

# Matting and Transparency

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*L.Wellmann 2002*

15-463: Computational Photography  
Alexei Efros, CMU, Fall 2007

# How does Superman fly?

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Super-human powers?

OR

Image Matting?

# “Pulling a Matte”

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## Problem Definition:

- The separation of an image  $C$  into
  - A foreground object image  $C_o$ ,
  - a background image  $C_b$ ,
  - and an alpha matte  $\alpha$
- $C_o$  and  $\alpha$  can then be used to composite the foreground object into a different image

## Hard problem

- Even if alpha is binary, this is hard to do automatically (background subtraction problem)
- For movies/TV, manual segmentation of each frame is infeasible
- Need to make a simplifying assumption...

# Average/Median Image

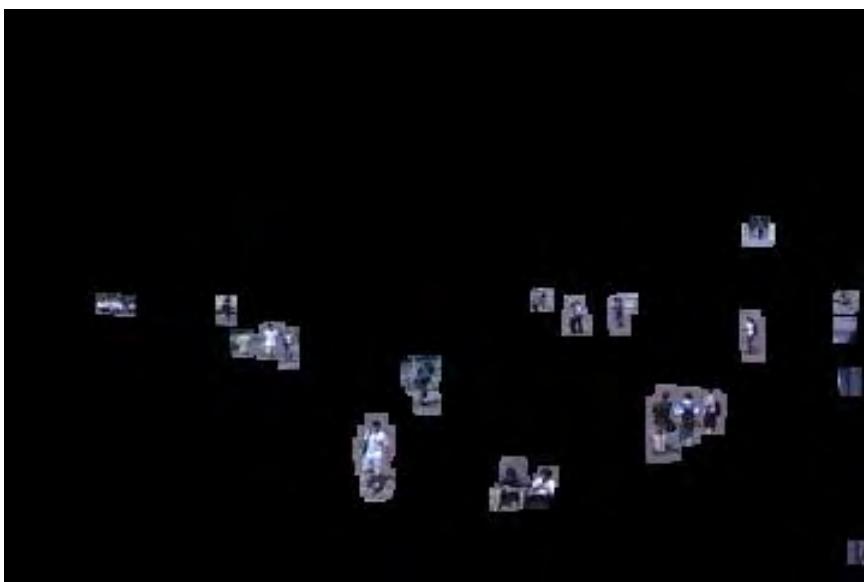
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What can we do with this?



# Background Subtraction

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# Crowd Synthesis (with Pooja Nath)

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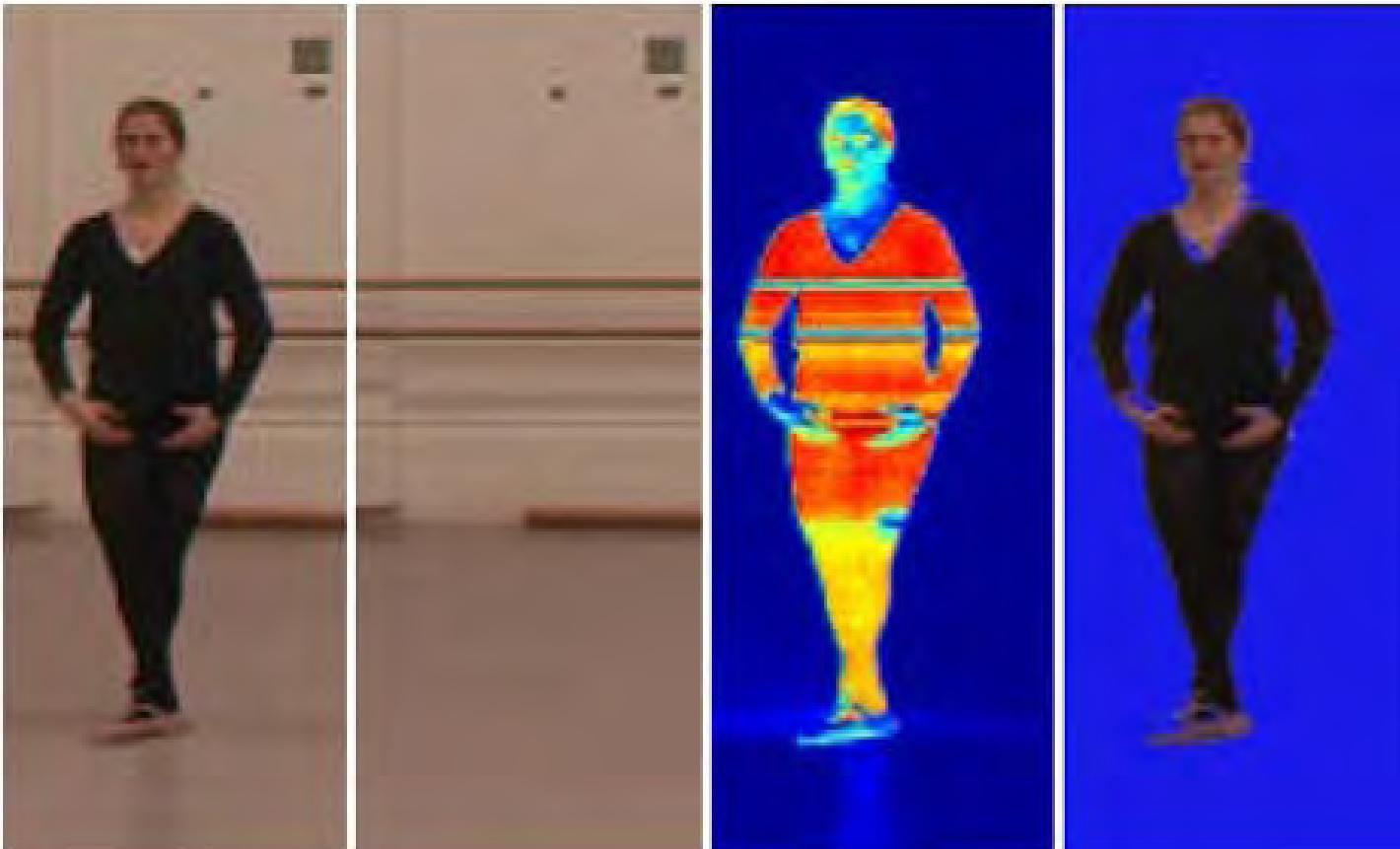


1. Do background subtraction in each frame
2. Find and record “blobs”
3. For synthesis, randomly sample the blobs, taking care not to overlap them

# Background Subtraction

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A largely unsolved problem...



One video  
frame

Estimated  
background

Difference  
Image

Thresholded  
Foreground  
on blue

# Blue Screen

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# Blue Screen matting

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Most common form of matting in TV studios & movies

Petros Vlahos invented blue screen matting in the 50s.

