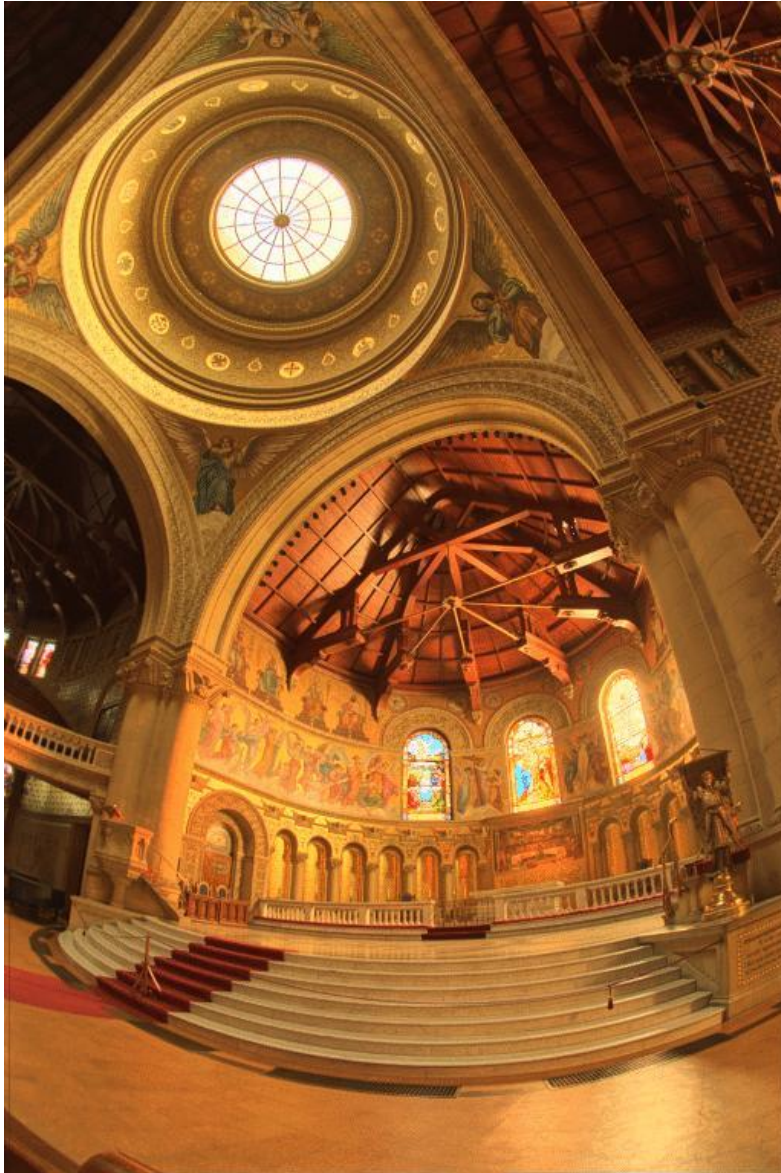
photographic
tonemapping



linear scaling
(map 10% to 1)



Compare with LDR images



Dealing with color

If we tonemap all channels the same, colors are washed out



Can you think of a way to deal with this?

Intensity-only tonemapping

tonemap
intensity



leave color
the same



How would you implement this?

Comparison

Color now OK, but some details are washed out due to loss of contrast



Can you think of a way to deal with this?

Low-frequency intensity-only tonemapping

tonemap low-frequency
intensity component



leave high-frequency
intensity component
the same



leave color the same



How would you implement this?

