

# Data-driven Methods: Faces

---



Portrait of Piotr Gibas  
© Joaquin Rosales Gomez

15-463: Computational Photography  
Alexei Efros, CMU, Fall 2007

# The Power of Averaging

---



# 8-hour exposure

---



© Atta Kim

# Figure-centric averages

---



Antonio Torralba & Aude Oliva (2002)

**Averages:** Hundreds of images containing a person are averaged to reveal regularities in the intensity patterns across all the images.

# More by Jason Salavon

---



Homes for Sale



109 Homes for Sale,  
Seattle/Tacoma



117 Homes for Sale,  
Chicagoland



124 Homes for Sale, The 5  
Boroughs



121 Homes for Sale,  
LA/Orange County



114 Homes for Sale,  
Dallas/Ft. Worth Metroplex



112 Homes for Sale,  
Miami-Dade County

More at: <http://www.salavon.com/>

# “100 Special Moments” by Jason Salavon

---



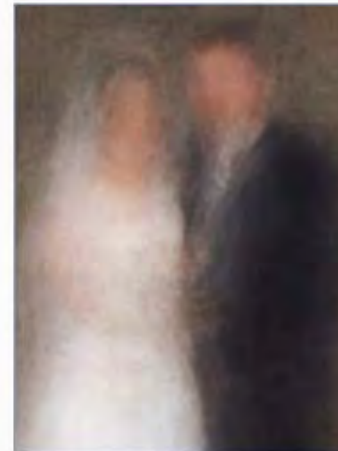
Little Leaguer



Kids with Santa



The Graduate



Newlyweds

Why  
blurry?

# Computing Means

---

Two Requirements:

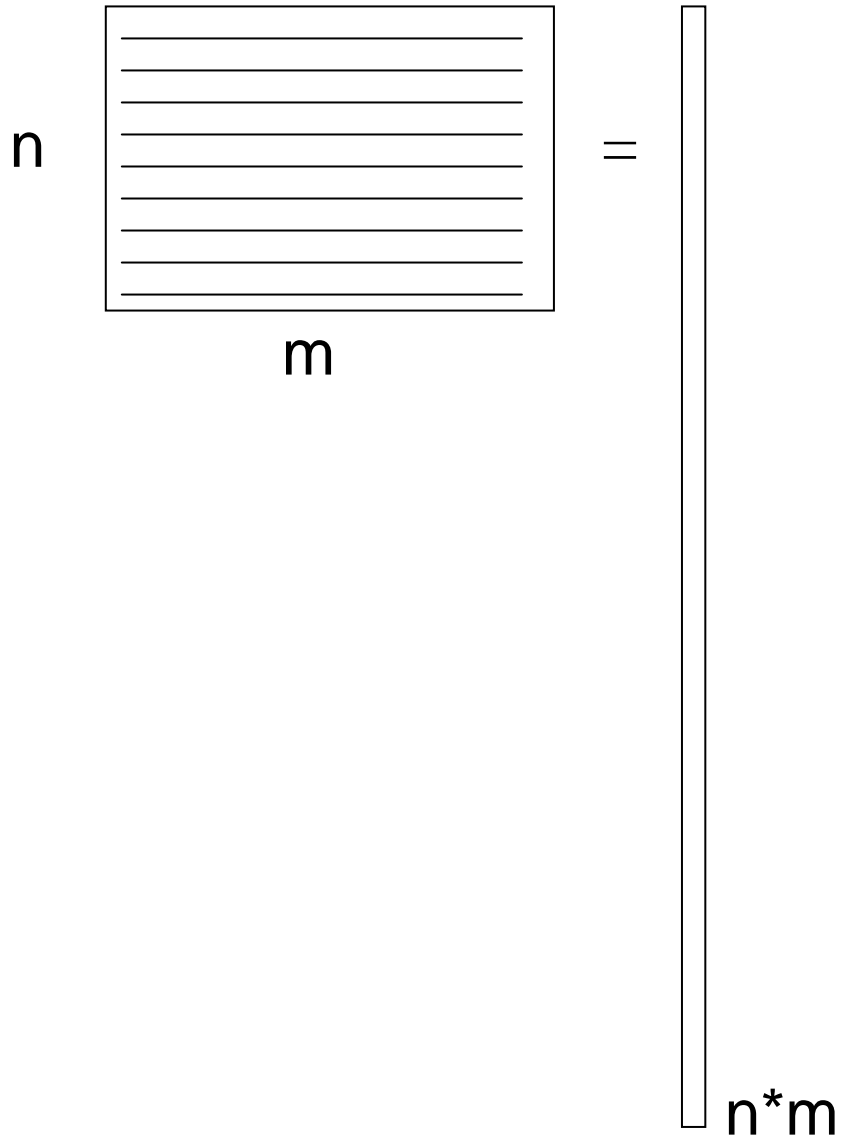
- Alignment of objects
- Objects must span a subspace

Useful concepts:

