### More Single View Geometry



*Cyclops* Odilon Redon 1904

...with a lot of slides stolen from Steve Seitz

15-463: Computational Photography Alexei Efros, CMU, Fall 2011

# Quiz: which is 1,2,3-point perspective

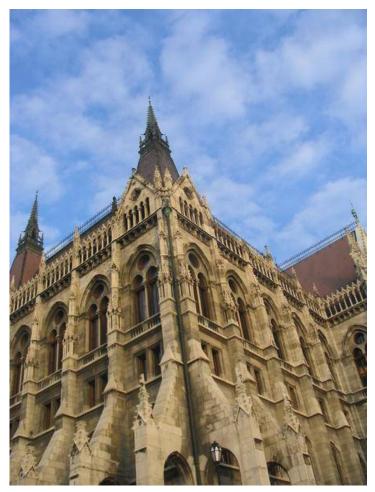


Image A

Image B

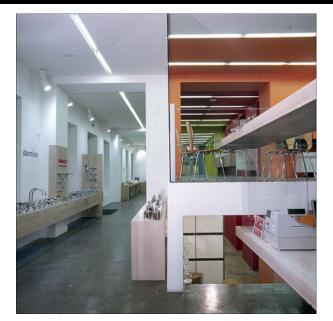




Image C

# Automatic Photo Pop-up



Original Image



**Geometric Labels** 



Fit Segments



Cut and Fold



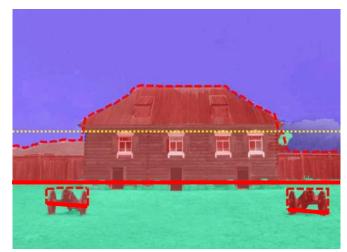
**Novel View** 

#### Results



Input Image



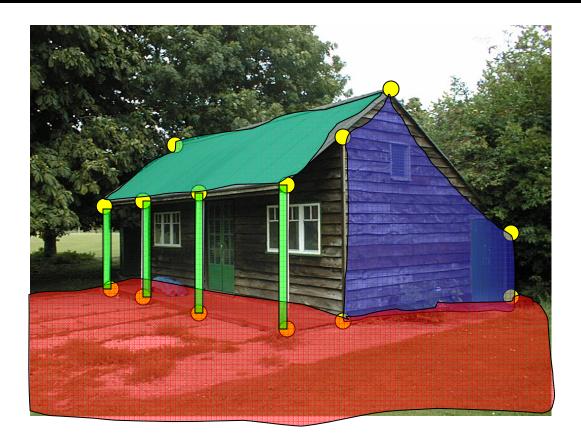


Cut and Fold



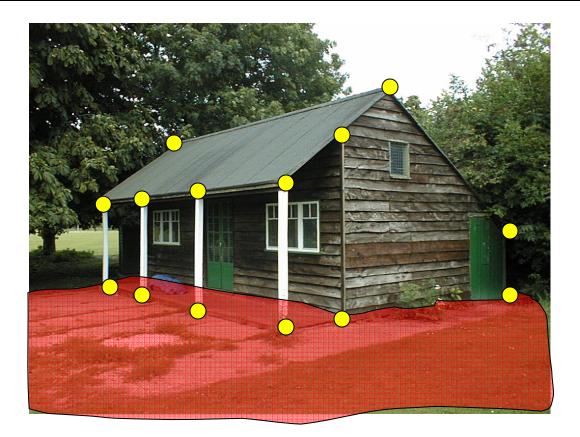
Automatic Photo Pop-up

#### How can we model more complex scene?



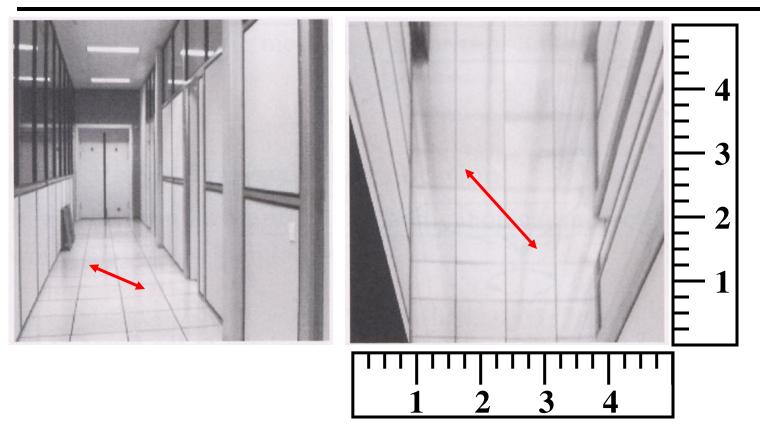
- 1. Find world coordinates (X,Y,Z) for a few points
- 2. Connect the points with planes to model geometry
  - Texture map the planes

