

Feature Matching and RANSAC

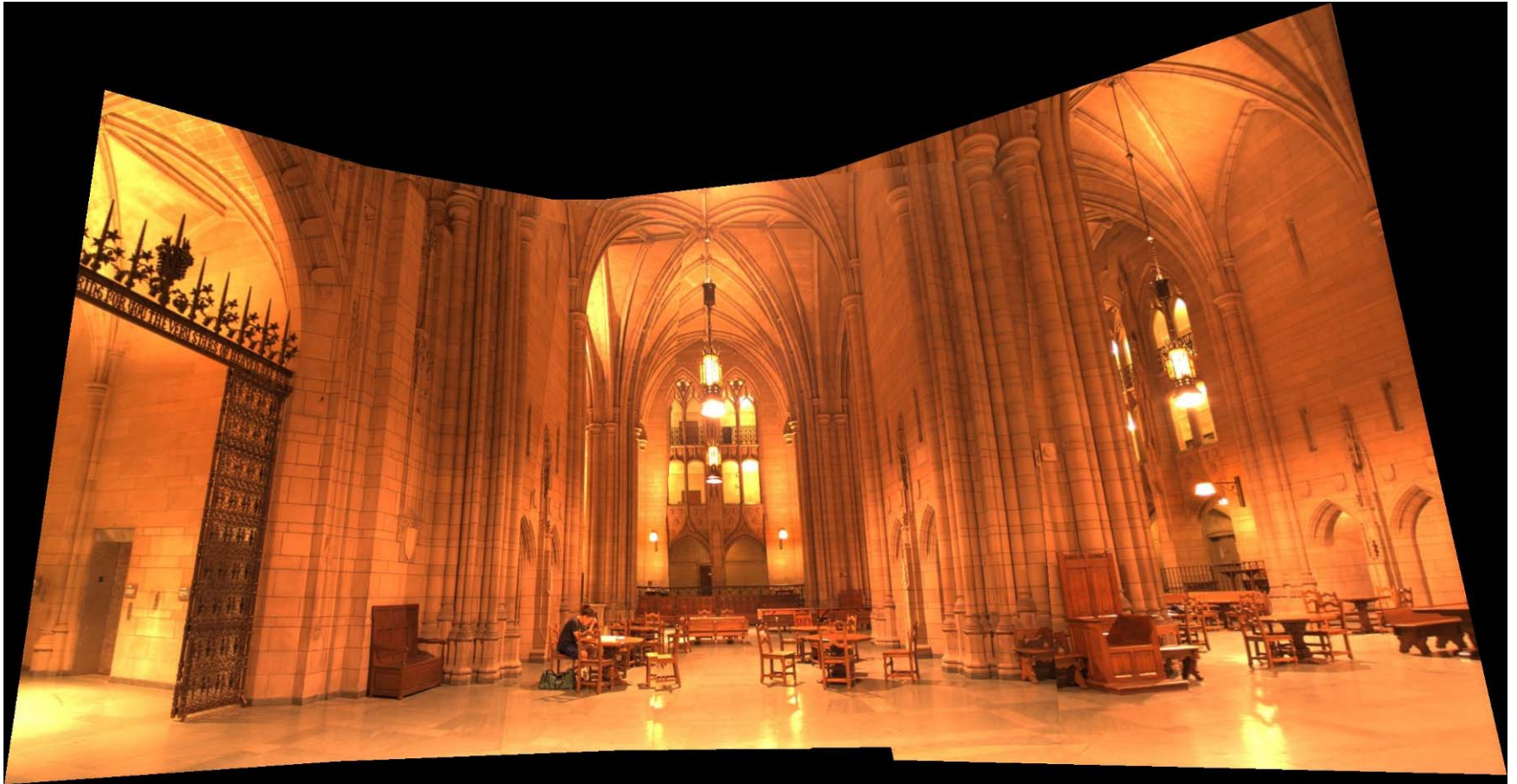


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*with a lot of slides stolen from
Steve Seitz and Rick Szeliski*

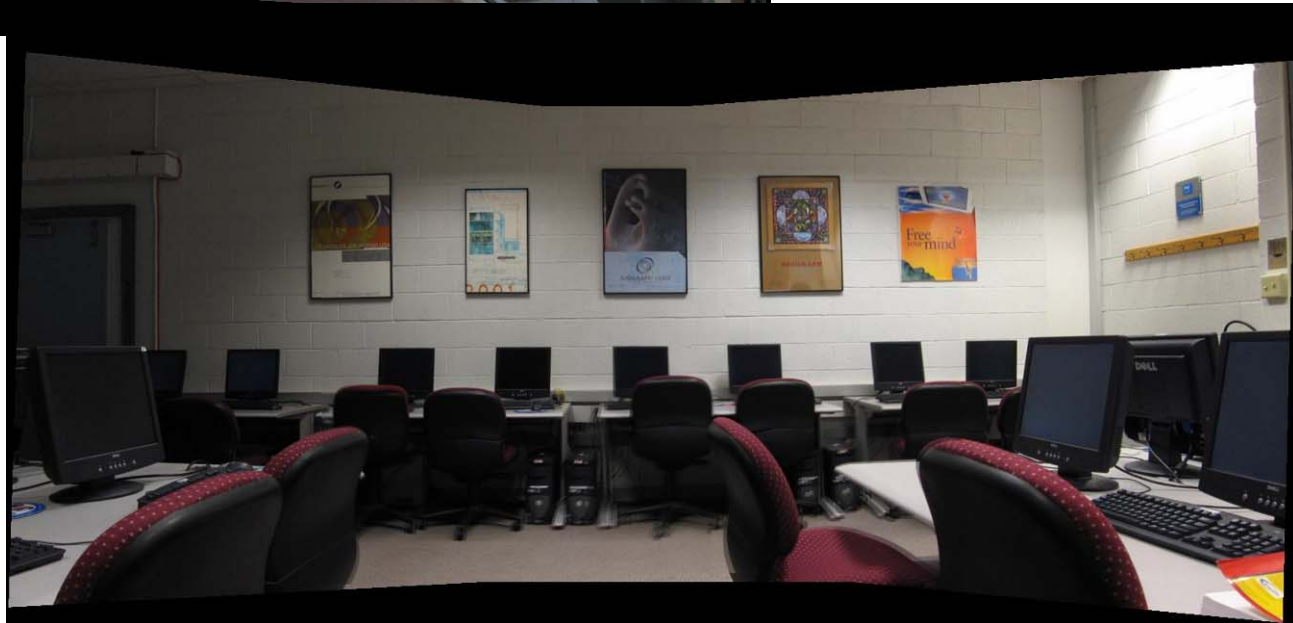
15-463: Computational Photography
Alexei Efros, CMU, Fall 2005

