

# High Dynamic Range Images

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*...with a lot of slides  
stolen from Paul Debevec*

15-463: Computational Photography  
Alexei Efros, CMU, Fall 2008

# The Grandma Problem



# Problem: Dynamic Range

The real world is  
high dynamic range.



1



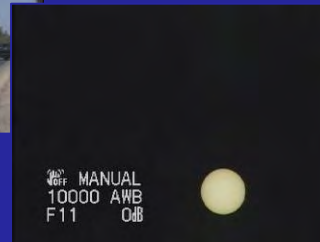
1500



25,000

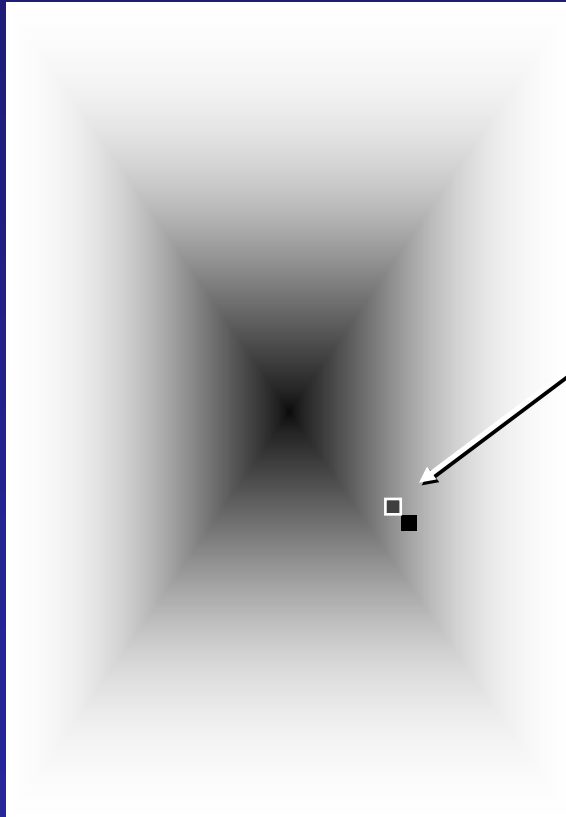


400,000



2,000,000,000

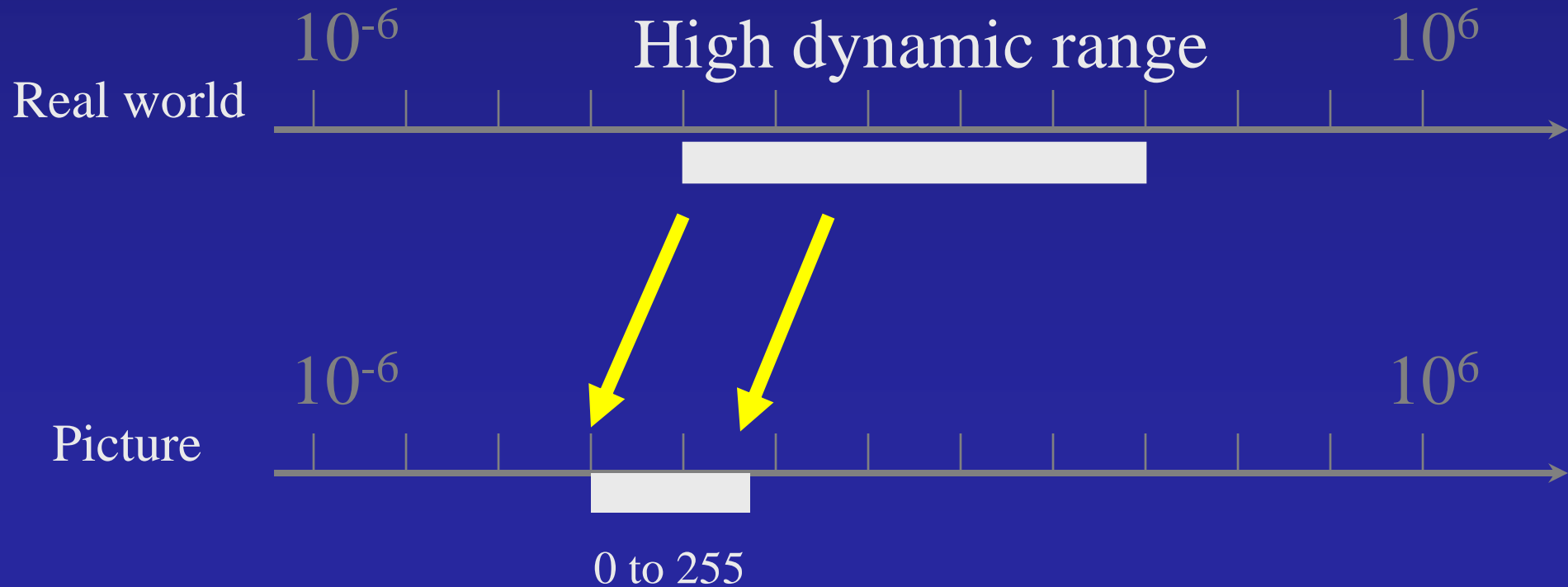
Image



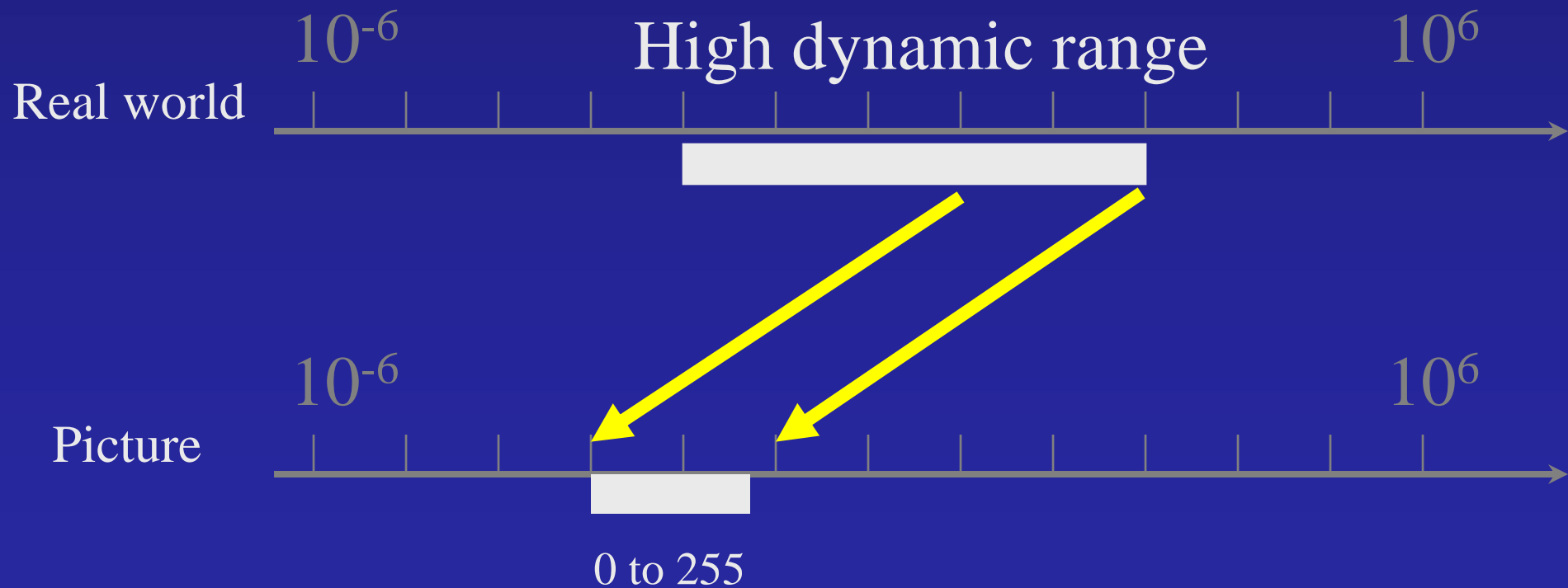
pixel (312, 284) = 42

42 photos?