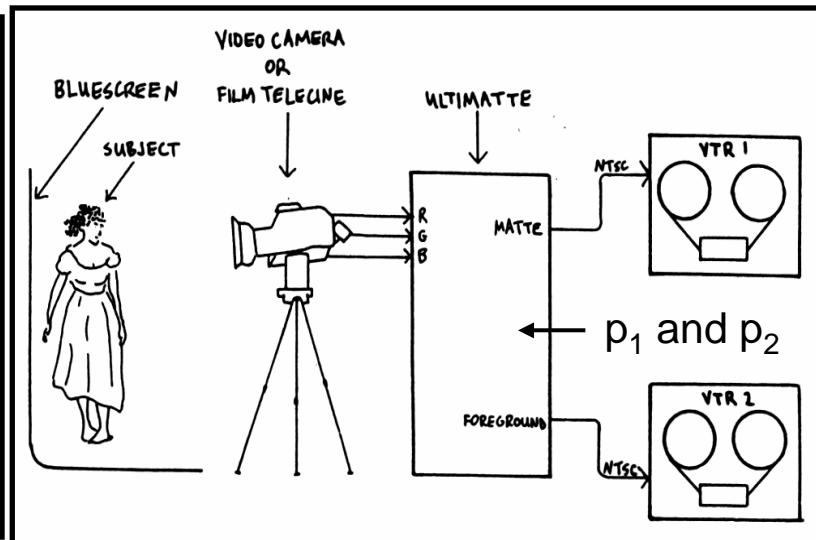
His Ultimatte® is still the most popular equipment. He won an Oscar for lifetime achievement.

A form of background subtraction:

- Need a known background
- Compute alpha as  $\text{SSD}(C, C_b) > \text{threshold}$ 
  - Or use Vlahos' formula:  $\alpha = 1 - p_1(B - p_2G)$
- Hope that foreground object doesn't look like background
  - no blue ties!
- Why blue?
- Why uniform?

# The Ultimatte

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# Blue screen for superman?

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# Semi-transparent mattes

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compositing glass with  
portrait using  
a semi -transparent matte

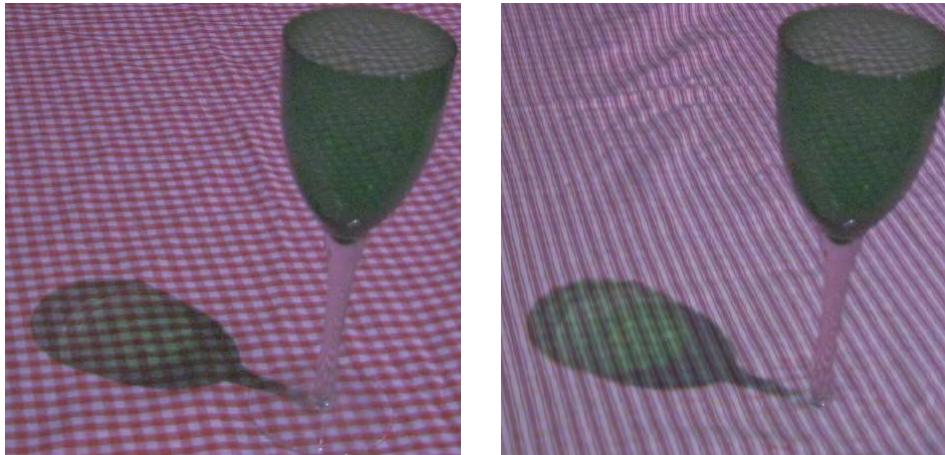


What we really want is to obtain a true alpha matte,  
which involves semi-transparency

- Alpha between 0 and 1

# Review: two issues

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Semi-transparent objects



Pixels too large

# Review: alpha channel

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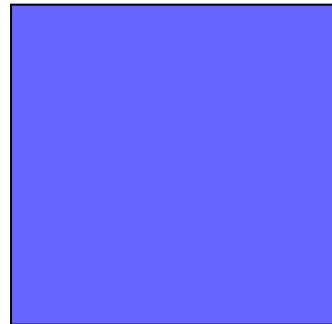
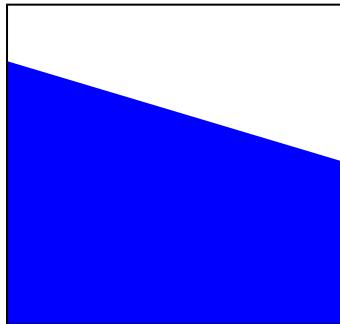
Add one more channel:

- `Image(R,G,B,alpha)`     *Sprite!*

Encodes transparency (or pixel coverage):

- Alpha = 1:              opaque object (complete coverage)
- Alpha = 0:              transparent object (no coverage)
- $0 < \text{Alpha} < 1$ :      semi-transparent (partial coverage)

Example:  $\text{alpha} = 0.7$



Partial coverage      or      semi-transparency

# Matting Problem: Mathematical Definition

For every pixel in the composite image,  
given

- backing color  $C_k = [R_k \ G_k \ B_k]$ , and
- composite pixel color  $C = [R \ G \ B]$

compute

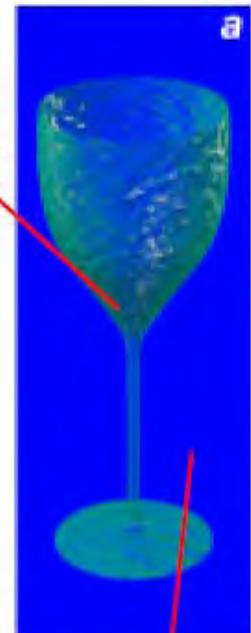
- foreground pixel color

$$C_o = [R_o \ G_o \ B_o \ \alpha_o] \quad (= [\alpha_o R_o \ \alpha_o G_o \ \alpha_o B_o])$$

such that

The matting  
equation

$$C = C_o + (1 - \alpha_o) C_k$$



$$\alpha_o = 0$$

# Why is general matting hard?

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Matting Equation:

$$C = C_o + (1 - \alpha_o) C_k$$

# Solution #1: No Blue!

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Matting Equation:

$$C = C_o + (1 - \alpha_o) C_k$$

- If we know that the foreground contains no blue, we have  $B_o = 0$
- This leaves us with 3 equations and 3 unknowns, which has exactly one solution

Main difficulty:

$$\begin{aligned} R &= \alpha_o R_o + (1 - \alpha_o) R_k && \leftarrow 3. \text{ Solve for } R_o \\ G &= \alpha_o G_o + (1 - \alpha_o) G_k && \leftarrow 2. \text{ Solve for } G_o \\ B &= B_k - \alpha_o B_k && \leftarrow 1. \text{ Solve for } \alpha_o \end{aligned}$$

# Solution #2: Gray or Flesh

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Matting Equation:

$$C = C_o + (1 - \alpha_o) C_k$$

- If we know that the foreground contains gray, that means that  $R_o = B_o = G_o$
- This leaves us with 3 equations and 2 unknowns

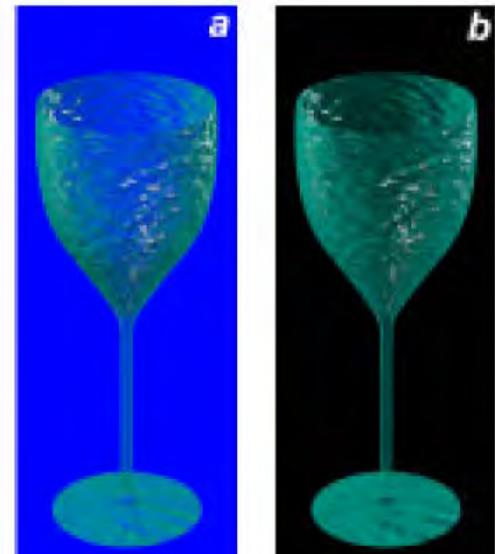
# Triangulation Matting (Smith & Blinn)

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Matting Equation:

$$C = C_o + (1 - \alpha_o) C_k$$

- Instead of reducing the number of unknowns, we could attempt to increase the number of equations
- One way to do this is to photograph an object of interest in front of two known but distinct backgrounds



How many equations?

