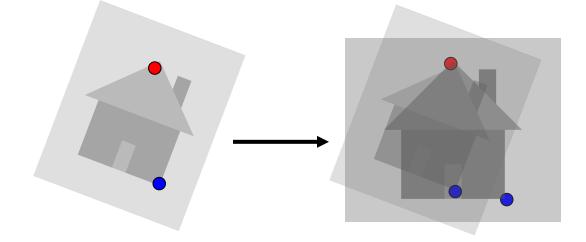
# Automatic Image Alignment



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with a lot of slides stolen from Steve Seitz and Rick Szeliski 15-463: Computational Photography Alexei Efros, CMU, Fall 2007

# Image Alignment



# How do we align two images automatically? Two broad approaches:

- Feature-based alignment
  - Find a few matching features in both images
  - compute alignment
- Direct (pixel-based) alignment
  - Search for alignment where most pixels agree

# Direct Alignment

#### The simplest approach is a brute force search (hw1)

- Need to define image matching function
  - SSD, Normalized Correlation, edge matching, etc.
- Search over all parameters within a reasonable range:

#### e.g. for translation:

```
for tx=x0:step:x1,
  for ty=y0:step:y1,
     compare image1(x,y) to image2(x+tx,y+ty)
  end;
end;
```

#### Need to pick correct x0, x1 and step

What happens if step is too large?

# Direct Alignment (brute force)

What if we want to search for more complicated transformation, e.g. homography?

$$\begin{bmatrix} wx' \\ wy' \\ w \end{bmatrix} = \begin{bmatrix} a & b & c \\ d & e & f \\ g & h & i \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

### Problems with brute force

#### Not realistic

- Search in O(N<sup>8</sup>) is problematic
- Not clear how to set starting/stopping value and step

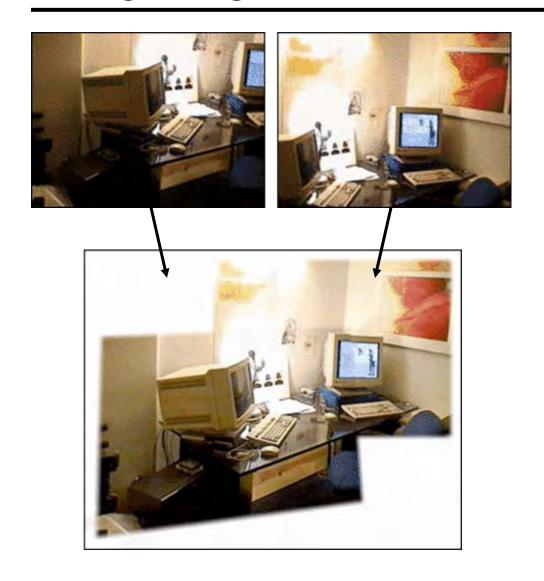
#### What can we do?

- Use pyramid search to limit starting/stopping/step values
- For special cases (rotational panoramas), can reduce search slightly to O(N<sup>4</sup>):
  - $H = K_1 R_2^{-1} K_2^{-1}$  (4 DOF: f and rotation)

#### Alternative: gradient decent on the error function

- i.e. how do I tweak my current estimate to make the SSD error go down?
- Can do sub-pixel accuracy
- BIG assumption?
  - Images are already almost aligned (<2 pixels difference!)</li>
  - Can improve with pyramid
- Same tool as in motion estimation

# Image alignment



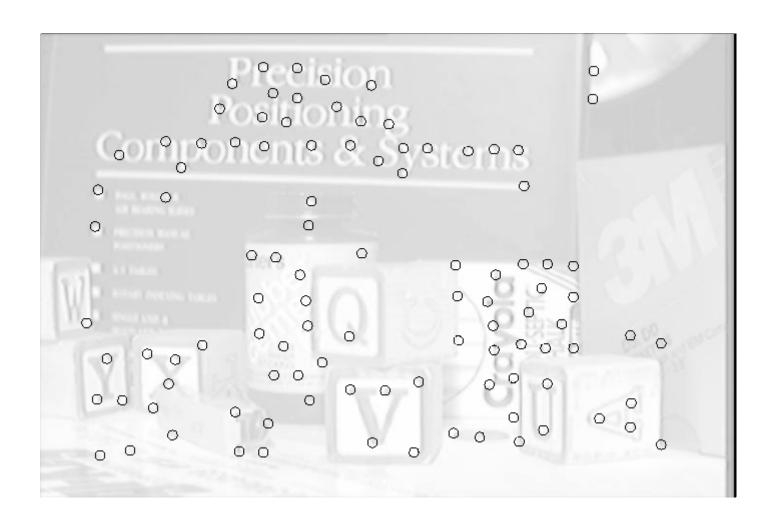
# Feature-based alignment

- 1. Find a few important features (aka Interest Points)
- 2. Match them across two images
- 3. Compute image transformation as per Project #3

#### How do we choose good features?

- They must prominent in both images
- Easy to localize
- Think how you did that by hand in Project #3
- Corners!

### **Feature Detection**



# Feature Matching

#### How do we match the features between the images?

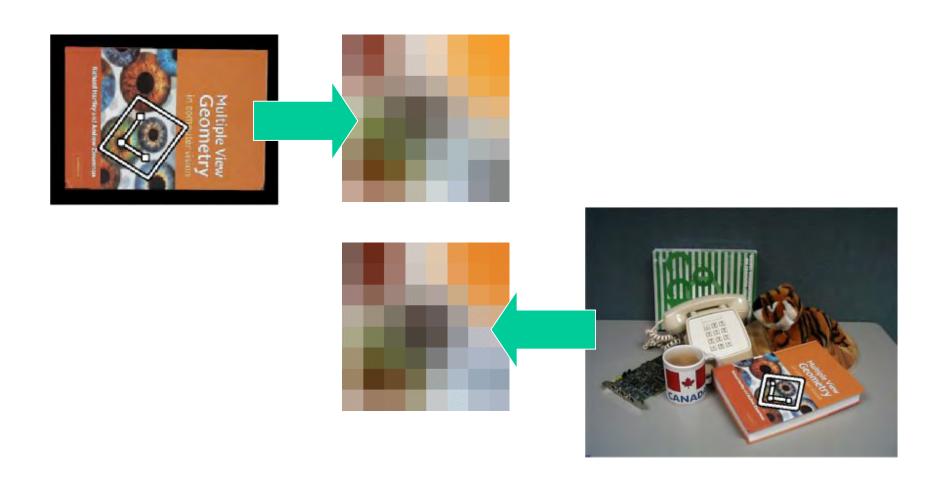
- Need a way to <u>describe</u> a region around each feature
  - e.g. image patch around each feature
- Use successful matches to estimate homography
  - Need to do something to get rid of outliers

#### Issues:

- What if the image patches for several interest points look similar?
  - Make patch size bigger
- What if the image patches for the same feature look different due to scale, rotation, etc.
  - Need an invariant descriptor

# **Invariant Feature Descriptors**

Schmid & Mohr 1997, Lowe 1999, Baumberg 2000, Tuytelaars & Van Gool 2000, Mikolajczyk & Schmid 2001, Brown & Lowe 2002, Matas et. al. 2002, Schaffalitzky & Zisserman 2002