Project #3 Showcase



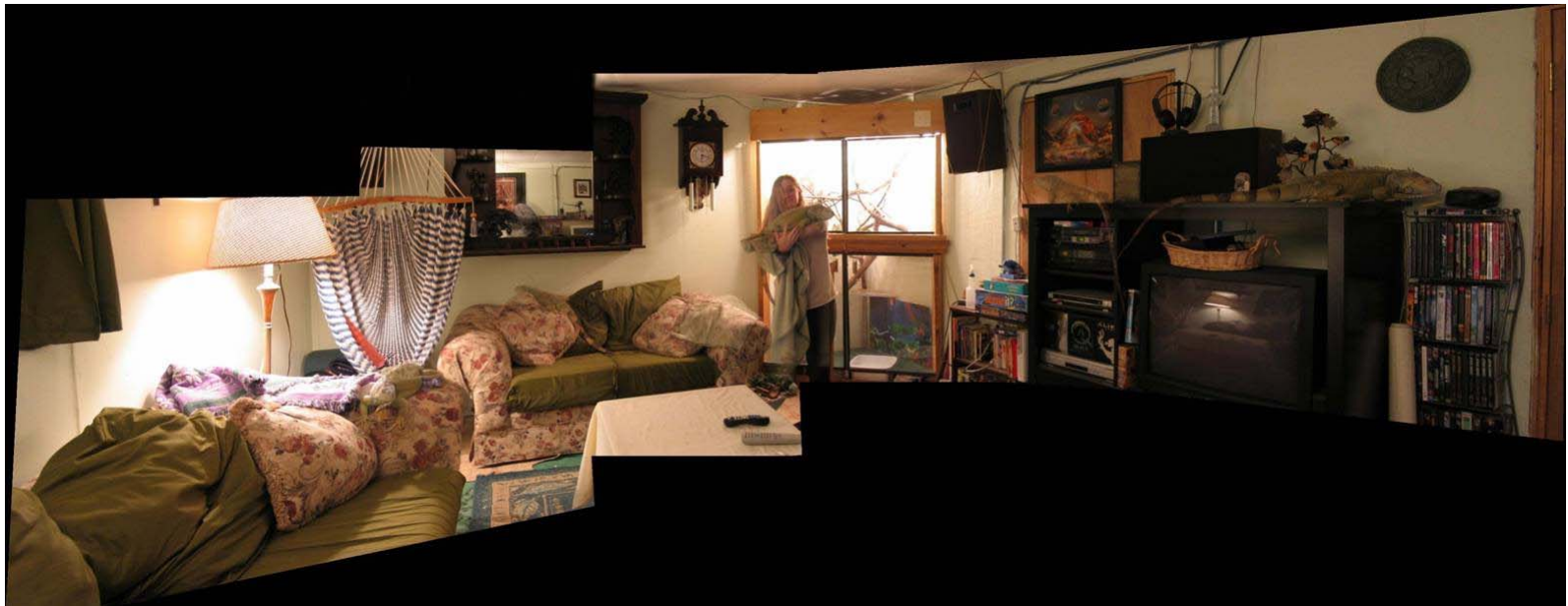
mrom

Project #3 Showcase

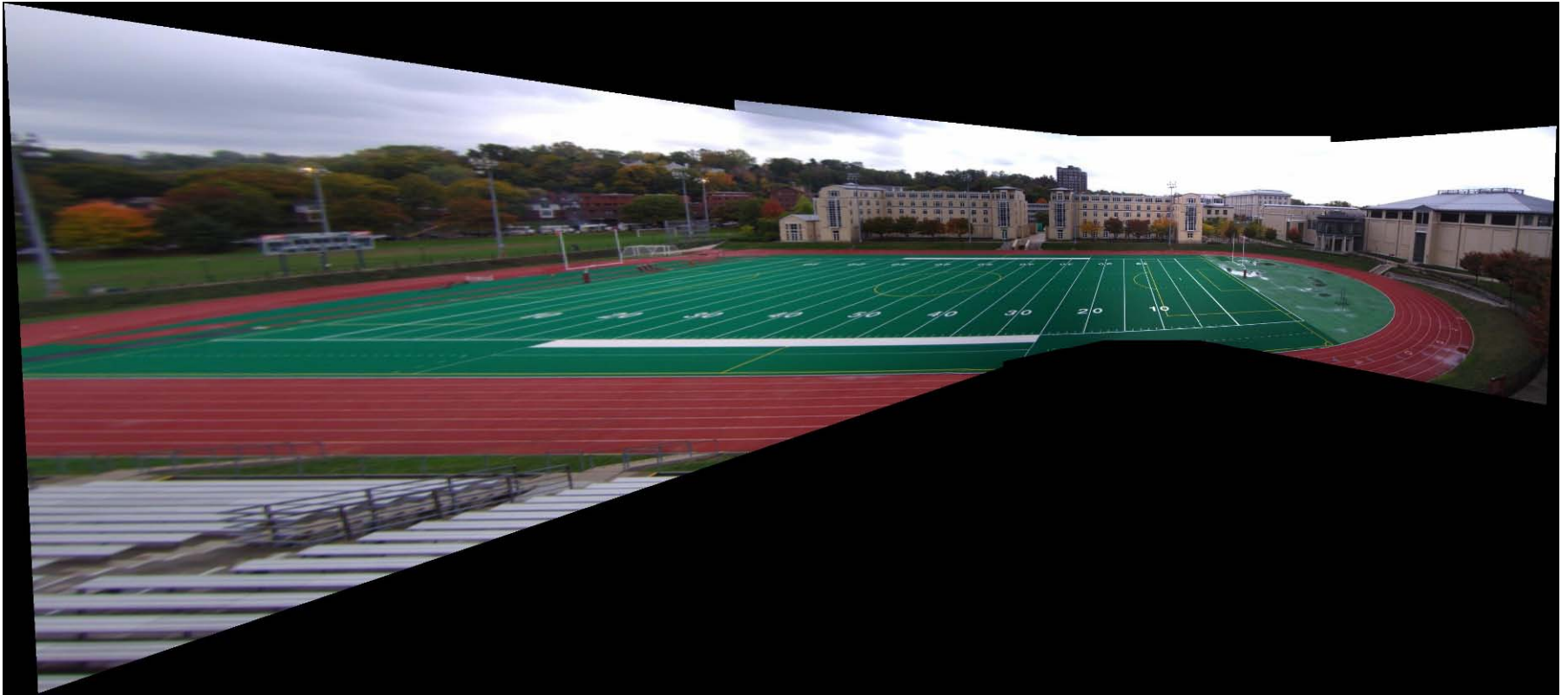


heegunl

Project #3 Showcase



Project #3 Showcase



lms

Project #3 Showcase



cmcamero

Project #3 Showcase



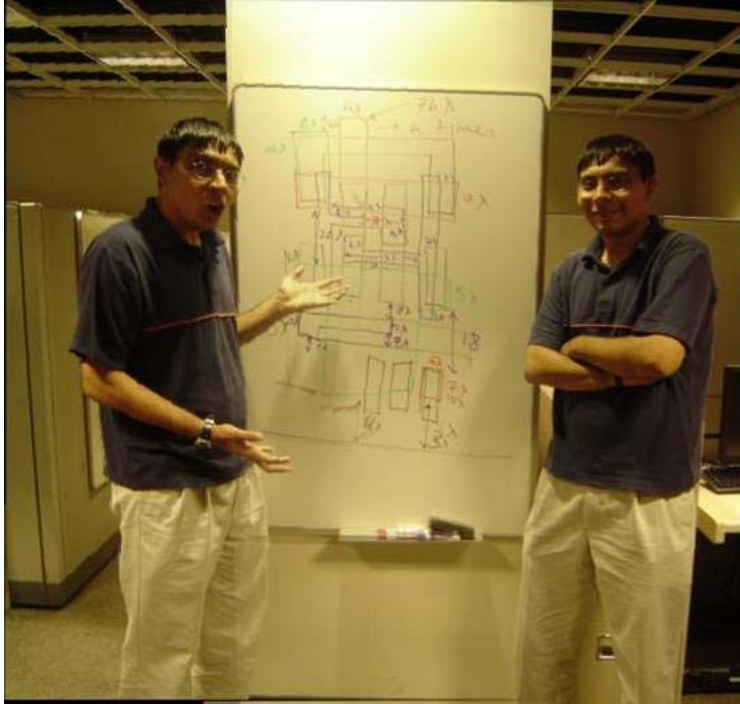
slim

Project #3 Showcase



cmcamero

Project #3 Showcase



slim

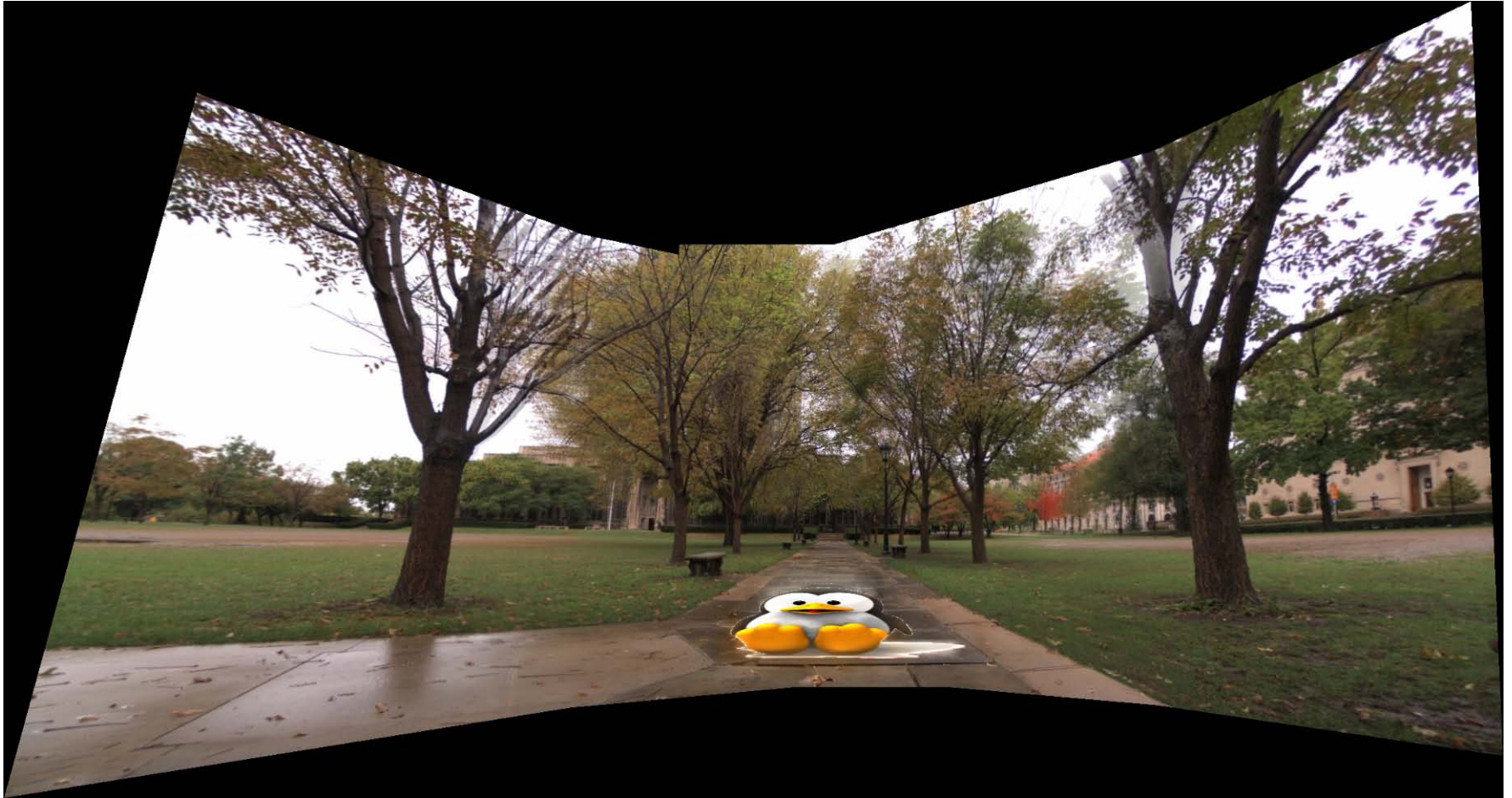


nvyas

Project #3 Showcase

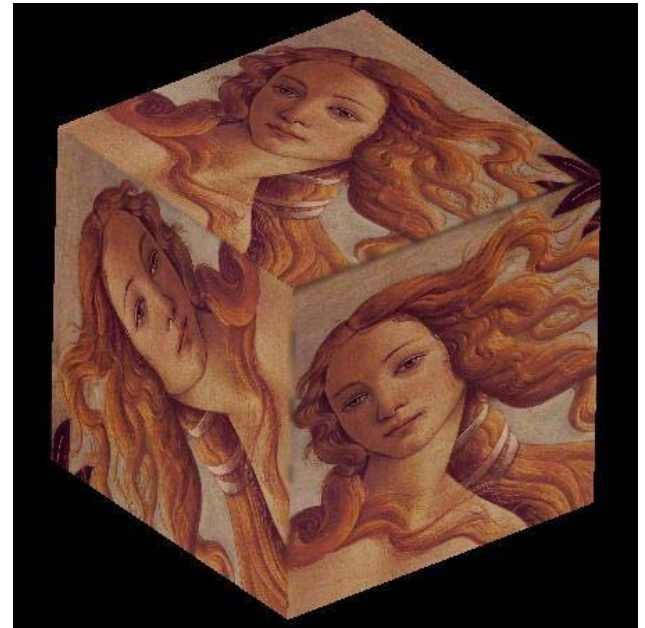
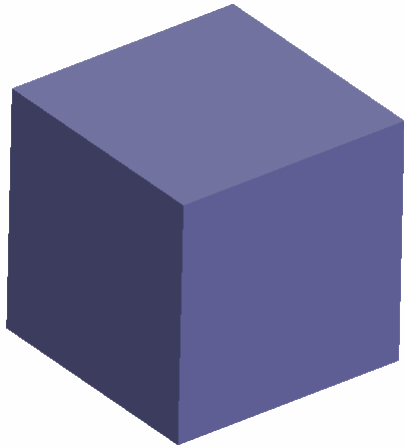


Project #3 Showcase



mrom

Project #3 Showcase



Project #3 Showcase



cmcamero

bhon



Project #3 Showcase



chenyuwu

Project #3 Showcase



Multi-Scale Oriented Patches

Interest points

- Multi-scale Harris corners
- Orientation from blurred gradient
- Geometrically invariant to rotation

Descriptor vector

- Bias/gain normalized sampling of local patch (8x8)
- Photometrically invariant to affine changes in intensity

[Brown, Szeliski, Winder, CVPR'2005]

Descriptor Vector

Orientation = blurred gradient

Rotation Invariant Frame

- Scale-space position (x, y, s) + orientation (θ)