# Finding world coordinates (X,Y,Z)



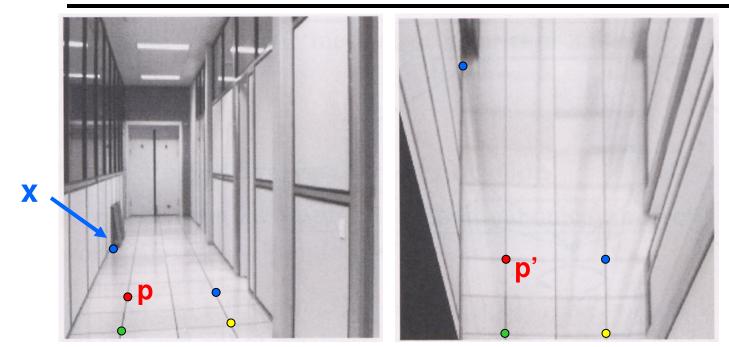
- 1. Define the ground plane (Z=0)
- 2. Compute points (X,Y,0) on that plane
- 3. Compute the *heights* Z of all other points

### Measurements on planes



Approach: unwarp, then measure What kind of warp is this?

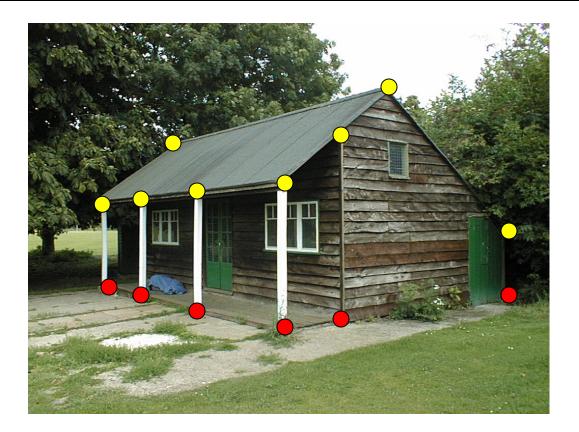
### Unwarp ground plane



Our old friend – the homography Need 4 reference points with world coordinates

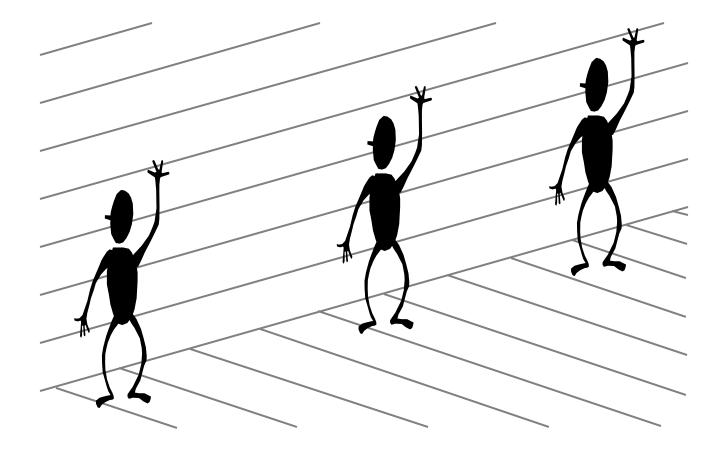
$$p = (x,y)$$
  
 $p' = (X,Y,0)$ 

# Finding world coordinates (X,Y,Z)

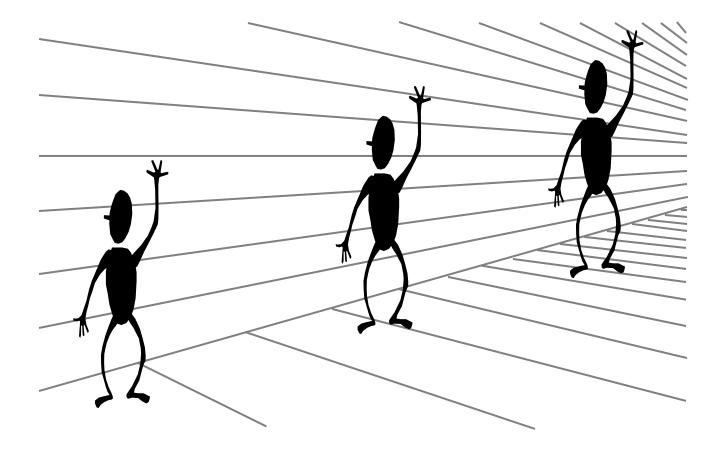


- 1. Define the ground plane (Z=0)
- 2. Compute points (X,Y,0) on that plane
- 3. Compute the *heights* Z of all other points