- Subpopulation means
- Deviations from the mean

# Images as Vectors

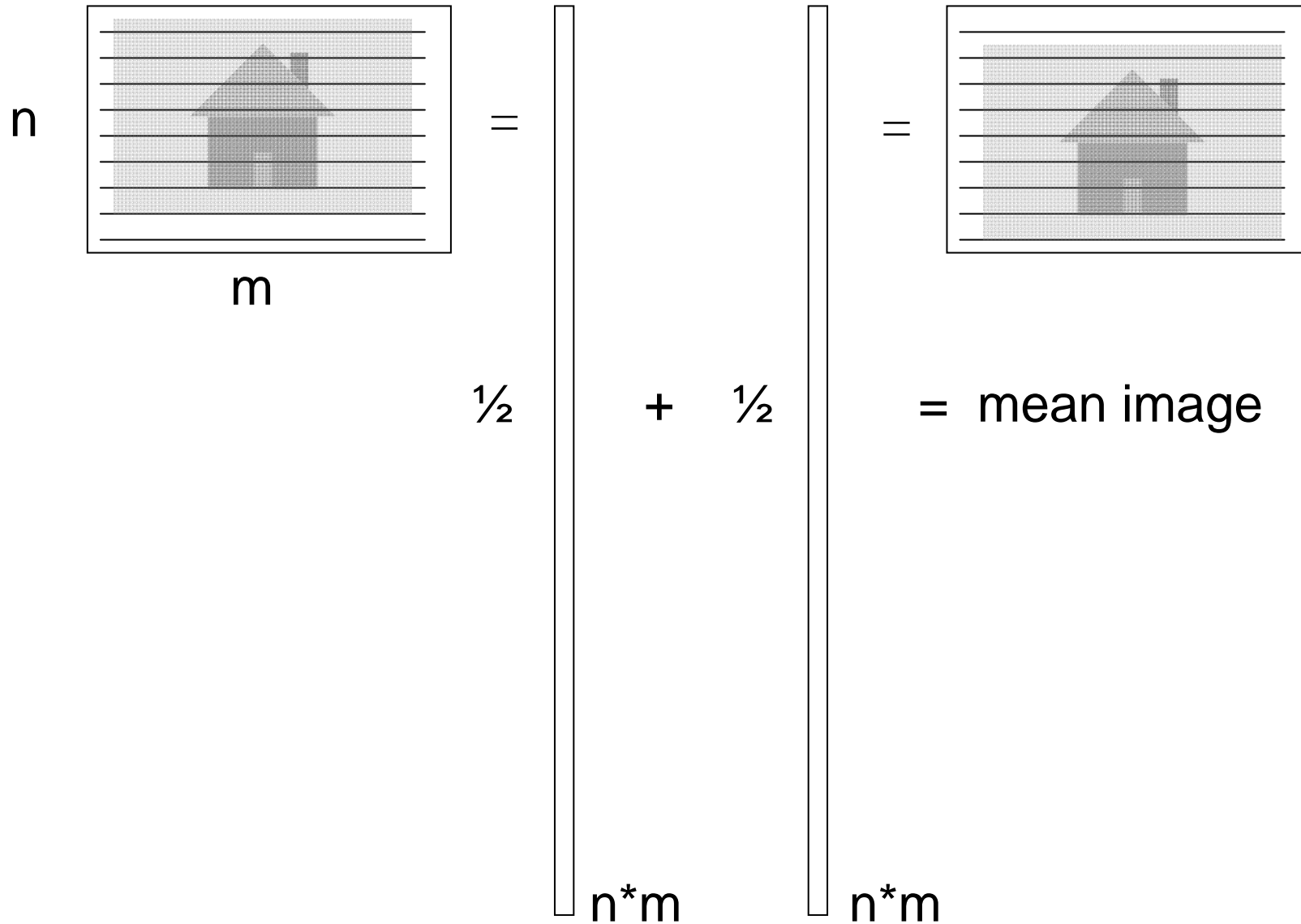
---





# Vector Mean: Importance of Alignment

---



# How to align faces?

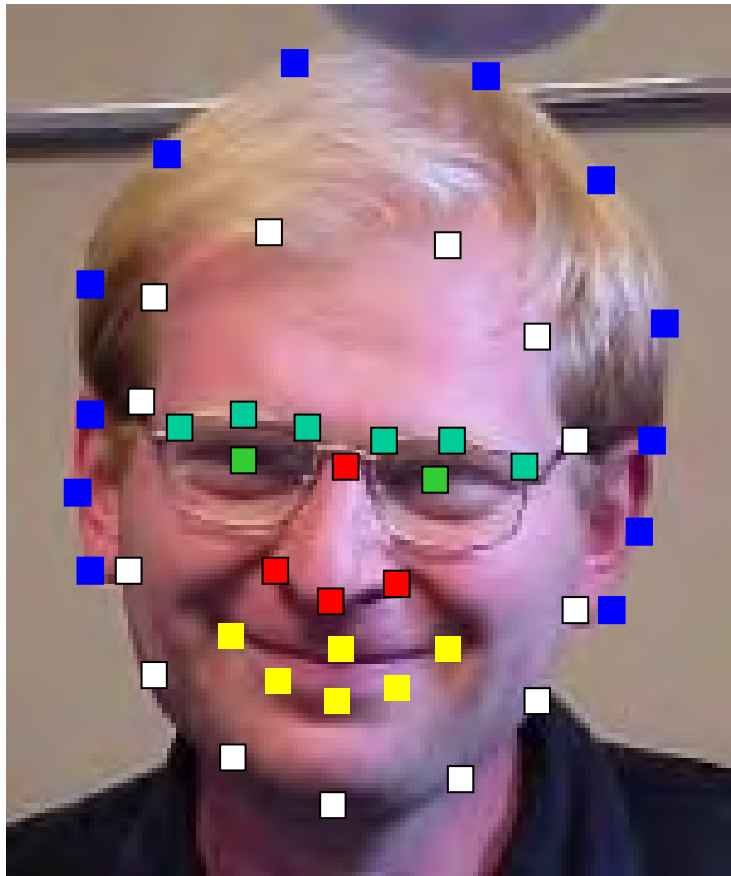
---



<http://www2.imm.dtu.dk/~aam/datasets/datasets.html>

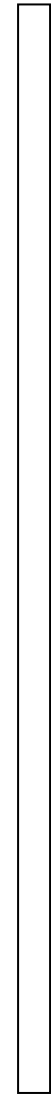
# Shape Vector

---



Provides alignment!