Detections at multiple scales

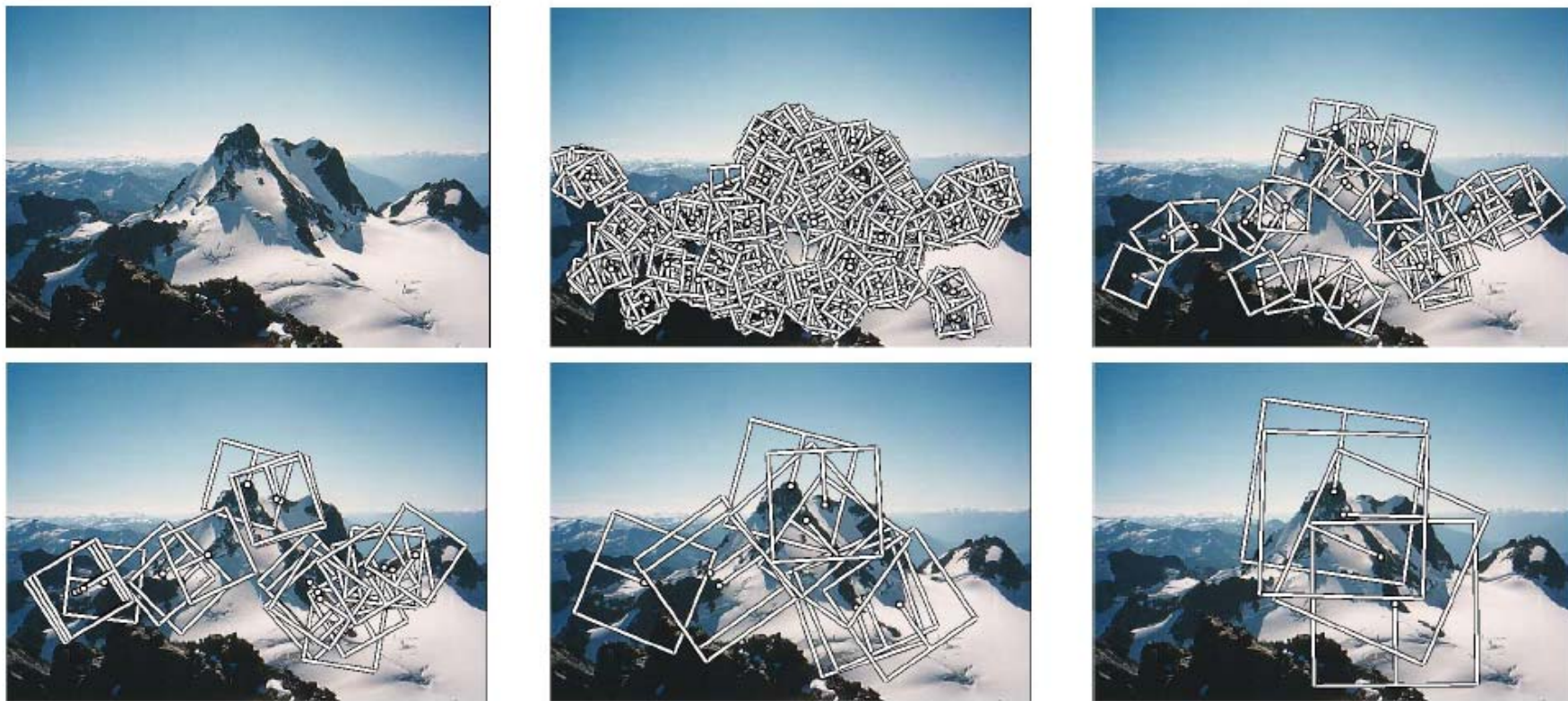


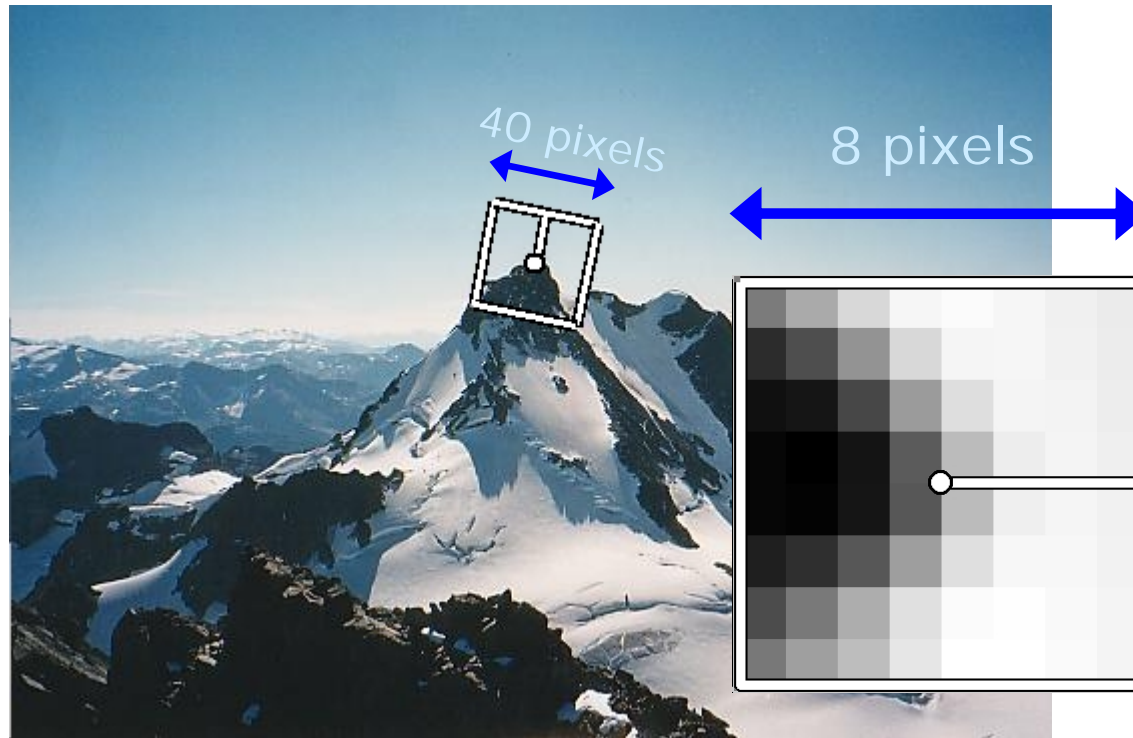
Figure 1. Multi-scale Oriented Patches (MOPS) extracted at five pyramid levels from one of the Matier images. The boxes show the feature orientation and the region from which the descriptor vector is sampled.

MOPS descriptor vector

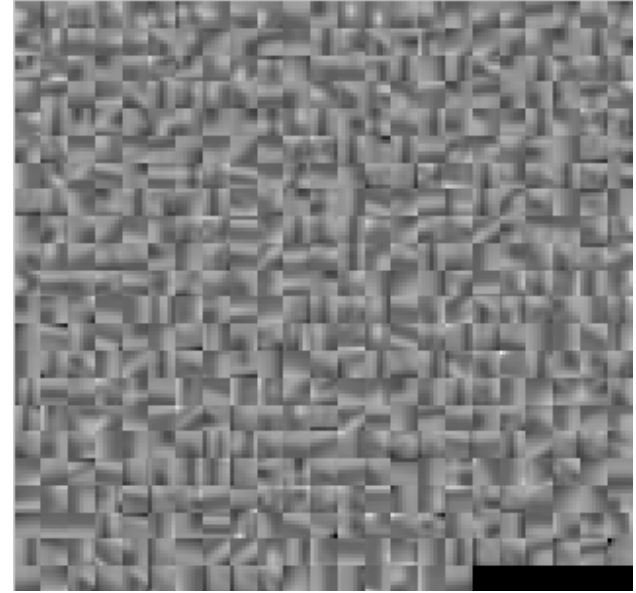
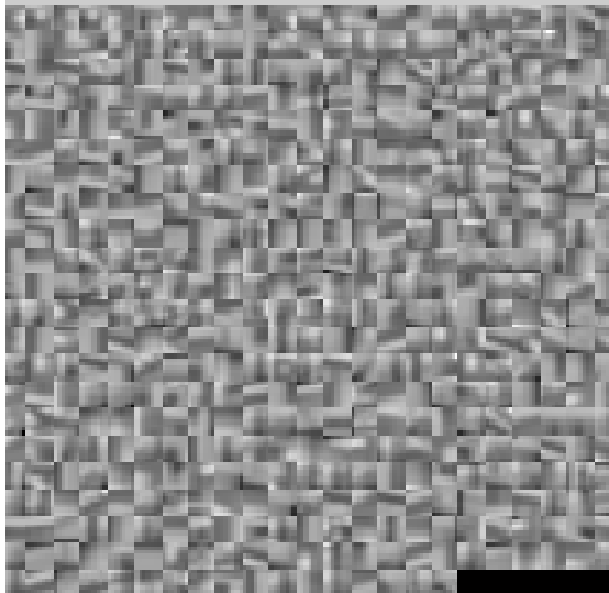
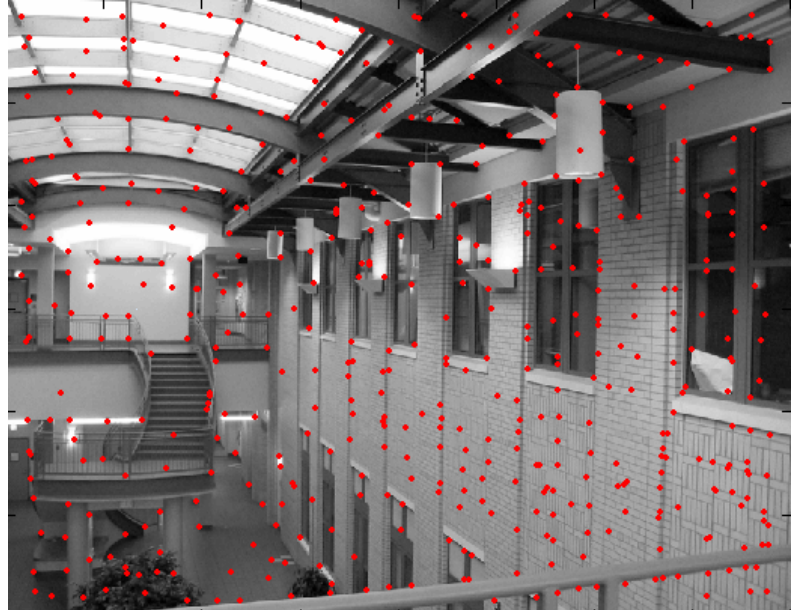
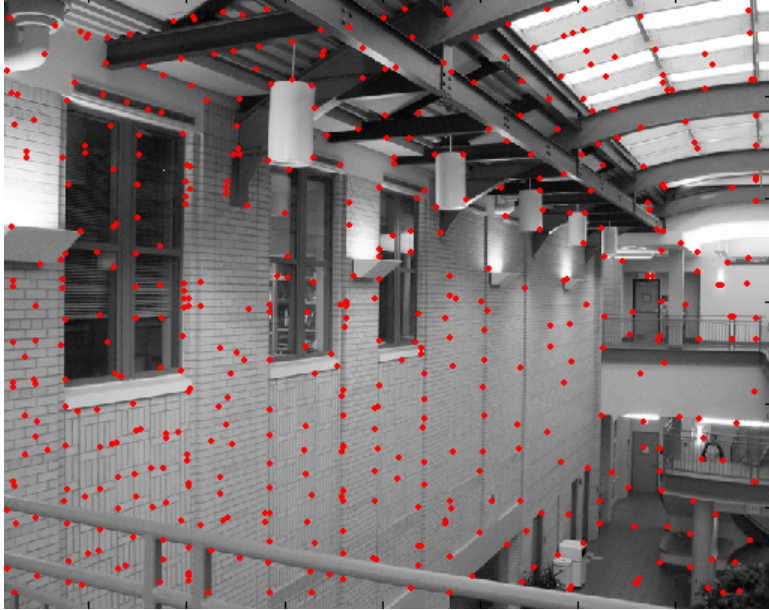
8x8 oriented patch