# Long Exposure

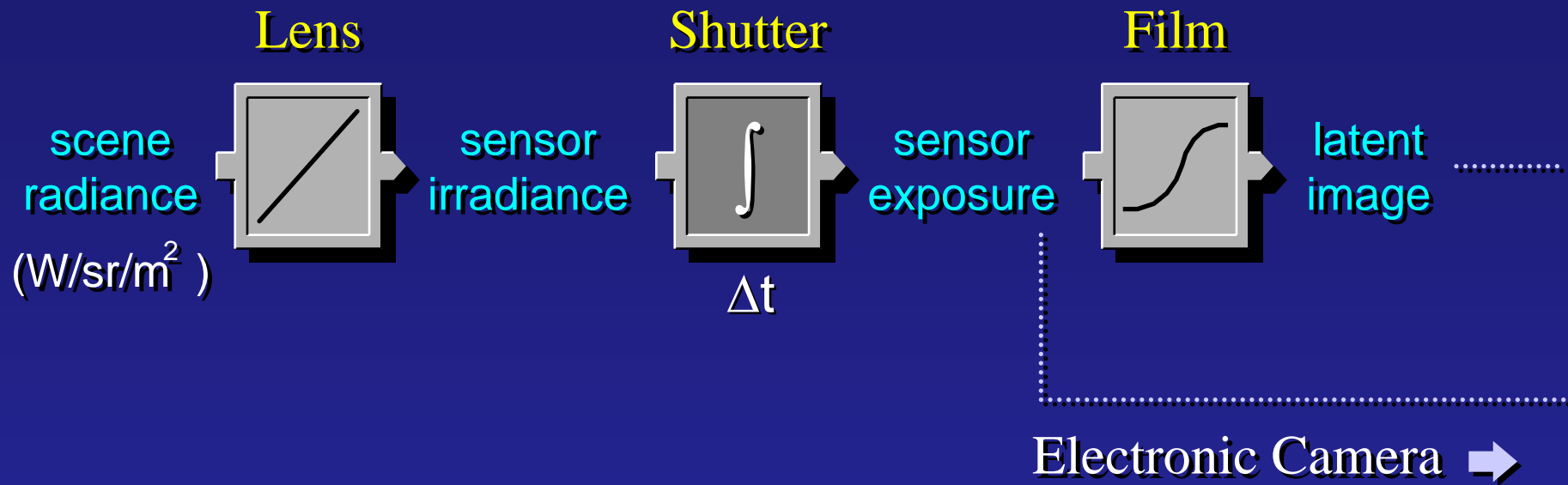


# Short Exposure



# Camera Calibration

- Geometric
  - How pixel **coordinates** relate to **directions** in the world
- Photometric
  - How pixel **values** relate to **radiance** amounts in the world