# Today's lecture

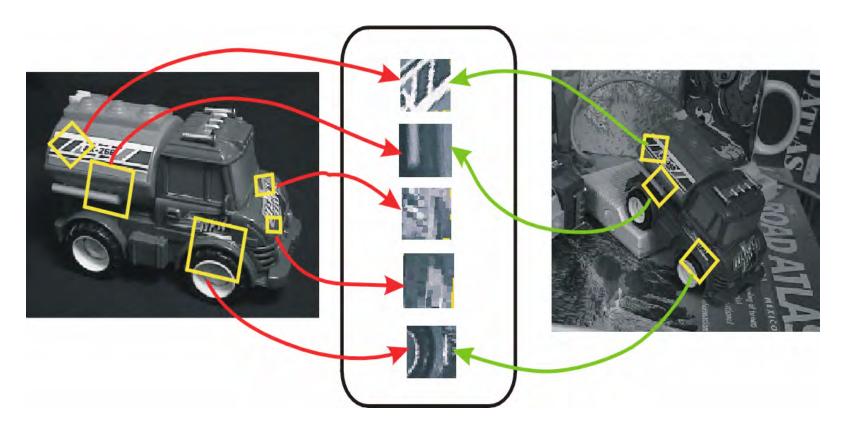
- Feature <u>detectors</u>
  - scale invariant Harris corners
- Feature <u>descriptors</u>
  - patches, oriented patches

#### Reading:

Multi-image Matching using Multi-scale image patches, CVPR 2005

### **Invariant Local Features**

Image content is transformed into local feature coordinates that are invariant to translation, rotation, scale, and other imaging parameters



**Features Descriptors** 

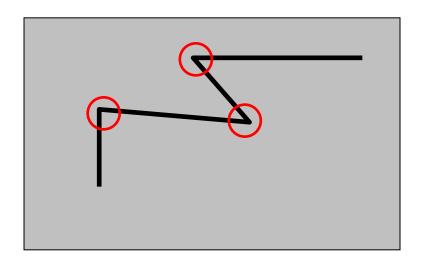
# **Applications**

### Feature points are used for:

- Image alignment (homography, fundamental matrix)
- 3D reconstruction
- Motion tracking
- Object recognition
- Indexing and database retrieval
- Robot navigation
- ... other

### Harris corner detector

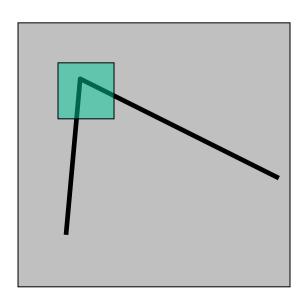
C.Harris, M.Stephens. "A Combined Corner and Edge Detector". 1988



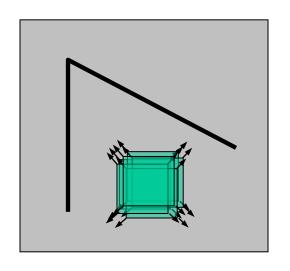
#### The Basic Idea

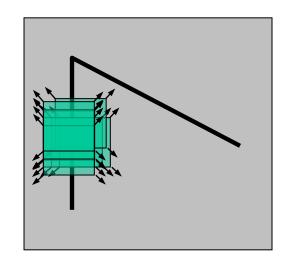
We should easily recognize the point by looking through a small window

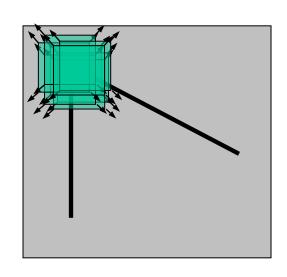
Shifting a window in *any direction* should give *a large* change in intensity



#### Harris Detector: Basic Idea





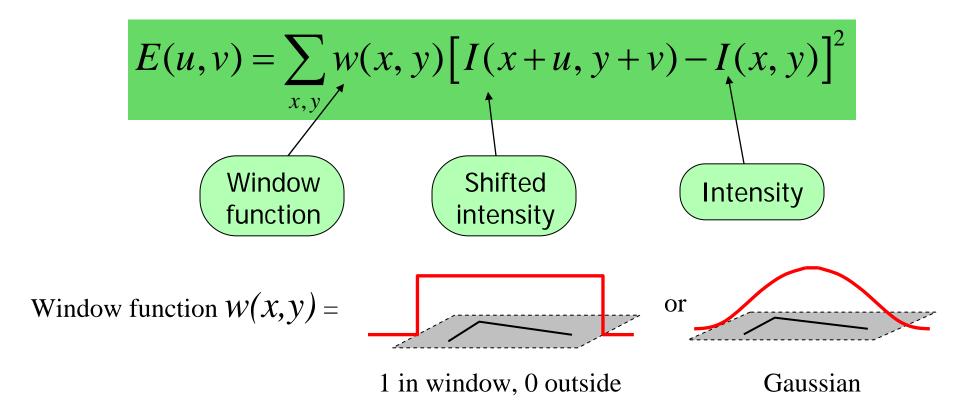


"flat" region: no change in all directions

"edge":
no change along
the edge direction

"corner": significant change in all directions

Change of intensity for the shift [u,v]:



For small shifts [u, v] we have a *bilinear* approximation:

$$E(u,v) \cong \begin{bmatrix} u,v \end{bmatrix} \quad M \quad \begin{bmatrix} u\\v \end{bmatrix}$$

where M is a  $2\times2$  matrix computed from image derivatives:

$$M = \sum_{x,y} w(x,y) \begin{bmatrix} I_x^2 & I_x I_y \\ I_x I_y & I_y^2 \end{bmatrix}$$

$$A^{T}A = \begin{bmatrix} \sum_{I_{x}I_{x}}^{I_{x}I_{x}} & \sum_{I_{y}I_{y}}^{I_{x}I_{y}} \\ \sum_{I_{x}I_{y}}^{I_{x}I_{y}} & \sum_{I_{y}I_{y}}^{I_{y}I_{y}} \end{bmatrix} = \sum_{I_{x}I_{y}}^{I_{x}I_{y}} [I_{x} I_{y}] = \sum_{I_{x}I_{y}}^{I_{x}I_{y}} \nabla I(\nabla I)^{T}$$

Classification of image points using eigenvalues of M:  $\lambda_1$  and  $\lambda_2$  are large,  $\lambda_1 \sim \lambda_2$ ; E increases in all directions  $\lambda_1$  and  $\lambda_2$  are small; E is almost constant "Flat" in all directions region