- Sampled at 5 x scale

Bias/gain normalisation: $I' = (I - \mu)/\sigma$



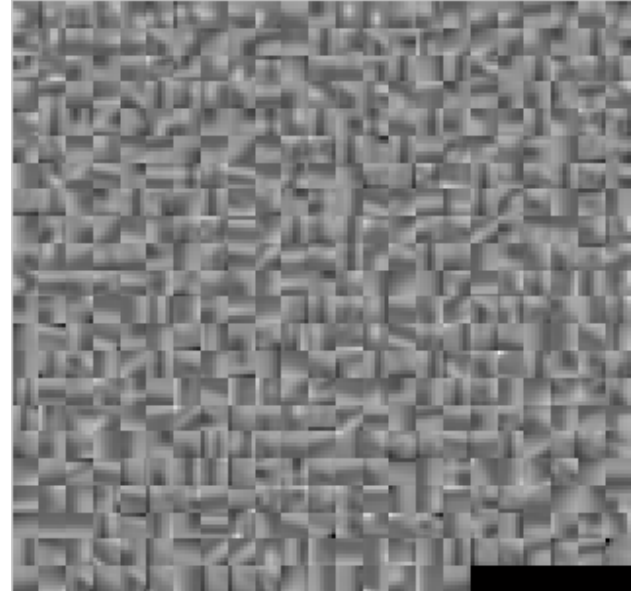
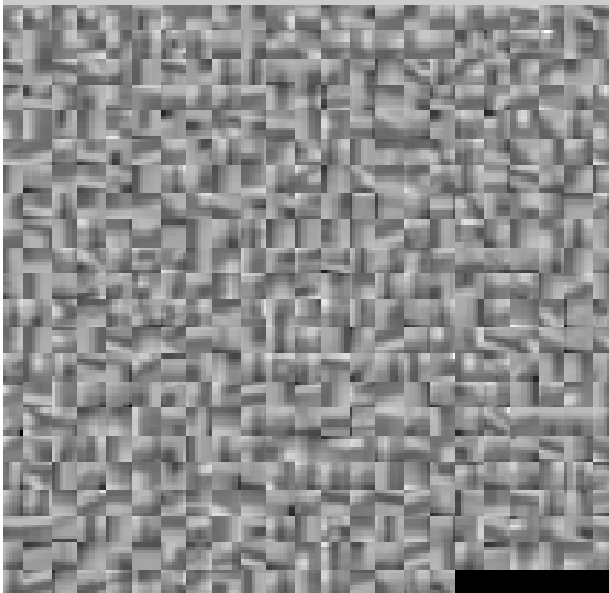
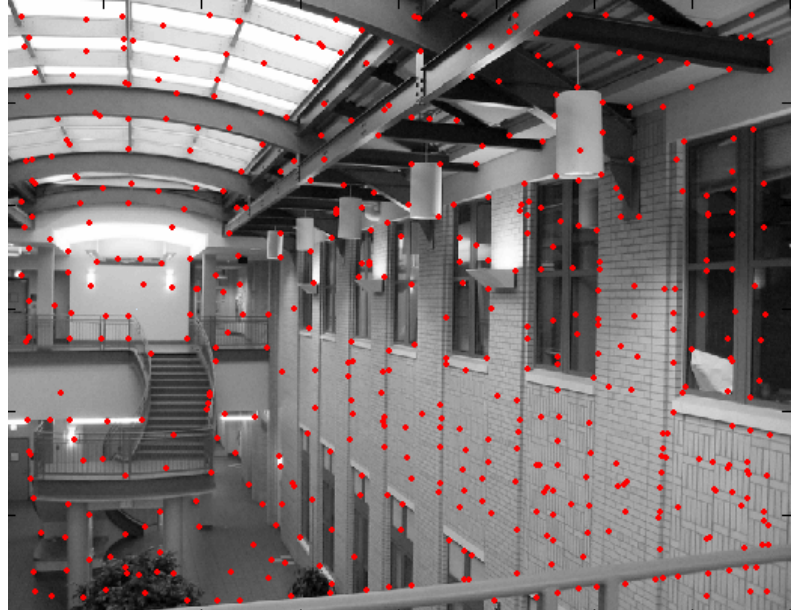
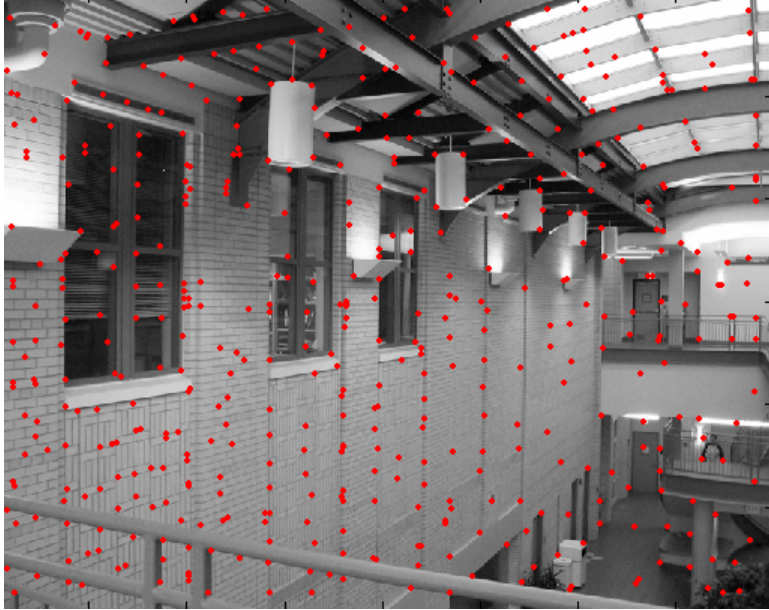
Feature matching



Feature matching

- Exhaustive search
 - for each feature in one image, look at *all* the other features in the other image(s)
- Hashing
 - compute a short descriptor from each feature vector, or hash longer descriptors (randomly)
- Nearest neighbor techniques
 - *k*-trees and their variants

What about outliers?

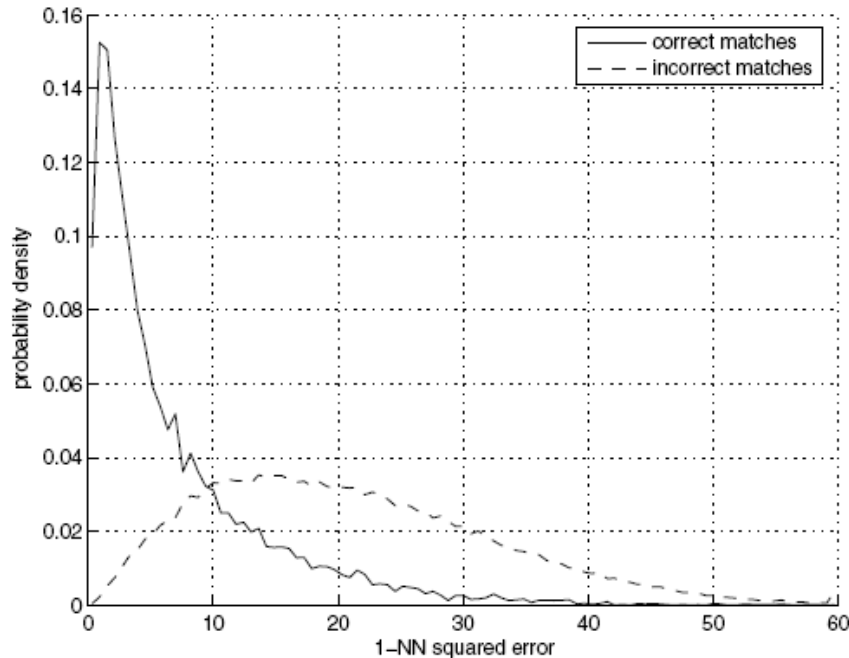


Feature-space outlier rejection

Let's not match all features, but only these that have “similar enough” matches?

How can we do it?

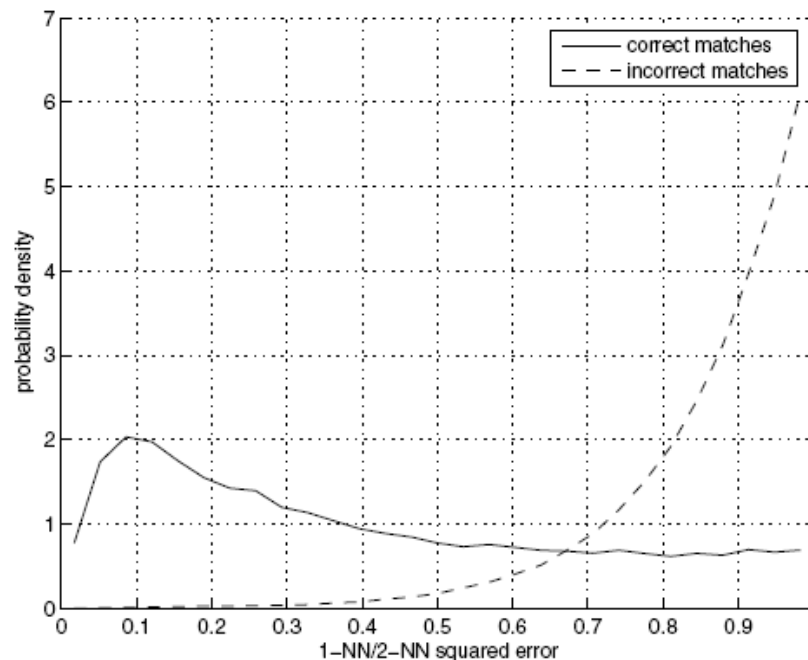
- $\text{SSD}(\text{patch1}, \text{patch2}) < \text{threshold}$
- How to set threshold?



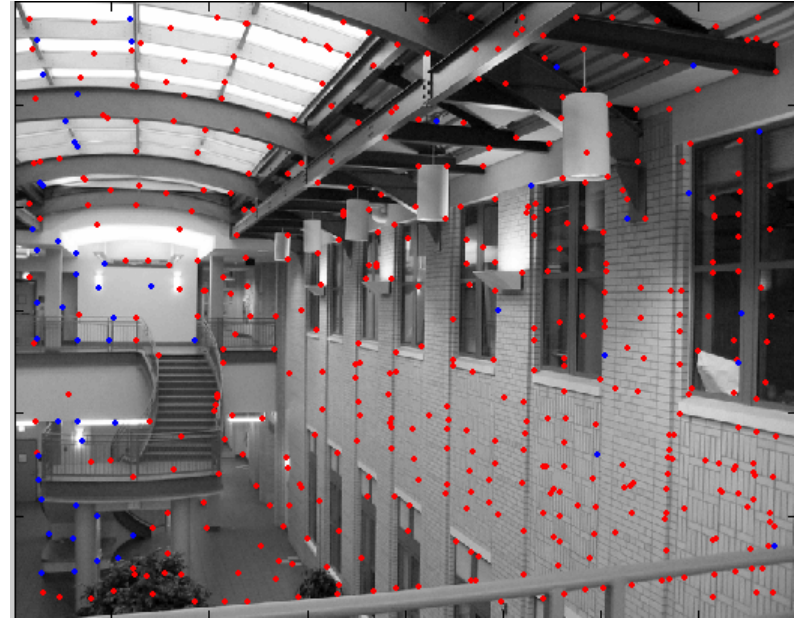
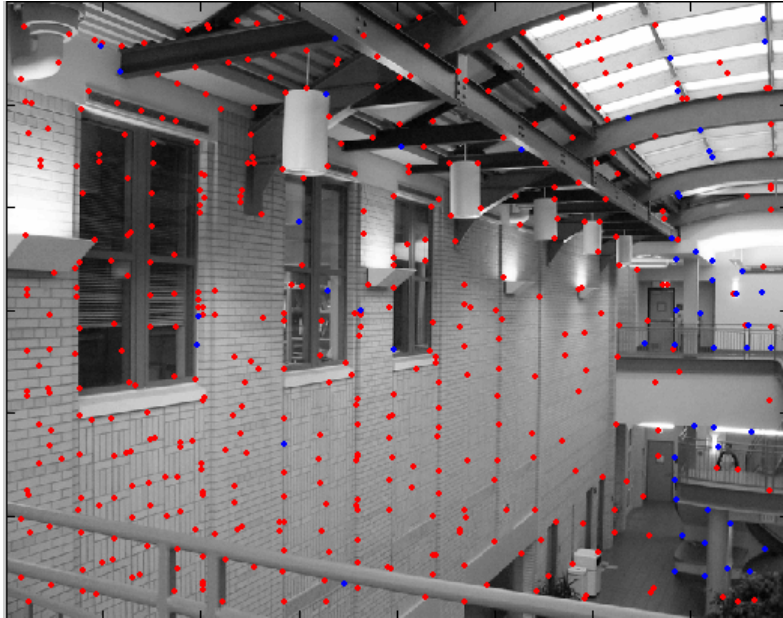
Feature-space outlier rejection

A better way [Lowe, 1999]:

- 1-NN: SSD of the closest match
- 2-NN: SSD of the second-closest match
- Look at how much better 1-NN is than 2-NN, e.g. 1-NN/2-NN
- That is, is our best match so much better than the rest?