# The Image Acquisition Pipeline

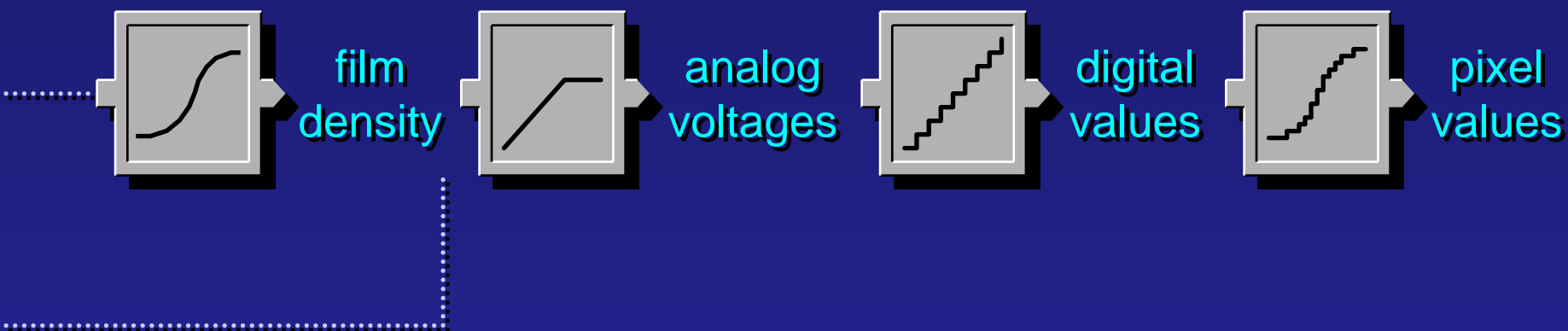


Development

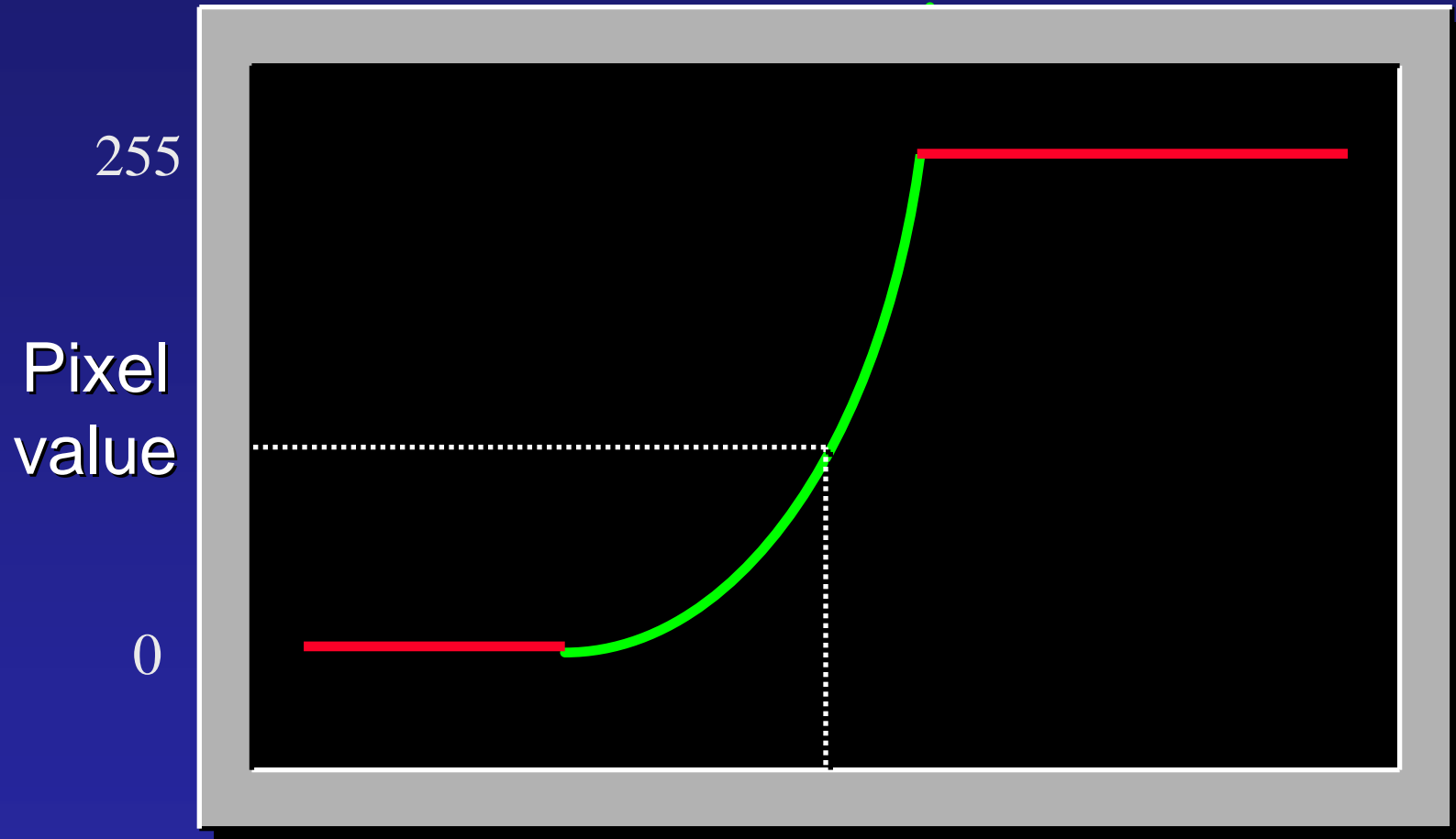
CCD

ADC

Remapping



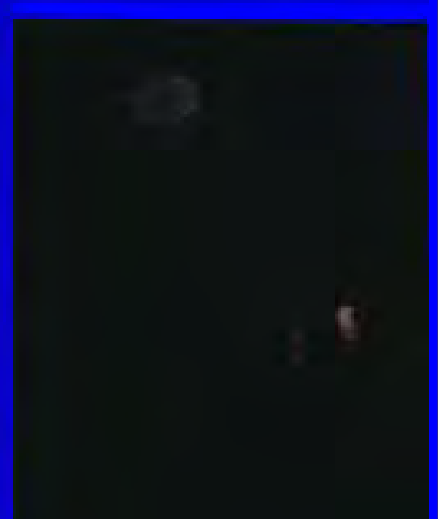
# Imaging system response function



$$\log \text{Exposure} = \log (\text{Radiance} * \Delta t)$$

(CCD photon count)

# Varying Exposure



# Camera is not a photometer!

- Limited dynamic range
  - ⇒ Perhaps use multiple exposures?
- Unknown, nonlinear response
  - ⇒ Not possible to convert pixel values to radiance
- Solution:
  - Recover response curve from multiple exposures, then reconstruct the *radiance map*

# Recovering High Dynamic Range Radiance Maps from Photographs



Paul Debevec  
Jitendra Malik



Computer Science Division  
University of California at Berkeley

August 1997

# Ways to vary exposure

- Shutter Speed (\*)
- F/stop (aperture, iris)
- Neutral Density (ND) Filters



# Shutter Speed

- **Ranges:** Canon D30: 30 to 1/4,000 sec.
- Sony VX2000: 1/4 to 1/10,000 sec.
- **Pros:**
  - Directly varies the exposure
  - Usually accurate and repeatable
- **Issues:**
  - Noise in long exposures

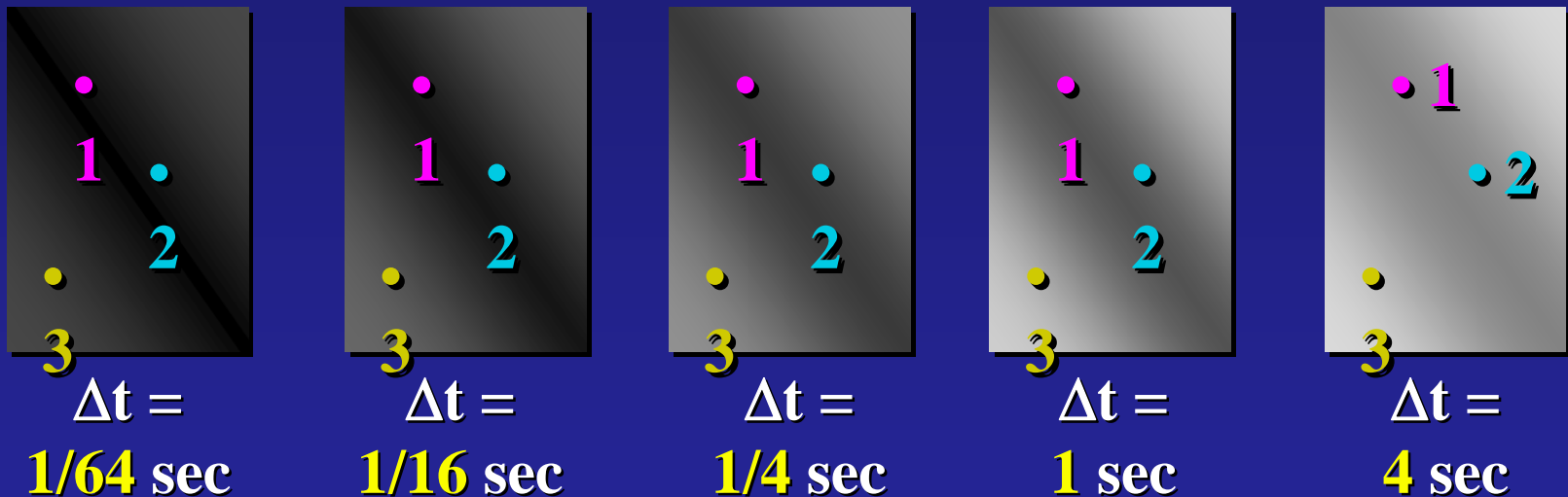
# Shutter Speed

- **Note: shutter times usually obey a power series – each “stop” is a factor of 2**
- **$\frac{1}{4}$ ,  $\frac{1}{8}$ ,  $\frac{1}{15}$ ,  $\frac{1}{30}$ ,  $\frac{1}{60}$ ,  $\frac{1}{125}$ ,  $\frac{1}{250}$ ,  $\frac{1}{500}$ ,  $\frac{1}{1000}$  sec**
- **Usually really is:**
- **$\frac{1}{4}$ ,  $\frac{1}{8}$ ,  $\frac{1}{16}$ ,  $\frac{1}{32}$ ,  $\frac{1}{64}$ ,  $\frac{1}{128}$ ,  $\frac{1}{256}$ ,  $\frac{1}{512}$ ,  $\frac{1}{1024}$  sec**