Measure of corner response:

$$R = \frac{\det M}{\operatorname{Trace} M}$$

$$\det M = \lambda_1 \lambda_2$$

$$\operatorname{trace} M = \lambda_1 + \lambda_2$$

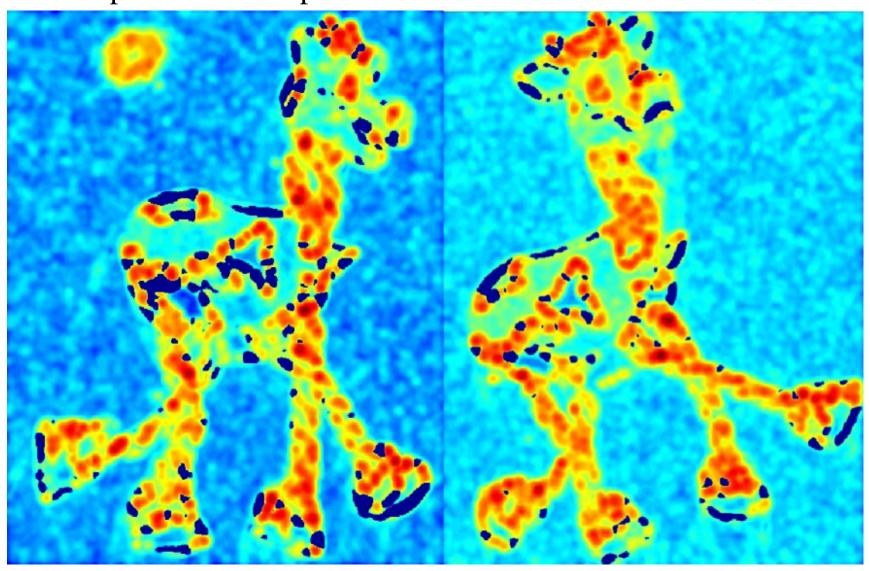
### Harris Detector

### The Algorithm:

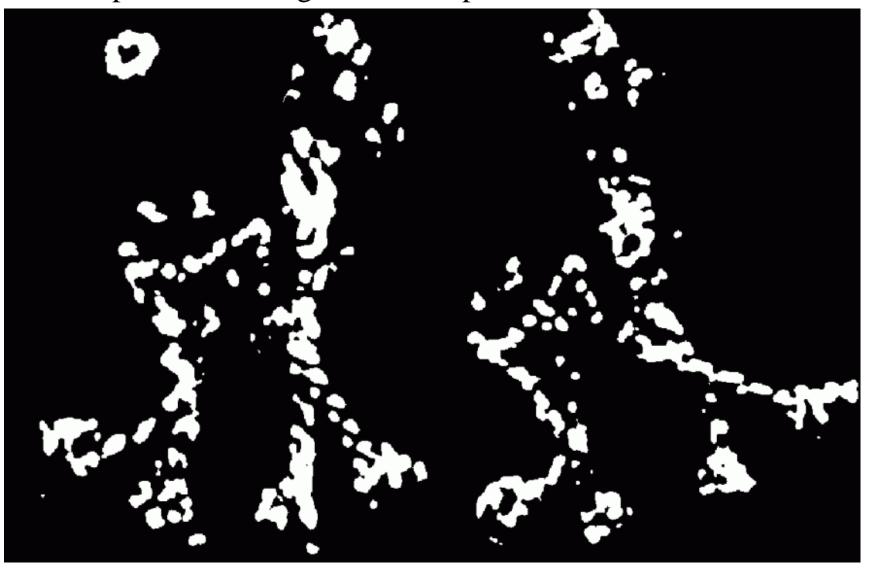
- Find points with large corner response function R
   (R > threshold)
- Take the points of local maxima of R



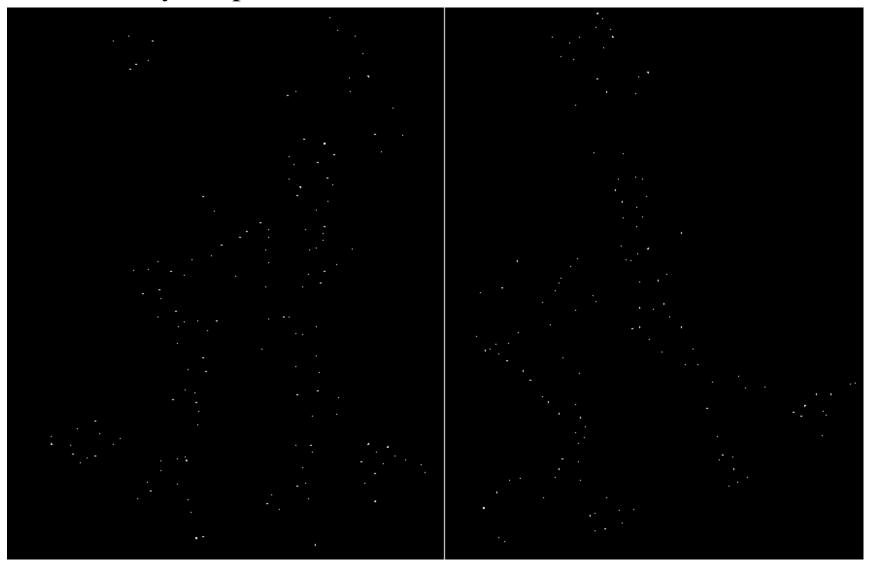
Compute corner response R



Find points with large corner response: *R*>threshold



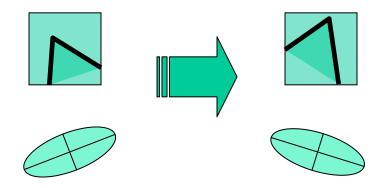
Take only the points of local maxima of R





# Harris Detector: Some Properties

Rotation invariance



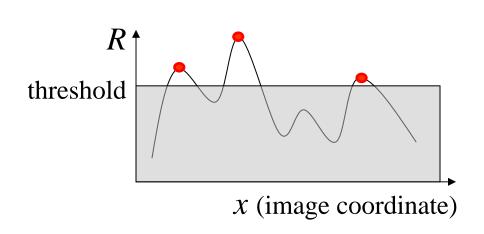
Ellipse rotates but its shape (i.e. eigenvalues) remains the same

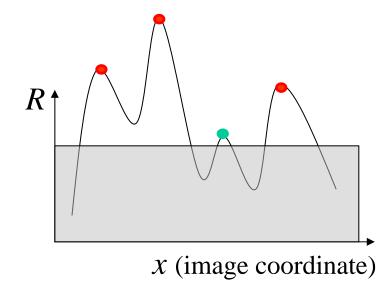
Corner response R is invariant to image rotation

# Harris Detector: Some Properties

Partial invariance to affine intensity change

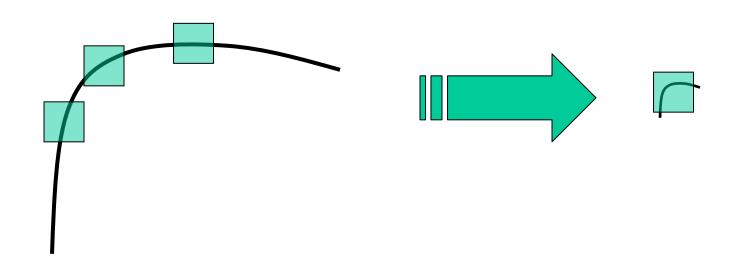
- ✓ Only derivatives are used => invariance to intensity shift  $I \rightarrow I + b$
- ✓ Intensity scale:  $I \rightarrow a I$





# Harris Detector: Some Properties

But: non-invariant to image scale!