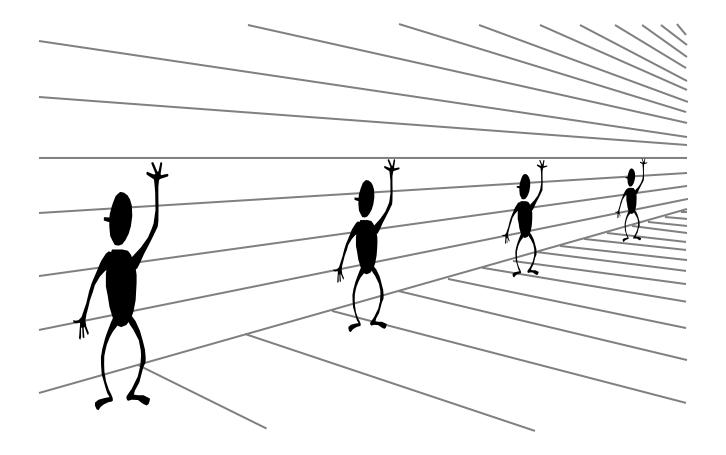
## Comparing heights



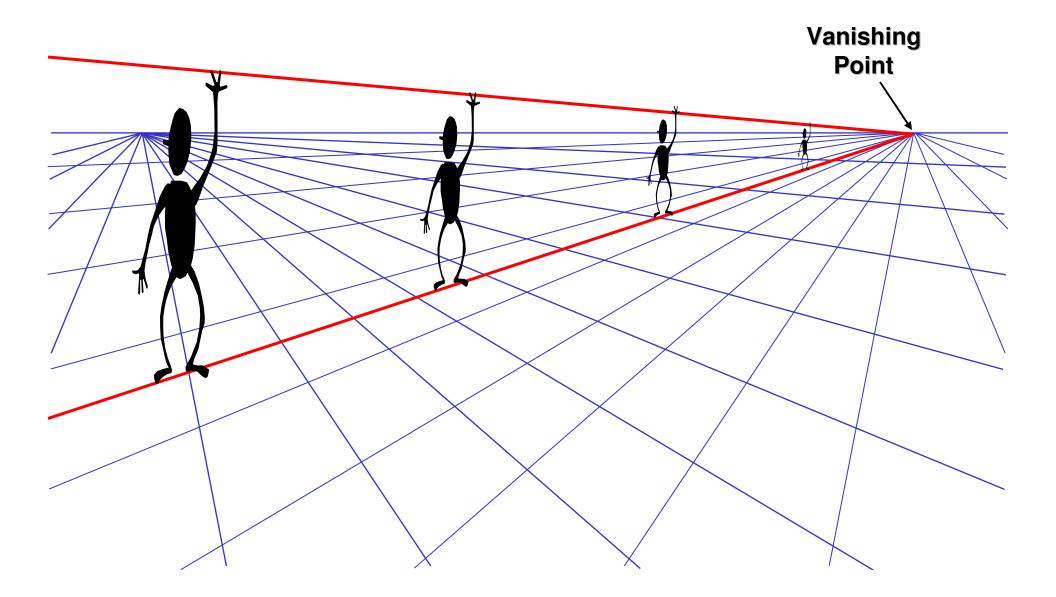
# Perspective cues



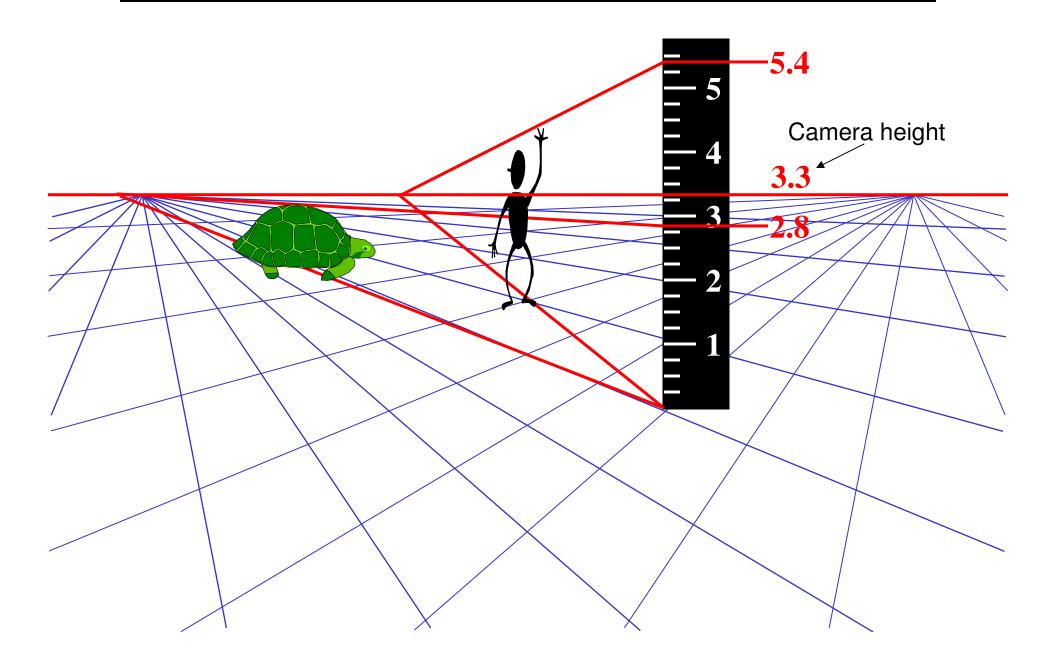
### Perspective cues



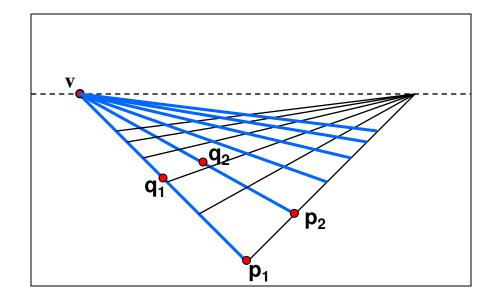
# Comparing heights



### Measuring height



# Computing vanishing points (from lines)



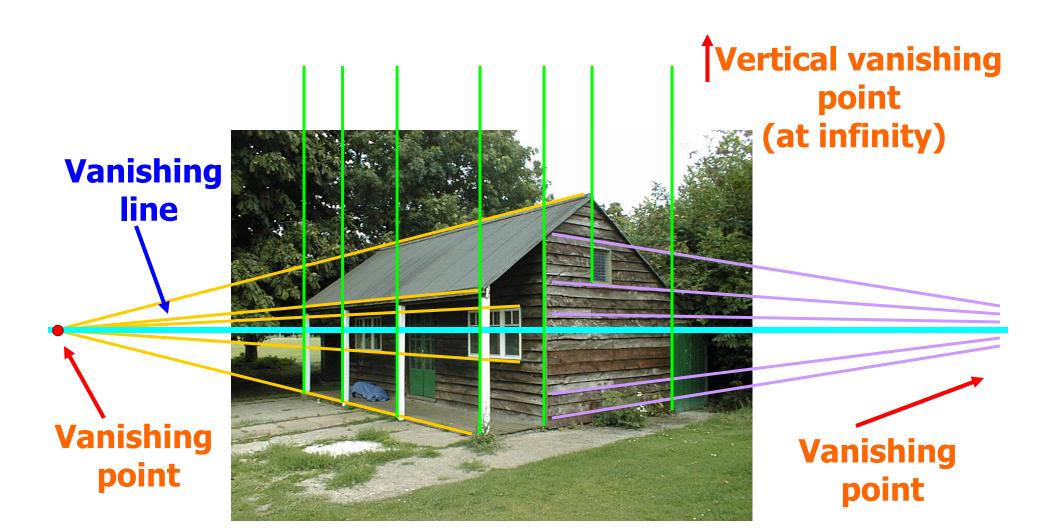
Intersect  $p_1q_1$  with  $p_2q_2$ 

$$v = (p_1 \times q_1) \times (p_2 \times q_2)$$

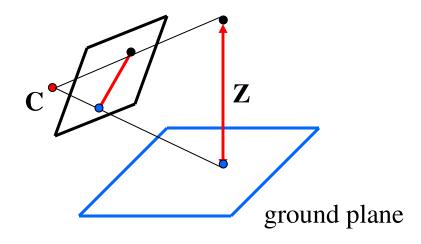
Least squares version

- Better to use more than two lines and compute the "closest" point of intersection
- See notes by <u>Bob Collins</u> for one good way of doing this:
  - <u>http://www-2.cs.cmu.edu/~ph/869/www/notes/vanishing.txt</u>