How many unknowns?

Does the background need to be constant color?

# The Algorithm

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For every pixel p in the composite image,

given

- backing color  $C_{k1} = [R_{k1} \ G_{k1} \ B_{k1}]$  at p,
- backing color  $C_{k2} = [R_{k2} \ G_{k2} \ B_{k2}]$  at p,
- composite pixel color  $C_1 = [R_1 \ G_1 \ B_1]$  at p, and
- composite pixel color  $C_2 = [R_2 \ G_2 \ B_2]$  at p,

solve the system of 6 equations

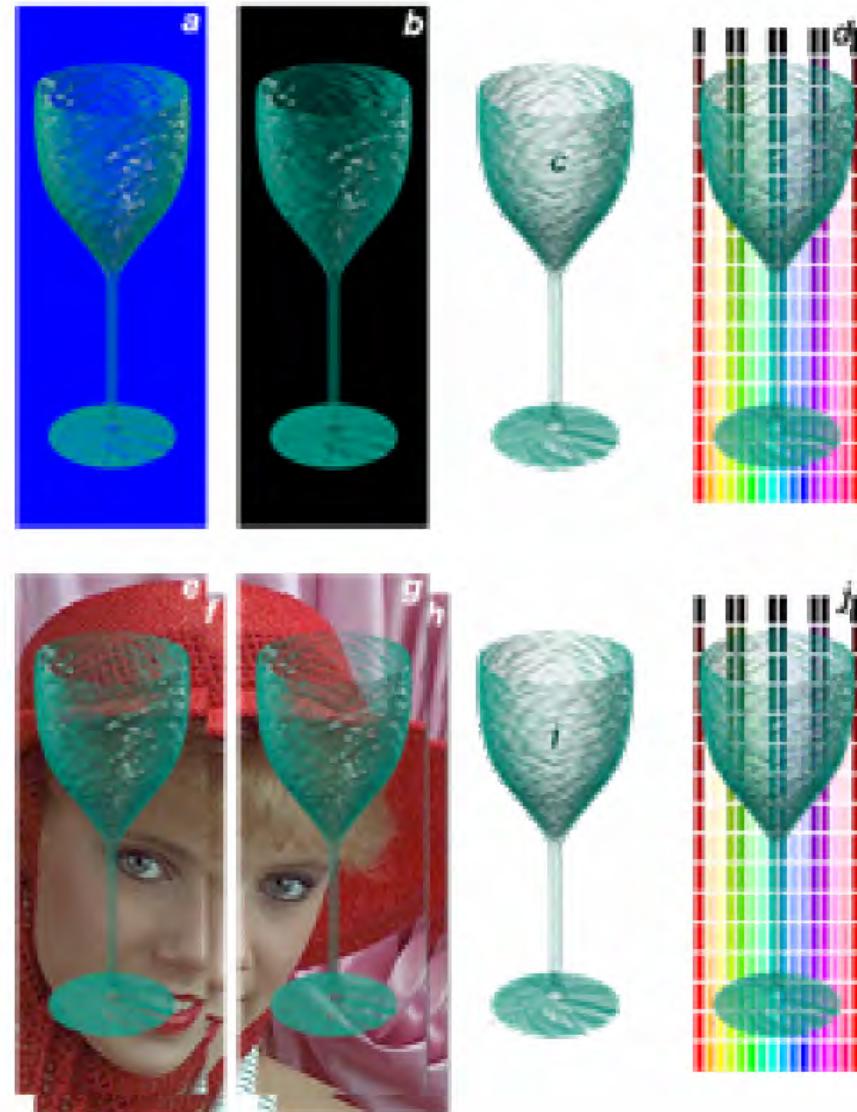
$$\begin{array}{ll} R_1 = \alpha_o R_o + (1 - \alpha_o) R_{k1} & R_2 = \alpha_o R_o + (1 - \alpha_o) R_{k2} \\ G_1 = \alpha_o G_o + (1 - \alpha_o) G_{k1} & G_2 = \alpha_o G_o + (1 - \alpha_o) G_{k2} \\ B_1 = \alpha_o B_o + (1 - \alpha_o) B_{k1} & B_2 = \alpha_o B_o + (1 - \alpha_o) B_{k2} \end{array}$$

for unknowns  $R_o, G_o, B_o, \alpha_o$

# Triangulation Matting Examples

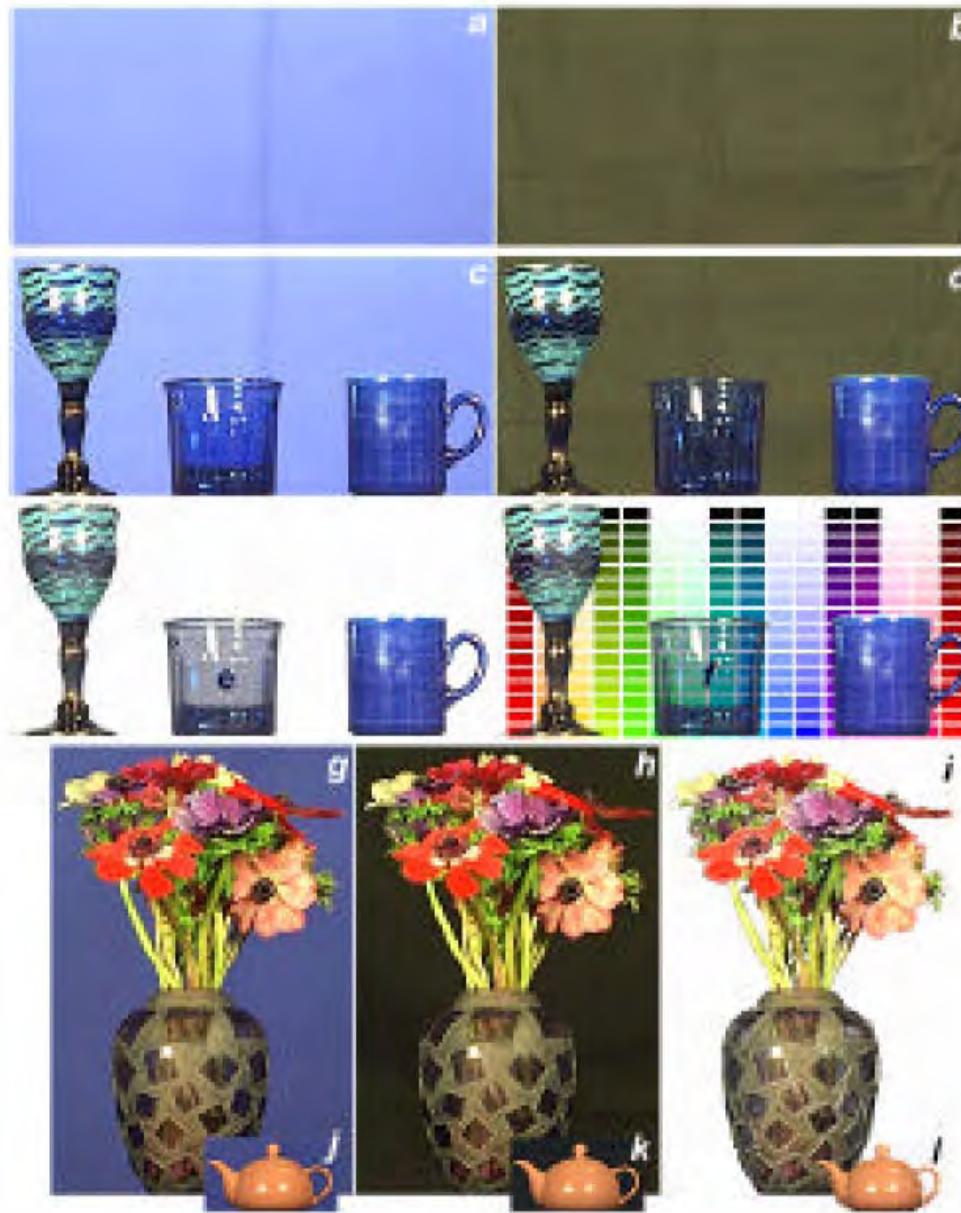
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From Smith & Blinn's  
SIGGRAPH'96 paper