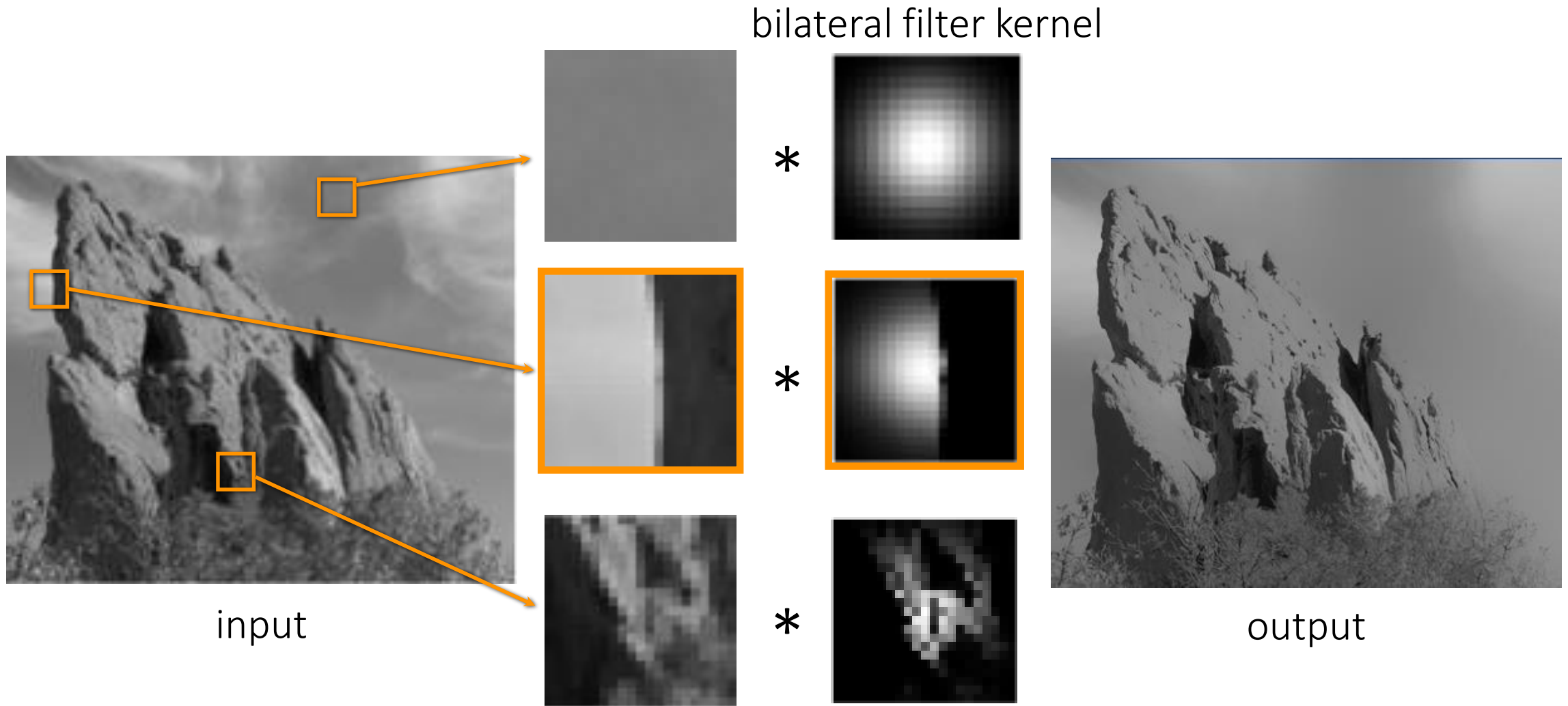
Comparison

We got nice color and contrast, but now we've run into the halo plague



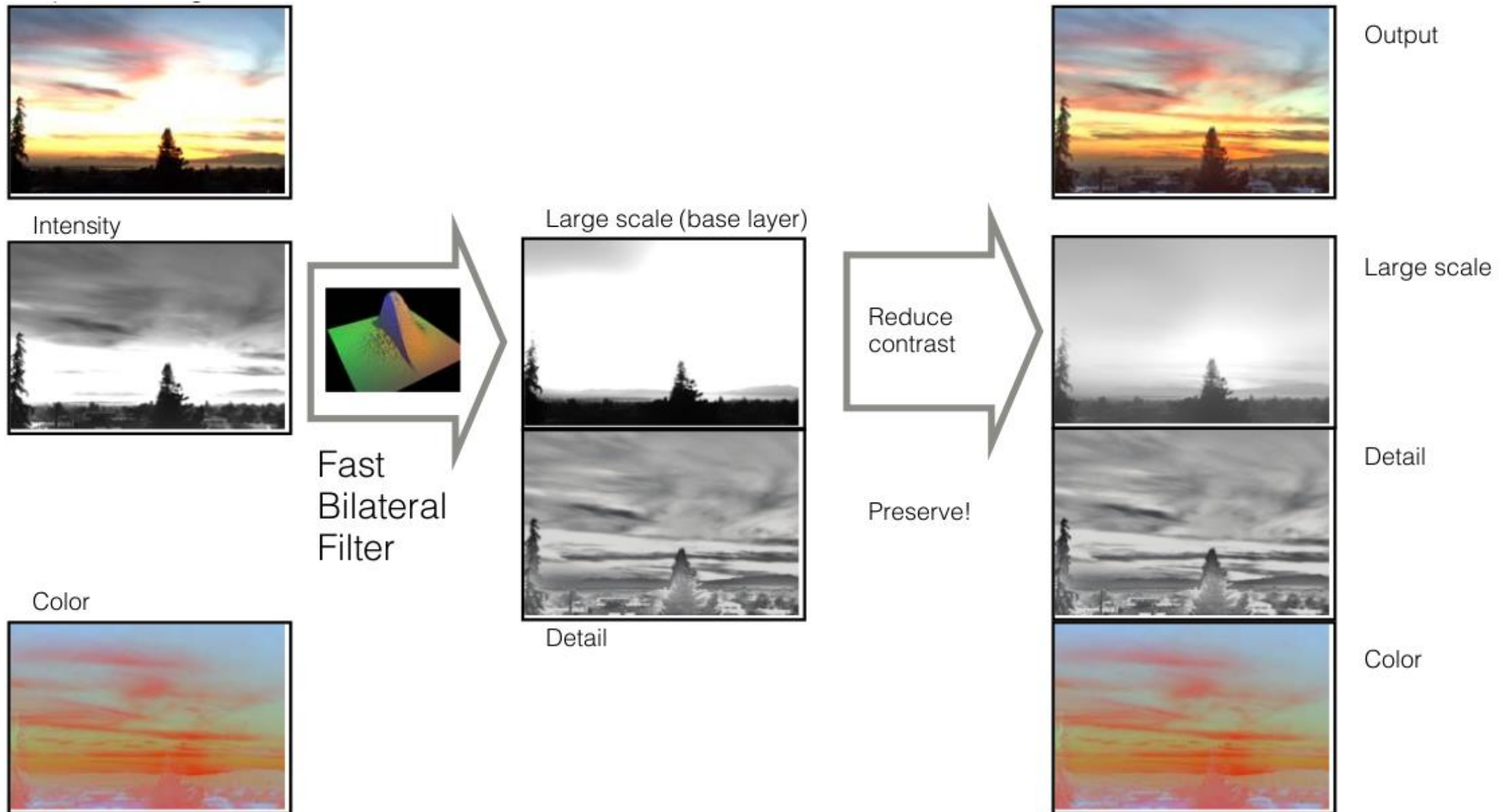
Can you think of a way to deal with this?

The bilateral filtering solution



Do not blur if there is an edge! More in lecture 7.

Tonemapping with bilateral filtering



Comparison

We fixed the halos without losing contrast





Gradient-domain merging and tonemapping

Compute gradients, scale and merge them, then integrate (solve Poisson problem).