### Criminisi '99



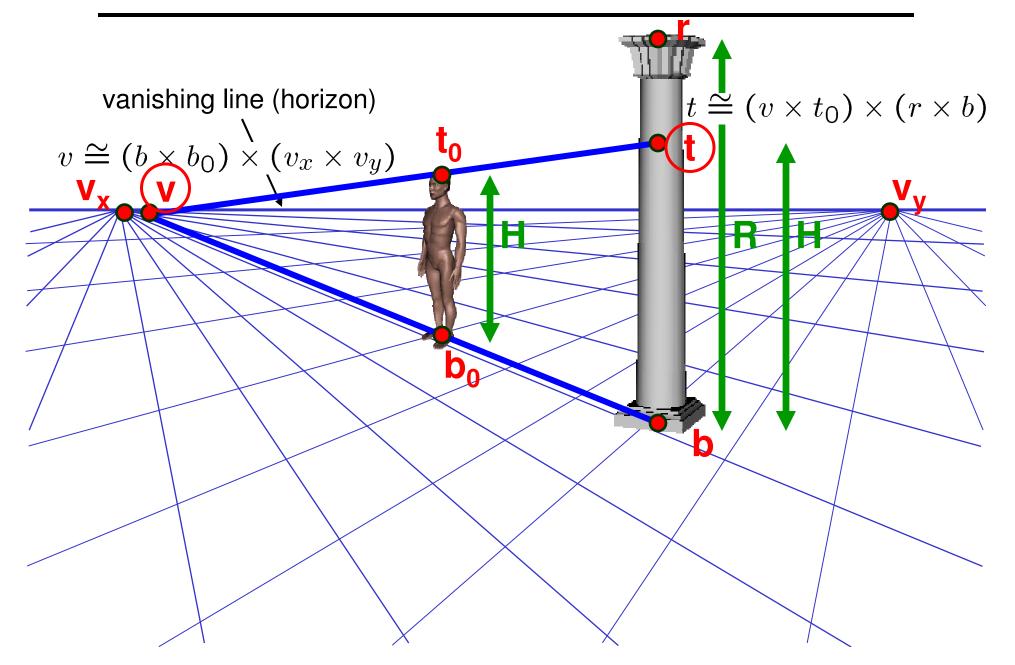
## Measuring height without a ruler



Compute Z from image measurements

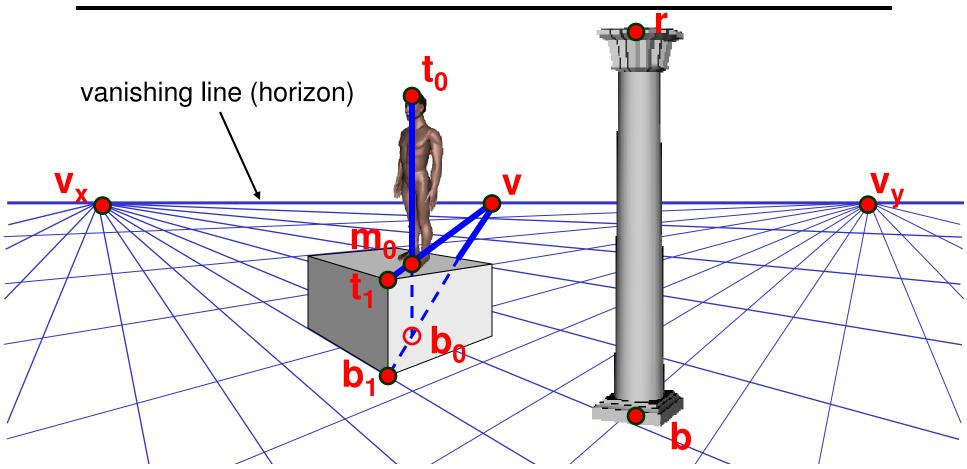
• Need more than vanishing points to do this