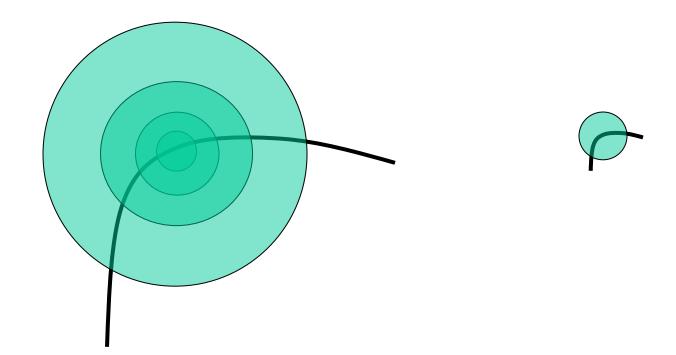


All points will be classified as edges

Corner!

### Scale Invariant Detection

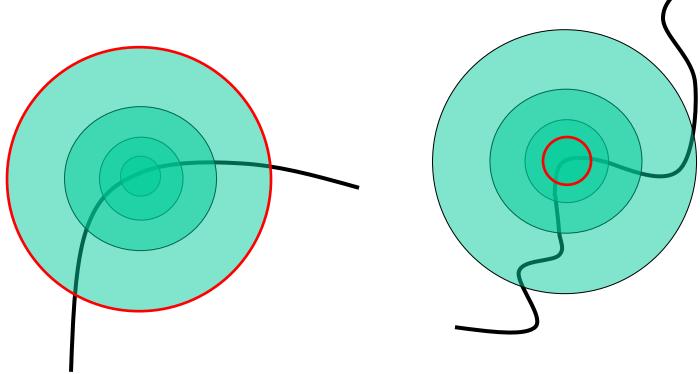
Consider regions (e.g. circles) of different sizes around a point Regions of corresponding sizes will look the same in both images



### Scale Invariant Detection

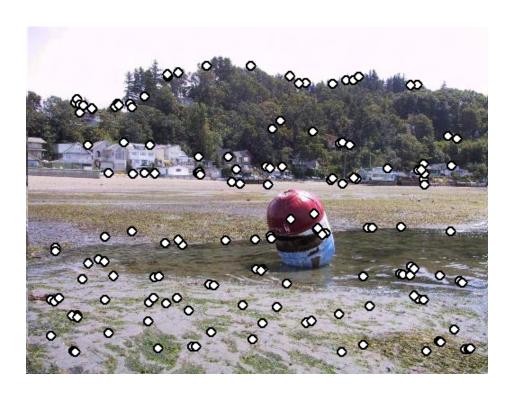
The problem: how do we choose corresponding circles *independently* in each image?

Choose the scale of the "best" corner



## Feature selection

Distribute points evenly over the image



## Adaptive Non-maximal Suppression

#### Desired: Fixed # of features per image

- Want evenly distributed spatially...
- Sort points by non-maximal suppression radius [Brown. Szeliski. Winder. CVPR'05]



(a) Strongest 250



(b) Strongest 500



(c) ANMS 250, r = 24

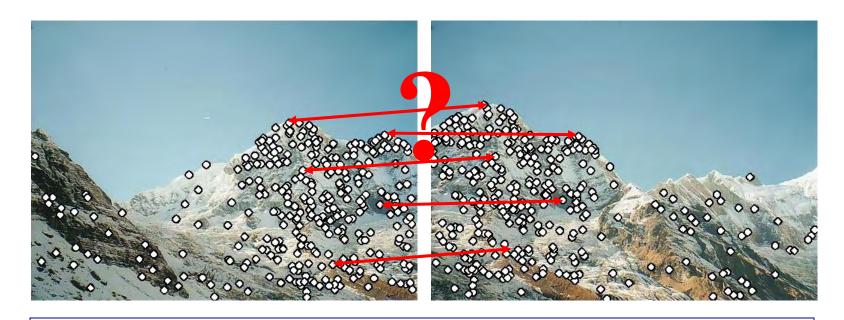


(d) ANMS 500, r = 16

# Feature descriptors

We know how to detect points

Next question: How to match them?



Point descriptor should be:

1. Invariant

2. Distinctive

# Descriptors Invariant to Rotation

#### Find local orientation

Dominant direction of gradient





• Extract image patches relative to this orientation

### Multi-Scale Oriented Patches

#### Interest points

- Multi-scale Harris corners
- Orientation from blurred gradient
- Geometrically invariant to rotation

#### Descriptor vector

- Bias/gain normalized sampling of local patch (8x8)
- Photometrically invariant to affine changes in intensity

[Brown, Szeliski, Winder, CVPR'2005]

## **Descriptor Vector**

#### Orientation = blurred gradient Rotation Invariant Frame

• Scale-space position (x, y, s) + orientation  $(\theta)$ 



### Detections at multiple scales

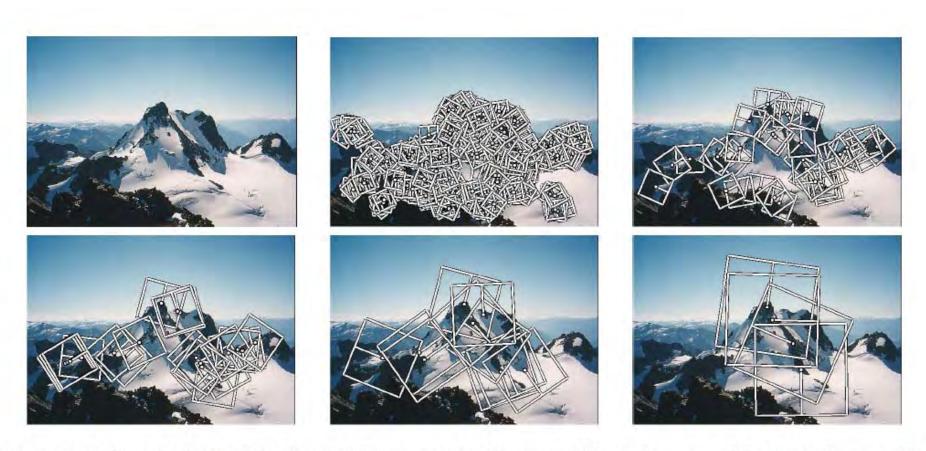


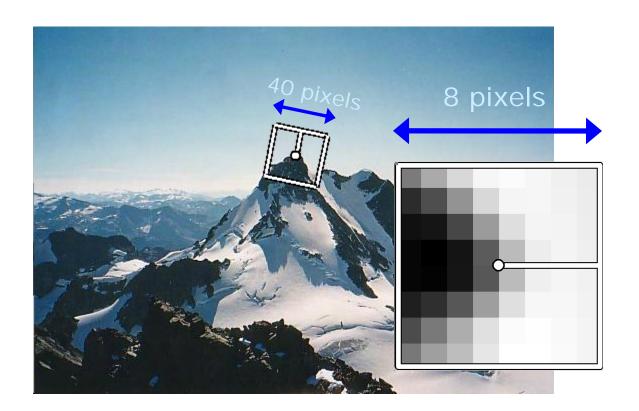
Figure 1. Multi-scale Oriented Patches (MOPS) extracted at five pyramid levels from one of the Matier images. The boxes show the feature orientation and the region from which the descriptor vector is sampled.