# The Algorithm

Image series



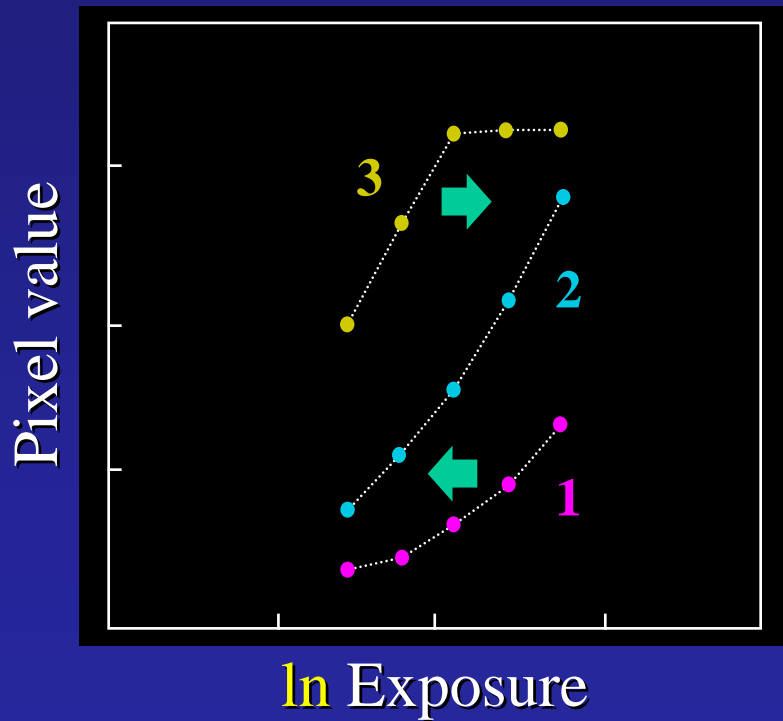
Pixel Value  $Z = f(\text{Exposure})$

$\text{Exposure} = \text{Radiance} \times \Delta t$

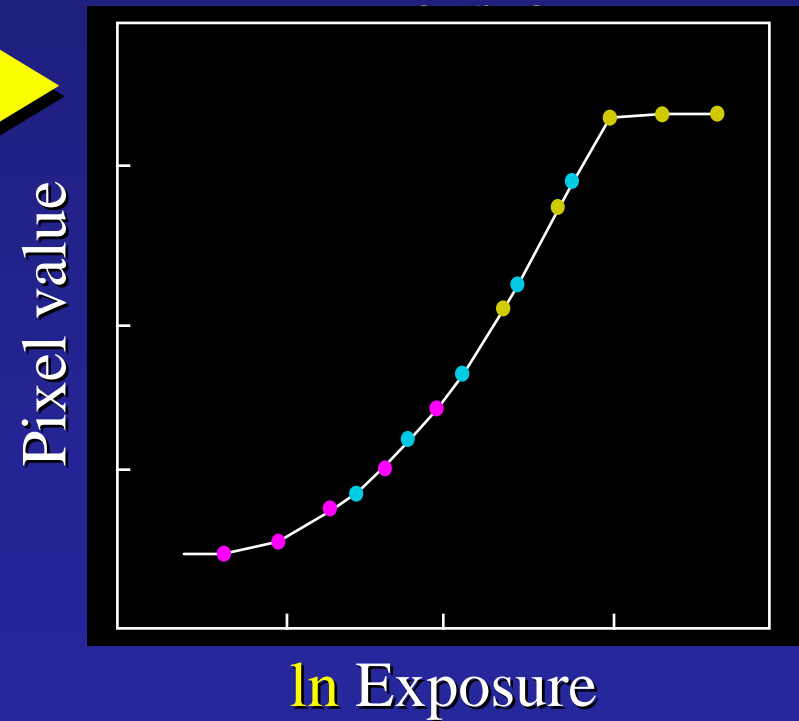
$\log \text{Exposure} = \log \text{Radiance} + \log \Delta t$

# Response Curve

Assuming unit radiance  
for each pixel



After adjusting radiances to  
obtain a smooth response



# The Math

- Let  $g(z)$  be the *discrete* inverse response function
- For each pixel site  $i$  in each image  $j$ , want:

$$\ln Radianc_e + \ln \Delta t_j = g(Z_{ij})$$

- Solve the overdetermined linear system:

$$\sum_{i=1}^N \sum_{j=1}^P \left[ \ln Radianc_e + \ln \Delta t_j - g(Z_{ij}) \right]^2 + \lambda \sum_{z=Z_{min}}^{Z_{max}} g''(z)^2$$

fitting term

smoothness term

# Matlab Code

```
function [g,lE]=gsolve(Z,B,l,w)

n = 256;
A = zeros(size(Z,1)*size(Z,2)+n+1,n+size(Z,1));
b = zeros(size(A,1),1);

k = 1;                                %% Include the data-fitting equations
for i=1:size(Z,1)
    for j=1:size(Z,2)
        wij = w(Z(i,j)+1);
        A(k,Z(i,j)+1) = wij; A(k,n+i) = -wij; b(k,1) = wij * B(i,j);
        k=k+1;
    end
end

A(k,129) = 1;                          %% Fix the curve by setting its middle value to 1
k=k+1;

for i=1:n-2                             %% Include the smoothness equations
    A(k,i)=l*w(i+1); A(k,i+1)=-2*l*w(i+1); A(k,i+2)=l*w(i+1);
    k=k+1;
end

x = A\b;                                %% Solve the system using SVD

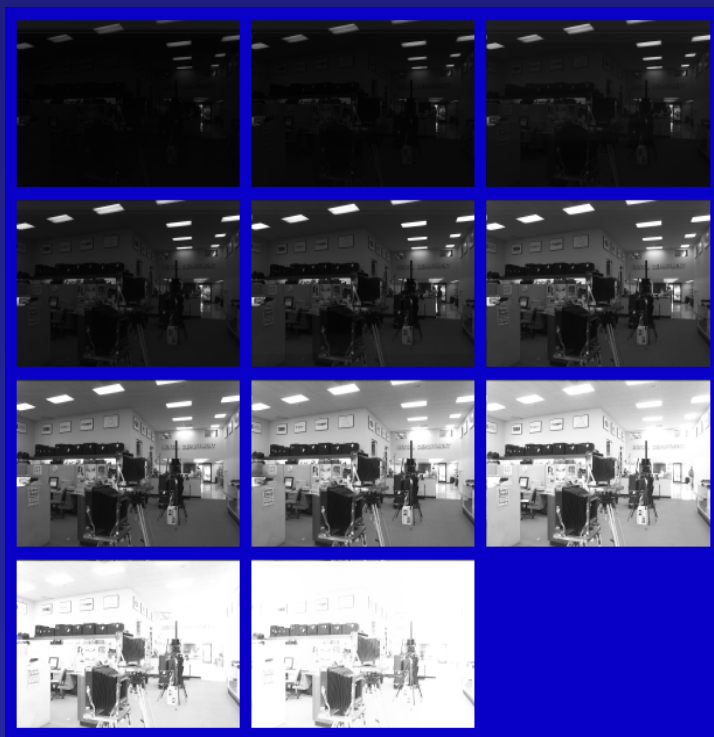
g = x(1:n);
lE = x(n+1:size(x,1));
```