# More Examples

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# More examples

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# Problems with Matting

Images do not look realistic

Lack of Refracted Light

Lack of Reflected Light

**Solution:**  
Modify the Matting Equation



# Environment Matting and Compositing

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slides by Jay Hetler

Douglas E. Zongker ~ Dawn M. Werner ~ Brian Curless ~ David H. Salsin

# Environment Matting Equation

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$$C = F + (1 - \alpha)B + \Phi$$

$C$  ~ Color

$F$  ~ Foreground color

$B$  ~ Background color

$\alpha$  ~ Amount of light that passes through the foreground

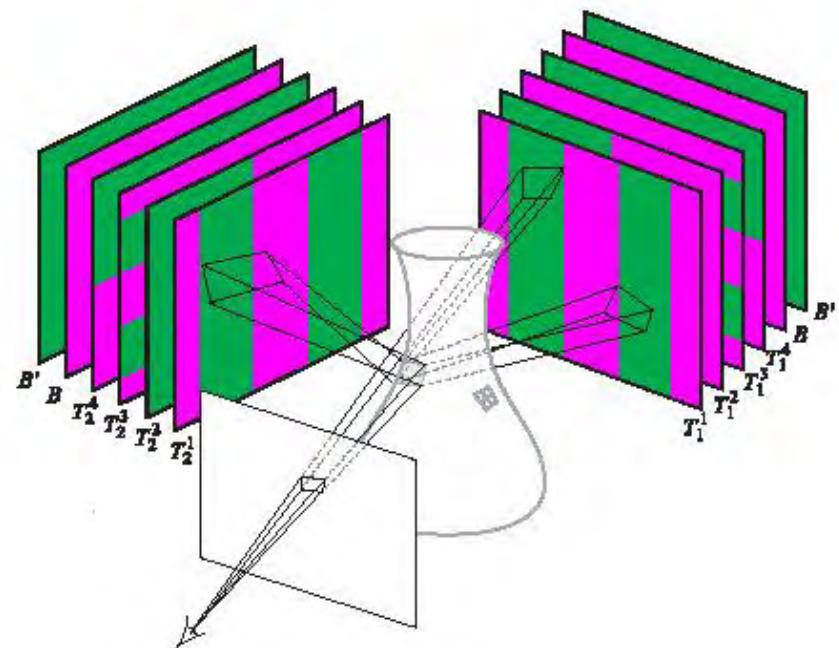
$\Phi$  ~ Contribution of light from Environment that travels through the object

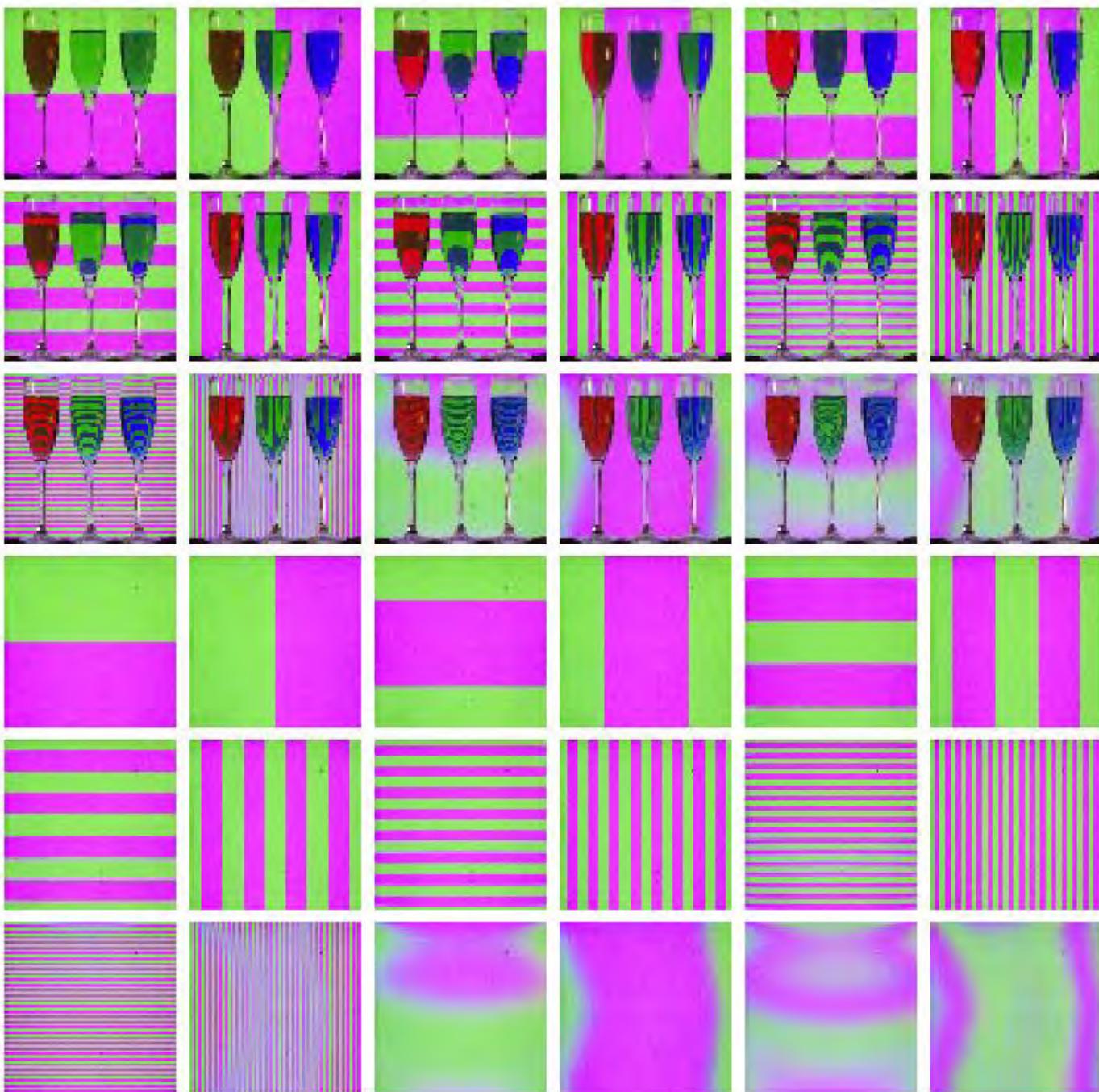
# Explanation of $\Phi$

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$$\Phi = \sum_{i=1}^m \int R_i(x) T_i(x) dx$$

R – reflectance image  
T – Texture image





Environment Mattes

# Performance

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Calibration

Matting: 10-20 minutes extraction time for each texture map (Pentium II 400Mhz)

Compositing: 4-40 frames per second

Real-Time?