=



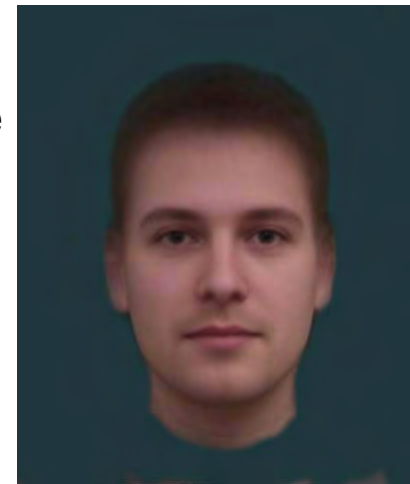
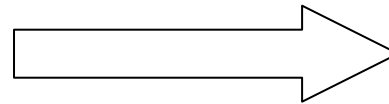
43

# Average Face

---

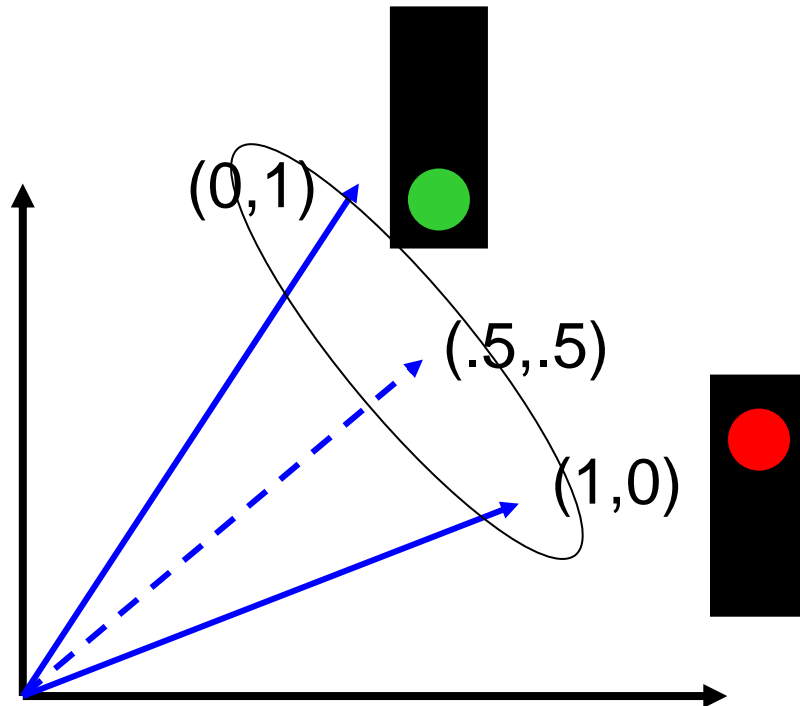


1. Warp to mean shape
2. Average pixels



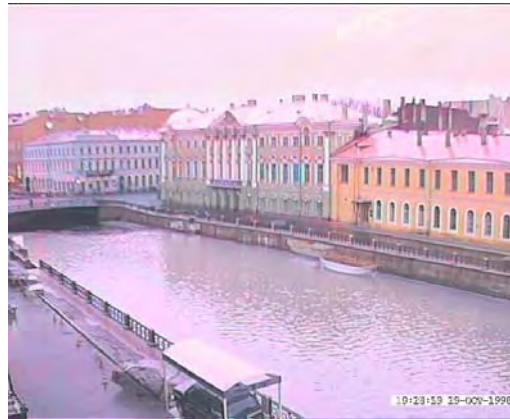
# Objects must span a subspace

---



# Example

---



mean

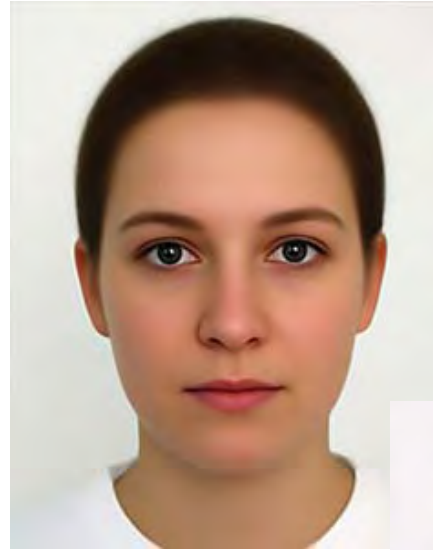
Does not span a subspace

# Subpopulation means

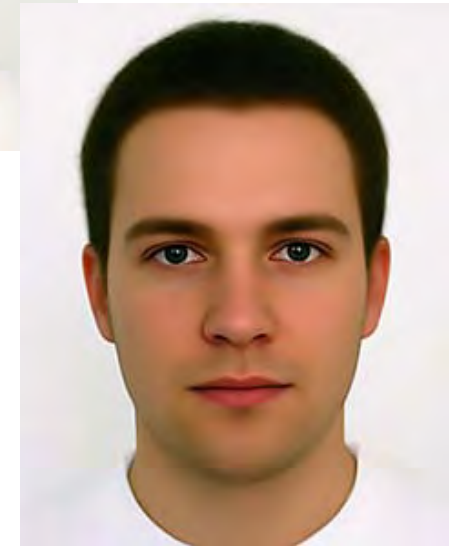
---

Examples:

- Happy faces
- Young faces
- Asian faces
- Etc.
- Sunny days
- Rainy days
- Etc.
- Etc.