## Measuring height



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# Measuring height

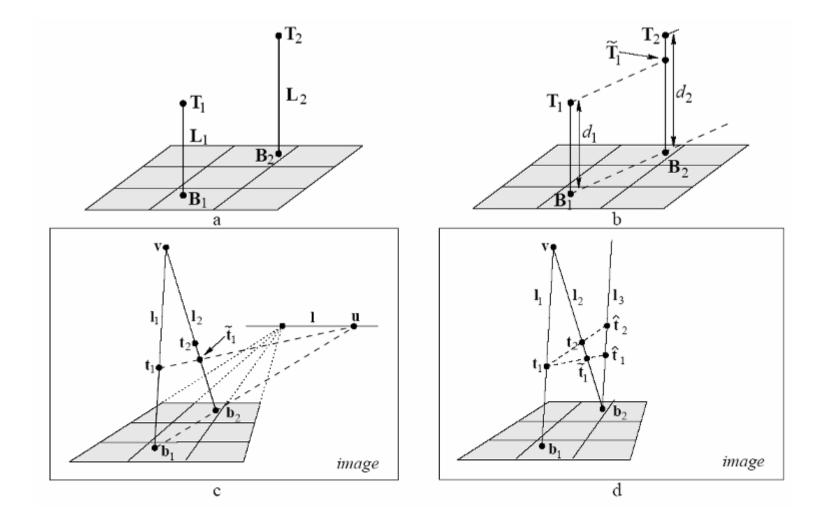


What if the point on the ground plane  $\mathbf{b}_0$  is not known?

- Here the guy is standing on the box
- Use one side of the box to help find  $\mathbf{b}_0$  as shown above

# What if $v_z$ is not infinity?





#### The cross ratio

- A Projective Invariant
  - Something that does not change under projective transformations (including perspective projection)

The cross-ratio of 4 collinear points

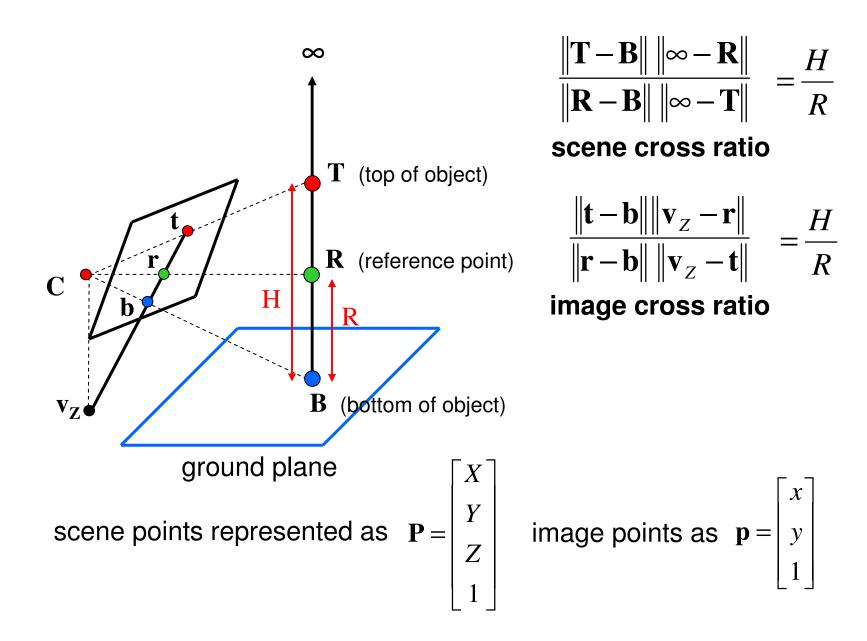
$$\mathbf{P}_{3} \mathbf{P}_{4} \qquad \frac{\left\|\mathbf{P}_{3}-\mathbf{P}_{1}\right\| \left\|\mathbf{P}_{4}-\mathbf{P}_{2}\right\|}{\left\|\mathbf{P}_{3}-\mathbf{P}_{2}\right\| \left\|\mathbf{P}_{4}-\mathbf{P}_{1}\right\|} \qquad \mathbf{P}_{i} = \begin{bmatrix} X_{i} \\ Y_{i} \\ Z_{i} \\ 1 \end{bmatrix}$$