# How much better is Environment Matting?



**Alpha Matte**

**Environment Matte**

**Photograph**

# How much better is Environment Matting?



**Alpha Matte**

**Environment Matte**

**Photograph**

# Movies!

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# Fast Separation of Direct and Global Images Using High Frequency Illumination

Shree K. Nayar

Gurunandan G. Krishnan

Columbia University

Michael D. Grossberg

City College of New York

Ramesh Raskar

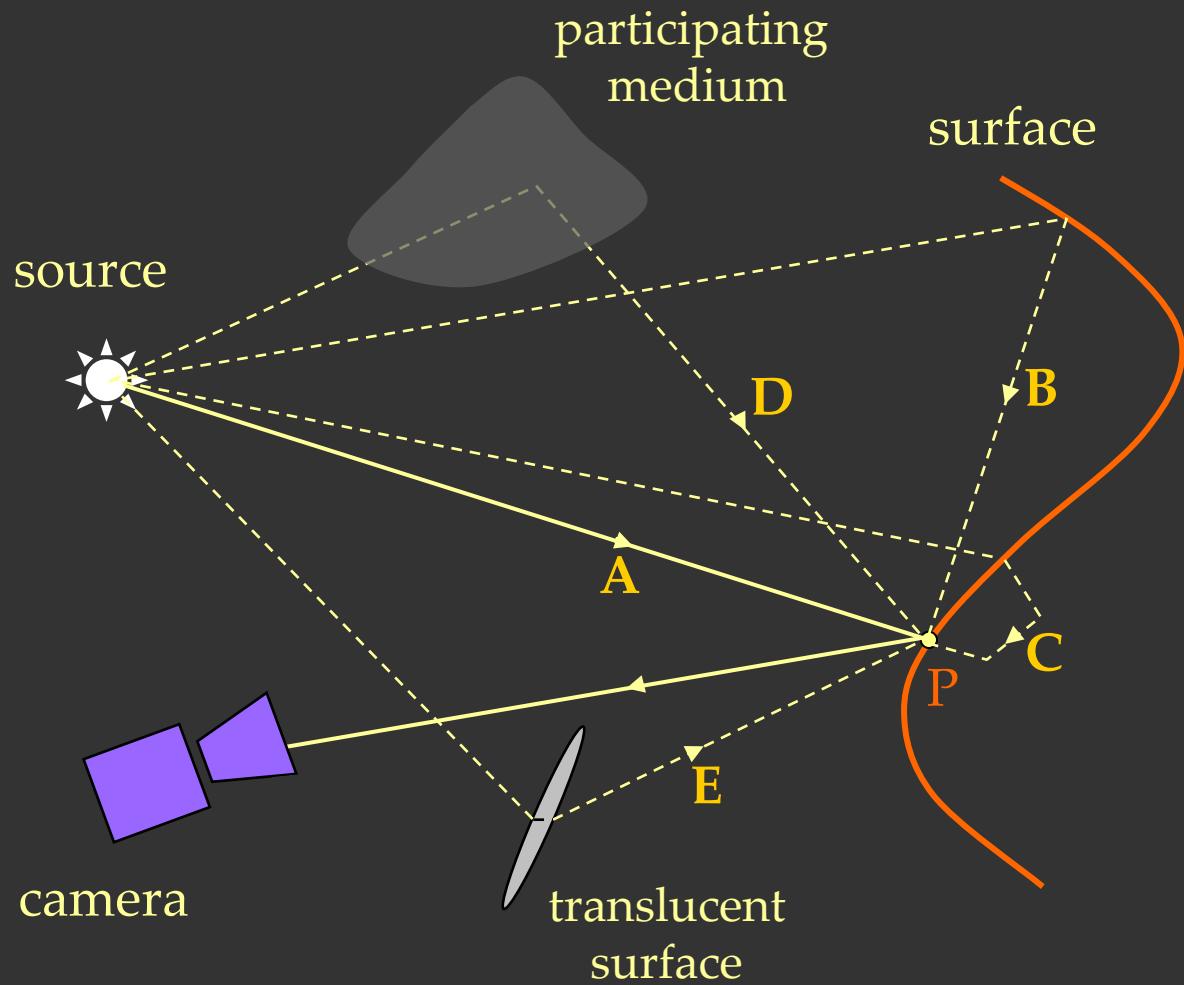
MERL

SIGGRAPH Conference

Boston, July 2006

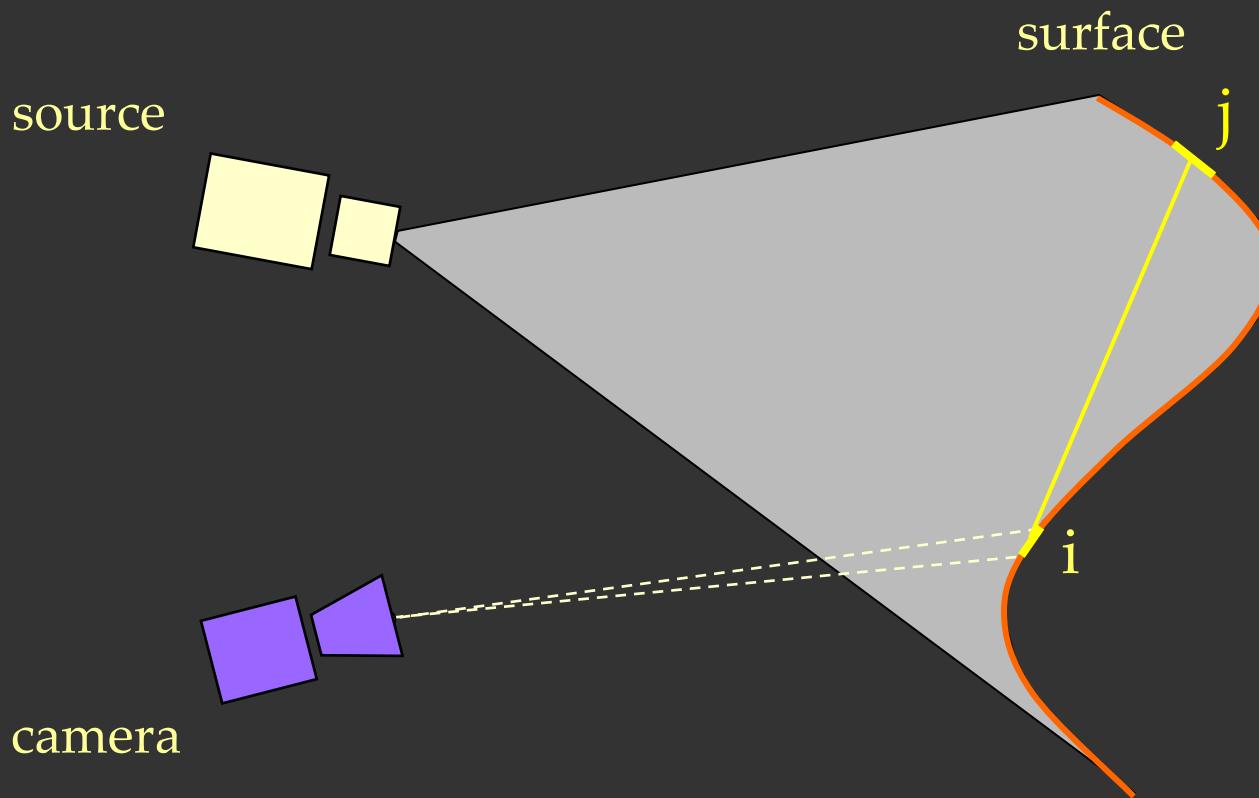
Support: ONR, NSF, MERL

# Direct and Global Illumination



- A : Direct
- B : Interreflection
- C : Subsurface
- D : Volumetric
- E : Diffusion