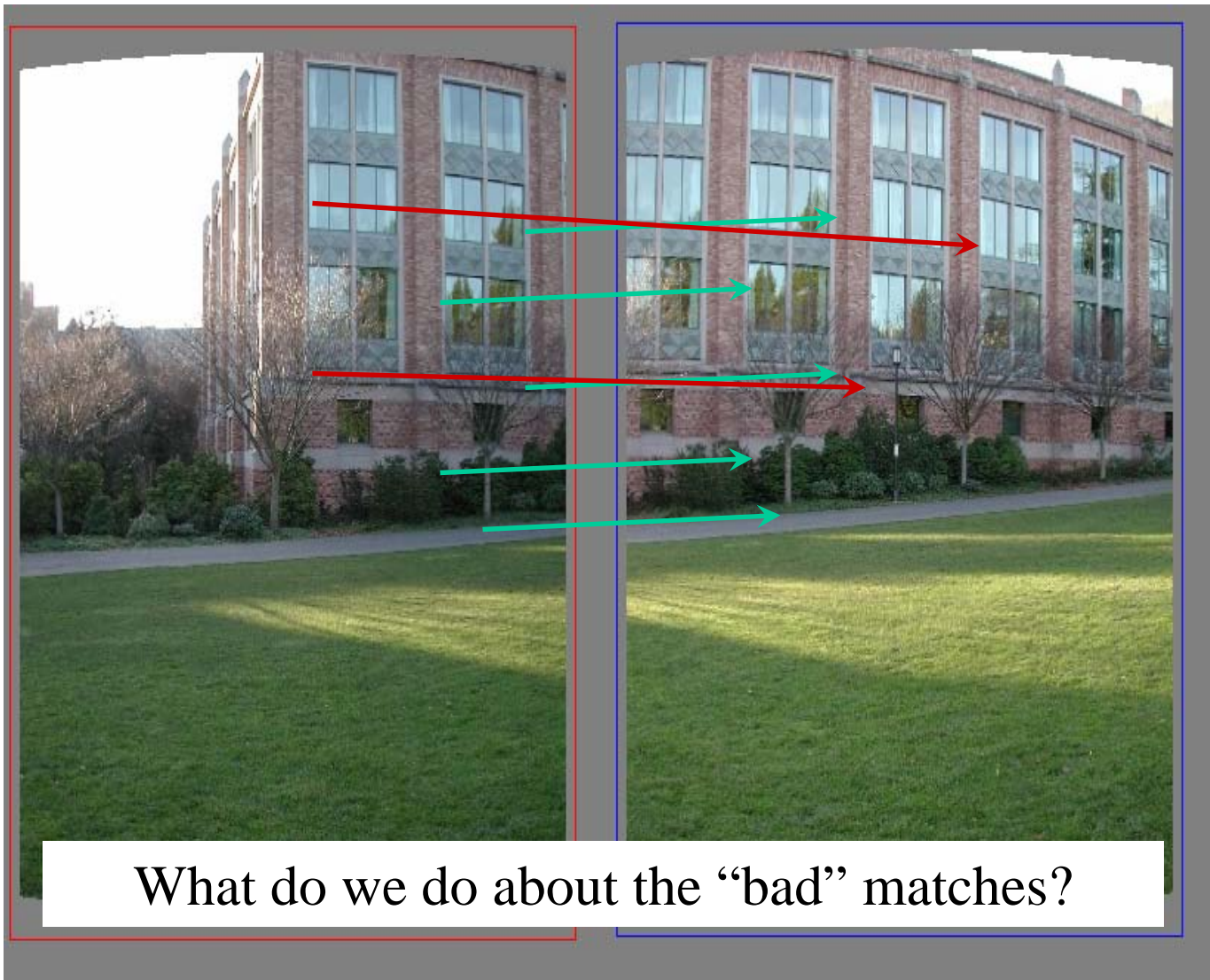
Feature-space outlier rejection



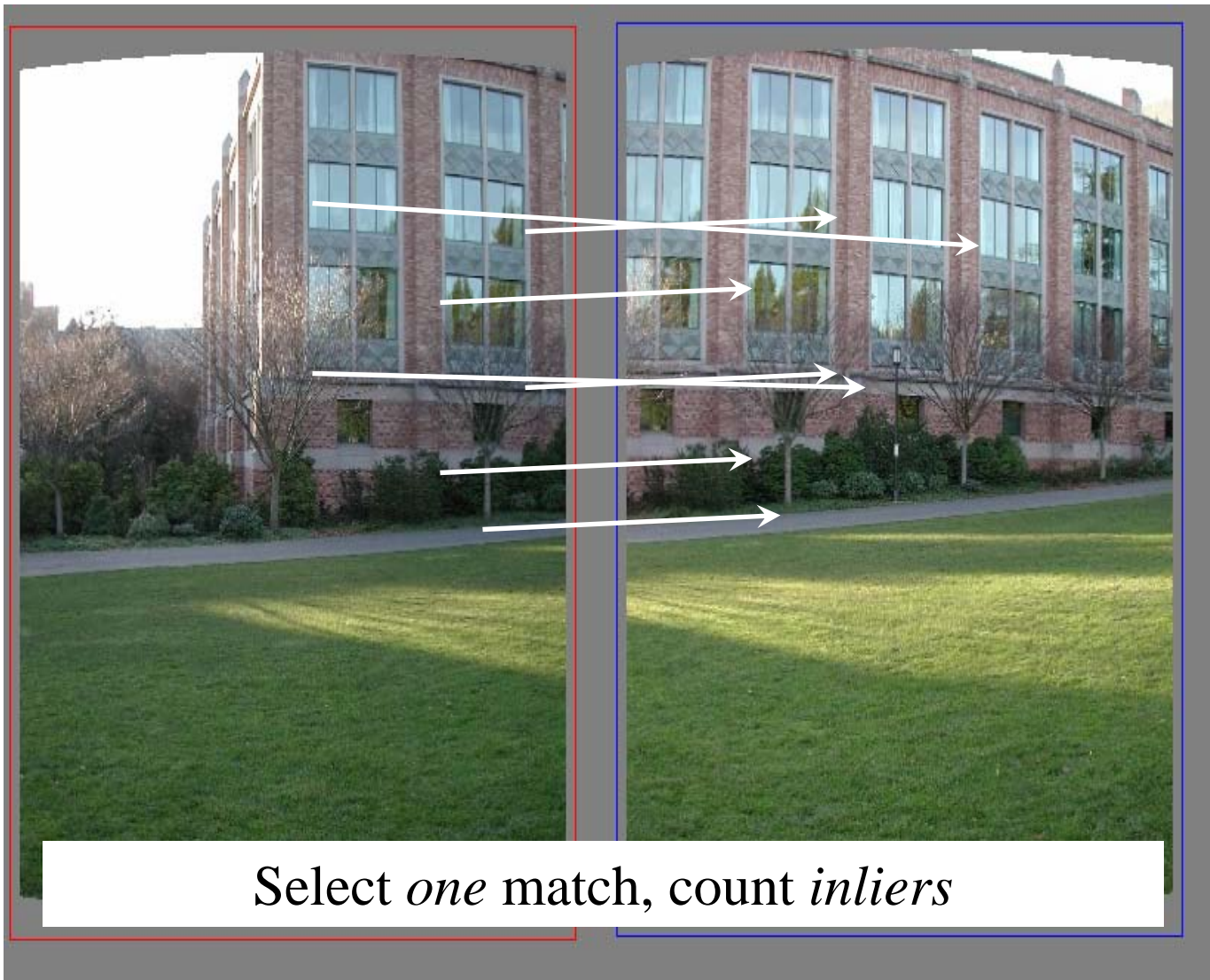
Can we now compute H from the blue points?

- No! Still too many outliers...
- What can we do?