Can permute the point ordering

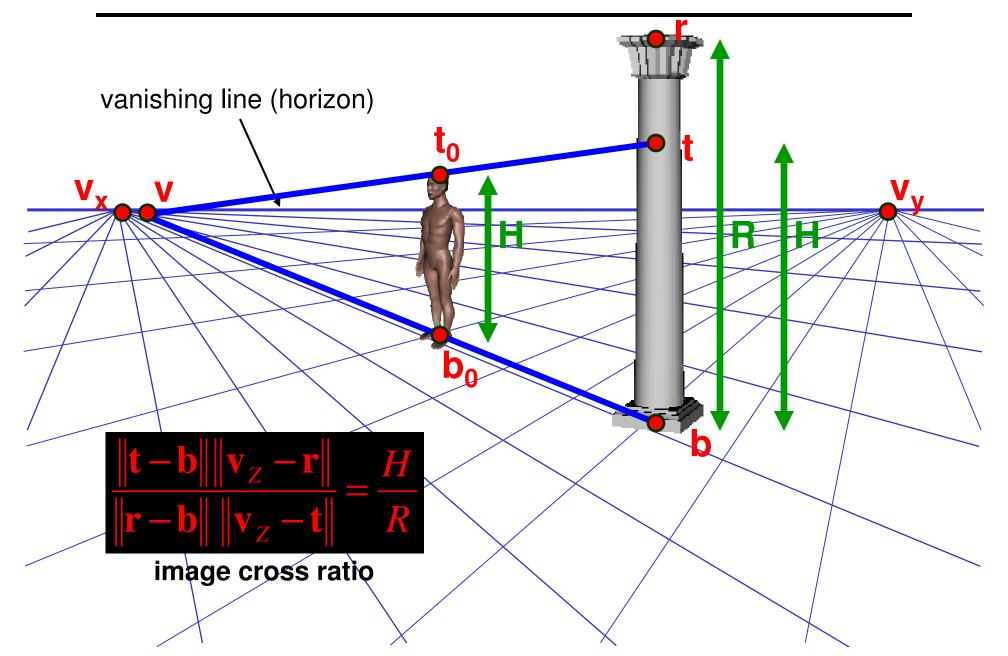
 $\frac{\|\mathbf{P}_1 - \mathbf{P}_3\| \|\mathbf{P}_4 - \mathbf{P}_2\|}{\|\mathbf{P}_1 - \mathbf{P}_2\| \|\mathbf{P}_4 - \mathbf{P}_3\|}$ 

• 4! = 24 different orders (but only 6 distinct values) This is the fundamental invariant of projective geometry

# Measuring height

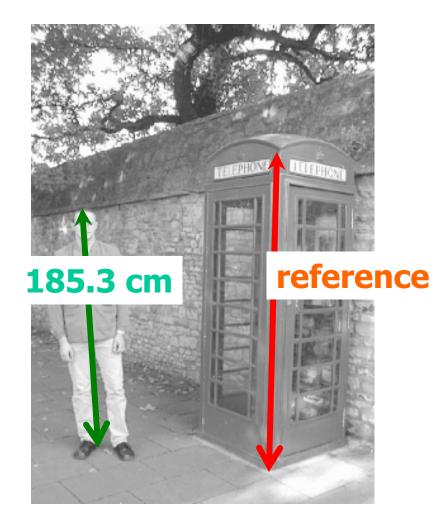


## Measuring height



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### Measuring heights of people



#### Here we go !

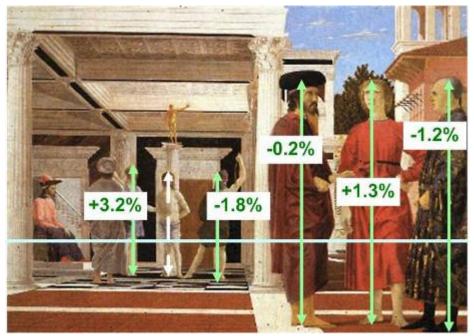
#### Forensic Science: measuring heights of suspects