Average female



Average male

# Deviations from the mean



Image  $X$



Mean  $\bar{X}$

=

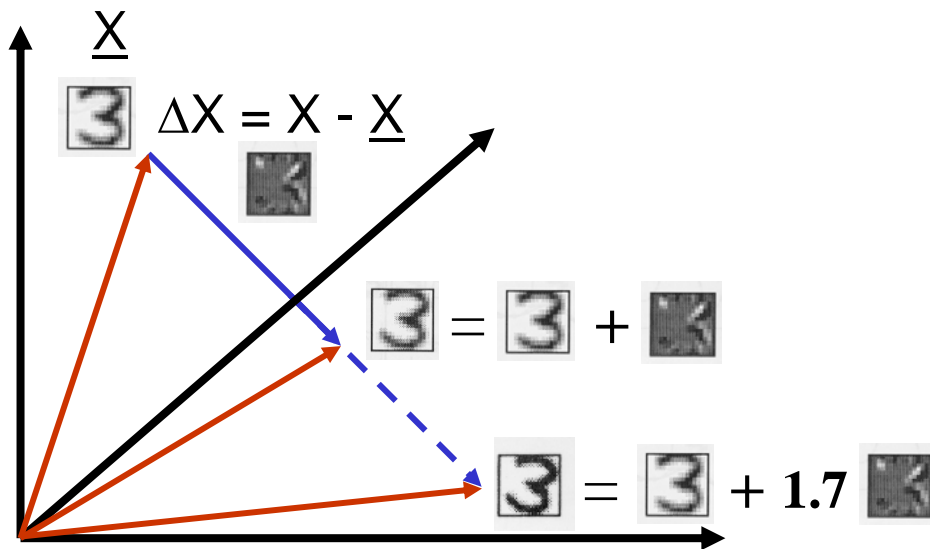


$$\Delta X = X - \bar{X}$$



# Deviations from the mean

---



---

# Manipulating Facial Appearance through Shape and Color

Duncan A. Rowland and David I. Perrett

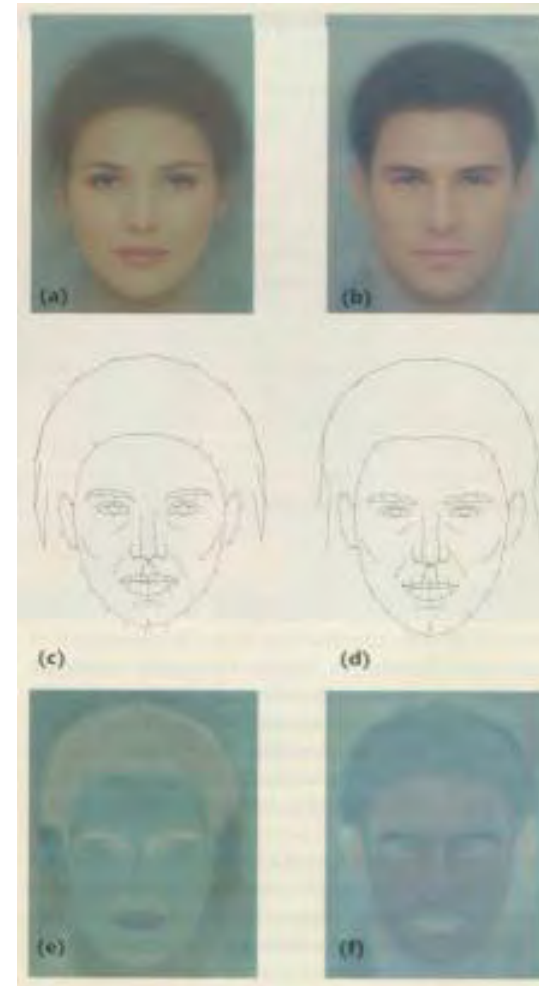
*St Andrews University*

IEEE CG&A, September 1995

# Face Modeling

---

Compute *average* faces  
(color and shape)



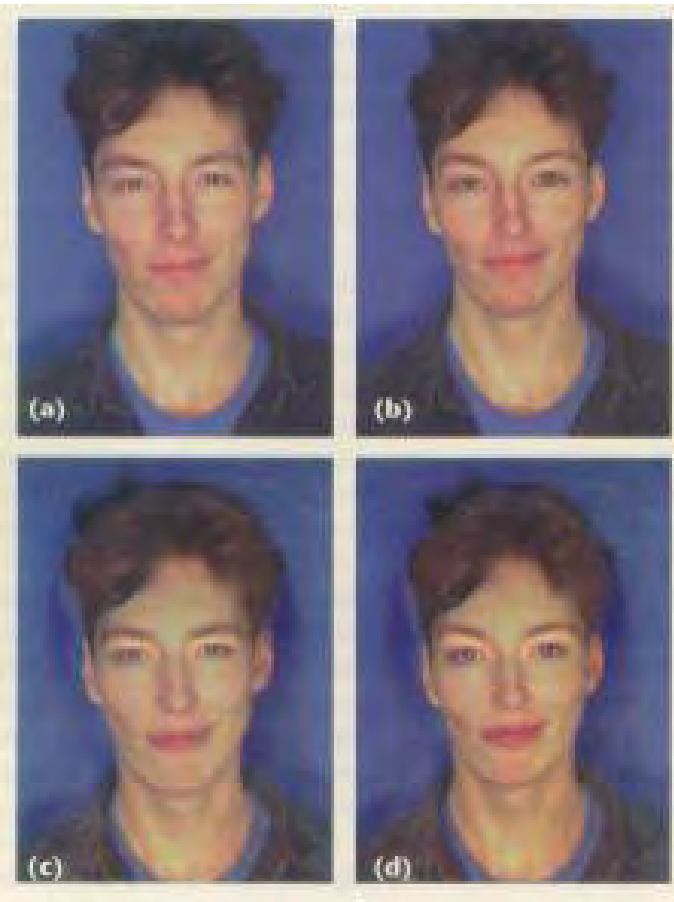
Compute *deviations*  
between male and  
female (vector and color  
differences)

