Computational light transport



15-463, 15-663, 15-862 Computational Photography Fall 2017, Lecture 22

http://graphics.cs.cmu.edu/courses/15-463

Course announcements

- Make-up lecture on Friday, noon-1:30pm, NSH 3002.
 - Same room and time as previous make-up lecture.
- Sign-up for final project checkpoint meeting.
 - Moved to Monday-Tuesday,
 - Email me if you cannot make it then.
- Any questions about homework 5?

Overview of today's lecture

- The light transport matrix.
- Image-based relighting.
- Photometric stereo.
- Optical computing using the light transport matrix.
- Dual photography.

Slide credits

These slides were directly adapted from:

• Matt O'Toole (Stanford).

The light transport matrix







How do these three images relate to each other?







How do these three images relate to each other?

the superposition principle







photo taken under two light sources =
sum of photos taken under each source individually

the superposition principle





photo taken under two light sources = sum of photos taken under each source individually

the superposition principle



why is the error not exactly zero?



photo taken under two light sources = sum of photos taken under each source individually



photo with light 1 turned on











Weight 1

1

X







photo with light 2 turned on

Weight 2

x 0







Weight 1

Weight 2

x







Weight 1 $_{x}$ l_{1} +













Weight 1 $\left| \begin{smallmatrix} \mathsf{ph}_{\mathsf{on}} \\ \mathsf{on} \end{smallmatrix} \right|_{\mathsf{X}} \left| \begin{smallmatrix} \mathsf{l}_{\mathsf{1}} \end{smallmatrix} \right| + \left| \begin{smallmatrix} \mathsf{ph}_{\mathsf{on}} \\ \mathsf{on} \end{smallmatrix} \right|_{\mathsf{X}}$











n pixel values









n pixel values

















Weight 1 \mathbf{I}_{1} +X



 $\mathbf{x} | \mathbf{l_2}$



 $n \times m$

case where we have a very large m?



Acquiring the Reflectance Field [Debevec et al. 2000]

image-based rendering & relighting





Reflectance field

Acquiring the Reflectance Field

image-based rendering & relighting



https://www.youtube.com/watch? v=mkzLLz1tXds

Debevec et al, SIG 2000

Acquiring the Reflectance Field



Light stage 6, Debevec et al., 2006

Photometric stereo

the light transport matrix

Sloan et al 02, Ng et al 03, Seitz et al 05, Sen et al 05, ...



transport matrix is a function of scene geometry, reflectance, etc.

Recovering Scene Geometry



"Mobile" Light Stage, Debevec et al., 2014

https://www.youtube.com/watch? v=4GiLAOtjHNo



camera pixel i and light source \jmath produce image intensity $\, {f t}_{ij}$



Diffuse reflections:



camera pixel i and light source j produce image intensity \mathbf{t}_{ij}



Diffuse reflections:

 $\mathbf{t}_{ij} = \rho_i (N_i \cdot L_j) l_j$ \tilde{L}_{i}



camera pixel i and light source j produce image intensity \mathbf{t}_{ij}



camera pixel i and light source j produce image intensity \mathbf{t}_{ij}

Diffuse reflections:

 $\mathbf{t}_{ij} = \rho_i (N_i \cdot L_j) l_j$ $= \tilde{N}_i \cdot \tilde{L}_i$ 3x1 vector, 3x1 vector, unknown known


Diffuse reflections:



camera pixel i and light source j produce image intensity \mathbf{t}_{ij}

What assumptions have we made here?



camera pixel i and light source j produce image intensity \mathbf{t}_{ij}

Diffuse reflections:

What is this? $\mathbf{t}_{ij} = \rho_i (N_i \cdot L_j) l_j$ $= \tilde{N}_i \cdot \tilde{L}_j$ 3x1 vector, 3x1 vector, x1 vector, xnown

simplifying assumptions: directional light source, convex object



 $n \times m$

Diffuse reflections:



simplifying assumptions: directional light source, convex object



recover surface normals + albedo by decomposing transport matrix $\, {igsin} \,$

Optical computing using the light transport matrix

Input images:







Height map

question: what are the challenges with analyzing ${f T}$?



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• matrix can be extremely large

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- matrix can be extremely large
- elements not directly accessible

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- matrix can be extremely large
- elements not directly accessible
- global structure poorly understood











find an illumination pattern that when projected onto scene, we get the same photo back (multiplied by a scalar)

project



capture



What do we call these patterns?

computing transport eigenvectors



eigenvector of a square matrix T when projected onto scene, we get the same photo back (multiplied by a scalar)

project



capture



numerical goal find ${\bf l},\lambda$ such that ${f Tl}=\lambda {f l}$ and λ is maximal

goal: find principal eigenvector of Tobservation: it is a fixed point of the sequence $1, T1, T^21, T^31, ...$

numerical domain

function $PowerIt(\mathbf{T})$

$\mathbf{l}_1 = \text{initial vector}$

$$\mathbf{for} \ i = 1 \ \mathrm{to} \ k \ \{ \mathbf{p}_i = \mathbf{Tl}_i \ \end{bmatrix}$$

$$\mathbf{l}_{i+1} = \mathbf{p}_i / \|\mathbf{p}_i\|_2$$

return \mathbf{l}_{i+1}

properties

- linear convergence [Trefethen and Bau 1997]
- eigenvalues must be distinct
- l₁ cannot be orthogonal to principal eigenvector

















goal: find principal eigenvector of Tobservation: it is a fixed point of the sequence $\mathbf{l}, \mathbf{Tl}, \mathbf{T^2l}, \mathbf{T^3l}, \ldots$

project

capture











How would you measure the light transport matrix T?

- matrix can be extremely large
- elements not directly accessible
- global structure poorly understood

How would you measure the light transport matrix T?

Exhaustive/naïve approach: turn on projector pixels one at a time and take a photo for each of them.

What does each photo correspond to in T?

How would you measure the light transport matrix T?

Exhaustive/naïve approach: turn on projector pixels one at a time and take a photo for each of them.

How many photos do we need to capture?

numerical goal given photo p, find illumination 1 that minimizes

remarks

- \mathbf{T} low-rank or high-rank
- ${f T}$ unknown & not acquired
- illumination sequence will be specific to input photo

input photo
inverting light transport





illumination

inverting light transport



input photo



actual illumination

Dual photography

Helmholtz reciprocity



References

Basic reading:

- Sloan et al., "Precomputed radiance transfer for real-time rendering in dynamic, low-frequency lighting environments," SIGGRAPH 2002.
- Ng et al., "All-frequency shadows using non-linear wavelet lighting approximation," SIGGRAPH 2003.
- Seitz et al., "A theory of inverse light transport," ICCV 2005. these three papers all discuss the concept of light transport matrix in detail.
- Debevec et al., "Acquiring the reflectance field of a human face," SIGGRAPH 2000. the paper on image-based relighting.
- Woodham et al., "Photometric stereo: A reflectance map technique for determining surface orientation from image intensity," IUSIA 1979.

the original photometric stereo paper.

• O'Toole and Kutulakos, "Optical computing for fast light transport analysis," SIGGRAPH Asia 2010.

the paper on eigenanalysis and optical computing using light transport matrices.

• Sen et al., "Dual photography," SIGGRAPH 2005.

the dual photography paper.

Additional reading:

- Peers et al., "Compressive light transport sensing," TOG 2009.
- Wang et al., "Kernel Nyström method for light transport," SIGGRAPH 2009. these two papers discuss alternative ways for efficient acquisition of the light transport matrix, using assumptions on its algebraic structure.