# Direct and Global Components: Interreflections



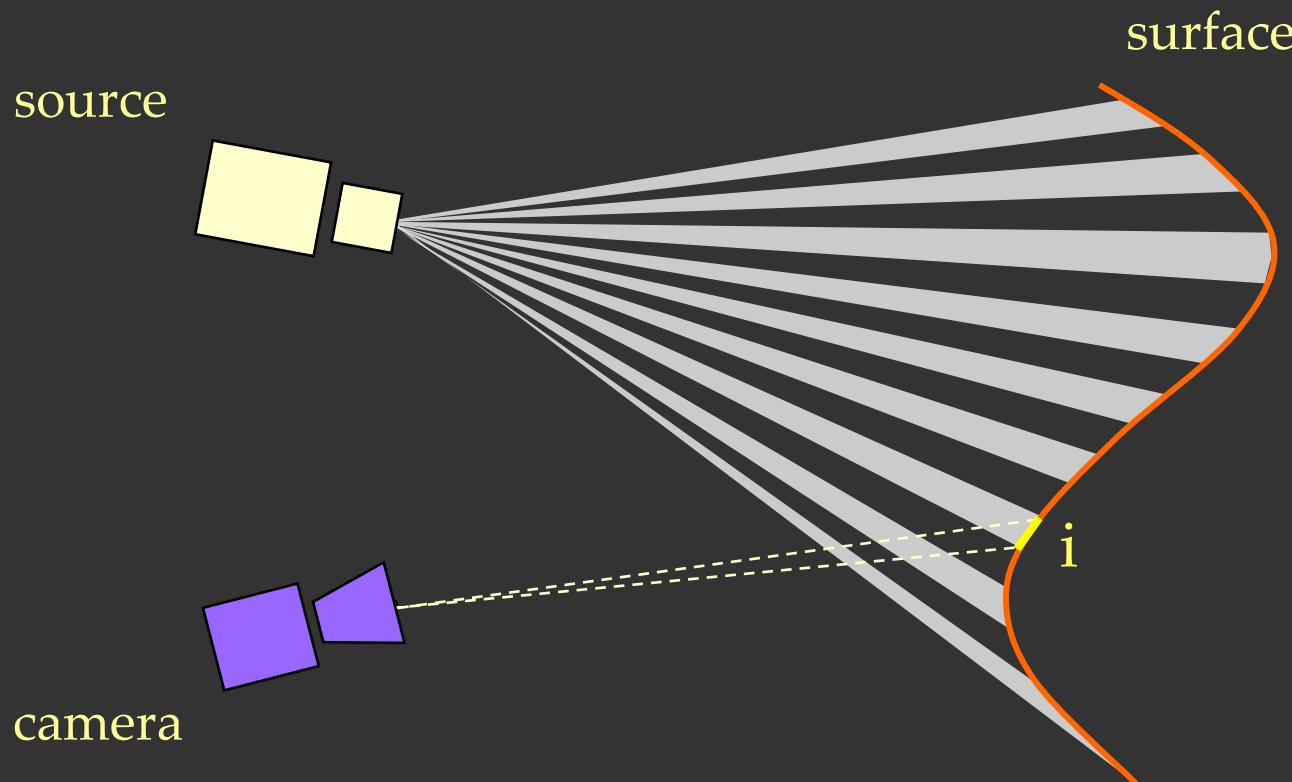
$$L[c, i] = L_d[c, i] + L_g[c, i]$$

radiance      direct      global

$$L_g[c, i] = \sum_P A[i, j] L[i, j]$$

BRDF and geometry

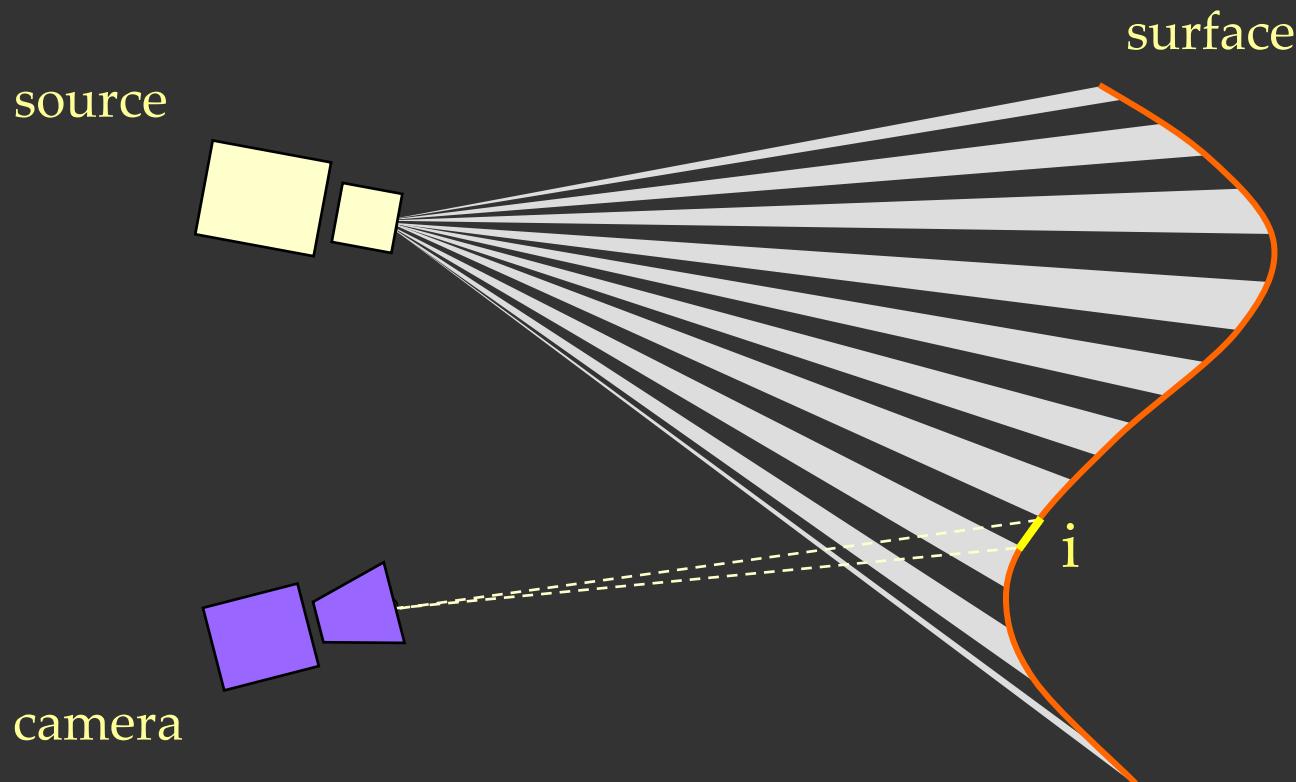
# High Frequency Illumination Pattern



$$L^+ [c, i] = L_d [c, i] + \alpha L_g [c, i]$$

fraction of activated source elements