# Changing gender

---

Deform shape and/or color of an input face in the direction of “more female”

original



shape

color

both

# Enhancing gender

---



more same **original** androgynous more opposite

# Changing age

---

Face becomes  
“rounder” and “more  
textured” and “grayer”

original



shape

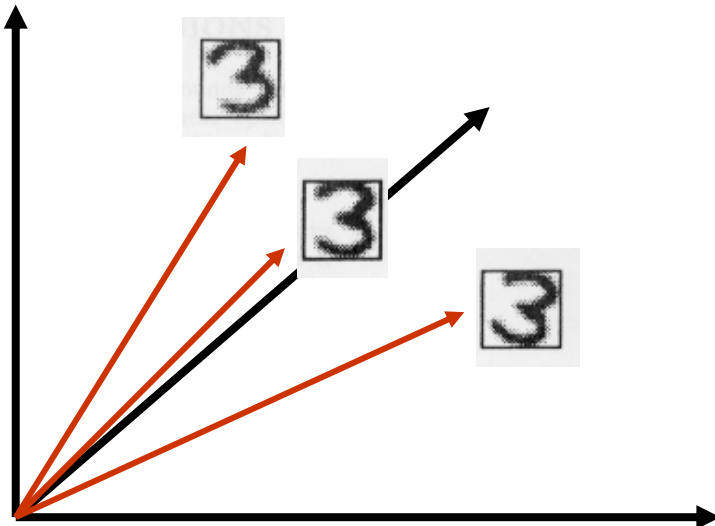
color



both

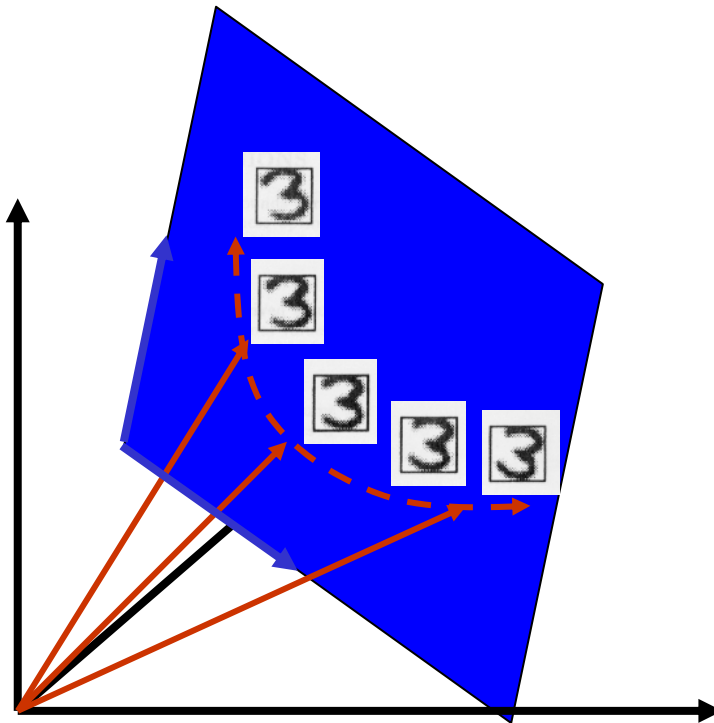
# Back to the Subspace

---



# Linear Subspace: convex combinations

---



Any new image  $X$  can be obtained as weighted sum of stored “basis” images.

$$X = \sum_{i=1}^m a_i X_i$$

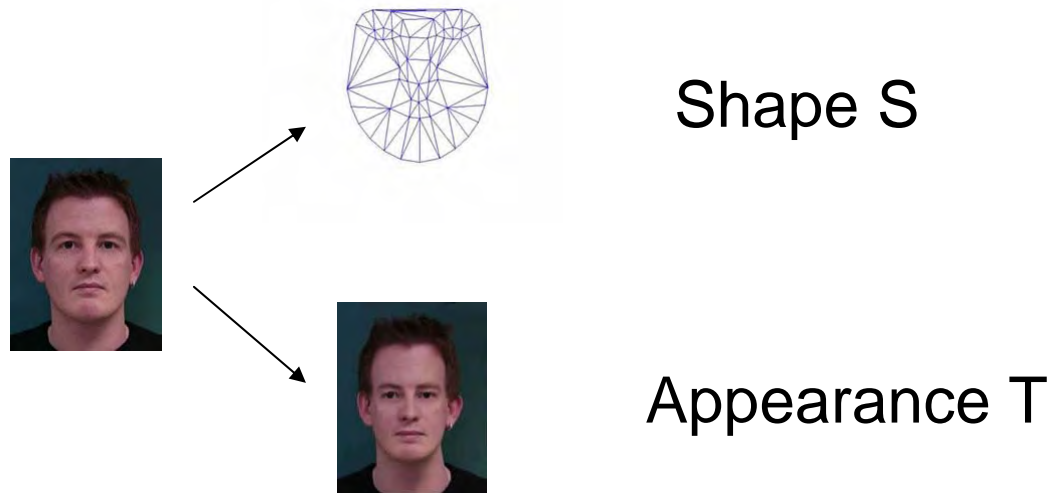
Our old friend, change of basis!  
What are the new coordinates of  $X$ ?



# The Morphable Face Model

---

The actual structure of a face is captured in the shape vector  $\mathbf{S} = (x_1, y_1, x_2, \dots, y_n)^T$ , containing the  $(x, y)$  coordinates of the  $n$  vertices of a face, and the appearance (texture) vector  $\mathbf{T} = (R_1, G_1, B_1, R_2, \dots, G_n, B_n)^T$ , containing the color values of the mean-warped face image.