# Results: Digital Camera

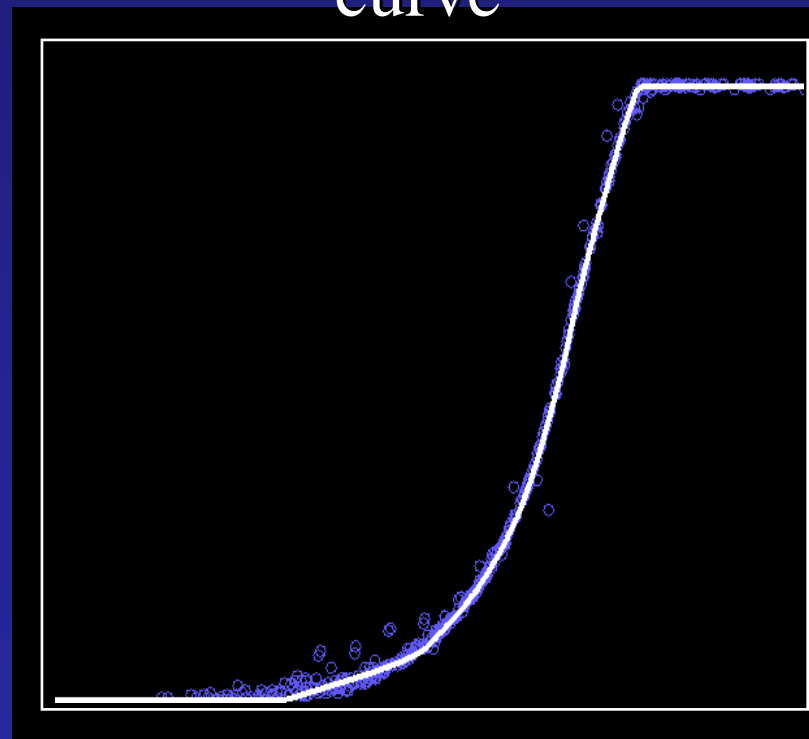
Kodak DCS460

1/30 to 30 sec

Recovered response  
curve



Pixel value



log Exposure

# Reconstructed radiance map

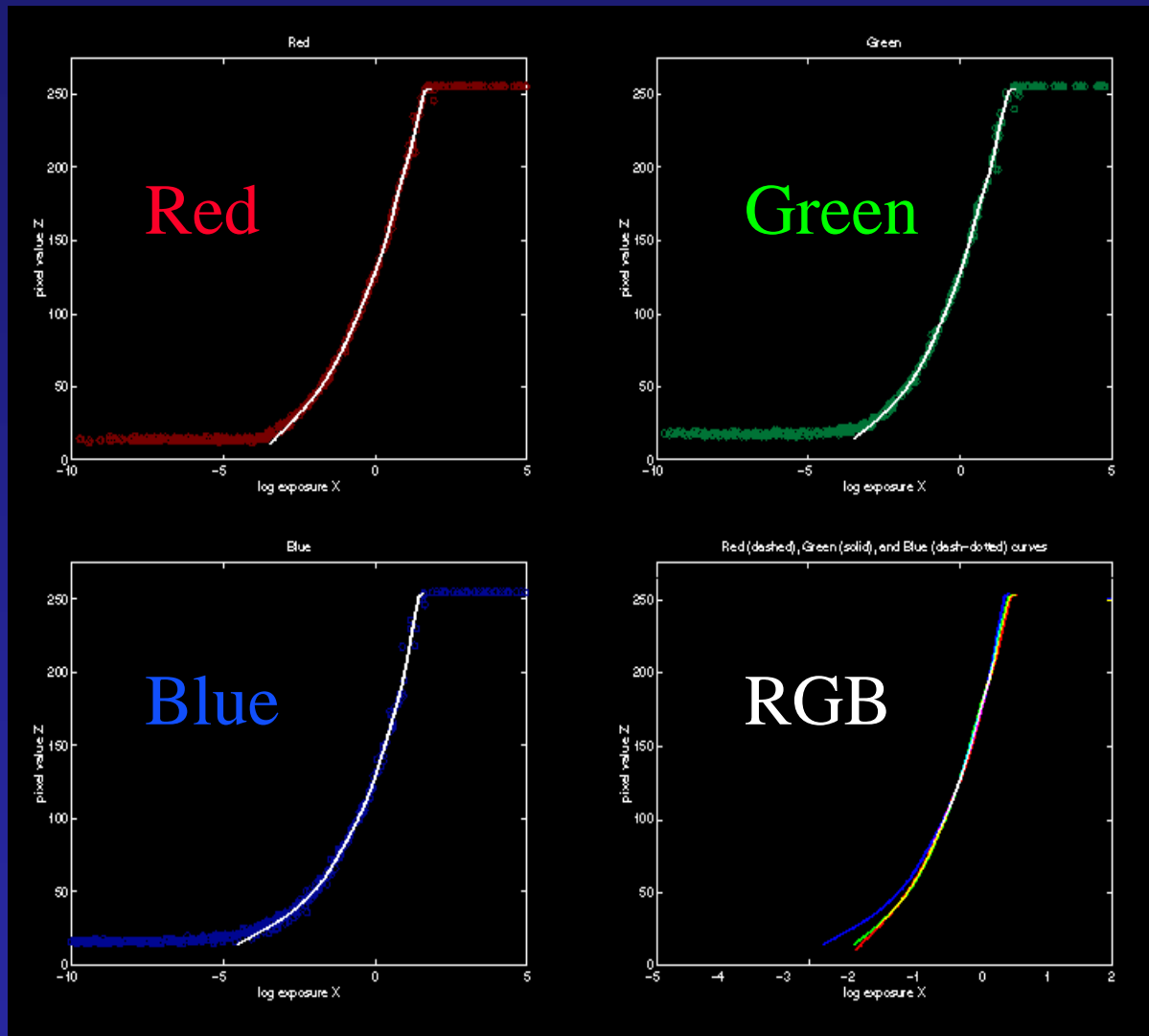


# Results: Color Film

- Kodak Gold ASA 100, PhotoCD



# Recovered Response Curves





# The Radiance Map

W/sr/m<sup>2</sup>

121.741

28.869

6.846

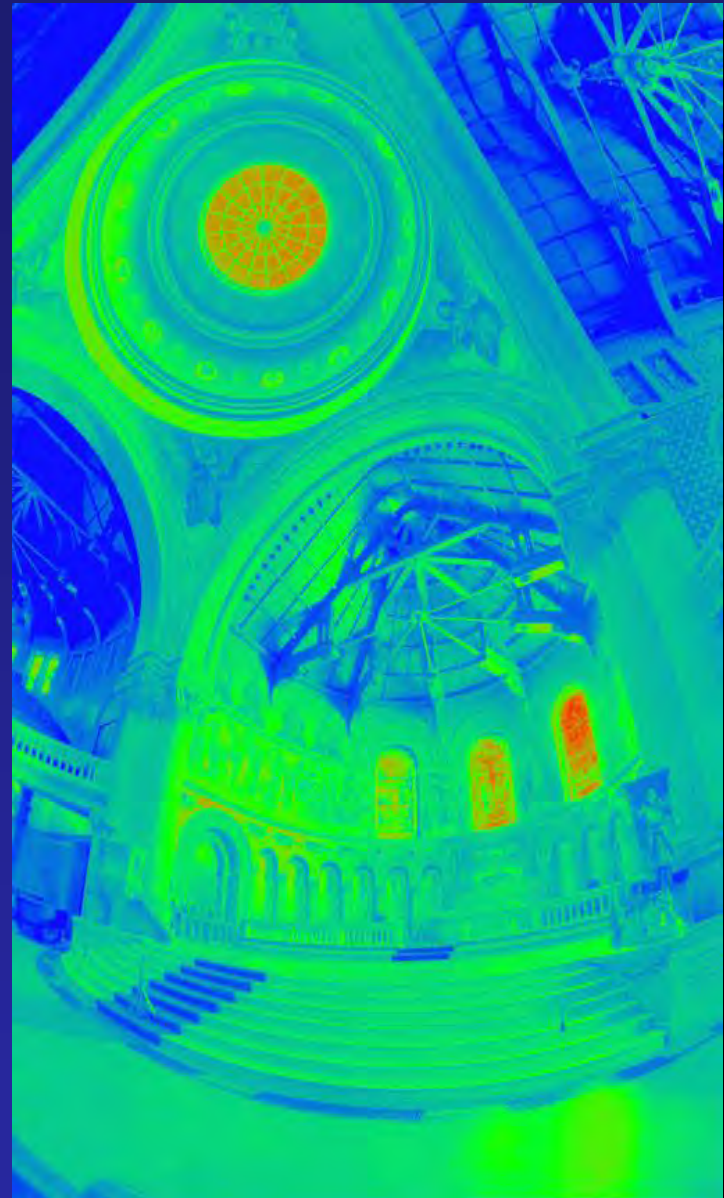
1.623

0.384

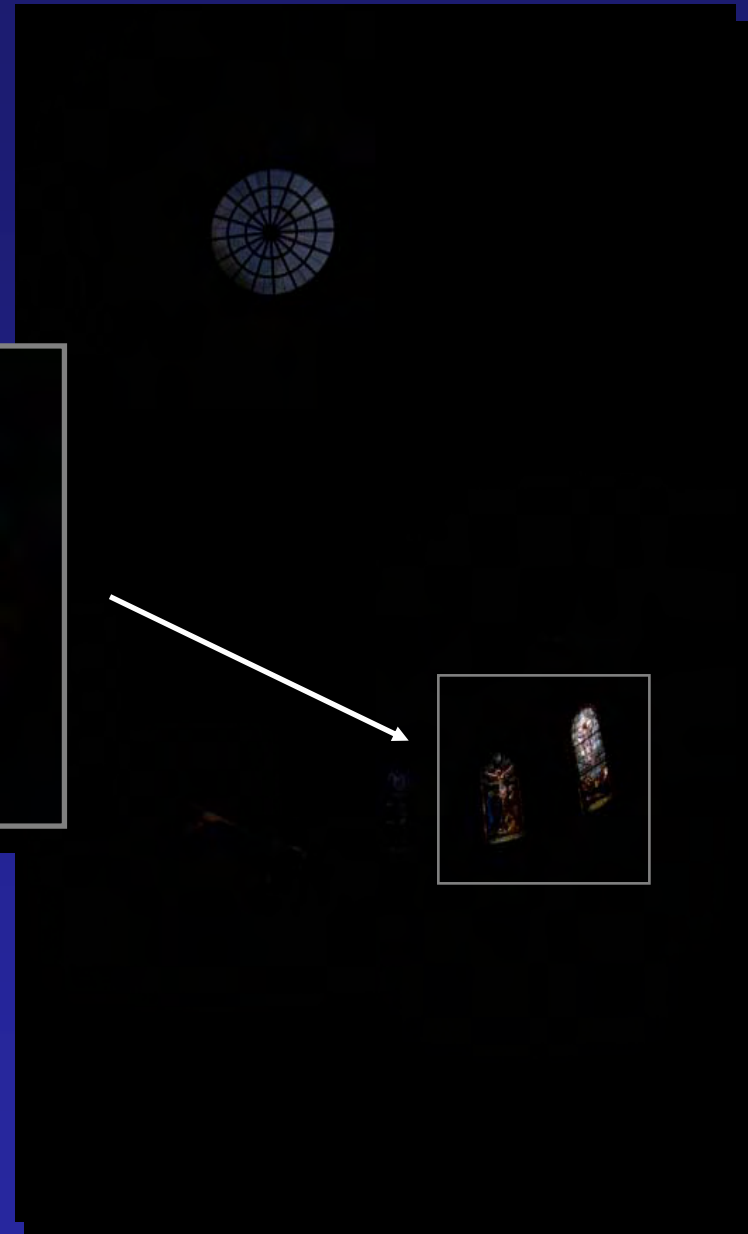
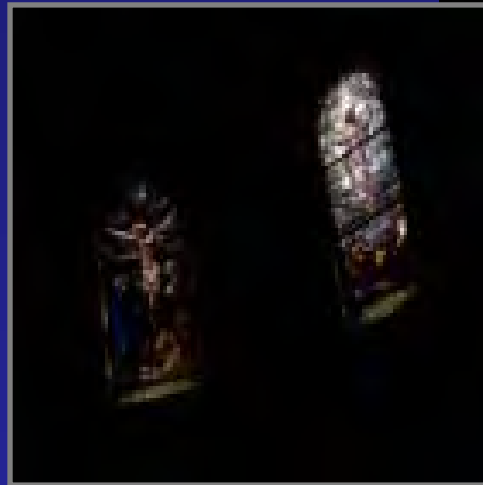
0.091

0.021

0.005



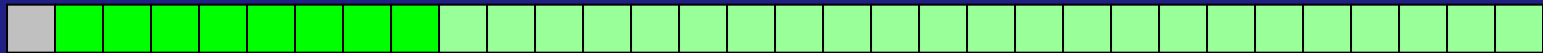
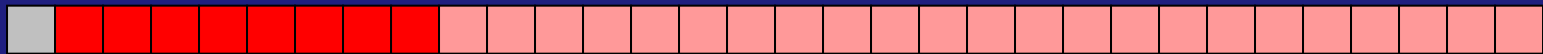
# The Radiance Map



Linearly scaled to  
display device

# Portable FloatMap (.pfm)

- 12 bytes per pixel, 4 for each channel