# High Frequency Illumination Pattern



$$L^+[c,i] = L_d[c,i] + \alpha L_g[c,i]$$

$$L^-[c,i] = (1 - \alpha) L_g[c,i]$$

fraction of activated source elements

# Separation from Two Images

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$$\alpha = \frac{1}{2} :$$

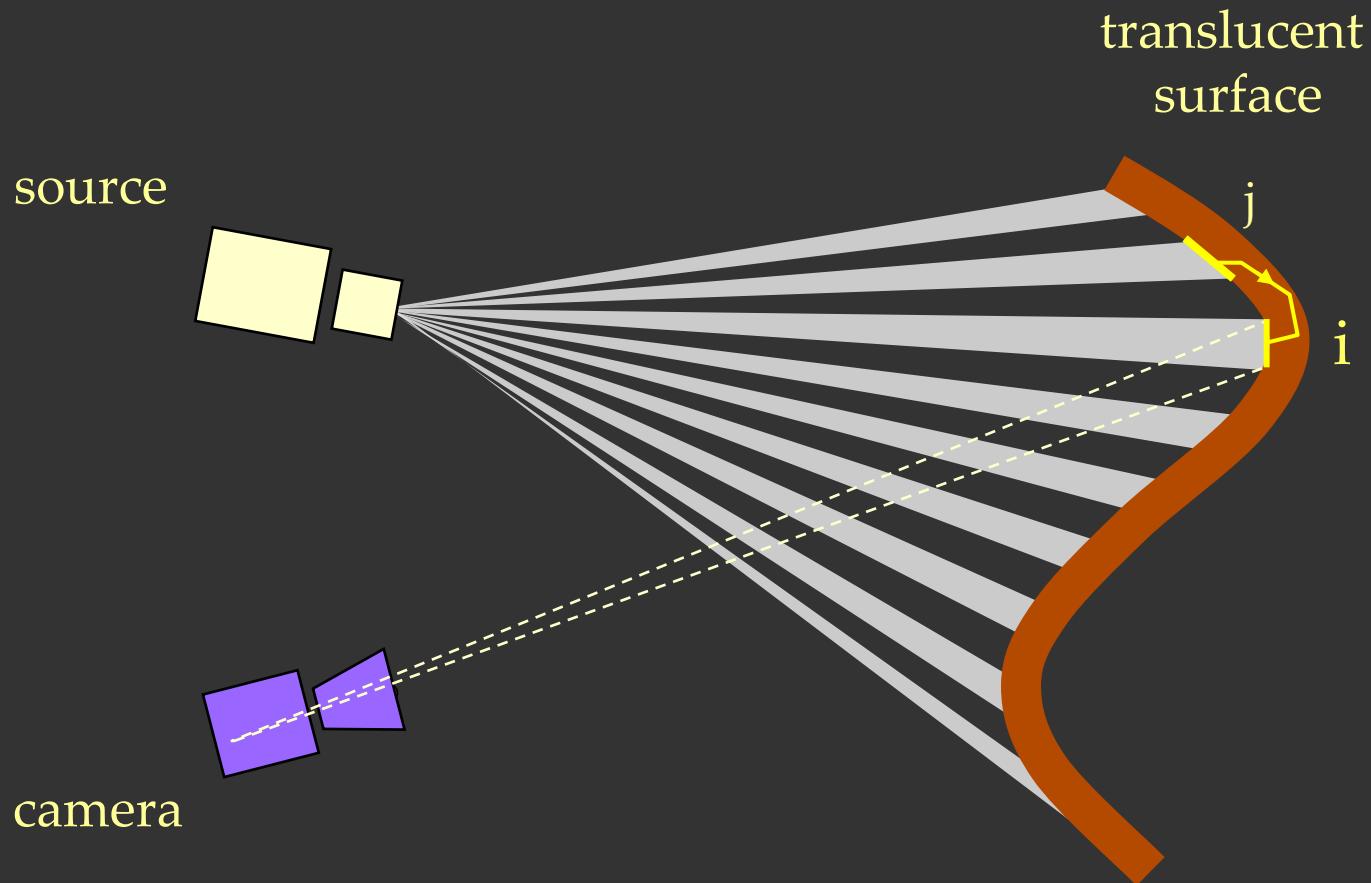
$$L_d = L_{\max} - L_{\min} , \quad L_g = 2L_{\min}$$

direct

global

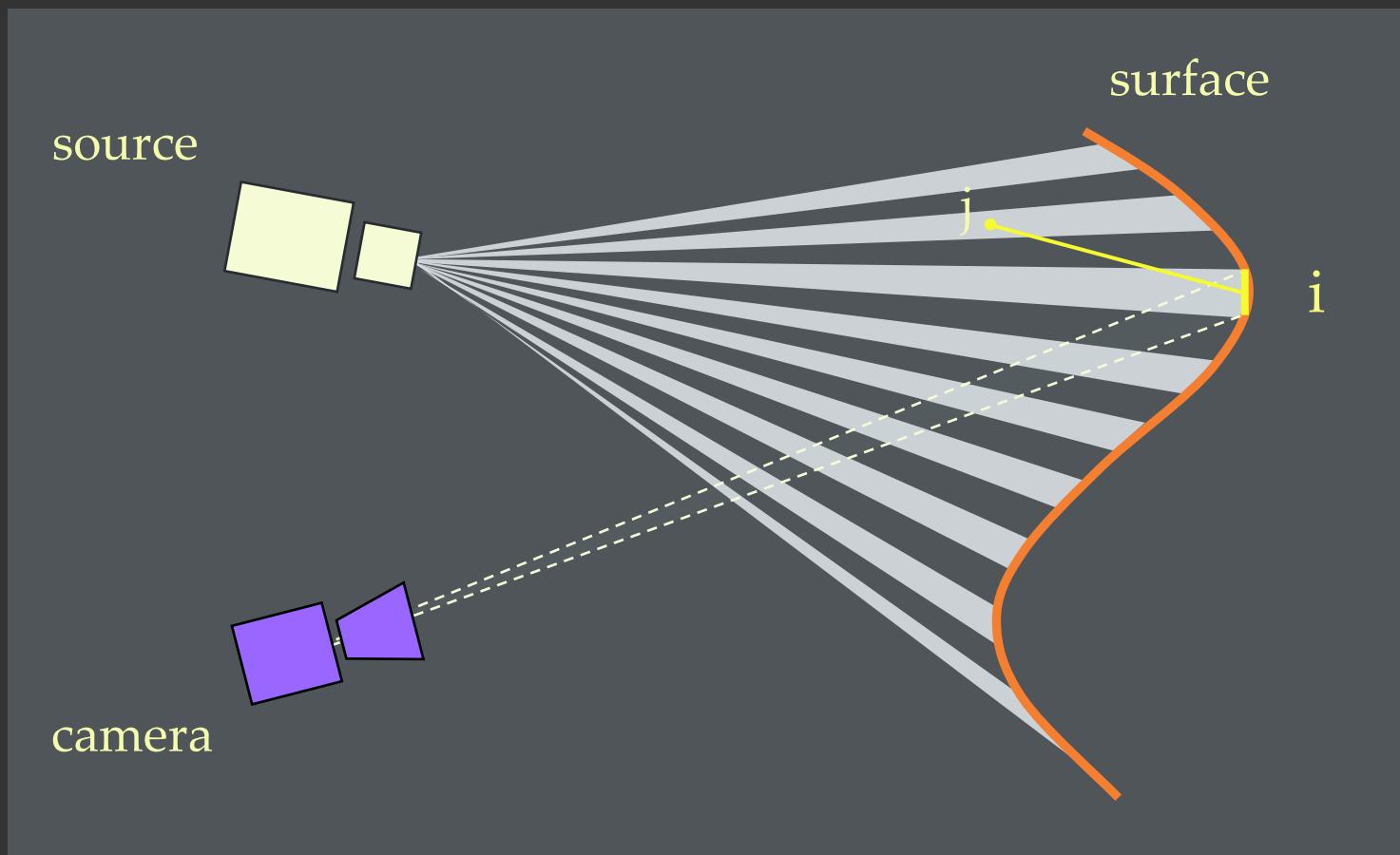
# Other Global Effects: Subsurface Scattering