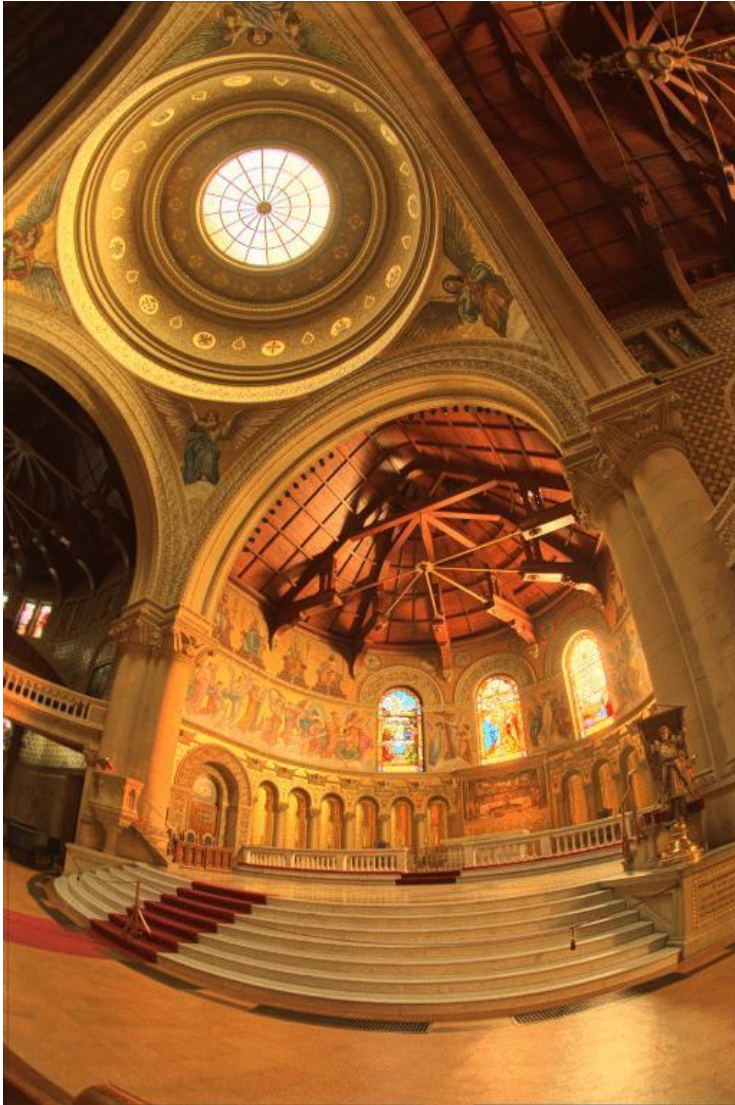
- More in lecture 8.



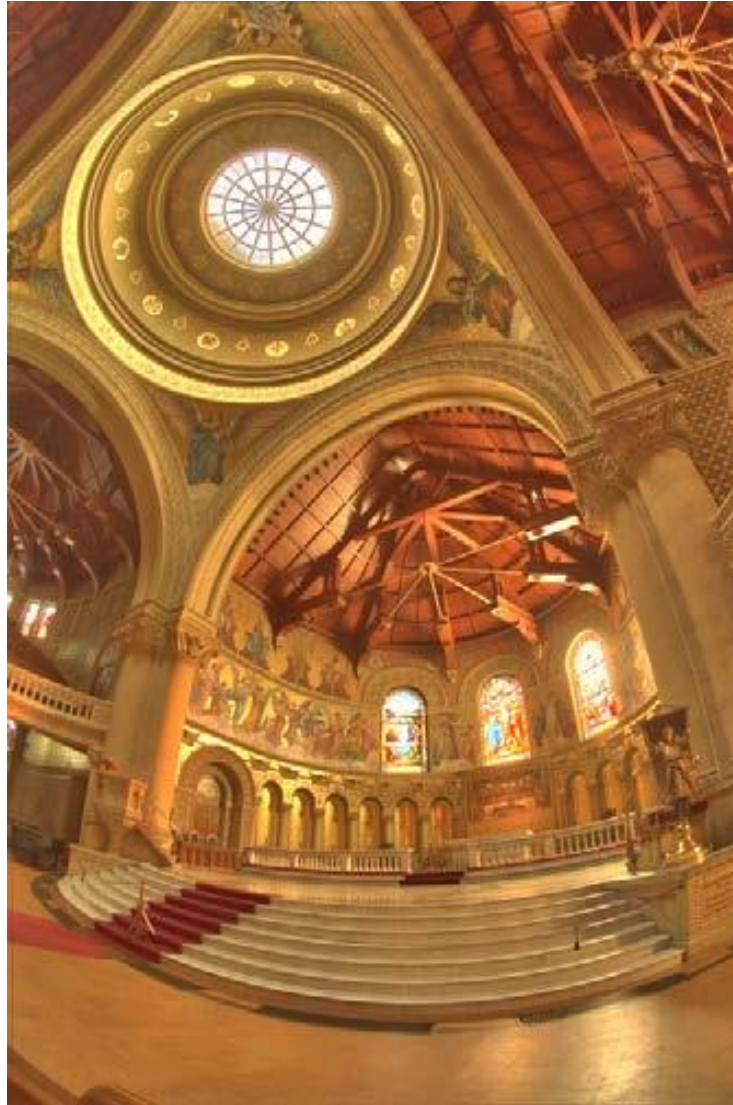
Gradient-domain merging and tonemapping



Comparison (which one do you like better?)