sign    exponent

mantissa

Text header similar to Jeff Poskanzer's .ppm image format:

```
PF
768 512
1
<binary image data>
```

Floating Point TIFF similar

# *Radiance Format* (.pic, .hdr)



$$(145, 215, 87, 149) =$$

$$(145, 215, 87) * 2^{(149-128)} =$$

$$(1190000, 1760000, 713000)$$

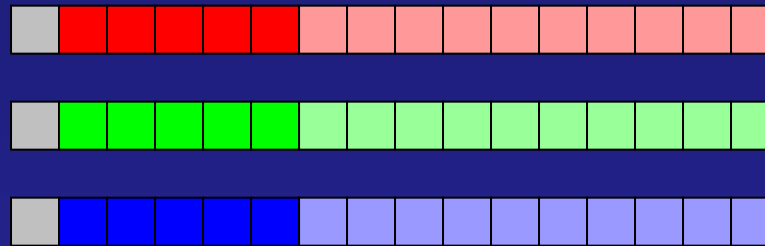
$$(145, 215, 87, 103) =$$

$$(145, 215, 87) * 2^{(103-128)} =$$

$$(0.00000432, 0.00000641, 0.00000259)$$

# *ILM's* OpenEXR (.exr)

- 6 bytes per pixel, 2 for each channel, compressed



sign    exponent    mantissa

- Several lossless compression options, 2:1 typical
- Compatible with the "half" datatype in NVidia's Cg
- Supported natively on GeForce FX and Quadro FX
- Available at <http://www.openexr.net/>

Now  
What?