## MOPS descriptor vector

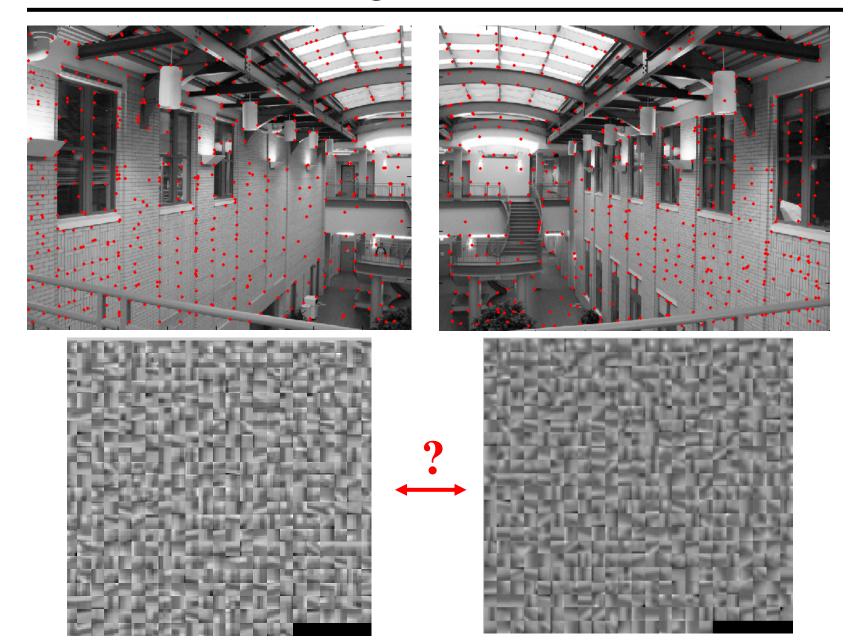
#### 8x8 oriented patch

• Sampled at 5 x scale

Bias/gain normalisation:  $I' = (I - \mu)/\sigma$ 



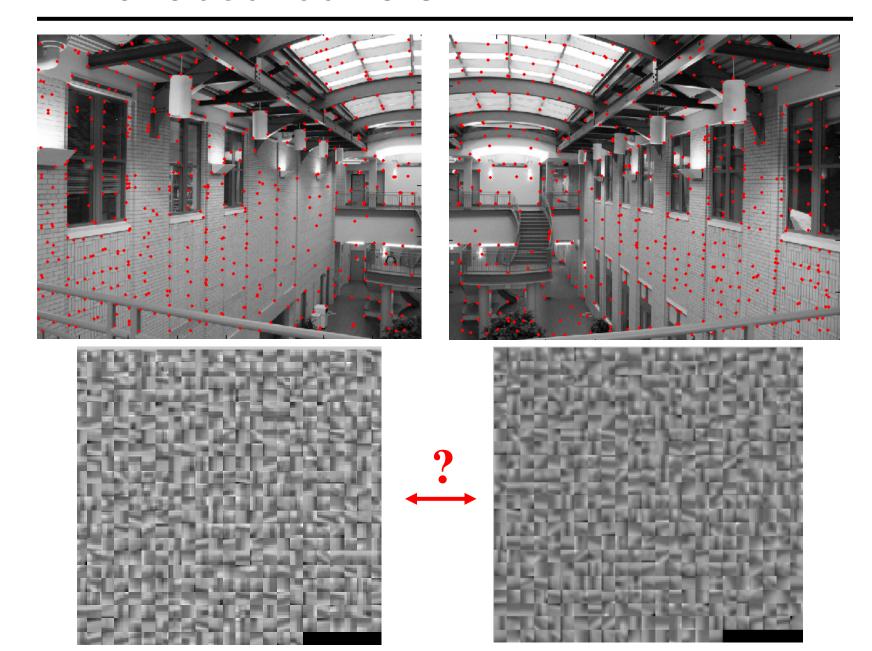
## Feature matching



## Feature matching

- Exhaustive search
  - for each feature in one image, look at all the other features in the other image(s)
- Hashing
  - compute a short descriptor from each feature vector, or hash longer descriptors (randomly)
- Nearest neighbor techniques
  - kd-trees and their variants

### What about outliers?

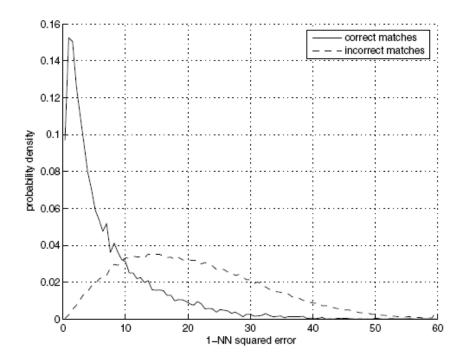


### Feature-space outlier rejection

Let's not match all features, but only these that have "similar enough" matches?

How can we do it?

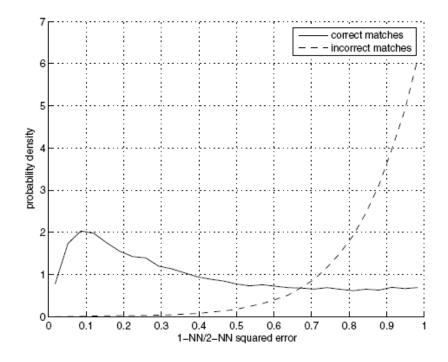
- SSD(patch1,patch2) < threshold</li>
- How to set threshold?



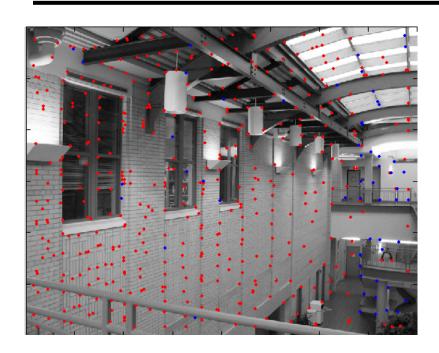
### Feature-space outlier rejection

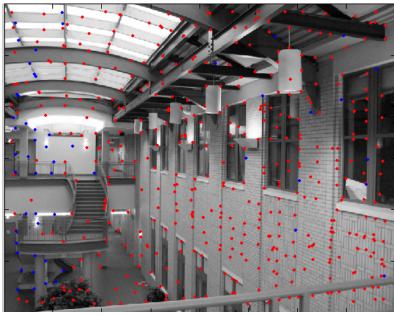
#### A better way [Lowe, 1999]:

- 1-NN: SSD of the closest match
- 2-NN: SSD of the <u>second-closest</u> match
- Look at how much better 1-NN is than 2-NN, e.g. 1-NN/2-NN
- That is, is our best match so much better than the rest?