# The Morphable face model

---

Again, assuming that we have  $m$  such vector pairs in full correspondence, we can form new shapes  $\mathbf{S}_{model}$  and new appearances  $\mathbf{T}_{model}$  as:

$$\mathbf{S}_{model} = \sum_{i=1}^m a_i \mathbf{S}_i \quad \mathbf{T}_{model} = \sum_{i=1}^m b_i \mathbf{T}_i$$

$$s = \alpha_1 \cdot \text{img}_1 + \alpha_2 \cdot \text{img}_2 + \alpha_3 \cdot \text{img}_3 + \alpha_4 \cdot \text{img}_4 + \dots = \mathbf{S} \cdot \mathbf{a}$$

$$t = \beta_1 \cdot \text{img}_1 + \beta_2 \cdot \text{img}_2 + \beta_3 \cdot \text{img}_3 + \beta_4 \cdot \text{img}_4 + \dots = \mathbf{T} \cdot \mathbf{b}$$

If number of basis faces  $m$  is large enough to span the face subspace then:

Any new face can be represented as a pair of vectors

$$(\alpha_1, \alpha_2, \dots, \alpha_m)^T \text{ and } (\beta_1, \beta_2, \dots, \beta_m)^T !$$

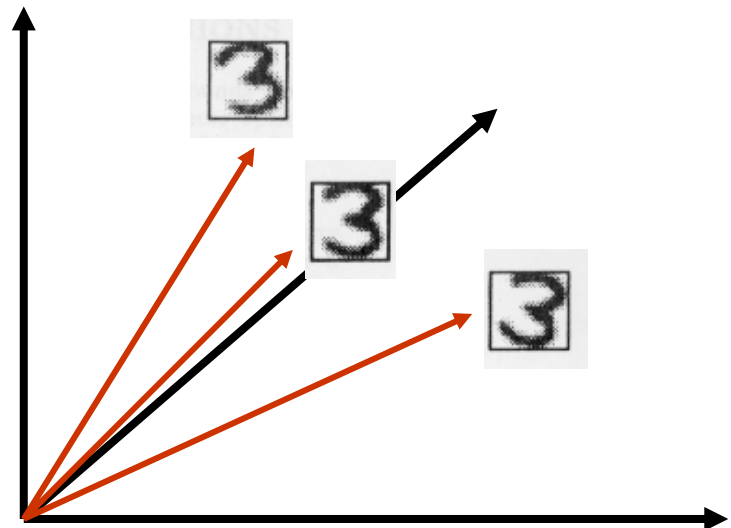
# Issues:

---

1. How many basis images is enough?
2. Which ones should they be?
3. What if some variations are more important than others?
  - E.g. corners of mouth carry much more information than haircut

Need a way to obtain basis images automatically, in order of importance!

But what's important?

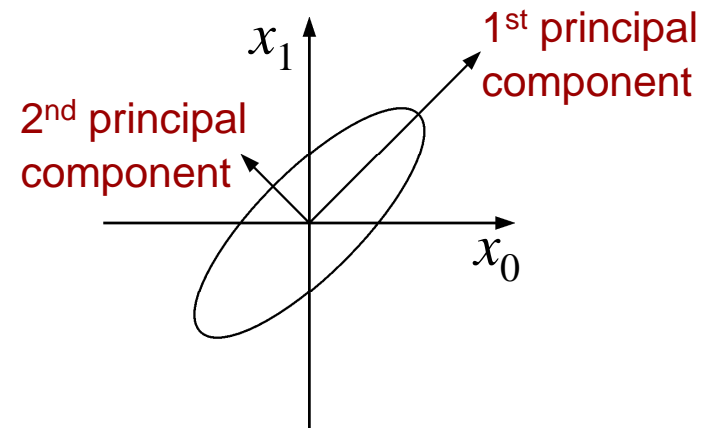
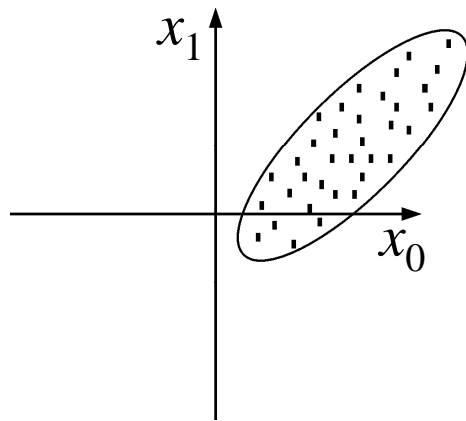