W/sr/m<sup>2</sup>

121.741

28.869

6.846

1.623

0.384

0.091

0.021

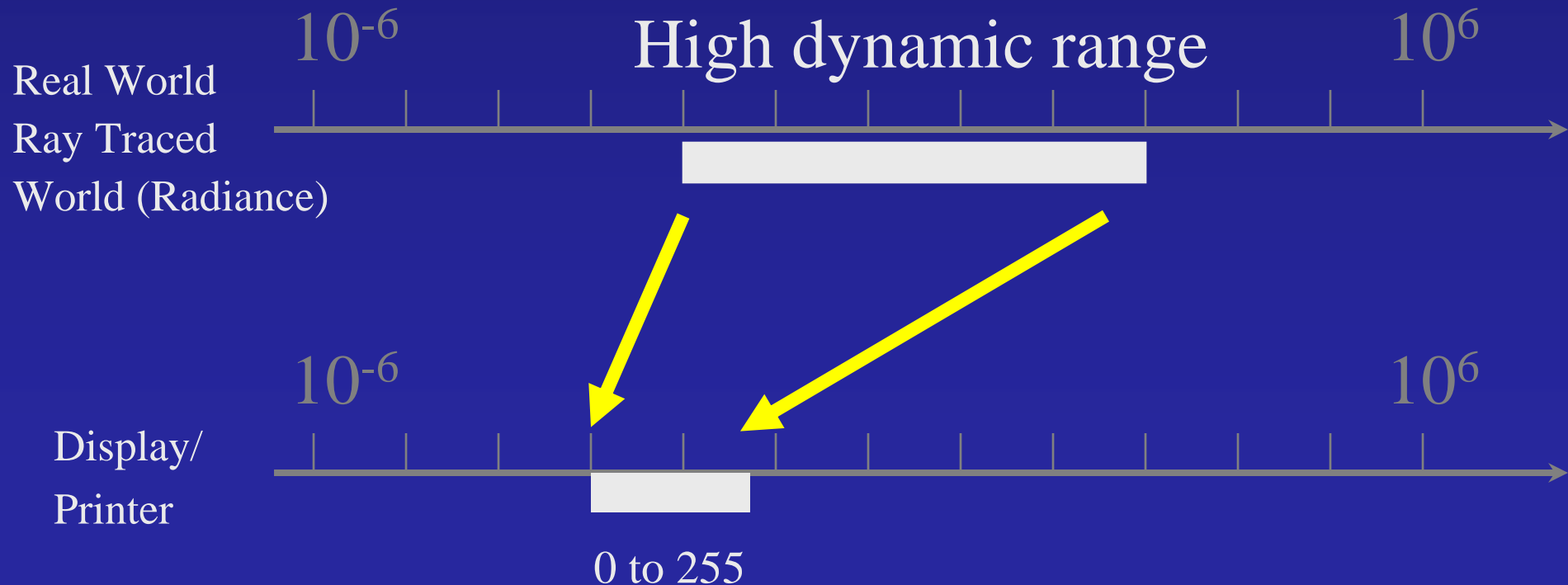
0.005



# Tone Mapping

- How can we do this?

Linear scaling?, thresholding? Suggestions?



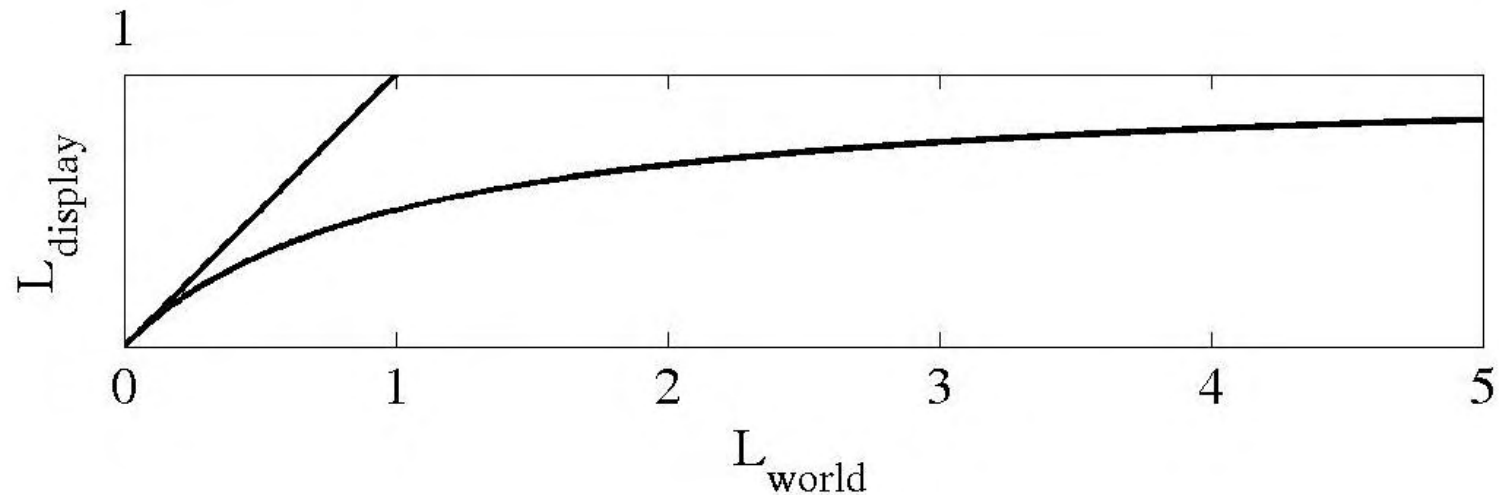
# Simple Global Operator

- Compression curve needs to
  - Bring everything within range
  - Leave dark areas alone
- In other words
  - Asymptote at 255
  - Derivative of 1 at 0