photographic



bilateral filtering



gradient-domain

Comparison (which one do you like better?)



bilateral filtering



gradient-domain

Comparison (which one do you like better?)

There is no ground-truth

- which one looks better is entirely subjective



bilateral filtering



gradient-domain

Tonemapping for a single image

Modern DSLR sensors capture about 3 stops of dynamic range.

- Tonemap single RAW file instead of using camera's default rendering.

result from image
processing pipeline
(basic tone
reproduction)

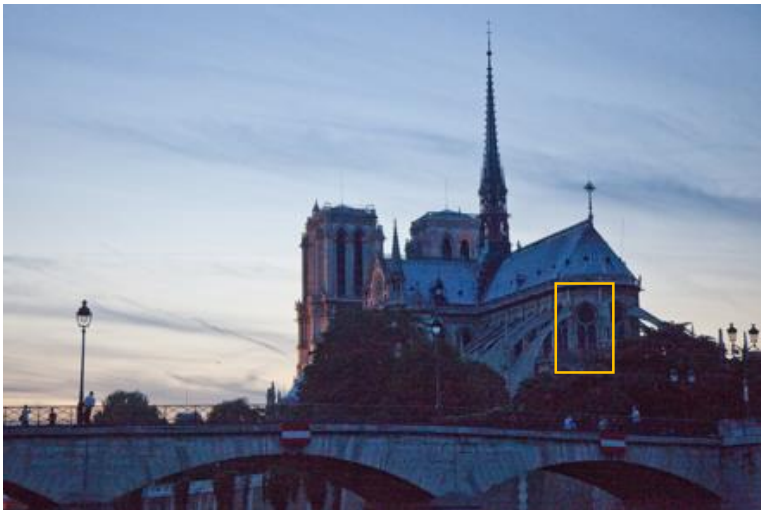


tonemapping using
bilateral filtering (I
think)

Tonemapping for a single image

Modern DSLR sensors capture about 3 stops of dynamic range.

- Tonemap single RAW file instead of using camera's default rendering.



Careful not to “tonemap” noise.

- Why is this not a problem with multi-exposure HDR?

Some notes about HDR and tonemapping

A note of caution

- HDR photography can produce very visually compelling results







A note of caution

- HDR photography can produce very visually compelling results
- It is also a very routinely abused technique, resulting in awful results









A note of caution

- HDR photography can produce very visually compelling results
- It is also a very routinely abused technique, resulting in awful results
- The problem is tonemapping, not HDR itself

A note about HDR today

- Most cameras (even phone cameras) have automatic HDR modes/apps
- Popular-enough feature that phone manufacturers are actively competing about which one has the best HDR
- The technology behind some of those apps (e.g., Google's HDR+) is published in SIGGRAPH and SIGGRAPH Asia conferences

Burst photography for high dynamic range and low-light imaging on mobile cameras

Samuel W. Hasinoff
Jonathan T. Barron

Dillon Sharlet
Florian Kainz
Google Research

Ryan Geiss
Jiawen Chen

Andrew Adams
Marc Levoy



Figure 1: A comparison of a conventional camera pipeline (left, middle) and our burst photography pipeline (right) running on the same cell-phone camera. In this low-light setting (about 0.7 lux), the conventional camera pipeline underexposes (left). Brightening the image (middle) reveals heavy spatial denoising, which results in loss of detail and an unpleasantly blotchy appearance. Fusing a burst of images increases the signal-to-noise ratio, making aggressive spatial denoising unnecessary. We encourage the reader to zoom in. While our pipeline excels in low-light and high-dynamic-range scenes (for an example of the latter see figure 10), it is computationally efficient and reliably artifact-free, so it can be deployed on a mobile camera and used as a substitute for the conventional pipeline in almost all circumstances. For readability the figure has been made uniformly brighter than the original photographs.