#### Assessing geometric accuracy

# Are the heights of the 2 groups of people consistent with each other?

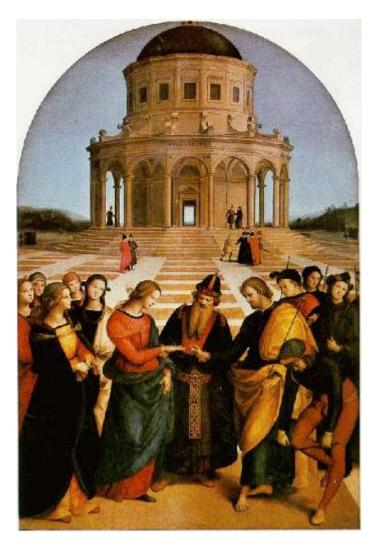




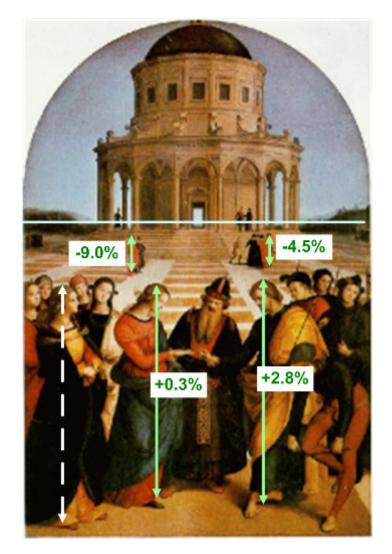
# *Flagellation*, Piero della Francesca

#### **Estimated relative heights**

#### Assessing geometric accuracy



*The Marriage of the Virgin*, Raphael



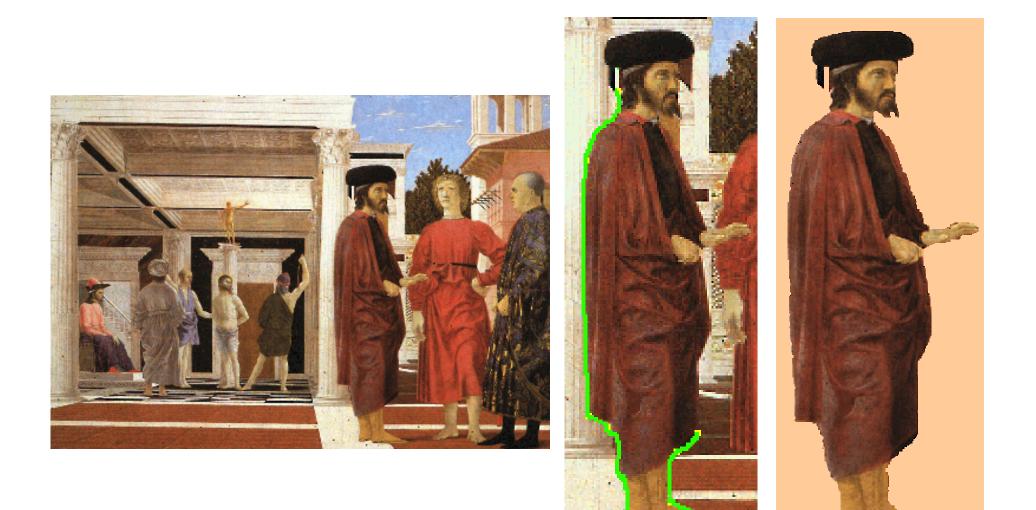
**Estimated relative heights** 

# Criminisi et al., ICCV 99

#### Complete approach

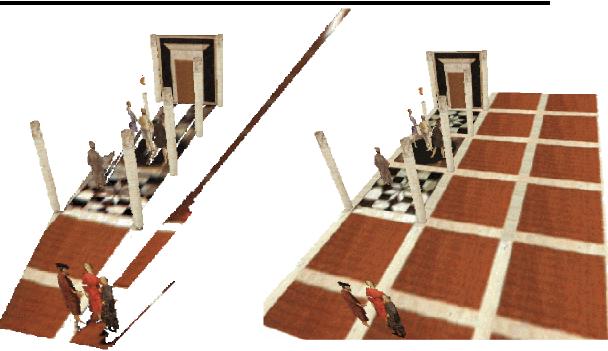
- Load in an image
- Click on lines parallel to X axis
  - repeat for Y, Z axes
- Compute vanishing points
- Specify 3D and 2D positions of 4 points on reference plane
- Compute homography H
- Specify a reference height
- Compute 3D positions of several points
- Create a 3D model from these points
- Extract texture maps
  - Cut out objects
  - Fill in holes
- Output a VRML model

#### Interactive silhouette cut-out



#### Occlusion filling





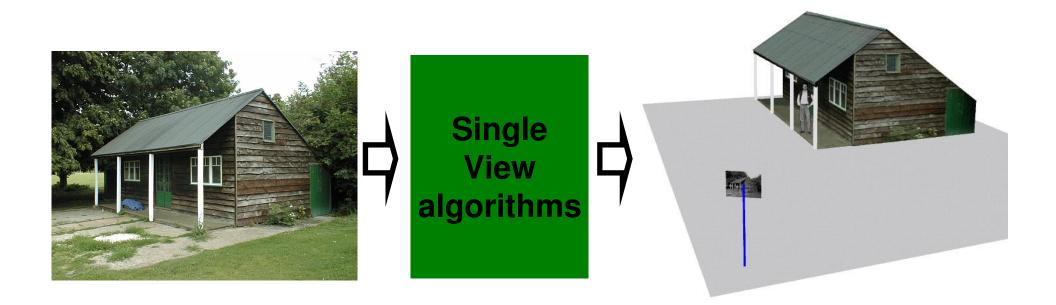
#### Geometric filling by exploiting:

- symmetries
- repeated regular patterns

**Texture synthesis** 

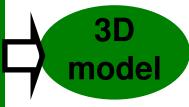
• repeated stochastic patterns

#### **Complete 3D reconstruction**





Planar measurements
Height measurements
Automatic vanishing point/line computation
Interactive segmentation
Occlusion filling
Object placement in 3D model



# A virtual museum @ Microsoft



A.Criminisi http://research.microsoft.com/~antcrim/