### Feature-space outliner rejection

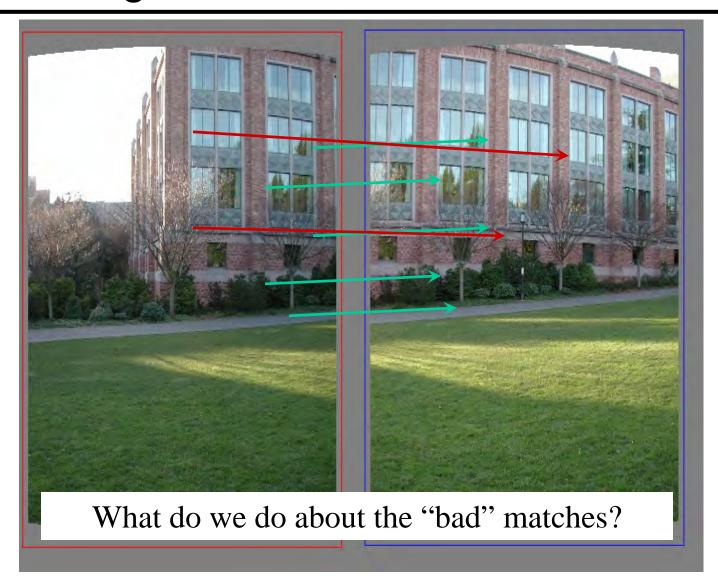




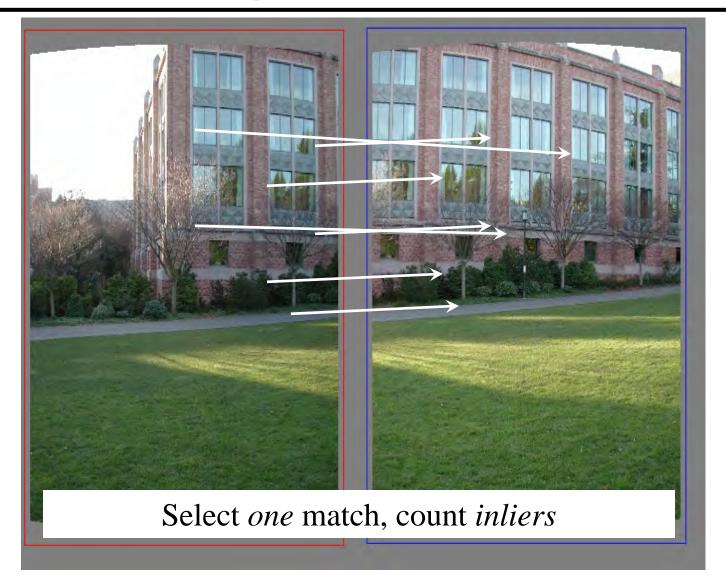
#### Can we now compute H from the blue points?

- No! Still too many outliers...
- What can we do?

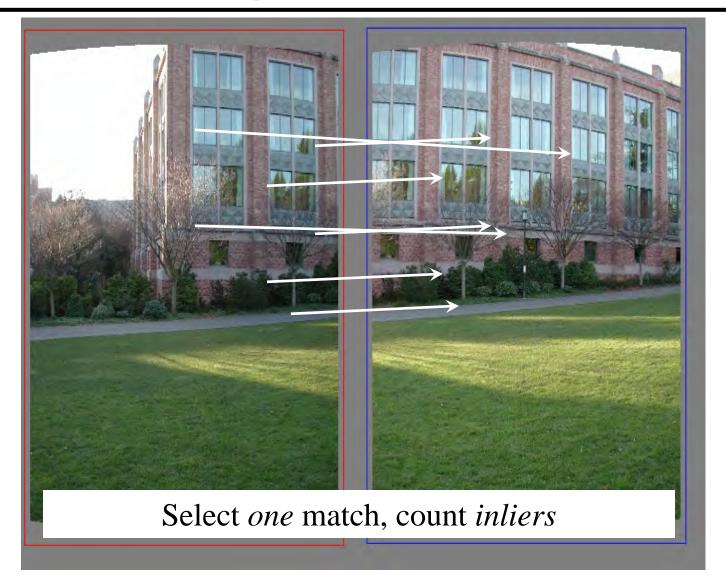
## Matching features



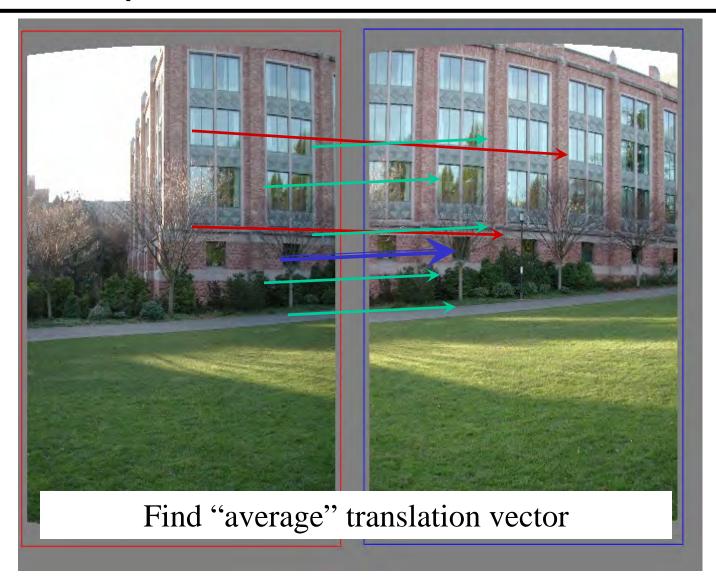
## RAndom SAmple Consensus



## RAndom SAmple Consensus



## Least squares fit

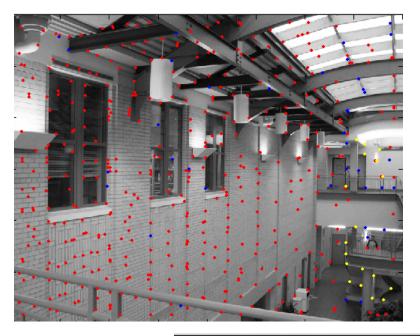


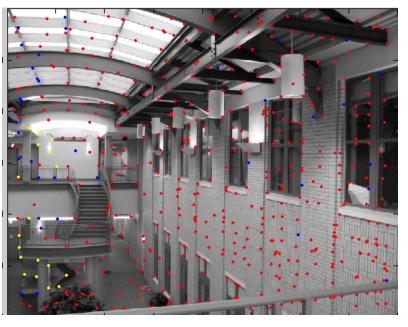
### RANSAC for estimating homography

#### RANSAC loop:

- Select four feature pairs (at random)
- 2. Compute homography H (exact)
- 3. Compute *inliers* where  $SSD(p_i', \mathbf{H} p_i) < \varepsilon$
- 4. Keep largest set of inliers
- Re-compute least-squares H estimate on all of the inliers