Abstract

Cell phone cameras have small apertures, which limits the number of photons they can gather, leading to noisy images in low light. They also have small sensor pixels, which limits the number of electrons each pixel can store, leading to limited dynamic range. We describe a computational photography pipeline that captures, aligns, and merges a burst of frames to reduce noise and increase dynamic range. Our system has several key features that help make it robust and efficient. First, we do not use bracketed exposures. Instead, we capture frames of constant exposure, which makes alignment more robust, and we set this exposure low enough to avoid blowing out highlights. The resulting merged image has clean shadows and high bit depth, allowing us to apply standard HDR tone mapping methods. Second, we begin from Bayer raw frames rather than the demosaicked RGB (or YUV) frames produced by hardware Image Signal Processors (ISPs) common on mobile platforms. This gives us more bits per pixel and allows us to circumvent the ISP's unwanted tone mapping and spatial denoising. Third, we use a novel FFT-based alignment algorithm and a hybrid 2D/3D Wiener filter to denoise and merge the frames in a burst. Our implementation is built atop Android's Camera2 API, which provides per-frame camera control and access to raw imagery, and is written in the Halide domain-specific language (DSL). It runs in 4 seconds on device (for a 12 Mpix image), requires no user intervention, and ships on several mass-produced cell phones.

Keywords: computational photography, high dynamic range

Concepts: •Computing methodologies → Computational photography; Image processing;

1 Introduction

The main technical impediment to better photographs is lack of light. In indoor or night-time shots, the scene as a whole may provide insufficient light. The standard solution is either to apply analog or digital gain, which amplifies noise, or to lengthen exposure time, which causes motion blur due to camera shake or subject motion. Surprisingly, daytime shots with high dynamic range may also suffer from lack of light. In particular, if exposure time is reduced to avoid

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References

Basic reading:

- Szeliski textbook, Sections 10.1, 10.2.
- Debevec and Malik, “Recovering High Dynamic Range Radiance Maps from Photographs,” SIGGRAPH 1997.
the paper that more or less started HDR imaging research in computer graphics.
- Reinhard et al., “Photographic Tone Reproduction for Digital Images,” SIGGRAPH 2002.
the photographic tonemapping paper, including a very nice discussion of the zone system for film.
- Durand and Dorsey, “Fast bilateral filtering for the display of high-dynamic-range images,” SIGGRAPH 2002.
the paper on tonemapping using bilateral filtering.
- Fattal et al., “Gradient Domain High Dynamic Range Compression,” SIGGRAPH 2002.
the paper on gradient-domain tonemapping.

Additional reading:

- Reinhard et al., “High Dynamic Range Imaging, Second Edition: Acquisition, Display, and Image-Based Lighting,” Morgan Kaufmann 2010
a very comprehensive book about everything relating to HDR imaging and tonemapping.
- Kuang et al., “Evaluating HDR rendering algorithms,” TAP 2007.
one of many, many papers trying to do a perceptual evaluation of different tonemapping algorithms.
- Debevec, “Rendering Synthetic Objects into Real Scenes: Bridging Traditional and Image-Based Graphics with Global Illumination and High Dynamic Range Photography,” SIGGRAPH 1998.
the original HDR light probe paper (we’ll see more about this in a later lecture).
- Hasinoff and Kutulakos, “Multiple-Aperture Photography for High Dynamic Range and Post-Capture Refocusing,” UofT TR 2009
a paper on doing HDR by aperture bracketing instead of exposure bracketing.
- Hasinoff et al., “Noise-Optimal Capture for High Dynamic Range Photography,” CVPR 2010
a paper on weighting different exposures based on a very detailed sensor noise model.
- Hasinoff et al., “Burst photography for high dynamic range and low-light imaging on mobile cameras,” SIGGRAPH Asia 2016
the paper describing Google’s HDR+.
- Ward, “The radiance lighting simulation and rendering system,” SIGGRAPH 1994
the paper that introduced (among other things) the .hdr image format for HDR images.