# Principal Component Analysis

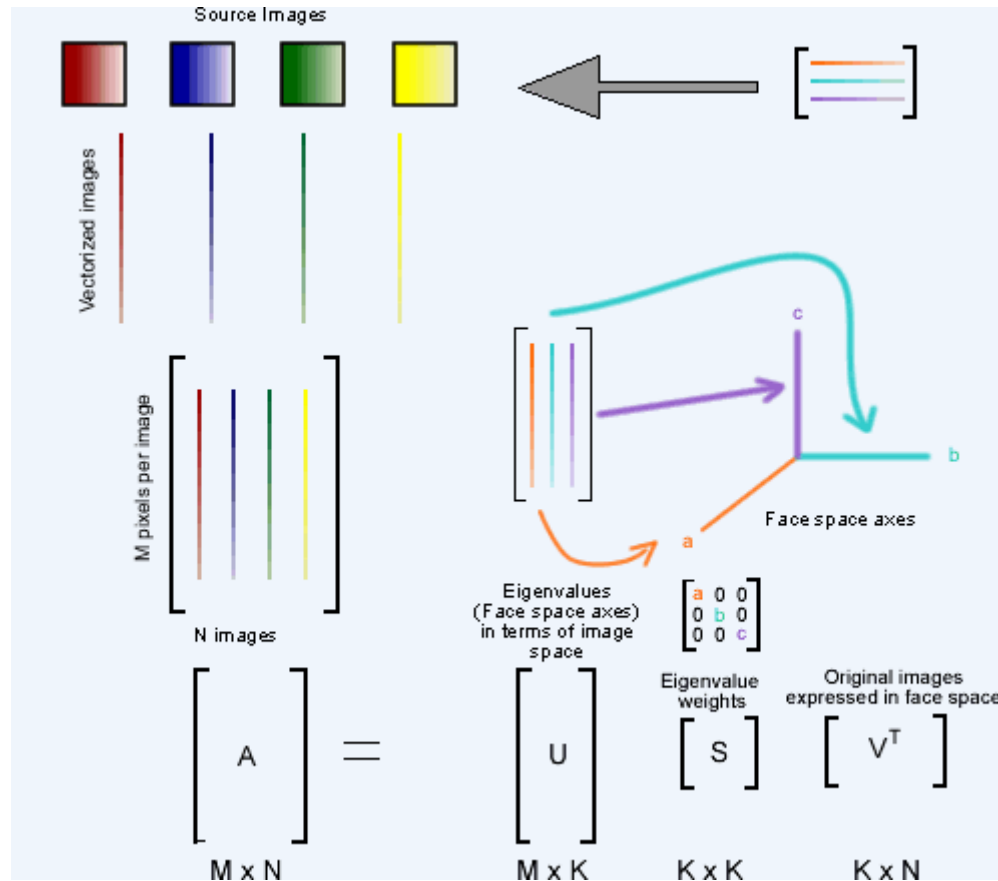
---

Given a point set  $\{\vec{p}_j\}_{j=1\dots P}$ , in an  $M$ -dim space, PCA finds a basis such that

- coefficients of the point set in that basis are uncorrelated
- first  $r < M$  basis vectors provide an approximate basis that minimizes the mean-squared-error (MSE) in the approximation (over all bases with dimension  $r$ )



# PCA via Singular Value Decomposition



$$[u, s, v] = \text{svd}(A);$$

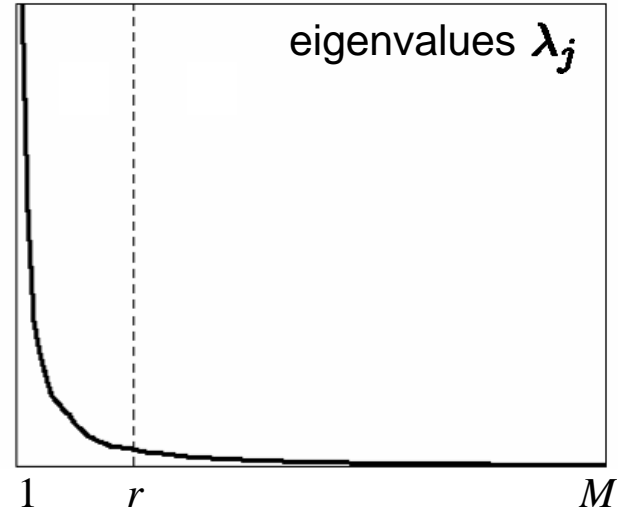
# Principal Component Analysis

---

## Choosing subspace dimension

$r$ :

- look at decay of the eigenvalues as a function of  $r$
- Larger  $r$  means lower expected error in the subspace data approximation

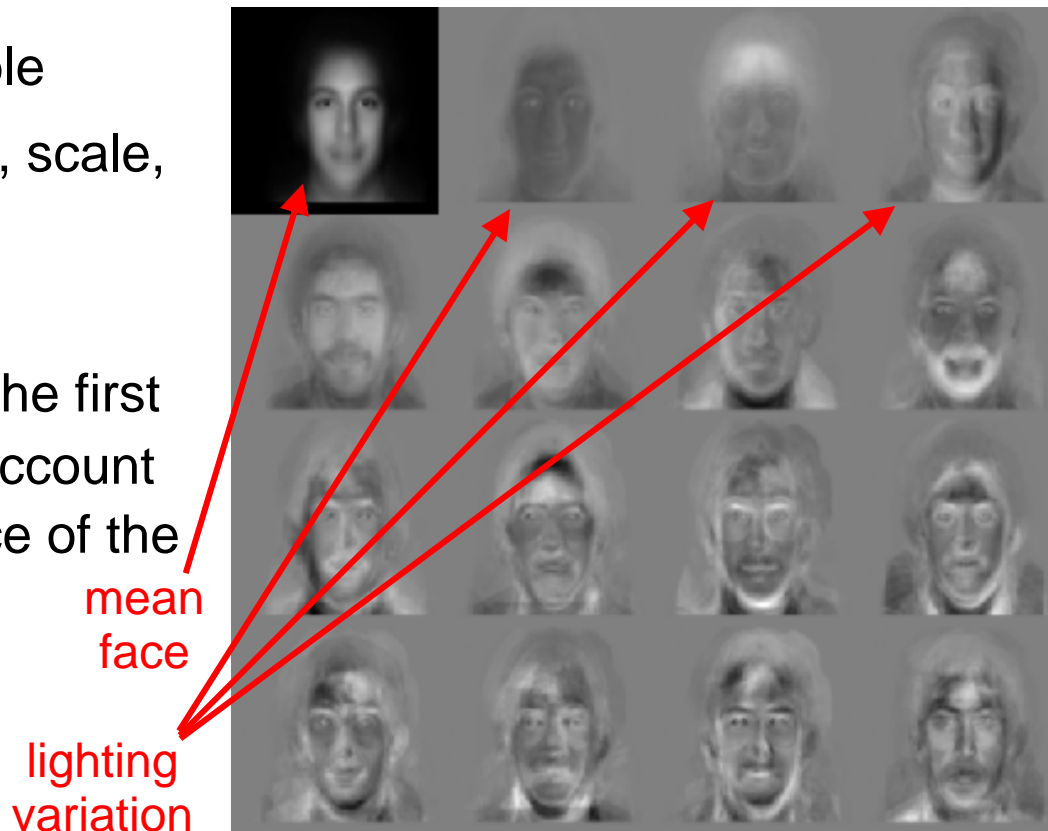


# EigenFaces

---

First popular use of PCA on images was for modeling and recognition of faces [Kirby and Sirovich, 1990, Turk and Pentland, 1991]

- Collect a face ensemble
- Normalize for contrast, scale, & orientation.
- Remove backgrounds
- Apply PCA & choose the first  $N$  eigen-images that account for most of the variance of the data.