## **RANSAC**







# Example: Recognising Panoramas

M. Brown and D. Lowe, University of British Columbia

#### 1D Rotations ( $\theta$ )

#### 1D Rotations ( $\theta$ )



#### 1D Rotations ( $\theta$ )



#### 1D Rotations ( $\theta$ )



- 2D Rotations (θ, φ)
  - Ordering ⇒ matching images

#### 1D Rotations ( $\theta$ )



- 2D Rotations (θ, φ)
  - Ordering ⇒ matching images

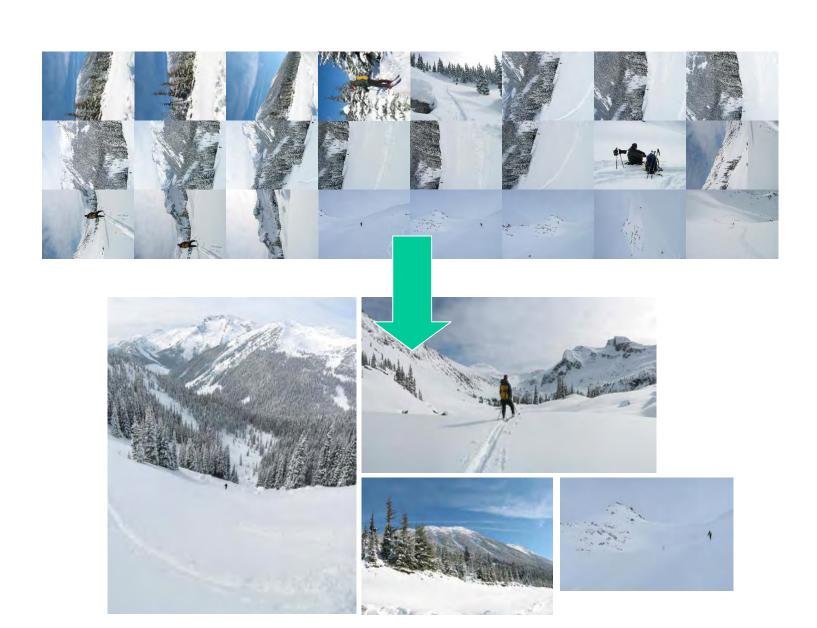


#### 1D Rotations ( $\theta$ )



- 2D Rotations (θ, φ)
  - Ordering ⇒ matching images





#### Overview

**Feature Matching** 

**Image Matching** 

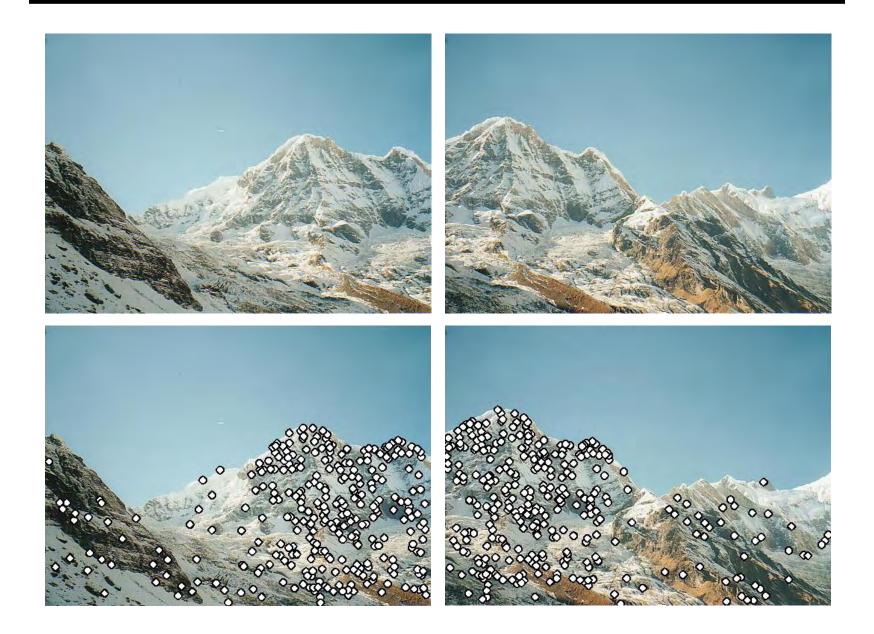
**Bundle Adjustment** 

Multi-band Blending

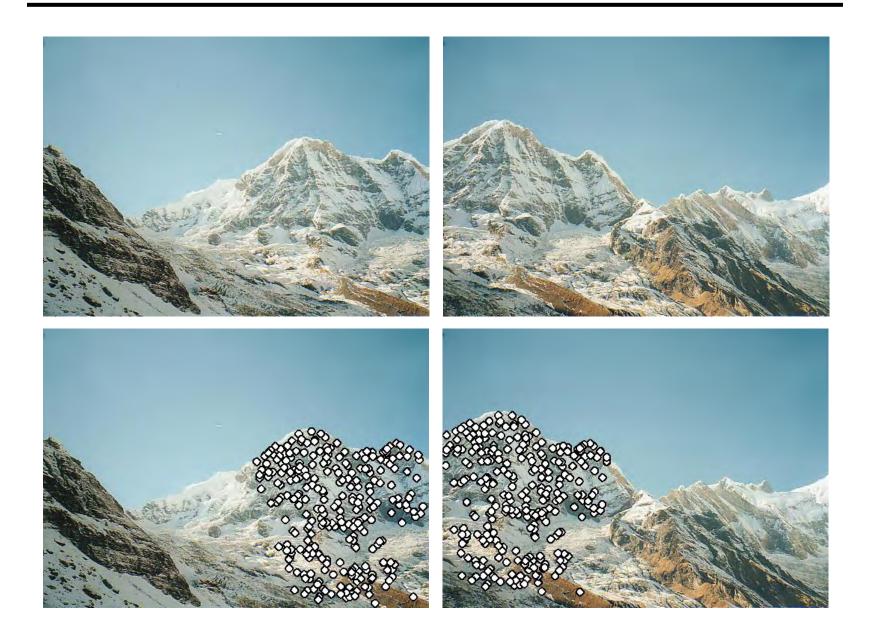
Results

Conclusions

# RANSAC for Homography



# RANSAC for Homography



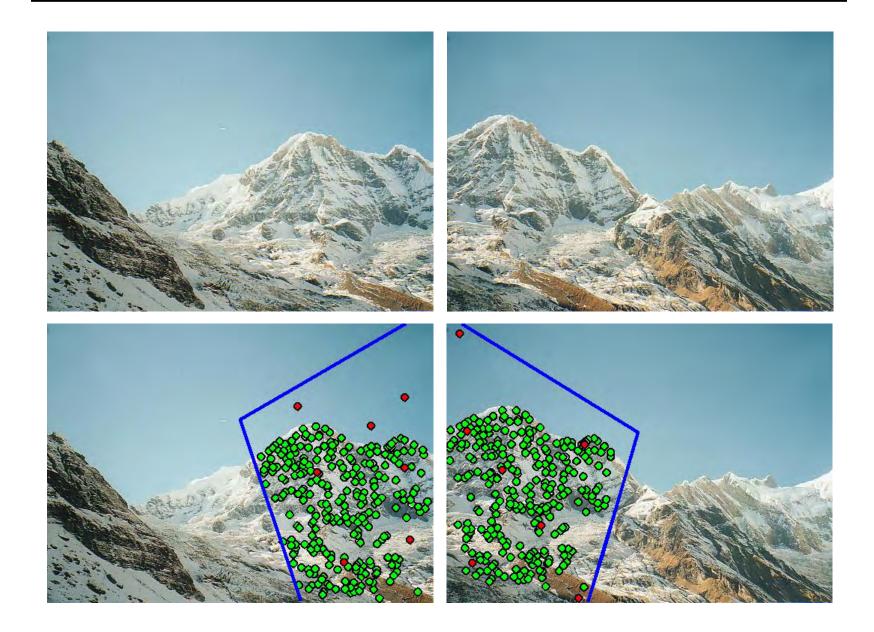
## RANSAC for Homography

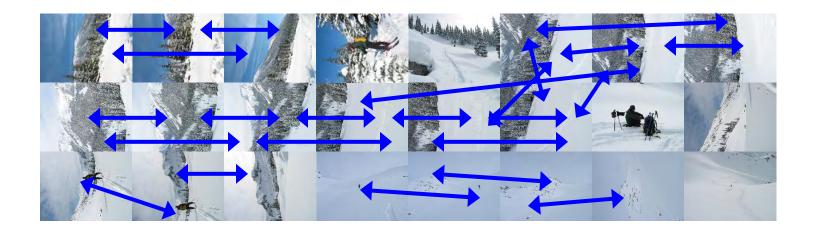


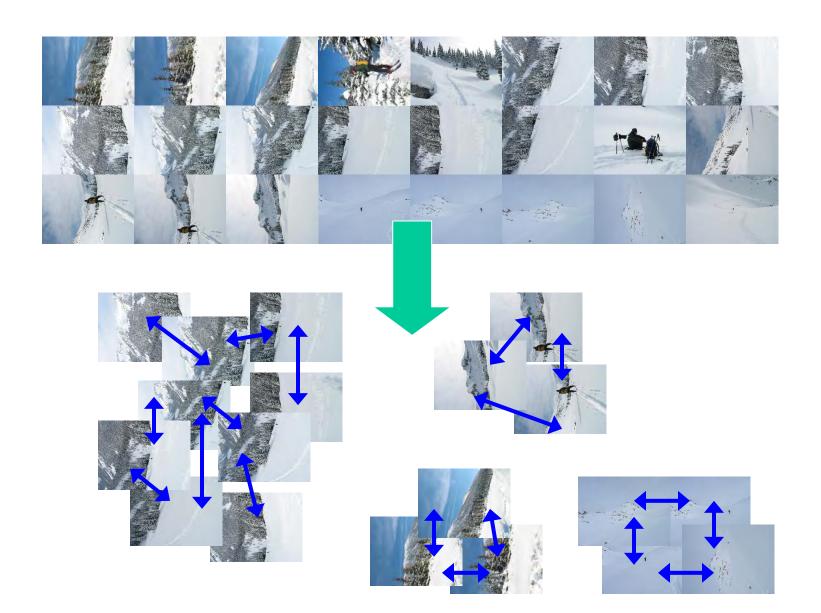


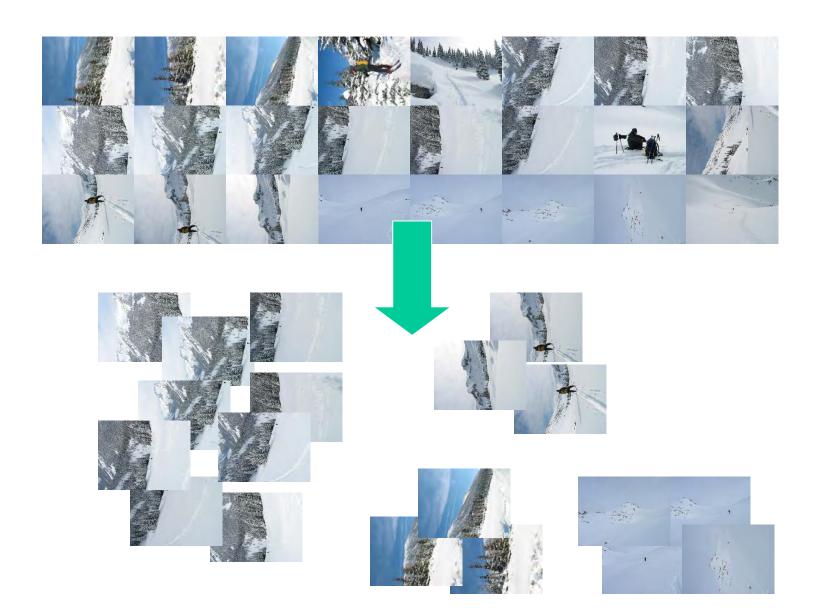