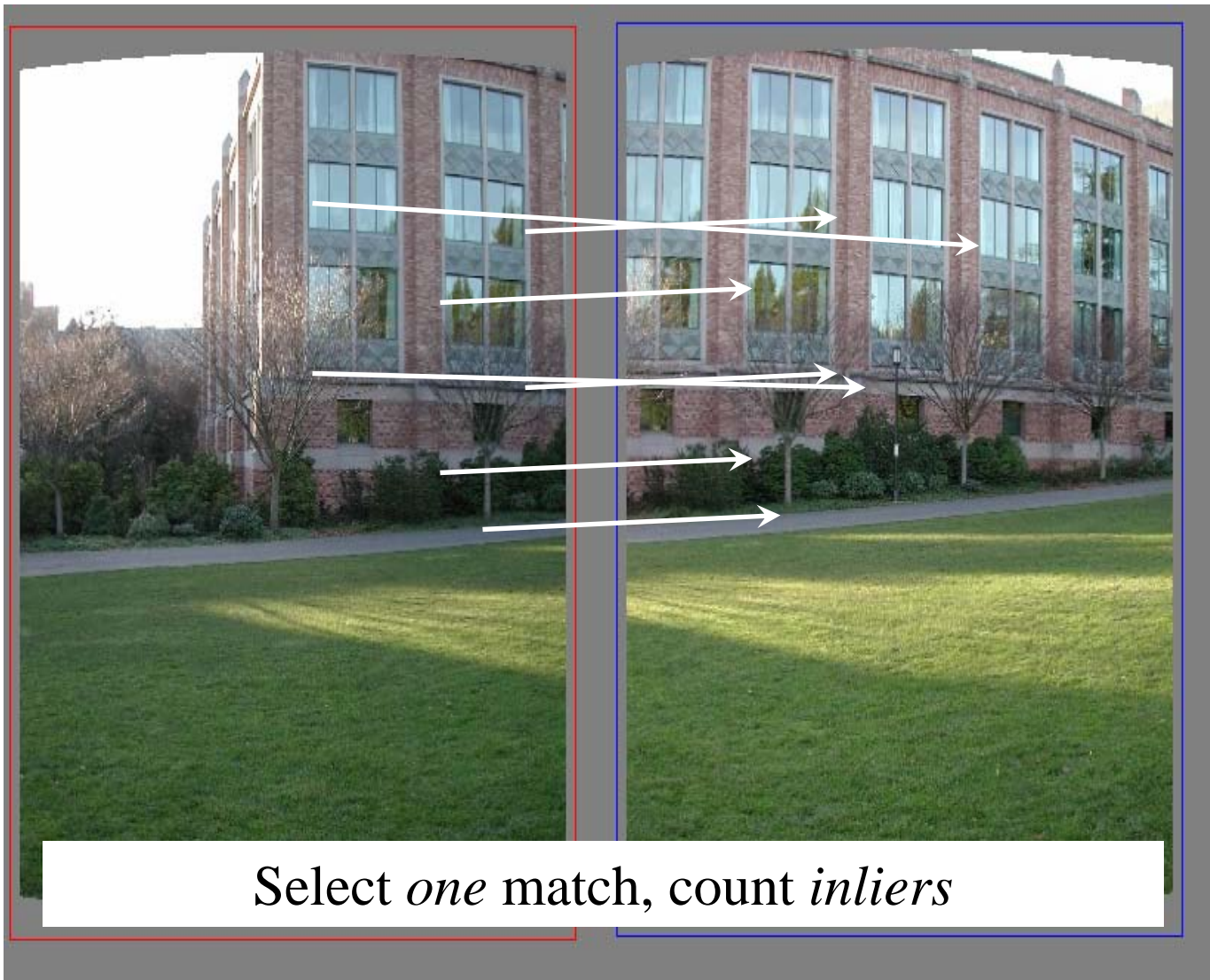
Matching features



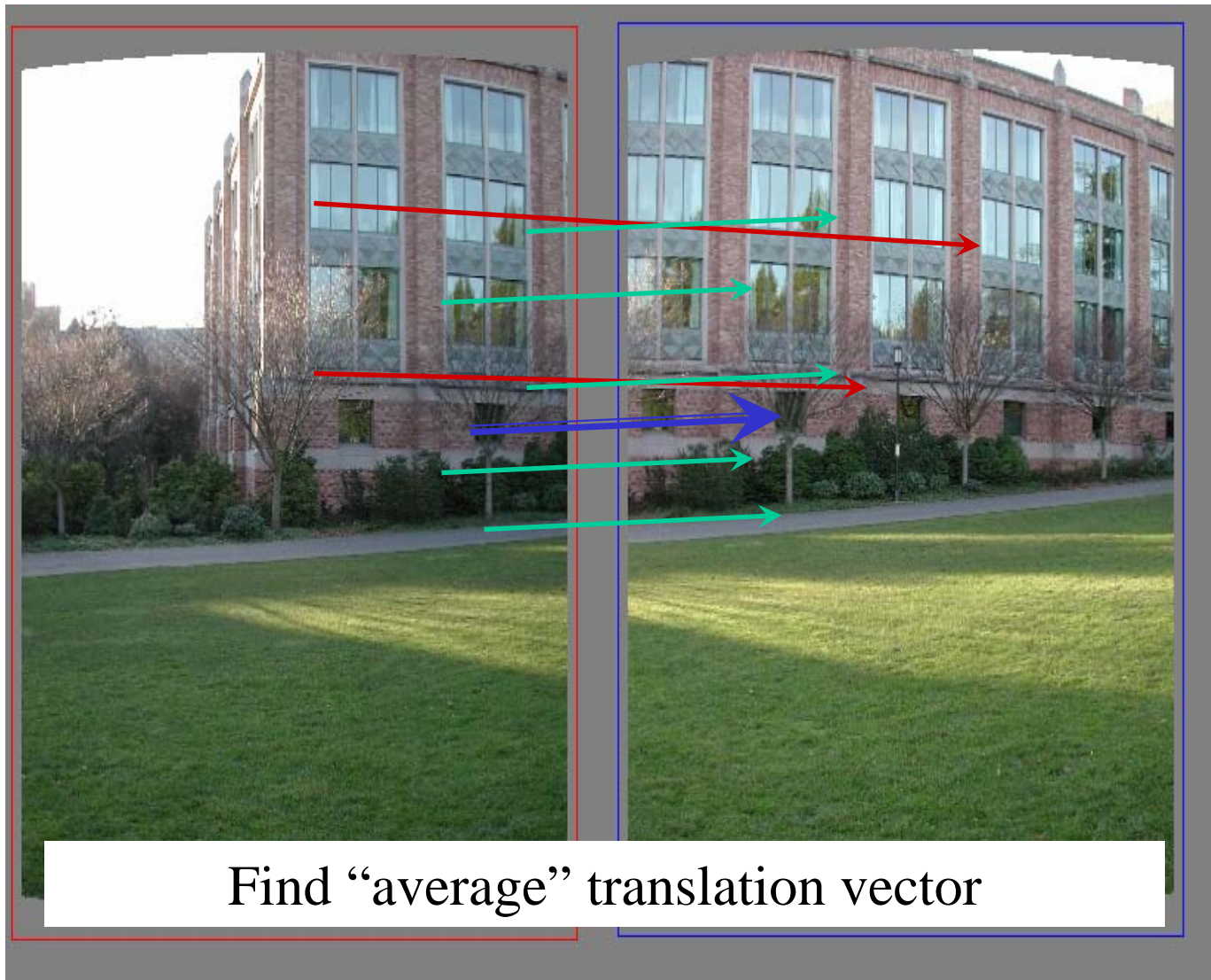
Random Sample Consensus



Random Sample Consensus




Least squares fit

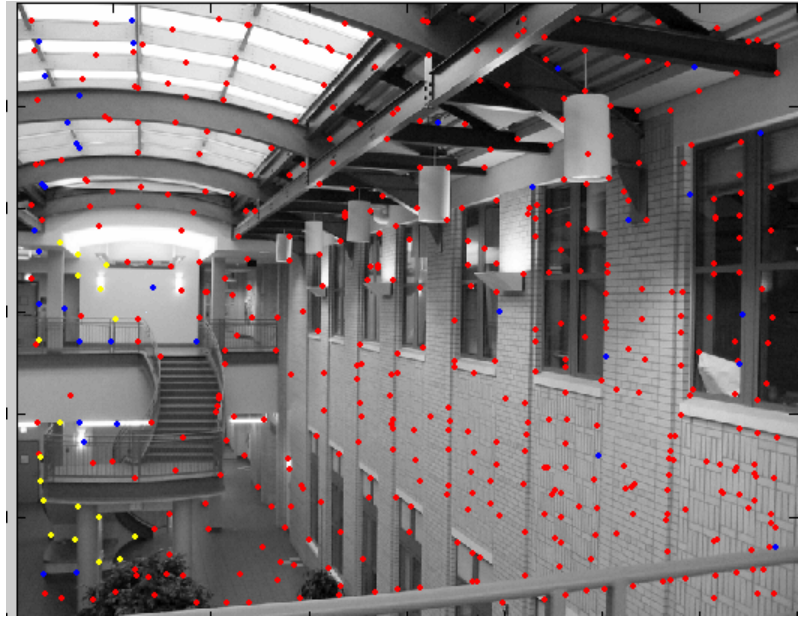
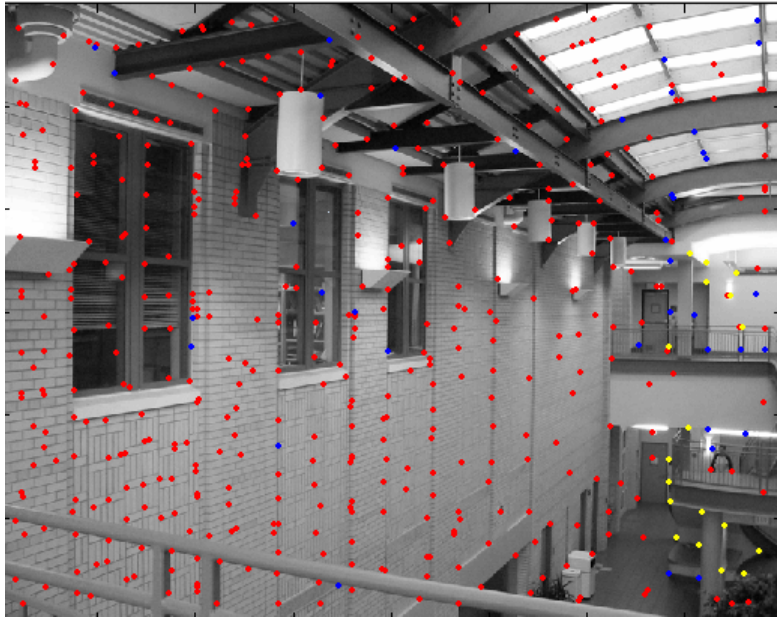


RANSAC for estimating homography

RANSAC loop:

- 
1. Select four feature pairs (at random)
 2. Compute homography H (exact)
 3. Compute *inliers* where $SSD(p_i', \mathbf{H} p_i) < \varepsilon$
 4. Keep largest set of inliers
 5. Re-compute least-squares H estimate on all of the inliers

RANSAC



Example: Recognising Panoramas

M. Brown and D. Lowe,
University of British Columbia

Why “Recognising Panoramas”?

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1D Rotations (θ)

- Ordering \Rightarrow matching images

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- 2D Rotations (θ, ϕ)
 - Ordering \nRightarrow matching images

Why “Recognising Panoramas”?

1D Rotations (θ)

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• 2D Rotations (θ, ϕ)

- Ordering \nRightarrow matching images



Why “Recognising Panoramas”?

1D Rotations (θ)

- Ordering \Rightarrow matching images

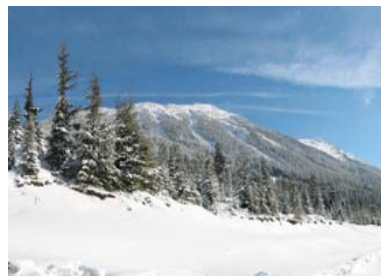
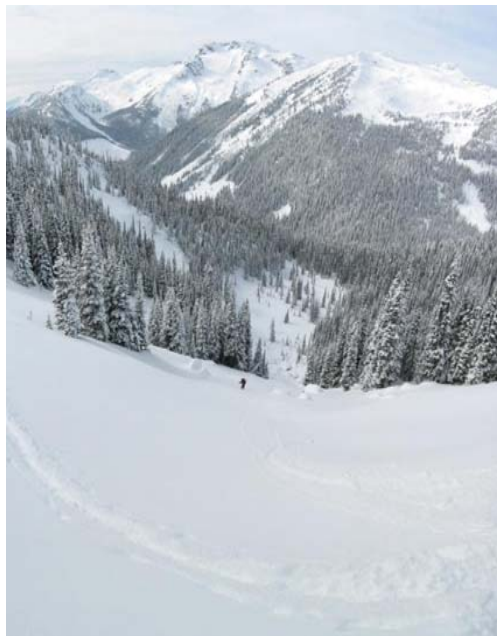
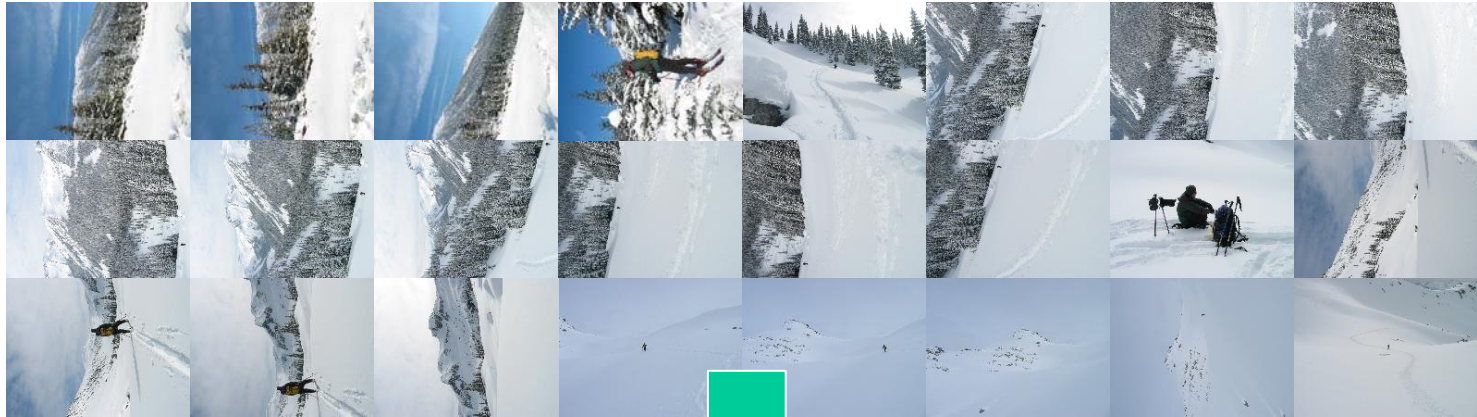


• 2D Rotations (θ, ϕ)

- Ordering \nRightarrow matching images



Why “Recognising Panoramas”?