# Global Operator (Reinhart et al)

$$L_{display} = \frac{L_{world}}{1 + L_{world}}$$



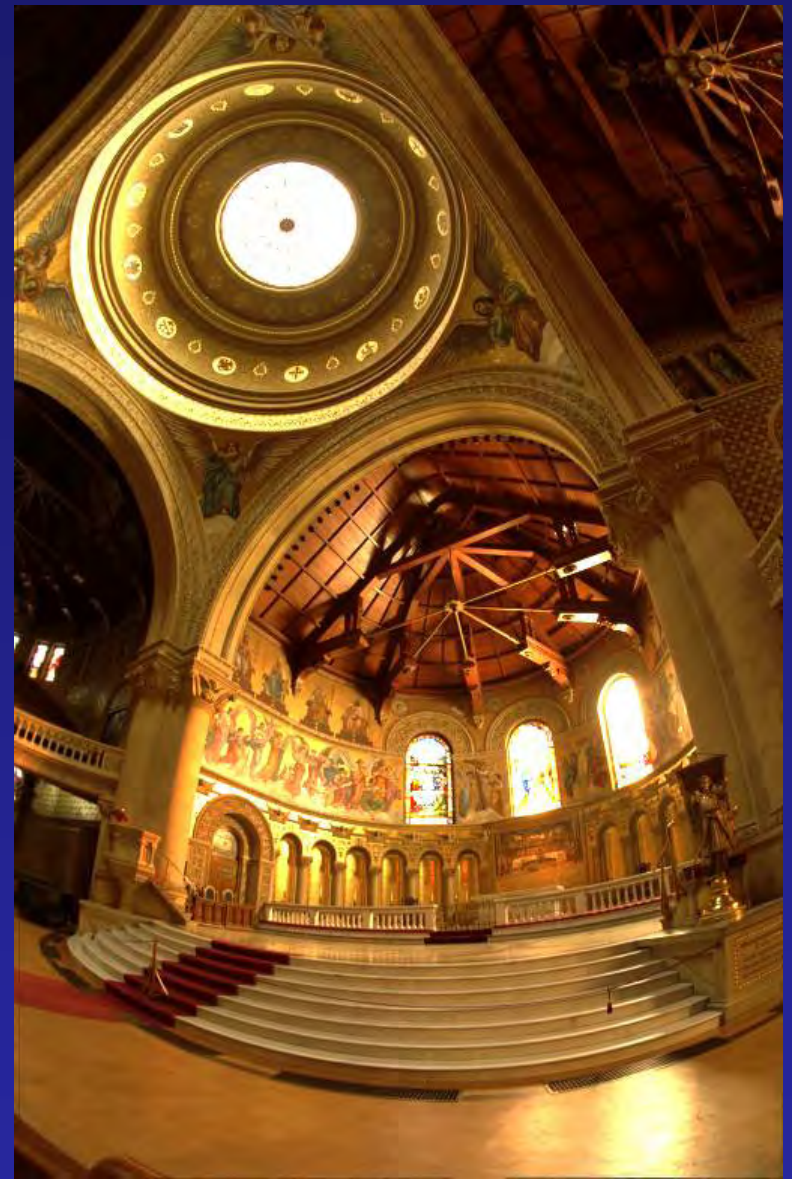
# Global Operator Results







Reinhart Operator

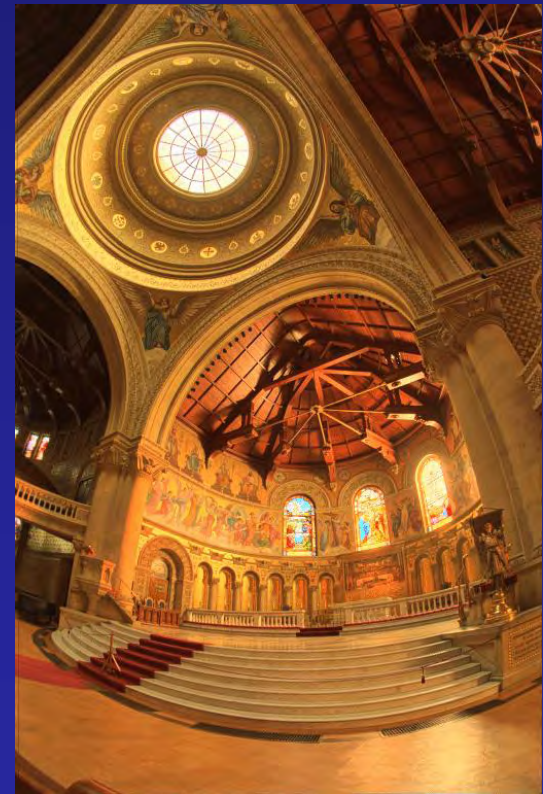


Darkest 0.1% scaled  
to display device

# What do *we* see?



Vs.



# What does the eye sees?

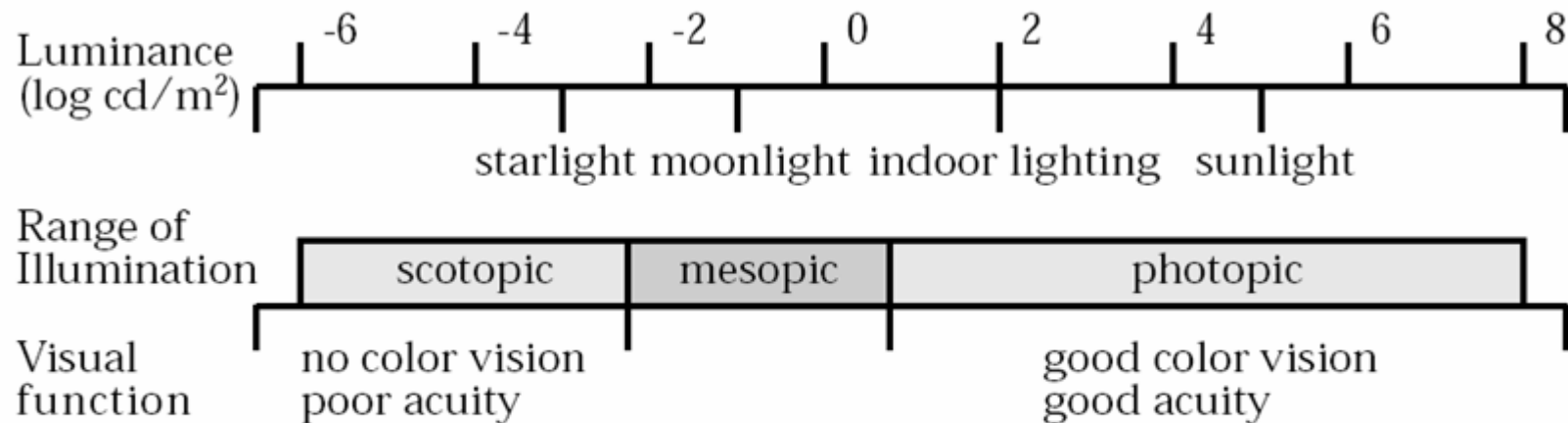
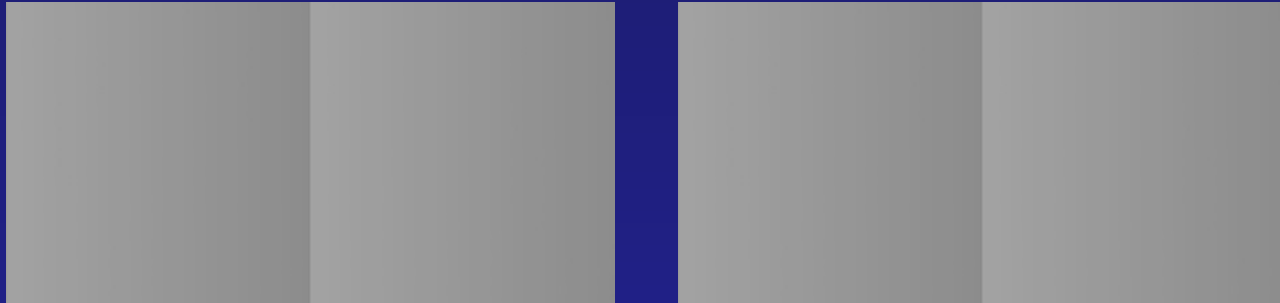


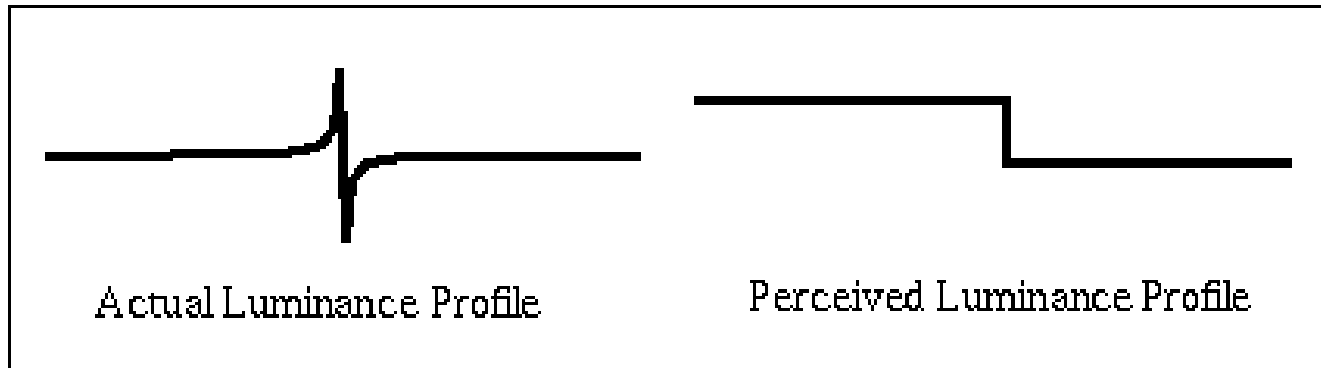
Figure 1: The range of luminances in the natural environment and associated visual parameters. After Hood (1986).

The eye has a huge dynamic range  
Do we see a true radiance map?

# Metamores



**Craik-O'Brien Cornsweet Effect**



Can we use this for range compression?

# Compressing Dynamic Range