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# Other Global Effects: Volumetric Scattering

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Diffuse  
Interreflections

Specular  
Interreflections

Diffusion

Volumetric  
Scattering

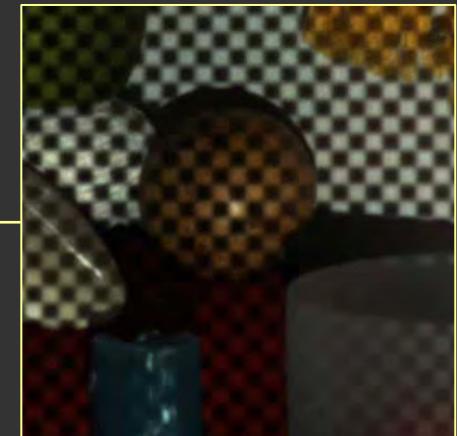
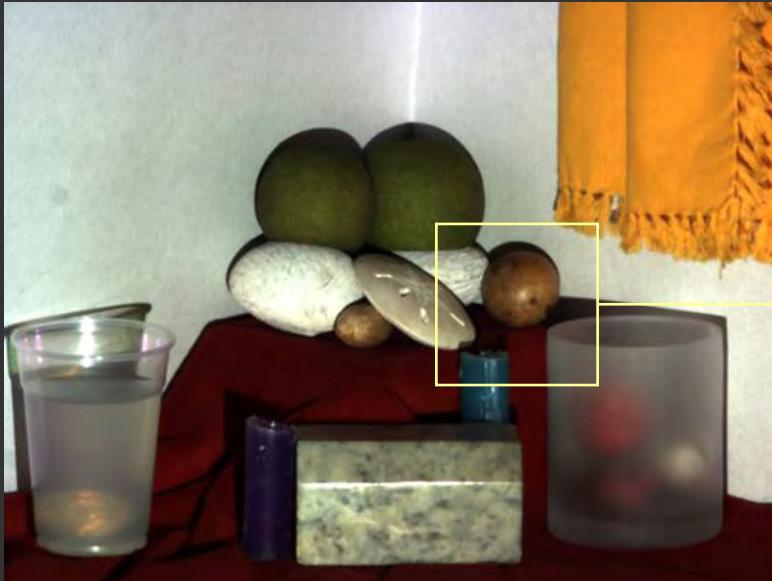
Subsurface  
Scattering



# Scene



Scene



Direct



Global

Real World Examples:  
Can You Guess the Images?

# Eggs: Diffuse Interreflections



Direct



Global

# Wooden Blocks: Specular Interreflections



Direct



Global

# Kitchen Sink: Volumetric Scattering



Volumetric Scattering:  
Chandrasekar 50, Ishimaru 78



Direct



Global

# Peppers: Subsurface Scattering



Direct



Global

# Hand



**Skin:** Hanrahan and Krueger 93,  
Uchida 96, Haro 01, Jensen et al. 01,  
Cula and Dana 02, Igarashi et al.  
05, Weyrich et al. 05



Direct



Global

# Face: Without and With Makeup

Without Makeup



Direct



Global



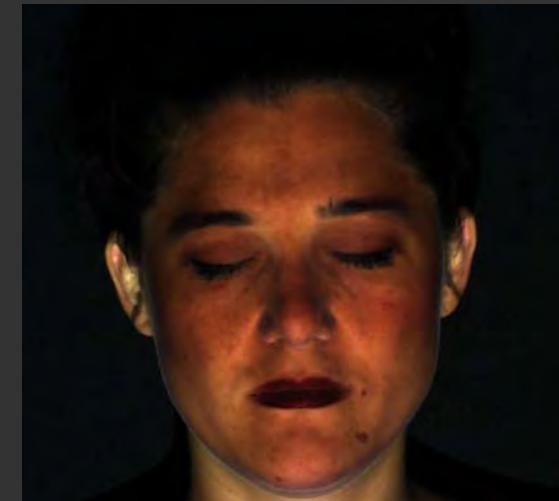
With Makeup



Direct



Global



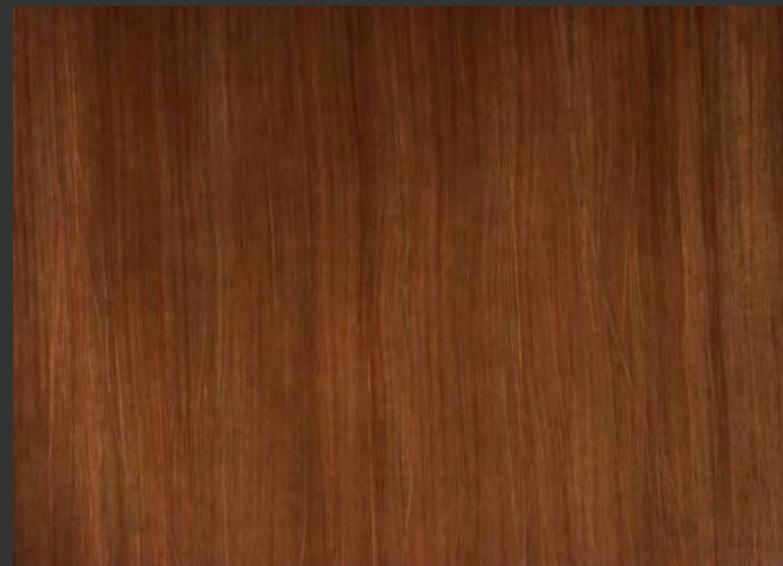
# Blonde Hair



**Hair Scattering:** Stamm et al. 77,  
Bustard and Smith 91, Lu et al. 00  
Marschner et al. 03



Direct



Global