Overview

Feature Matching

Image Matching

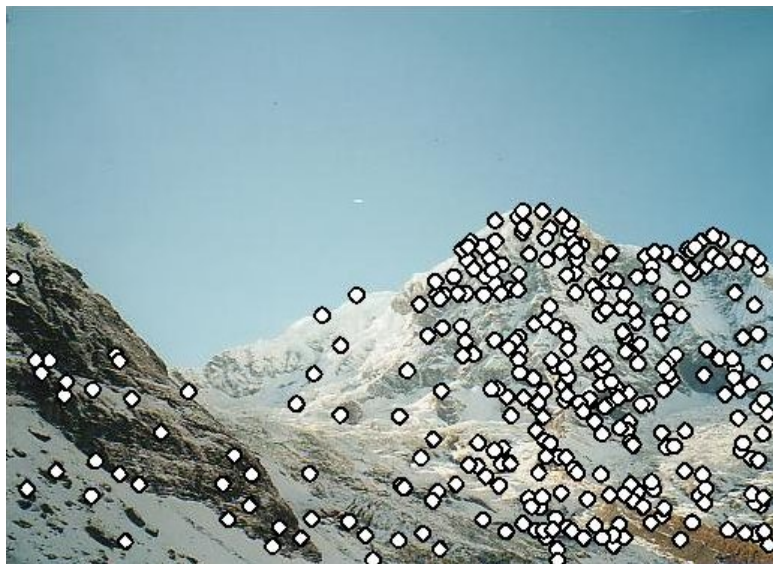
Bundle Adjustment

Multi-band Blending

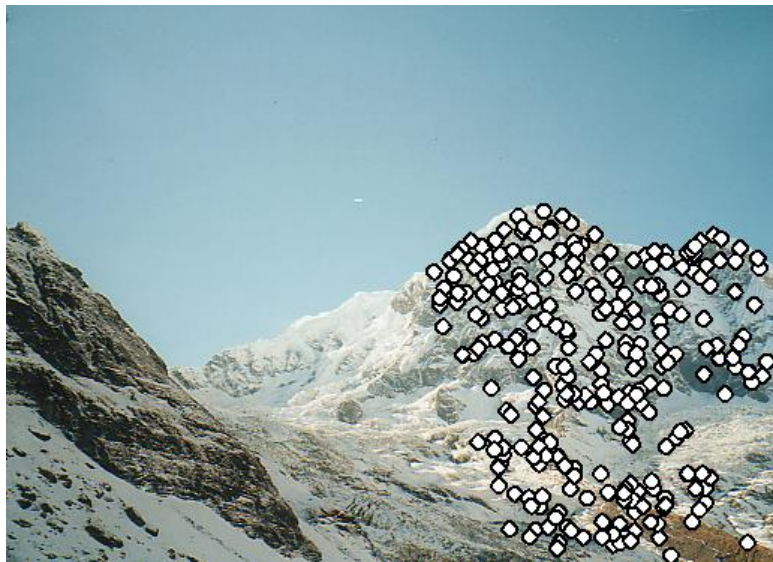
Results

Conclusions

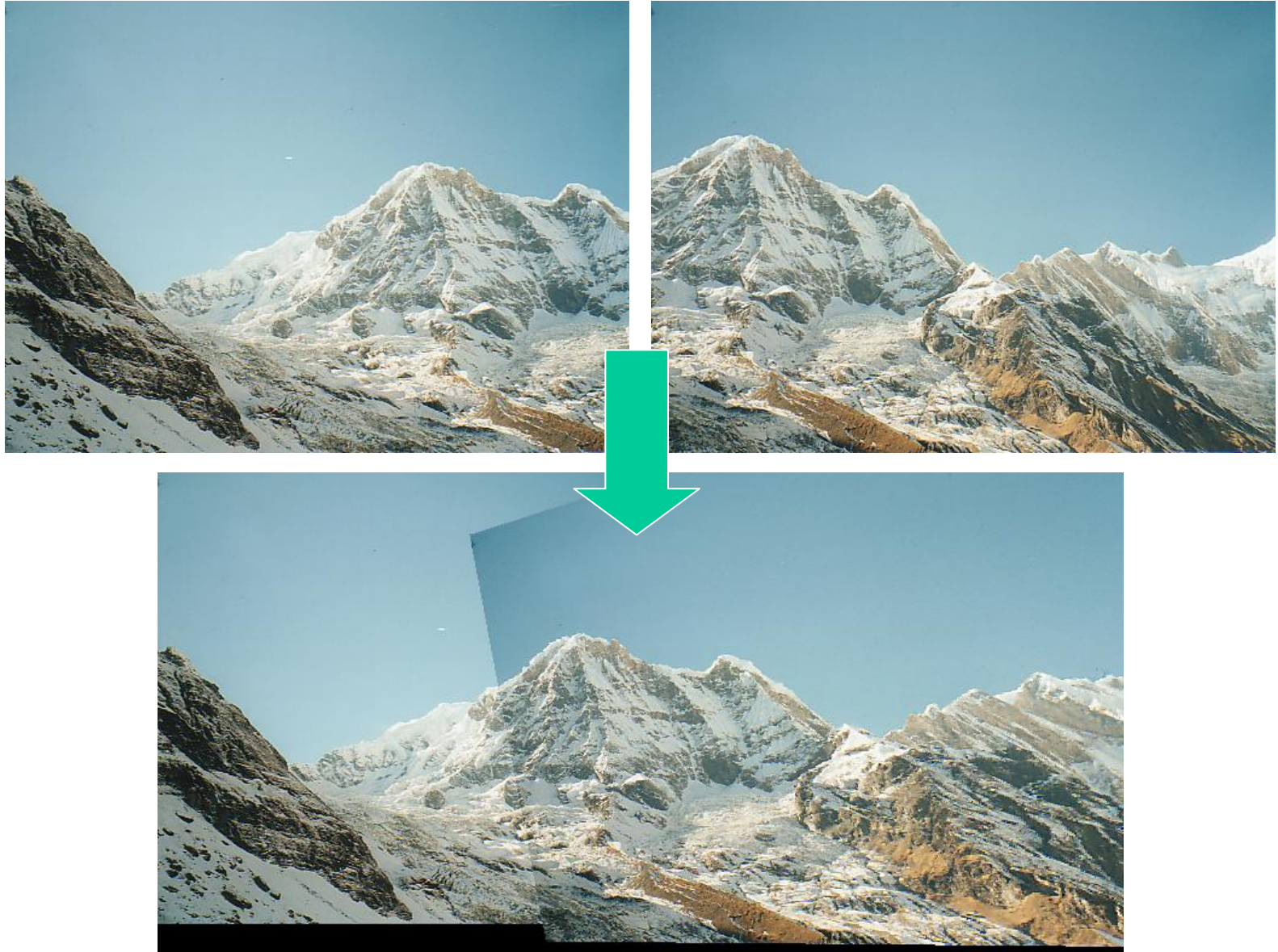
RANSAC for Homography



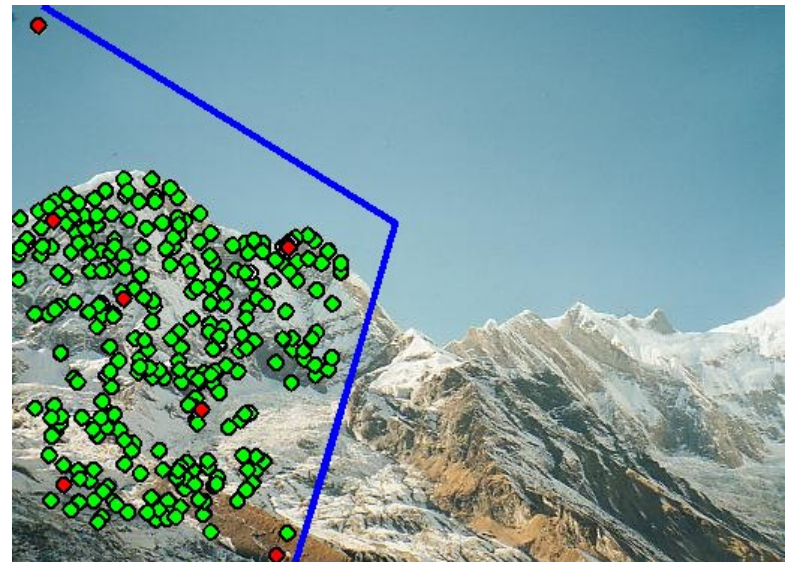
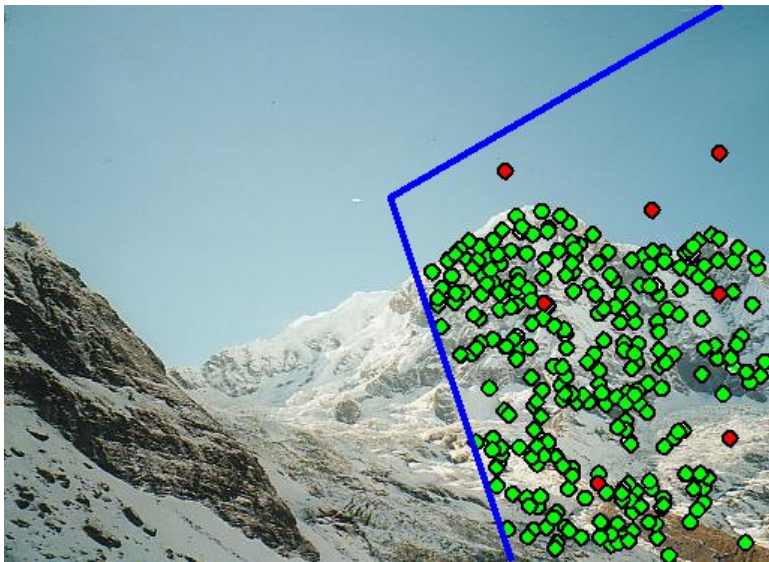
RANSAC for Homography