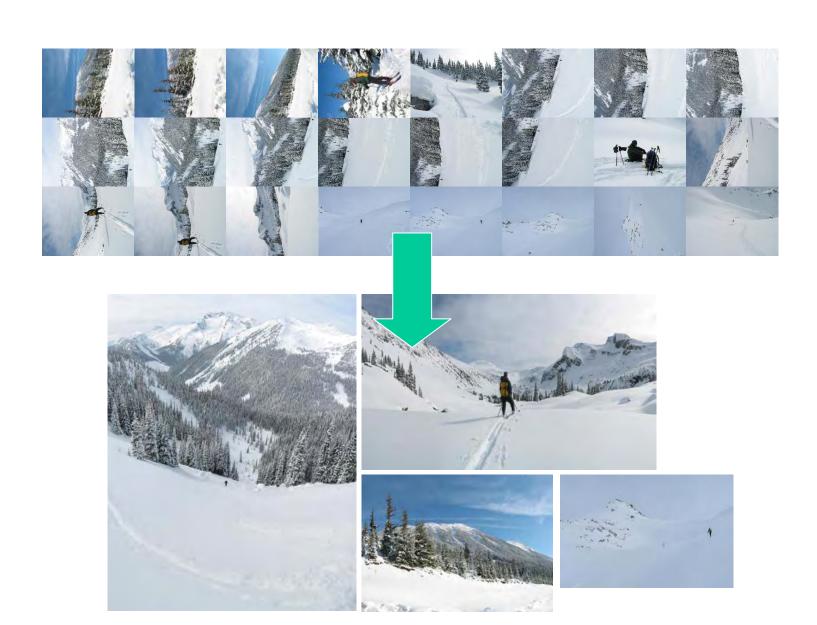
### Probabilistic model for verification











## Homography for Rotation

Parameterise each camera by rotation and focal length

$$\mathbf{R}_i = e^{[\boldsymbol{\theta}_i]_{\times}}, \quad [\boldsymbol{\theta}_i]_{\times} = \begin{bmatrix} 0 & -\theta_{i3} & \theta_{i2} \\ \theta_{i3} & 0 & -\theta_{i1} \\ -\theta_{i2} & \theta_{i1} & 0 \end{bmatrix}$$

This gives pairwise  $\mathbf{K}_i = egin{bmatrix} f_i & 0 & 0 \\ 0 & f_i & 0 \\ 0 & 0 & 1 \end{bmatrix}$ 

$$\tilde{\mathbf{u}}_i = \mathbf{H}_{ij} \tilde{\mathbf{u}}_j$$
,  $\mathbf{H}_{ij} = \mathbf{K}_i \mathbf{R}_i \mathbf{R}_j^T \mathbf{K}_j^{-1}$ 

## Bundle Adjustment

New images initialised with rotation, focal length of best matching image



### Bundle Adjustment

New images initialised with rotation, focal length of best matching image



## Multi-band Blending

#### Burt & Adelson 1983

• Blend frequency bands over range  $\propto \lambda$ 



## Results