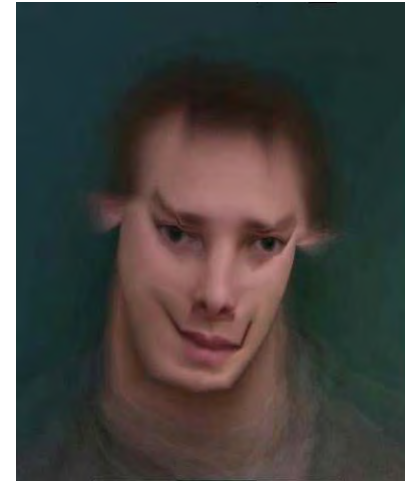
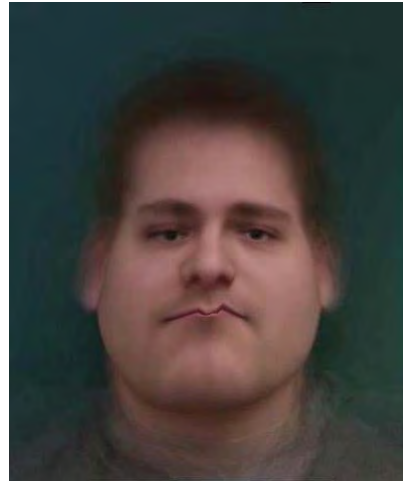
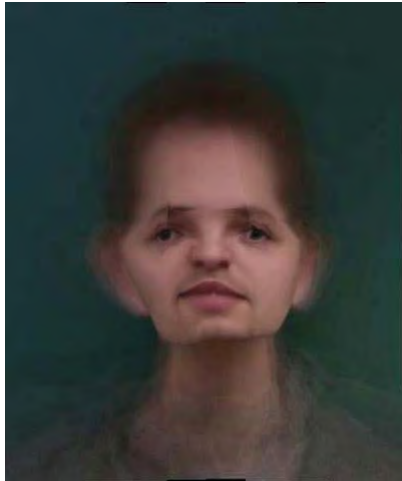


# First 3 Shape Basis

---



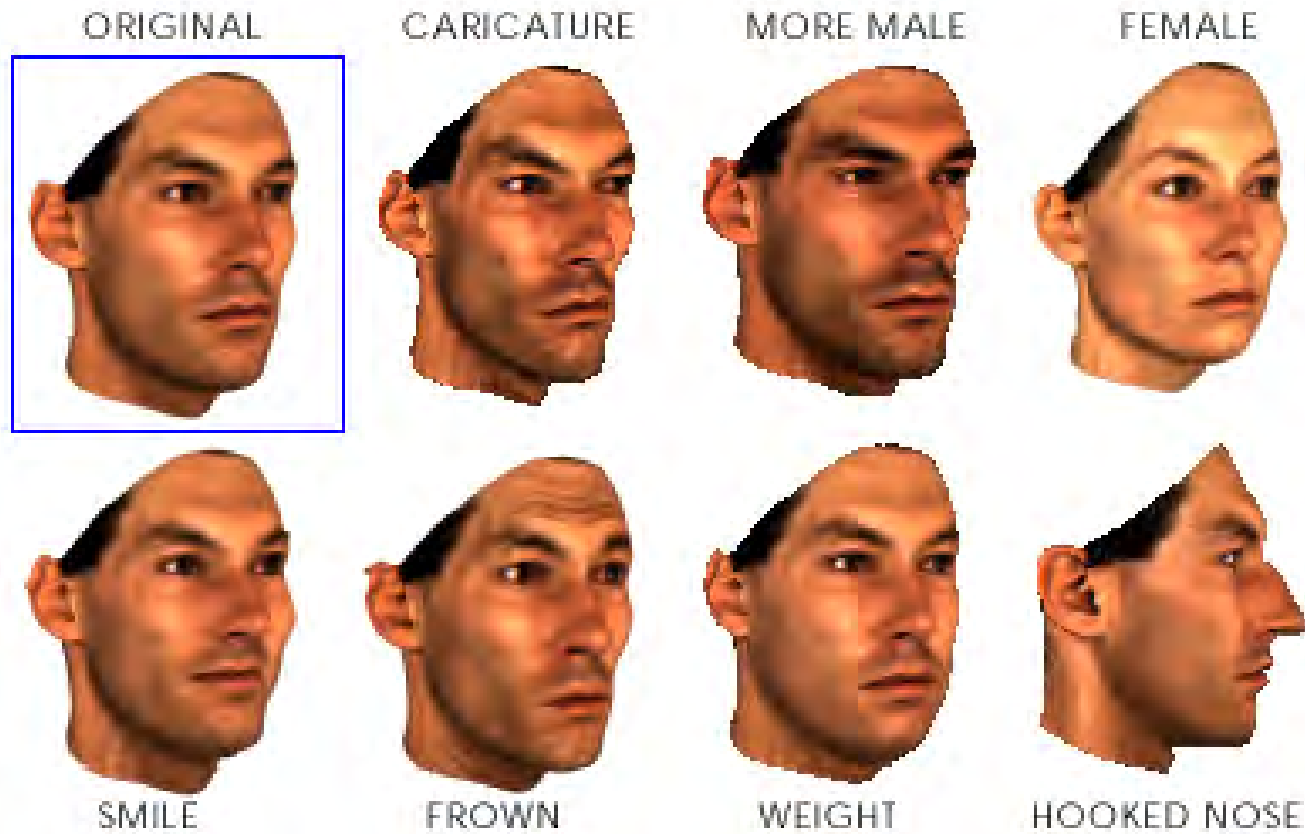
Mean appearance





# Using 3D Geometry: Blinz & Vetter, 1999

---



show SIGGRAPH video