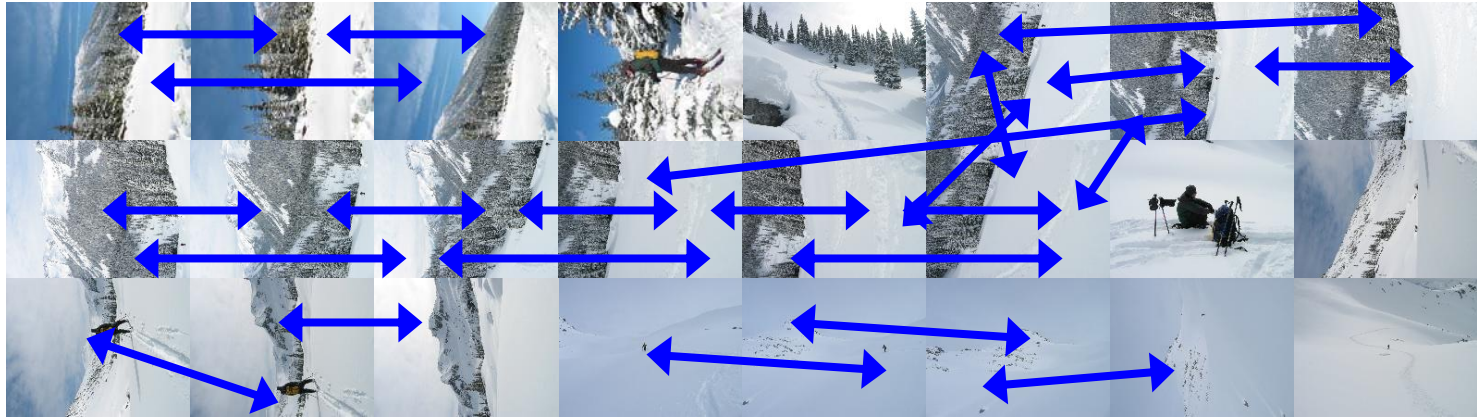
RANSAC for Homography



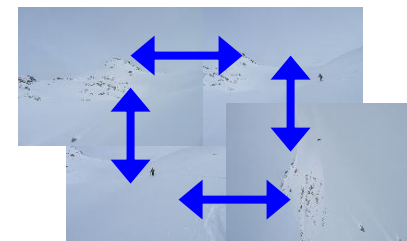
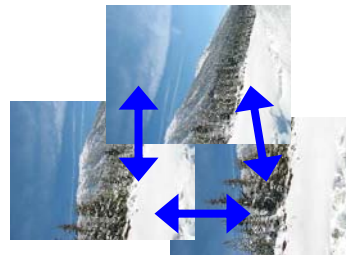
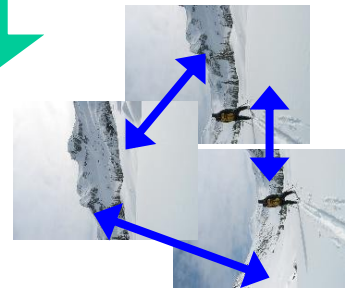
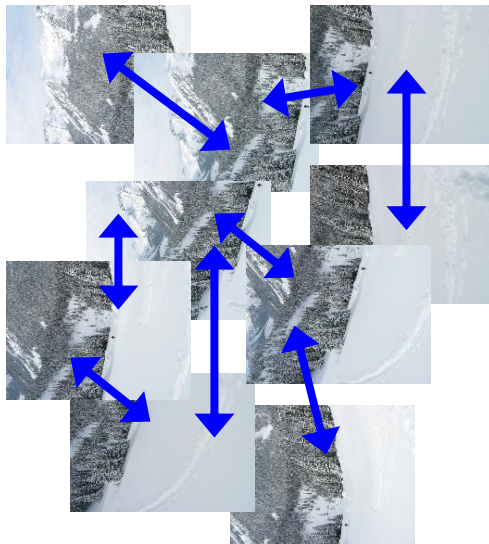
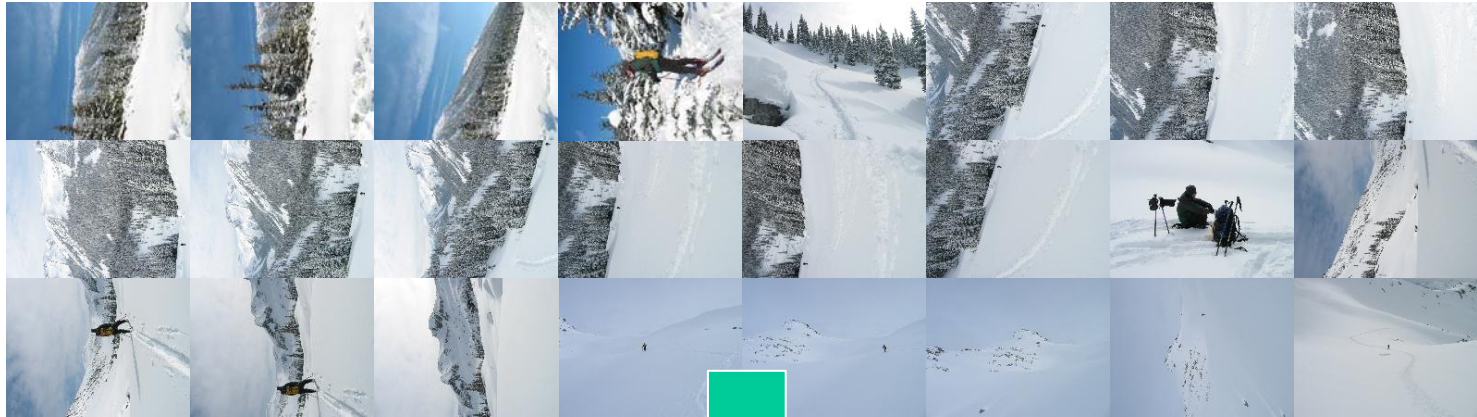
Probabilistic model for verification



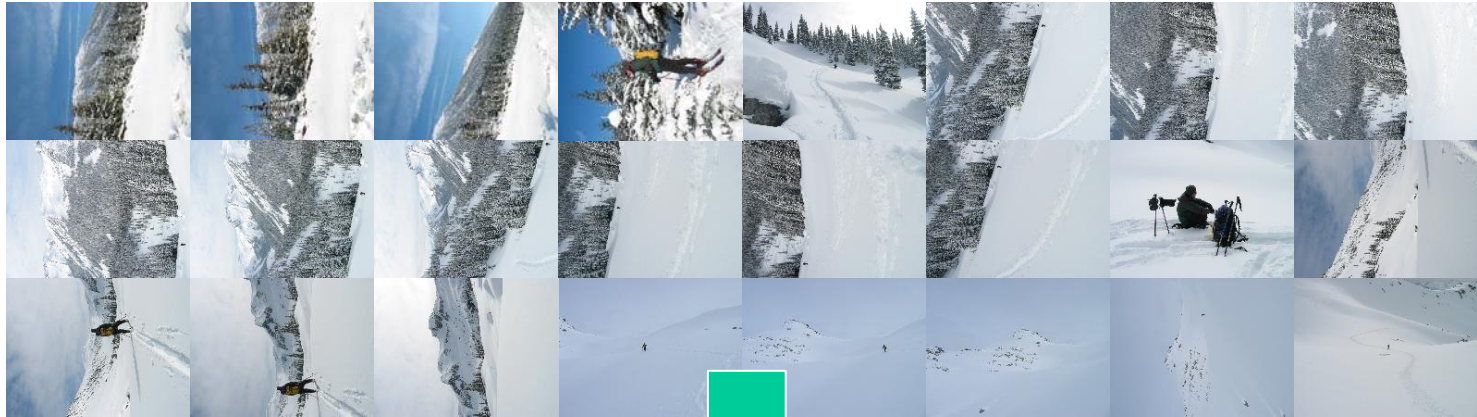
Finding the panoramas



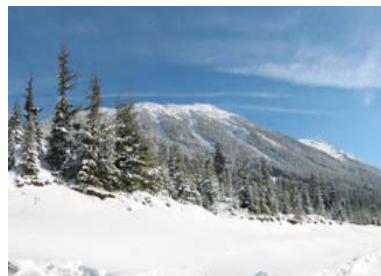
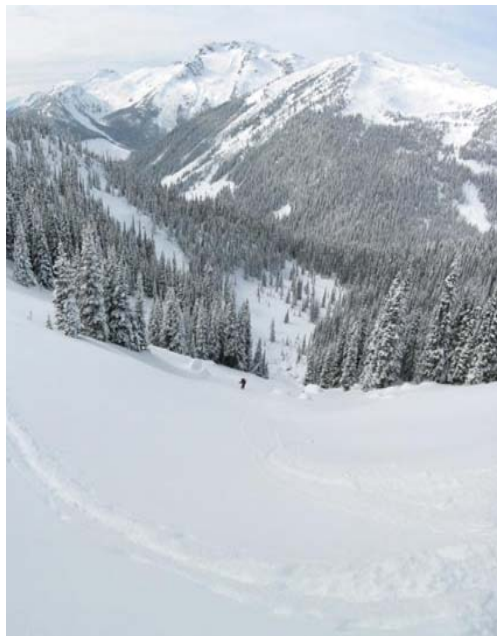
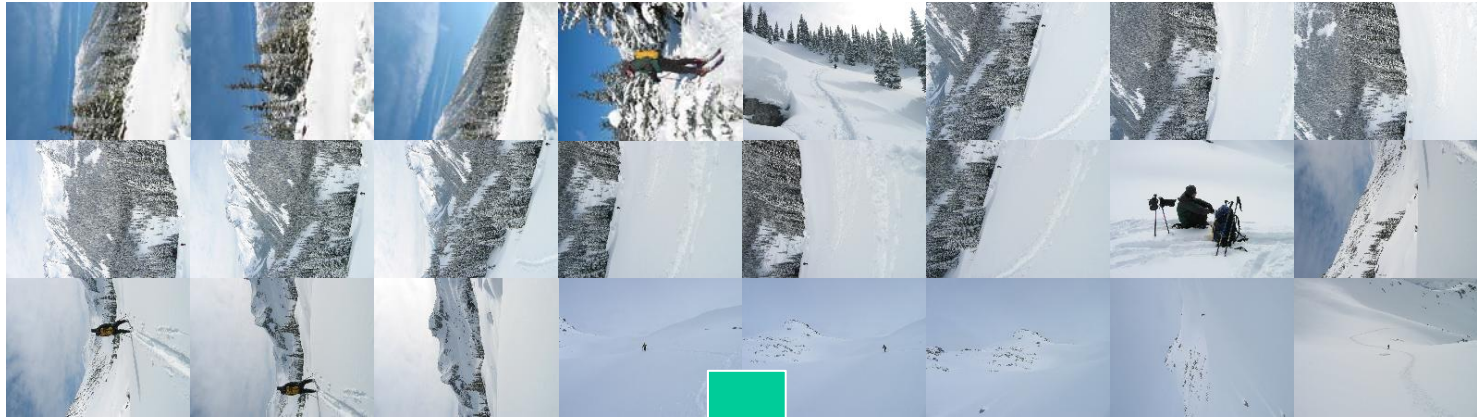
Finding the panoramas



Finding the panoramas



Finding the panoramas



Homography for Rotation

Parameterise each camera by rotation and focal length

$$\mathbf{R}_i = e^{[\boldsymbol{\theta}_i]_{\times}}, \quad [\boldsymbol{\theta}_i]_{\times} = \begin{bmatrix} 0 & -\theta_{i3} & \theta_{i2} \\ \theta_{i3} & 0 & -\theta_{i1} \\ -\theta_{i2} & \theta_{i1} & 0 \end{bmatrix}$$

This gives pairwise $\mathbf{K}_i = \begin{bmatrix} f_i & 0 & 0 \\ 0 & f_i & 0 \\ 0 & 0 & 1 \end{bmatrix}$

$$\tilde{\mathbf{u}}_i = \mathbf{H}_{ij} \tilde{\mathbf{u}}_j, \quad \mathbf{H}_{ij} = \mathbf{K}_i \mathbf{R}_i \mathbf{R}_j^T \mathbf{K}_j^{-1}$$

Bundle Adjustment

New images initialised with rotation, focal length of best matching image



Bundle Adjustment

New images initialised with rotation, focal length of best matching image



Multi-band Blending

Burt & Adelson 1983

- Blend frequency bands over range $\propto \lambda$



Results

